

A Semi-Structural Framework for Measuring Credit Cycles in Europe*

João G. Oliveira[†] Ana Pereira[‡]

October 13, 2021

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Abstract

We develop a framework for evaluating the accumulation of cyclical systemic risk using a set of unobserved component models of credit to the private sector. The structure of these models is derived from theory to assign an economic interpretation to the early warning signals issued by our proposed indicator. This indicator is computed using only the information available to the policymaker when deciding on a policy stance. It depends only on a small set of variables that are usually available with a sufficiently long length. Its leading properties regarding the detection of systemic financial crises are tested against the Basel gap for several European countries. The evaluation exercise relies on a set of metrics commonly used in the context of early-warning systems of crises and is performed both in-sample and out-of-sample. The latter exercise allows us to assess the usefulness of including our measure in a risk monitoring system designed to be used regularly by policymakers. We conclude that our proposed model-based indicator ranks well when compared to the Basel gap, even in the most demanding out-of-sample exercise.

Keywords: Credit cycle; Business cycle; Financial crises; Forecasting; State space; Bayesian methods

JEL Classification: E30; E37; E60; G01

*We thank members of the ECB Cyclical Risk Analysis Group, and seminar participants at the Lisbon Macro Workshop and the Joint BdP/ECB/ESRB Workshop 2018 for helpful comments and suggestions. We thank Jan Hannes Lang and Cosimo Izzo for providing us with their early-warning performance routines. The views expressed in this paper are solely the responsibility of the authors and should not be interpreted as reflecting the views of Banco de Portugal or the Eurosystem.

[†]Nova School of Business and Economics.

[‡]Banco de Portugal and ISEG.

1 Introduction

Surges in lending have often been associated with the onset of financial stress and with increased severity of recessions both in the theoretical ([Lorenzoni, 2008](#); [Bianchi and Mendoza, 2010](#); [Bianchi, 2011](#);) and in the empirical literature ([Borio et al., 2001](#); [Drehmann et al., 2012](#); [Schularick and Taylor, 2012](#); [Ziemann, 2012](#)). This relationship has been at the centre of recent efforts by policymakers and institutions aimed at curbing the build-up of vulnerabilities in the financial sector ([BCBS, 2010a](#); [ESRB, 2014](#)). In fact, the countercyclical capital buffer (CCyB), a recently introduced capital-based macroprudential policy instrument, aims at increasing bank requirements in periods of increased lending in order to prevent credit supply restrictions during financial stress events ([BCBS, 2010b](#)).

However, in practice not all peaks in the so-called credit cycle coincide with financial stress ([Drehmann et al., 2012](#)) and the extent of overborrowing in the economy is difficult to identify ([Bianchi and Mendoza, 2010](#)). This creates a tradeoff for policymakers, given that *ex-ante* restrictions imposed on economic agents are costly, but so are missed crisis signals, which may lead to severe recessions in investment and consumption. Thus, accurate and timely information on the phase of the credit cycle and the likelihood of a financial crisis is key when deciding on a policy stance. Another important aspect for creating a policy stance is the need to have credit cycle measures that allow the identification of the underlying drivers.

In this paper, we investigate the leading properties of a credit-based indicator for the detection of financial systemic crises by measuring the difference between observed credit in the economy and a reference level derived from theory ([Kiyotaki and Moore, 1997](#); [Iacoviello, 2005](#)) in which the quantity of credit in the economy depends on the expected value of collateral and the repayment effort exerted by borrowers. This reference level is obtained from an unobserved components model estimated with Bayesian methods, which rely on Gibbs sampling framework and [Carter and Kohn \(1994\)](#) algorithm.

These methods have the advantage of working relatively well in short samples and do not impose the need of having a parsimonious model. In addition, some of the identification problems that may arise under classical estimation are more easily overcome when resorting to these methods. We test the properties of our proposed measure by using a novel dataset on financial crises in European countries (Lo Duca et al., 2017) and a set of metrics commonly used in the context of early-warning systems of crises (Kaminsky et al., 1998; Alessi and Detken, 2011; Drehmann and Juselius, 2014).¹ The signalling properties regarding systemic financial crises are assessed both in-sample and out-of-sample, as a good real-time performance is paramount for policymaking purposes. The credit-to-GDP gap, known as the Basel gap and proposed by Borio and Lowe (2002), is defined as the competing benchmark early-warning indicator. This choice is grounded in the fact that this is one of the best univariate early-warning indicator regarding systemic financial crises (Detken et al. (2014)) and its use is prescribed in the EU current regulatory toolkit concerning macroprudential policy instruments.

Our findings indicate that our proposed model-based measure of credit cycles ranks well in comparison to the Basel gap. Our measure does not consistently outperform the Basel gap across all metrics in the in-sample evaluation exercise, but in the out-of-sample evaluation exercise it seems to be a better indicator than the Basel gap to detect early on that a crisis event is approaching. In particular, the signalling regarding systemic financial crises provided by our measure occurs in a timely and persistent manner, allowing for a gradual implementation of preemptive macroprudential policy actions with time to become effective. Adding to the good early-warning performance of our measure, is the fact of being a small scale multivariate indicator dependent of variables that are straightforwardly available with a sufficient long time span. In addition, its semi-structural nature allows policymakers to assign an economic interpretation to the early-warning signals. As such, we argue that there is compelling arguments and evidence that sug-

¹The benchmark crisis definition used in this paper is the set of systemic crisis which are not purely foreign in origin, and have macroprudential relevance.

gests the usefulness of including our measure, jointly with others, in a risk monitoring system designed for policy purposes, in particular in those with a macroprudential nature.

Our paper is related to the literature on the measurement of the financial/credit cycle, starting with [Claessens et al. \(2011\)](#), [Drehmann et al. \(2012\)](#), and [Aikman et al. \(2015\)](#). Several authors have built on this work to cover different sets of countries or testing the robustness of those findings to different methods (e.g.: [Hiebert et al., 2015](#); [Galati et al., 2016](#); [Rünstler and Vlekke, 2017](#)). More recently, [Durdu and Zhong \(2021\)](#) analyse to which extent the drivers of the bank credit cycle differ from that of nonbank credit cycles. We contribute to this literature by investigating whether the properties of a reference credit level obtained from an unobserved component model hold in a pseudo real-time environment.

Our paper is also related to the early-warning system literature (e.g., [Alessi et al., 2015](#); [Coudert and Idier, 2016](#)). This literature typically uses a large set of indicators to estimate the probability that a financial crisis occurs within a given horizon. Those indicators are then often aggregated into a single composite index, which inherits the leading properties of its components, such as proposed by [Lang et al. \(2019\)](#). The drawback of these methods is that, although they may be attractive in quantitative terms due to their high success rate in predicting financial crises, they are frequently difficult to interpret and explain in the context of defining a policy stance. We contribute to this stream of the literature by developing a credit cycle indicator with a straightforward economic interpretation.

Finally, this paper is related to the literature on defining a reference level of credit in the economy. In contrast to a purely statistical approach (e.g. the Basel Gap), [Buncic and Melecky \(2014\)](#) and [Albuquerque et al. \(2014\)](#) set up linear regression models that explain credit to the private non-financial sector using variables such as potential GDP, the unemployment rate, and financial development indicators. In the same vein, [Galán](#)

and Mencia (2018) propose to extract a credit cycle using an unobserved components model. A drawback of these approaches is that model construction and variable choice is often based on heuristics, rather than on a formal derivation of the equations. In alternative, Drehmann and Juselius (2015) use a multivariate, co-integration approach to estimate a model of leverage and debt service, based on the work of Kiyotaki and Moore (1997). Our paper is closest to Lang and Welz (2018), who use the theoretical framework of Eggertsson and Mehrotra (2014) to derive an equation for the trend of household credit. They then estimate credit cycles for a set of European countries with a state space formulation and use those estimates as early-warning indicators of systemic financial crises. We complement their work by considering total credit instead of only household credit, given that this is one of the target variable related to the implementation of the countercyclical capital buffer.

Our paper is organized as follows. Section 2 presents the theoretical background, the empirical model to be estimated and our measure of the credit cycle. Section 3 provides an overview of the data used in estimation and discusses the transformations used. Section 4 presents the results from model estimation and performance tests of our measure relative to the Basel gap. Section 5 concludes

2 Model

Our goal is to measure the distance between observed credit and a reference credit level. We assume that the reference credit level is close to the one described in Iacoviello (2005), which applies the framework in Kiyotaki and Moore (1997) to a standard monetary DSGE. In the economy of Iacoviello (2005), the long-run level of aggregate debt is constrained by the availability of collateral and a key source of macroeconomic fluctuations are shocks that affect its value.

The existence for collateral in Kiyotaki and Moore (1997) and Iacoviello (2005) stems

from the need to overcome limited commitment problems, i.e., because agents cannot commit to repayment in advance, lenders are given a claim on the borrowers assets, which generally take the form of a durable good. In reality, there are several other frictions that generate fluctuations in credit markets (e.g., liquidity crises, bank frauds, etc). In fact, [Cordoba and Ripoll \(2004\)](#) show that collateral constraints have a very modest amplification potential when used in standard DSGE models. Thus, the relative stability of the quantity of credit implied by collateral constraints is ideal for the purpose of measuring reference credit. The residual, i.e., the difference between observed credit and reference credit, will contain all other frictions.

The model is as follows. We assume that there are two types of borrowers: households and firms, both with measure 1. Each period, agents start with a given level of assets, k_t , which can be used as collateral to obtain loans. Thus, for each agent type, credit is limited by the value of collateral:²

$$R_t c_t \leq M k_t \mathbb{E}_t [q_{t+1}], \quad (1)$$

where c_t is the amount of credit borrowed by an agent, R_t is the gross nominal interest rate, M is the loan-to-value (LTV) ratio, q_{t+1} is the asset price next period, and k_t is the quantity of collateral. This expression implies that the value of repayment cannot exceed a fraction of the expected value of the asset provided as collateral. If it did, the borrower would simply default on its obligations and keep the funds. Note that, in the case of firms, project cash flows cannot be pledged, as they can threaten to withdraw their efforts in order to force a reduction in the value of repayment after the contract has been signed (see [Kiyotaki and Moore, 1997](#) for a discussion).

In a setting without uncertainty, [Kiyotaki and Moore \(1997\)](#) show that 1 holds with equality in equilibrium, i.e., agent borrow up to the maximum. [Iacoviello \(2005\)](#) argues that 1 holds with equality in a stationary equilibrium if uncertainty is small enough

²Individual subscripts are suppressed because all agents are assumed to be identical within their types.

such that agents do not need to engage in precautionary saving. We integrate 1 over households and firms. Rearranging the resulting expression and dividing both sides by the price of consumption goods, we can express the observed level of debt as a function of debt service and the expected relative price of collateral:

$$\frac{C_t}{P_t} = \frac{M_t K_t}{R_t} \mathbb{E}_t \left[\frac{Q_{t+1}}{P_t} \right], \quad (2)$$

where capital letters indicate aggregate values. Note that we allow the loan-to-value to change across time in order to capture changes in the economic and financial environment, which is a key element in our formulation. We take the natural logarithm of 2 and arrive to the following equation for real credit.

$$\ln \left(\frac{C_t}{P_t} \right) = \ln M_t + \ln K_t - \ln R_t + \ln \left[\mathbb{E}_t \left(\frac{Q_{t+1}}{P_t} \right) \right] + \epsilon_t, \quad (3)$$

Then, we assume that credit limits, $\ln M_t$, may be decomposed into a trend and a cycle component and specify 3 as an unobserved components model that recasted in a state space structure takes the following form:

$$\ln \left(\frac{C_t}{P_t} \right) = \mu_t^M + c_t^M + \ln K_t - \ln R_t + \ln \left[\mathbb{E}_t \left(\frac{Q_{t+1}}{P_t} \right) \right] + \epsilon_t, \quad (4)$$

$$c_t^M = \sum_{i=1}^h \rho_i c_{t-i}^M + \varepsilon_t^M, \quad (5)$$

$$\mu_t^M = \mu_{t-1}^M + v_{t-1}^M + \zeta_t^M, \quad (6)$$

$$v_t^M = v_{t-1}^M + \zeta_t^M. \quad (7)$$

where μ_t^M and c_t^M are, respectively, the trend and cycle components of $\ln M_t$. This specification follows the structural time series model introduced by (Harvey, 1991) where equation 4 is the observation or measurement equation that relates the vector of observed variables to state unobserved variables, explanatory variables and a measurement error

and equations 5 to 7 are the state or transition equations. The cycle component in 5 is modelled as an autoregressive process of order h with parameters ρ_i , $i = 1, \dots, h$. The stochastic trend component is defined as a random walk process with a slope where equation 6 models the trend level and equation 7 models the trend slope as a random walk process. Both the level and the slope of the trend are allowed to vary over time to easily accommodate any structural changes occurring in the trend of credit limits. Implicitly, we assume that credit will differ from its reference level for a combination of three reasons: (i) measurement error, ϵ_t ; (ii) structural changes in credit limits, μ_t^M ; and (iii) cyclical changes in credit limits, c_t^M . All innovations in the model are assumed to be jointly normally distributed, with zero mean and the following variance covariance matrix:

$$\text{Var} \begin{pmatrix} \begin{bmatrix} \epsilon_t \\ \epsilon_t^M \\ \zeta_t^M \\ \zeta_t^M \end{bmatrix} \end{pmatrix} = \begin{bmatrix} \sigma_\epsilon^2 & 0 \\ 0 & R \end{bmatrix}, \quad (8)$$

where σ_ϵ^2 is the variance of the measurement error, ϵ_t , and R is the 3×3 covariance matrix of state variable innovations. All innovations are serially uncorrelated and independent of each other.

Iacoviello (2005) interprets the loan-to-value ratio, M_t , as a parameter of the economy for implementability reasons. With the present framework, we are able to define the loan-to-value as a time-varying unobserved component and to estimate it using the Kalman filter. Critically, movements in the estimate for M_t can indicate changing credit standards or changes in the precautionary behavior of borrowers, reflecting shifts in the supply or demand for credit.

We impose unit coefficients on the amount of collateral that may be posted, the gross interest rate, and on the expected relative price of collateral. The reason for this choice is the assumption that the framework in Iacoviello (2005) is a reasonable description of the

behavior of agents in credit markets in a stationary equilibrium, and that any deviation of observed credit from the reference credit level is either due to observational error or changes in the willingness to lend/borrow, which are orthogonal to the set of observable fundamentals.

To estimate 4, we require a series of one-step ahead forecasts for the price of collateral, Q_t . We assume that it can be decomposed into a trend-cycle process as proposed by [Harvey \(1991\)](#), which we write in state space form as:

$$\begin{aligned} Q_t &= \mu_t^Q + c_t^Q + \epsilon_t^Q, \\ c_t^Q &= \sum_{i=1}^h \phi_i c_{t-i}^Q + \varepsilon_t^Q, \\ \mu_t^Q &= \mu_{t-1}^Q + \nu_{t-1}^Q + \xi_t^Q, \\ \nu_t^Q &= \nu_{t-1}^Q + \zeta_t^Q. \end{aligned} \tag{9}$$

where c_t^Q and μ_t^Q are the time-varying unobserved components of asset prices (trend and cycle, respectively). Again, the cycle component is modelled as an autoregressive process of order h , where ϕ_i are the corresponding autoregressive parameters, and the trend component is defined as a first order autoregressive process with stochastic level and slope. As in equations 4 to 7, all innovations are assumed to be Gaussian, with zero mean and a covariance matrix of the form:

$$\text{Var} \left(\begin{bmatrix} \epsilon_t^Q \\ \varepsilon_t^Q \\ \xi_t^Q \\ \zeta_t^Q \end{bmatrix} \right) = \begin{bmatrix} \sigma_{\epsilon^Q}^2 & 0 \\ 0 & V \end{bmatrix}, \tag{10}$$

where $\sigma_{\epsilon^Q}^2$ is the variance of the observational error, ϵ^Q , and V is the 3×3 covariance matrix of state variable innovations. All innovations are serially uncorrelated and inde-

pendent of each other. We assume that agents use this model to form expectations about future collateral prices. Thus, we use the forecasts from this model to estimate the system in equations 4 to 7. In the Appendix we present the state space formulation of model equations 4 to 7 and 9 in matrix form.

We use Bayesian methods, namely Gibbs sampling framework and [Carter and Kohn \(1994\)](#) algorithm, to estimate the parameters in 4 to 7 and 9 and the Kalman filter to obtain estimates of the unobserved components in the models. These methods have the advantage of working relatively well in the context of short time series samples and do not impose the need for a parsimonious model. Estimation and filtering is performed using only past and contemporaneous information (pseudo real-time) to mimic as much as possible the information set available to policymakers in each period. This procedure yields a distribution of estimates of the cycle in credit limits, c_t^M , where the median of those estimates in each period is denoted by $c_{t|t}^M$. The credit cycle indicator (CCI) is then defined as:

$$CCI_t = c_{t|t}^M, \quad (11)$$

The CCI is basically a factor that is usually suggested in the literature as a driver of many of the historical systemic financial crises preceded by credit booms (inter alia [Dell’Ariccia et al., 2012](#)), the degree of restrictiveness in credit limit. When credit limits are somewhat more loose due to demand and/or supply related factors, the capacity of borrowers to take on more debt tends to increase. Thus, in light of the proposed model this cycle determines the deviations of real credit from its reference value, as expressed in 4, apart from the observation error. On the practical side, the CCI has some advantages as well: (i) it provides an economic interpretation for credit cycle developments; and (ii) its linear form allows to easily decompose the results along driving factors.

3 Data

We estimate the model described in the previous section for 13 European countries, covering the sample period 1970Q1 - 2017Q3.³ However, data availability varies across countries. Table 1 summarizes the data used in the estimation of the model and in the performance tests and their sources. The measure of credit in the economy is total

Table 1: Data overview

Variable	Description	Source
<i>Model</i>		
Credit (C_t)	Total credit to the non-financial private sector	Quarterly Sector Accounts, Eurostat
Prices (P_t)	Harmonised index of consumer prices (2015=1)	Main Economic Indicators, OECD
Capital (K_t)	Capital at constant 2015 prices, structures	Penn World Table version 9.0
Investment	Investment in dwellings and other structures	World Economic Outlook, OECD
Interest rate (R_t)	Gross 3-months money market rate	Financial Market Data, ECB - SDW
		Main Economic Indicators, OECD
House prices (Q_t)	Residential property price index	Residential Property Price Index Statistics, ECB - SDW
<i>Performance tests</i>		
Basel gap	Real time HP-filtered credit to GDP ($\lambda = 400,000$)	Authors' calculations
Systemic financial crisis	Binary variable (=1 during crisis periods)	Lo Duca et al. (2017)

Note: SDW stands for Statistical Data Warehouse.

credit, including both loans and securities, granted by all sectors to the domestic non-financial private sector. Lending to governments and financial institutions is excluded from the credit aggregate given that they are not modelled in our framework.⁴ This variable is then deflated using the harmonised index of consumer prices (HICP), given that consumption is the numeraire good.

We use the stock of structures in the economy as a proxy for the amount of collateral available in each year.⁵ Data from the Penn World Table (PWT) have annual frequency and are only available until 2014. We linearly interpolate the series in order to obtain quarterly data and extend it to 2017Q3 using quarterly data on investment in dwellings and other structures. Our choice is grounded in a number of reasons: (i) the major role

³The countries are Austria, Belgium, Germany, Denmark, Spain, Finland, France, United Kingdom, Greece, Ireland, Italy, the Netherlands, and Portugal.

⁴Furthermore, lending dynamics to these sectors are not considered when deciding on CCyB stance.

⁵The stock of structures also includes government property, but as we are only interested in the dynamics and not the level of credit, this is not an issue.

of housing in lending to households; (ii) the link between housing and credit booms (Dell’Ariccia et al., 2012); and (iii) the fact that structures are often a significant component of firm assets and are more easily seizable in case of default when compared to other assets which can be moved or have high depreciation rates.

Note that we are not assuming that banks demand collateral on every loan or that the collateral is correctly valued. Rather, our reasoning is that a banking system which is more stringent in terms of collateral requirements is more resilient in case of massive counterparty defaults, all else equal.⁶ A corollary is that credit market dynamics should follow closely those of collateral markets, which forms the basis for our measurement of reference credit.

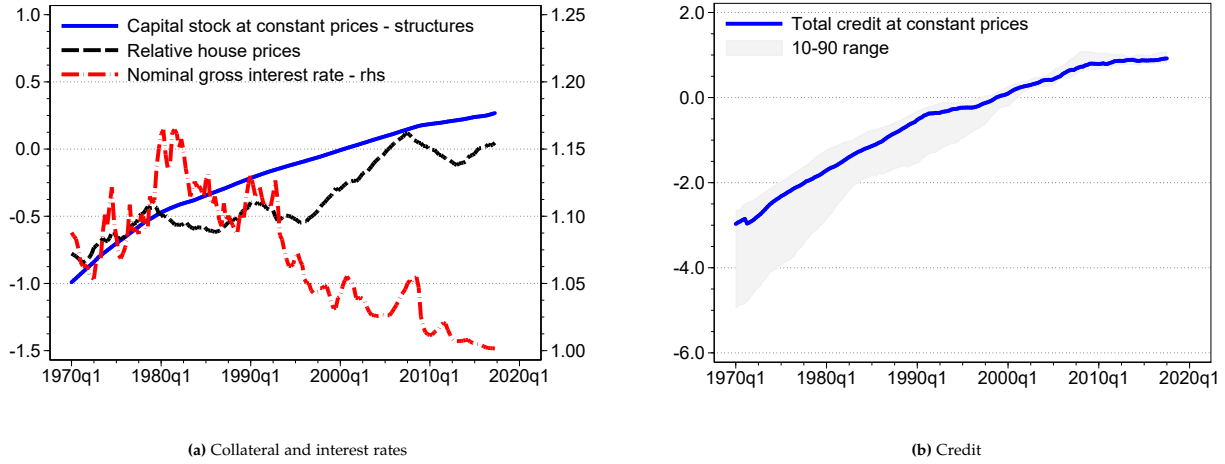
We use the gross 3-month money market rate as a proxy for the nominal repayment rate of borrowers, due to the availability of long time series and to its role as a reference for interest rate fixing of both household and firm lending.

We use the residential property price index as a proxy for collateral prices. Whenever possible the index is backcasted using the price of structures from the PWT, which is linearly interpolated to obtain a series with quarterly frequency. We then deflate the index using the HICP.

Figure 1 shows the behaviour of the data used in estimation over the sample period. Viewing Figure 1a in light of the proposed model indicates that the median reference credit in the sample should trend upwards for three reasons: (i) increase in the availability of collateral in the economy, as suggested by the steady climb in the stock of structures; (ii) growth in relative house prices indicates that collateral has become more valuable and can thus be posted for a greater amount of credit; and (iii) the drop in the nominal interest rate since the 1980s implies that repayment effort has been substantially

⁶In the run-up to the financial crisis, only 35% of all NFC loans by US commercial banks were secured by collateral (data from FRED). This feature is related with the business of short-term lending, which is often unsecured. However, Duval et al. (2017) find evidence that US firms with higher roll-over risk suffered greater productivity slowdowns in the aftermath of the financial crisis. This implies both that banks which are more heavily exposed to this type of lending are more vulnerable and that over-reliance on short-term funding by firms amplifies the effects of unforeseen credit constraints.

Figure 1: Cross-country data



Notes: the stock of capital, the relative house prices and total credit were normalized with respect to their 2000Q4 value for each country and then log-transformed. Total credit is the total credit granted to households and non-financial corporations. The charts show the yearly cross-sectional median of each series. The 10-90 range is the interval between the 10th and the 90th percentiles.

reduced for borrowers. This observation appears to be consistent with the data on Figure 1b. Furthermore, the apparent cyclical behaviour of relative house prices is coherent with boom and bust cycles, which motivates the framework we have presented.

In the performance tests, we compare our new credit cycle measure with that of the Basel gap. As proposed by [Borio and Lowe \(2002\)](#), this latter indicator is the real time estimate of the cycle in the ratio between total credit to the non-financial private sector and GDP using the one-sided Hodrick-Prescott filter with a smoothing parameter of 400,000. The rationale for comparing our credit cycle measure with the Basel gap is its prominent use as a signalling indicator of cyclical imbalances and in guiding the setting of CCyB rates for dealing with excessive credit.⁷ It is the recommended indicator in the CCyB guidance provided by the Basel Committee of Banking Supervision ([BCBS, 2010b](#)), and its use is inscribed in European Union law ([European Parliament and Council of the European Union, 2014](#)). The relative performance of the CCI is assessed on the basis of two evaluation exercises that comprise a set of commonly used metrics. Firstly, the early-warning properties of the CCI for signalling systemic financial crises are evaluated in-

⁷The Basel gap is considered as one of the best univariate signalling indicators for systemic financial crises as discussed, among others, in [Borio and Lowe \(2002\)](#) and [Dekten et al. \(2014\)](#)

sample and then out-of-sample. For that we use a binary indicator of systemic financial crises, drawn from a recent database of financial crises in European Union countries by [Lo Duca et al. \(2017\)](#). The details on the metrics are provided below in Section 4. This framework follows current practice for early-warning of financial crises exercises ([Lang and Welz, 2018](#); [Aikman et al., 2018](#)).

4 Results

Estimation details and assumptions

To obtain the CCI estimates, as given in equation 11, the objects to be estimated are the unobserved components $c_t^M, \mu_t^M, v_t^M, c_t^Q, \mu_t^Q$ and v_t^Q , the variances σ_ϵ^2 and $\sigma_{\epsilon^Q}^2$, the covariance matrices V and R and the set of parameters ϕ_i and ρ_i . We start by estimating sequentially the model in equation 9 and then the model in equations 4 to 7 using Bayesian methods. Bayesian methods have the advantage of working well with short time series samples and do not impose the need of having a parsimonious model. The former advantage is particularly important in a setting as ours in which the models are estimated in a real-time context. Furthermore, Bayesian methods can help to overcome identification problems that may arise in the maximization of the likelihood function under classical estimation of this type of models.⁸

We assume an inverse Gamma prior distribution for the variances of the observation errors (σ_ϵ^2 and $\sigma_{\epsilon^Q}^2$) and an inverse Wishart for the covariance matrices of the state variable innovations (V and R). In the latter case, we also impose that the standard deviation of trend shocks is lower than the standard deviation of cyclical shocks by a factor of 0.001 ([Rünstler and Vlekke, 2017](#) and [Melolinna and Tóth, 2019](#)). In the case of matrix V , the scale matrix of the prior distribution is set to the identity matrix. The

⁸As pointed out by [Primiceri \(2005\)](#) and [Melolinna and Tóth \(2019\)](#), the application of classical estimation to state space models might imply likelihood functions which have a flat surface, complicating the optimization problem, or multiple peaks, some of which not feasible from a policymakers perspective.

degrees of freedom are set to 5 for R and V to guarantee that the prior distributions are proper. This choice of scale matrices defines the parameter space in which we believe the covariance matrix should move while choosing a small value for the degrees of freedom implies uninformative priors, i.e. prior distributions that have a negligible influence in the estimated parameters.⁹ In terms of the inverse Gamma prior distributions, we impose a value of 1 to the scale parameter and 3 to the degrees of freedom. The prior values for the distribution hyperparameters are the ones commonly used to specify uninformative and proper prior inverse Gamma distributions. The initial values for the variances of the observation errors and for the covariance matrices of the state variable innovations are set, respectively, to the scale parameters and matrices of the respective prior distributions.

These prior distributions were chosen on the basis of the range of admissible values for the parameters, the inverted Gamma and the inverted Wishart only assume positive values. Also, these priors follow the standard practice in related literature (among others, [Melolinna and Tóth, 2019](#) and [Tóth, 2021](#)) as they are natural conjugate priors to data likelihood functions set to Normal. This property facilitates the use of approaches based on Gibbs sampling algorithm, as it is our case.

We assume a multivariate Normal prior distribution for the unknown autoregressive parameters of the cyclical component of real total credit and collateral prices. For the ϕ_i parameters, the prior mean is set to the vector of OLS coefficient estimates obtained from fitting an $AR(h)$ process to a cycle estimate, obtained from computing the difference between observed collateral prices and a Hodrick Prescott trend (filter with a smoothing parameter of 1,600) using the first 39 sample observations. The covariance matrix of the normal prior is set to the estimated version of the covariance matrix of OLS coefficient estimates. The same approach is used to define the hyperparameters of the prior distri-

⁹The inverse Wishart distribution (inverse-Gamma distribution is the univariate version) is defined by the scale matrix that positions the distribution in the desirable parameter space and the degrees of freedom that set the certainty about the information in the scale matrix. Thus, the higher the degrees of freedom the more informative is the inverse Wishart distribution (see [Schuurman et al., 2016](#)).

bution for the ρ_i parameters using instead real total credit. Based on the literature for measuring output gaps using unobserved components models, previous studies, such as [Rünstler and Vlekke \(2017\)](#), [Lang and Welz \(2018\)](#) and [Galán and Mencia \(2018\)](#), have assumed that the cycle component of a credit aggregate follows an AR(2) process. In addition, [Claessens et al. \(2012\)](#), [Hiebert et al. \(2015\)](#) and [Rünstler and Vlekke \(2017\)](#) find evidence of similar cyclical dynamics between collateral prices and credit. Hence, in both models we set $h = 2$.¹⁰ The initial values for the parameters of the cyclical components are set to the prior means.

Finally, the cyclical components are initialised at zero, while the level and the slope of the stochastic trends are initialised using sample information. The initial value for the trend level is set equal to the first sample observation of either collateral prices or real total credit. While the initial value for the trend slope is set to the first value of the times series that results from taking the first differences of either collateral prices or real total credit. The initial state covariance matrix is assumed to be the identity matrix in both unobserved components models. Table 2 summarizes the characteristics of the chosen prior distributions.

Provided with initial values and prior distributions, we estimate the parameters by drawing from the conditional posterior using the Gibbs sampling algorithm with 5,000 replications and rejecting the first 2,000 draws. First, the Kalman filter is used to obtain recursively the unobserved components of both models. Then, the backward recursion algorithm described in [Carter and Kohn \(1994\)](#) is used to obtain the mean and variance of the distribution of the state variables (those that are not observable) that will feed into the conditional posterior distribution of the parameters. Finally, conditional on the state variables, we draw the matrices V and R from an inverse Wishart distribution, σ_ϵ^2 and $\sigma_{\epsilon Q}^2$ from an inverse Gamma and the ϕ_i and ρ_i parameters from a Normal distribution. In the

¹⁰For the cases of Austria and Portugal we did not obtained a stationary cycle with $h = 2$ in the model for real total credit. So, we increased the lags of the cyclical component until convergence to a stationary cycle was attained. This happened when we set $h = 3$.

Table 2: Prior distributions

<i>Collateral prices model</i>					
Parameter	Equation	Distribution	l.b	u.b	Parameters
ϕ_1	State	Normal	$-\infty$	$+\infty$	mean: $\phi_1^{\hat{OLS}}$, std: $\hat{\sigma}_{\phi_1}^{2,OLS}$
ϕ_2	State	Normal	$-\infty$	$+\infty$	mean: $\phi_2^{\hat{OLS}}$, std: $\hat{\sigma}_{\phi_2}^{2,OLS}$
$\sigma_{\xi^Q}^2$	State	Inv. Wishart	0	$+\infty$	scale: 1, df: 5
$\sigma_{\xi^Q}^2$	State	Inv. Wishart	0	$+\infty$	scale: 1, df: 5
$\sigma_{\xi^Q}^2$	State	Inv. Wishart	0	$+\infty$	scale: 1, df: 5
$\sigma_{\epsilon^Q}^2$	Obser.	Inv. Gamma	0	$+\infty$	scale: 1, df: 3
<i>Real total credit model</i>					
Parameter	Equation	Distribution	l.b	u.b	Parameters
ρ_1	State	Normal	$-\infty$	$+\infty$	mean: $\rho_1^{\hat{OLS}}$, std: $\hat{\sigma}_{\rho_1}^{2,OLS}$
ρ_2	State	Normal	$-\infty$	$+\infty$	mean: $\rho_2^{\hat{OLS}}$, std: $\hat{\sigma}_{\rho_2}^{2,OLS}$
$\sigma_{\xi^M}^2$	State	Inv. Wishart	0	$+\infty$	scale: 1, df: 5
$\sigma_{\xi^M}^2$	State	Inv. Wishart	0	$+\infty$	scale: 0.001, df: 5
$\sigma_{\xi^M}^2$	State	Inv. Wishart	0	$+\infty$	scale: 0.001, df: 5
σ_{ϵ}^2	Obser.	Inv. Gamma	0	$+\infty$	scale: 1, df: 3

Note: L.b. stands for lower bound and u.b. stands for upper bound.

latter case, random draws from the Normal posterior conditional distribution are taken until a stationary cyclical component is obtained, given that our prior belief is that the cyclical components are stationary. In addition, to guarantee that the cyclical component has an oscillating movement the random draws also have to fulfill the requirement of delivering complex roots.

Early-warning signaling performance

The use of a signalling approach to study the early-warning properties of indicators regarding crisis events was first introduced by Kaminsky et al. (1998) and Kaminsky and Reinhart (1999) in the context of currency crises.¹¹ This approach assumes a non-linear relationship between the indicator and the crisis event variable and has been considerably used in the aftermath of the Great Financial Crisis as a tool to assess which

¹¹ According to this approach, an indicator issues a signal regarding a crisis event if it is above/below a certain threshold level within a specific period prior (vulnerable period) to the crisis.

indicators are better suited to signal in a timely manner that a systemic financial crisis is imminent (among others [Dekten et al., 2014](#), [Lo Duca et al., 2017](#)).

In our specific case, the early-warning properties of the CCI and the Basel gap for signalling systemic financial crises are assessed individually, in-sample and out-of-sample for the pooled set of countries in terms of the following standard metrics:

AUROC: The Area Under the Receiver Operating Characteristic (AUROC) curve is a summary measure of the signalling performance of an indicator regarding crises. The receiver operating curve plots the noise ratio (false positive rate) against the signal ratio (true positive ratio) for every possible signalling threshold. The AUROC varies between 0 and 1, a value of 0.5 indicates an uninformative indicator and a value of 1 indicates a perfect early-warning indicator. The AUROC allows ranking indicators according to their ability to predict crises without the need to specify a threshold.

Relative usefulness: The relative usefulness of an indicator is defined in [Alessi and Detken \(2011\)](#) as $U = \frac{\min(\theta, 1-\theta) - L}{\min(\theta, 1-\theta)}$, where L represents a policymaker loss function defined as $L = \theta \text{Type I error} + (1 - \theta) \text{Type II error}$ and θ the policymaker preference for not missing a crisis (risk aversion or relative preferences parameter).¹² It quantifies the usefulness of considering the signal issued by an indicator versus disregarding it. In our analysis, the preference parameter takes the values of 0.5 (policymaker has balanced preferences) or 0.7 (policymaker prefers not to miss a crisis). The balanced preferences scenario is the most commonly used in the related literature as it avoids taking any stance about the policymaker's relative risk aversion between the two types of error. However, [Borio and Drehmann \(2009\)](#) and [Betz et al. \(2014\)](#), among others, argue that policymakers may be more averse to missing a crisis, especially after the Global Financial Crisis, since the costs of a crisis are higher than the costs of taking preemptive measures even in the case of a false alarm. The higher is the relative usefulness the better the indicator and, ac-

¹²Type I error is the percentage of vulnerable periods that are not correctly predicted (missed vulnerable periods) and type II error (false vulnerable periods) is the percentage of non-vulnerable periods incorrectly signalled as vulnerable periods.

according to [Lo Duca et al. \(2017\)](#), a good early-warning indicator should present a relative usefulness of at least 0.25.

False negative rate and false positive rate: The false negative rate is the share of missed vulnerable periods (type I error rate) and the false positive rate is the share of false alarms of vulnerable periods (type II error rate). For very low values of the signalling threshold the rate of false negatives will be low while the rate of false positives will be high. The opposite will occur if the signalling threshold is very high. The optimal threshold level was defined as the one that maximizes the relative usefulness for a grid of indicator values and for a specific value of the policymaker preference parameter. The policymaker knows that it's impossible to detect in advance all crisis events but its credibility is also questioned if these two errors are deemed too high. The goal is to strike a balance between the two rates while assuring that their magnitude is acceptable from a policy perspective. Following [Lo Duca et al. \(2017\)](#), we define as acceptable for a good early-warning indicator if type I error and type II error rates are below 0.5 and 0.6, respectively.

$P(Vuln | signal) - P(Vuln)$: Difference between the probability of being in a vulnerable period conditional on a signal issued by the indicator and the unconditional probability of being in a vulnerable period. If the indicator anticipates systemic financial crisis then the conditional probability should be higher than the unconditional probability.

Lead time: Following [Kaminsky et al. \(1998\)](#), the leading time of an indicator is measured as the average number of quarters in which the first signal is issued. While useful for assessing the indicators ability to anticipate crisis, the above metrics are uninformative on how timely are the indicators. As macroprudential policy is seen as the first line of defence against risks to financial stability then a good early-warning indicator should signal a crisis a reasonable number of quarters ahead to allow a timely/promptly deployment of the available instruments to address risks and prevent crisis from occurring.

Persistence: This metric complements the previous one to the extent that measures the persistence of the signals issued by the indicator during the vulnerable period relative to non-vulnerable periods. A value above one means that the signals are more persistent within the vulnerable period than in non-vulnerable periods. This provides information to the policymaker on how well the indicator performs in disentangling vulnerable periods from non-vulnerable periods.

In the analysis, only the systemic financial crises with macroprudential relevance are considered. This set of crisis events is divided in two categories, one that only considers crises with a domestic origin and another one that considers crises with a domestic or foreign origin. In total there are 15 crisis events with a domestic origin and 19 crisis events with a domestic or foreign origin in our sample. These crises are described in detail in [Lo Duca et al. \(2017\)](#) but one feature is their clustering around the Great Financial Crisis.

The AUROC is computed assuming two prediction horizons (vulnerable periods).¹³ The first one considers a 12 to 5 quarters window prior to crisis start and the second one a 20 to 5 quarters window prior to crisis start. These choices are motivated by the fact that there are lags in data availability and in the implementation of some macroprudential tools, e.g the CCyB has a 1 year lag, and by the fact that it is unknown how early should an indicator issue a signal so that macroprudential policy actions can be implemented in time to be effective. Both reasons require the use of an indicator that detects early on in the cycle the emergence of cyclical systemic risk. The remaining metrics introduced above are computed only for the shorter prediction horizon.

Even though the indicators are both computed in real-time, all metrics in the in-sample exercise are computed as if the full sample of information was available to the

¹³Period prior to crisis start within which an indicator is expected to have the ability to signal that a systemic financial crisis is likely to occur in the future. The binary variable associated to the prediction horizon is set to 1 in the quarters within the prediction horizon, to missing for the quarters before a crisis event and for the crisis period to account for post-crisis and crisis bias as proposed by [Bussiere and Fratzscher \(2006\)](#) and to 0 otherwise.

policymaker at the time he has to judge whether a crisis is imminent. Considering that in practice this does not occur and that good in-sample signalling performance does not guarantee a good out-of-sample signalling performance, we also evaluate the signalling performance of each indicator by performing a quasi real-time exercise.¹⁴ Following [Lo Duca et al. \(2017\)](#), all metrics above are computed for each quarter t with all available information up to that point considering a data lag of 3 years.¹⁵ The recursive procedure starts in the first quarter of 2000 and ends in the second quarter of 2017. From a policy perspective, it can be argued that the out-of-sample signalling performance of the indicator should receive more weight on balance as it mimicks a situation more close to that faced by policymakers.

¹⁴Lags in the publication of the indicators are not considered in this exercise.

¹⁵A data lag of 3 years is considered due to choice of using a prediction horizon between 12 and 5 quarters ahead of the crisis (information used to compute the indicators).

Table 3: Results for the in-sample and out-of-sample signalling performance exercises

	<i>Only crises with domestic origin</i>		<i>All crises</i>	
<i>Panel (a): In-sample exercise</i>	Basel gap	CCI	Basel gap	CCI
AUROC: 12 to 5 horizon	0.71	0.72	0.67	0.67
AUROC: 20 to 5 horizon	0.69	0.58	0.68	0.55
Balanced preferences ($\theta = 0.5$)				
Relative usefulness	0.35	0.40	0.27	0.29
False negative rate	0.20	0.32	0.29	0.34
False positive rate	0.45	0.29	0.44	0.37
P(Vuln signal)-P(Vuln)	0.06	0.10	0.06	0.08
Persistence	1.79	2.38	1.61	1.77
Lead time (quarters)	12	10	11	10
Unbalanced preferences ($\theta = 0.7$)				
Relative usefulness	0.08	0.25	0.08	0.14
False negative rate	0.20	0.08	0.00	0.07
False positive rate	0.45	0.57	0.92	0.70
P(Vuln signal)-P(Vuln)	0.06	0.05	0.01	0.03
Persistence	1.79	1.61	1.08	1.33
Lead time (quarters)	12	12	12	12
<i>Panel (b): Out-of-sample exercise</i>	Basel gap	CCI	Basel gap	CCI
AUROC (mean): 12 to 5 horizon	0.72	0.74	0.69	0.65
AUROC (mean): 20 to 5 horizon	0.68	0.55	0.69	0.51
Balanced preferences ($\theta = 0.5$)				
Relative usefulness	0.07	0.37	-0.11	0.22
False negative rate	0.36	0.18	0.46	0.24
False positive rate	0.57	0.46	0.65	0.54
P(Vuln signal)-P(Vuln)	0.02	0.10	-0.03	0.06
Persistence	1.11	1.80	0.83	1.41
Lead time (quarters)	12	11	12	11
Unbalanced preferences ($\theta = 0.7$)				
Relative usefulness	-0.29	0.05	-0.60	0.04
False negative rate	0.28	0.18	0.38	0.09
False positive rate	0.64	0.54	0.70	0.74
P(Vuln signal)-P(Vuln)	0.02	0.07	-0.02	0.04
Persistence	1.13	1.53	0.87	1.23
Lead time (quarters)	12	11	12	12

The results of the early-warning signalling performance exercise are presented in Table 3. Panel (a) displays the evaluation metrics for the in-sample exercise and panel (b) the evaluation metrics for the out-of-sample exercise.

In-sample results

The AUROC values for the two indicators are above 0.5 for the two prediction horizons and sets of crises, meaning that they are both useful in anticipating systemic financial crises. For the prediction horizon of 12 to 5 quarters, the AUROC values are virtually the same across indicators whereas for the prediction horizon of 20 to 5 quarters the Basel gap slightly outperforms our model-based indicator. As such, the signalling properties of the model-based indicator seem to be concentrated in a prediction horizon that is close to the materialization of the crisis but still 3 to 1 years ahead, which is still in our view a reasonable horizon for macroprudential policymakers to take preemptive action. In fact, [Lo Duca et al. \(2017\)](#), among others, focus their univariate early-warning signalling performance exercises in this prediction window. As the CCI is more volatile than the Basel gap due to the fact that the trend of the CCI adjusts more rapidly to recent developments, it is not surprisingly that, when a 20 to 5 quarters prediction horizon is considered, the early-warning properties of the CCI tend to decrease close to a point in which the indicator is no longer informative. When crises with a foreign origin are also considered, the signalling power of both indicators tends to deteriorate, implying that the indicators seem better suited to anticipate systemic financial crises driven by domestic imbalances.

For both indicators, the relative usefulness and the difference between the conditional and unconditional probability of being in a vulnerable period are always positive meaning that they provide additional information to the policymaker's decision process. However, the relative usefulness of the model-based indicator is always higher than that of the Basel gap, especially in the case of unbalanced preferences.

In terms of the false negative rate, it seems that the CCI leads to a slightly higher

share of missed vulnerable periods (at most 32%) than the Basel gap in the case of balanced policymaker preferences. Opposite results are obtained in the case of unbalanced preferences. However, the CCI issues less false alarms than the Basel gap. The exception being the case in which only crises with domestic origin and unbalanced preferences are considered. For most scenarios, the two indicators verify the guiding values put forward by [Lo Duca et al. \(2017\)](#) to deem an indicator as an acceptable early-warning indicator.

Overall in terms of average leading time, the two competing indicators exhibit leading properties regarding crisis as desirable. Under the scenario of balanced preferences of the policymaker, the Basel gap issues the first signal regarding a crisis before the CCI, but we argue that the difference is not substantial. On average and considering the crises with domestic origin, the two indicators issue the first signal around 3 years before crisis start. The average lead time is somehow shorter, between 10 and 11 quarters, for the larger set of systemic financial crisis. Nevertheless, we argue that this difference is not worrisome from a policy perspective to the extent that it does not preclude the implementation of preemptive measures, even though they may have to be implemented at a slightly higher pace. Under the scenario of unbalanced preferences, the indicators show the same average leading time.

In terms of persistence of the signals, the CCI ranks above the Basel gap for the majority of the cases, the exception being the scenario in which only domestic crises and unbalanced policymaker preferences are considered. But even in this case the difference in the metric between indicators is the lowest across all scenarios. Overall, the signals issued by the two indicators are between 1 and 2 times more persistent in periods that precede crisis than in the so-called normal periods.

Out-of-sample results

Overall the signalling properties of the indicators become weaker in a setting that resembles more closely the decision environment faced by policymakers. The deterioration in

the relative usefulness and in the difference between the conditional and unconditional probability of being in a vulnerable period of the Basel gap is evidence that its good in-sample signalling properties seem not hold in a out-of-sample performance exercise. In contrast, the in-sample signalling properties of the model-based indicator seem to be confirmed by the out-of-sample exercise. The performance of the Basel gap in terms of issuing bad signals, either in terms of missing crisis or issuing false alarms, declines. For the CCI the results are less clear-cut but in most cases there is also a deterioration in the share of bad signals issued.

Nonetheless, in terms of the AUROC, most of the conclusions drawn from the in-sample exercise are still valid. The Basel gap seems to marginally outperform the CCI in most scenarios and the AUROC values of both indicators seem to deteriorate when crises with a foreign origin are also considered in the analysis. Also, unchanged in comparison to the in-sample exercise is the fact that the two indicators send the first signal around 3 years before a crisis start, a desirable property from a policymaker perspective if he wants to consider the implementation of preemptive measures. The persistence of the signals issued by the indicators in advance of crises deteriorates only slightly, implying that the indicators are still useful for anticipating crises in a real-time scenario. However, there is an exception. When all crises are considered, the signal persistence of the Basel gap seems to be higher in tranquil periods than in vulnerable periods.

The main conclusion from this analysis is that our proposed model-based indicator ranks very well in comparison with one of the most used univariate early-warning indicator, more so in the most demanding out-of-sample exercise. But the CCI has the advantage of being a small scale multivariate indicator embedding the orthodox view that financial crises result from mutually reinforcing forces that drive the financial sector and the real sector of the economy ([Kindleberger, 2000](#) and [Minsky, 1982](#)). As a result, it allows policymakers to assign an economic interpretation to early-warning signals and build a narrative about the drivers of a systemic financial crisis. Notice that the compar-

ison between the two indicators is extremely fair to the extent that both indicators are computed in real time and their early-warning signaling performance is evaluated both in-sample and out-of-sample, the latter mimicking as close as possible the environment in which policymakers are called to take a decision on deploying policy instruments. We argue that this is not always the case in related literature in which it is not possible to disentangle whether the better properties of an indicator come from the fact that unknown information to the policymaker at the decision time is used in the computation of the indicator. Another take away from this analysis is the fact that the signaling regarding systemic financial crises provided by the CCI occurs in a timely and persistence manner that may allow for preemptive and better informed policy actions.

Panels (a) and (b) of Figures 2 and 3 show the dynamics of the Basel gap and CCI before and after systemic financial crisis events for the two sets of crises considered in this analysis. On average, the Basel gap is positive more than four years prior to the start of a systemic financial crisis and tends to consistently increase until two years prior to the start of a systemic financial crisis. This is particularly true when only crises with a domestic origin are considered. One year ahead of the crisis the gap seems to stabilize and once the crisis event occurs a long deleveraging period takes place lasting on average more than four years. The CCI shows a similar dynamic for the two sets of crises considered. The CCI steeply increases in the 16 to 1 quarter window prior to a systemic financial crisis start, implying that there seems to be information content regarding the signalling of systemic financial crises. After that point, the CCI decreases in line with the adjustment process that usually takes place after a crisis. In contrast with the Basel gap, the CCI returns to positive values more rapidly, a result that mimics the different recovery paces across countries. For both indicators, positive and increasing values are observed during the quarters that precede systemic financial crises, meaning that is the combination of the level with the change in the indicator that provides information about future crisis events. For the vast majority of countries these results hold even

though there is evidence of some cross country heterogeneity.

Overall, both indicators seem useful in identifying periods in which cyclical systemic risk starts to accumulate, providing time to implement preemptive macroprudential measures either to mitigate risk or to increase financial system resilience against shocks. The CCI should be seen as an additional model-based indicator for the assessment of cyclical systemic risk and as such its use for creating a policy stance should be complemented by additional information provided by other indicators of credit cycle. This is in line with the findings of [Galán and Mencia \(2018\)](#) and with the guidance provided by the ESRB Recommendation on setting countercyclical buffer rates.

Figure 2: Distribution around systemic financial crises with domestic origin.

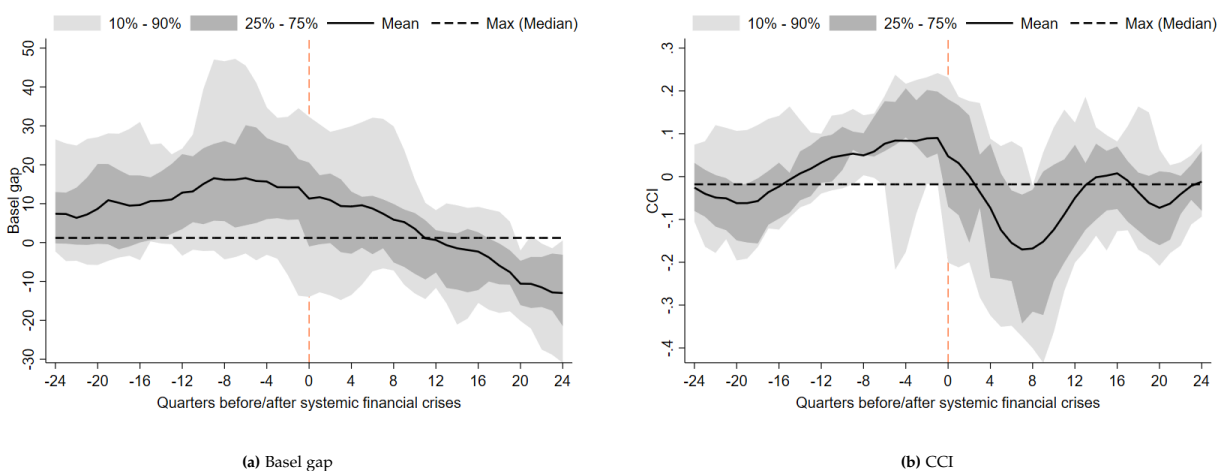
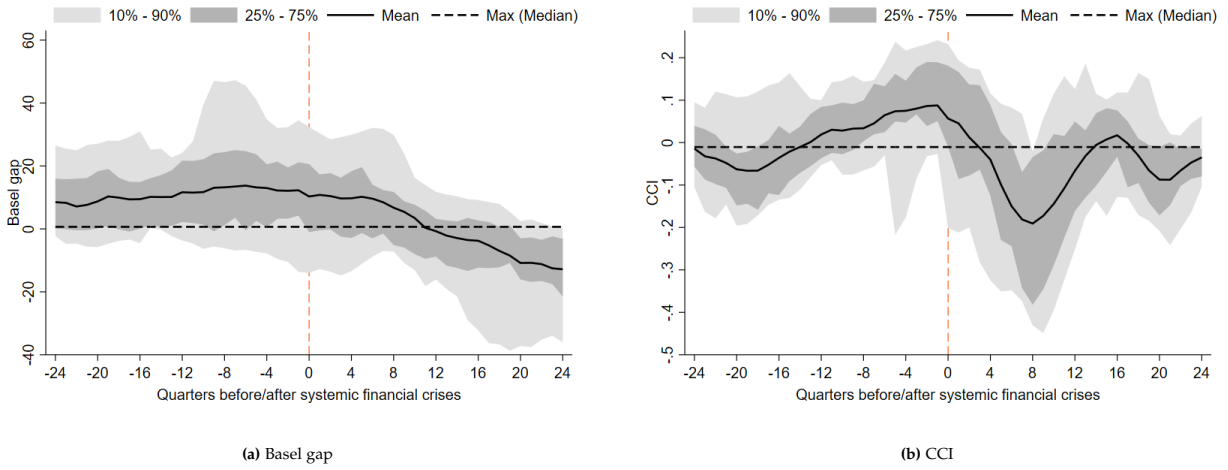


Figure 3: Distribution around systemic financial crises with domestic/foreign origin.



5 Conclusion

For future work we may consider applying this framework separately to household credit and NFC credit.

Appendix

This appendix provides an overview of the models in state space form. Consider the following general state space model consisting of an observation equation and a state equation:

$$Y_t = H\beta_t + AZ_t + e_t,$$

$$\beta_t = \mu + F\beta_{t-1} + v_t,$$

with $e_t \sim N(0, R)$, $v_t \sim N(0, Q)$ and $Cov(e_t, v_t) = 0$. Y_t is a $k_1 \times 1$ vector of observed data, H is a $k_1 \times k_2$ coefficient matrix of the state variables in the observation equation, β_t is a $k_2 \times 1$ vector of state variables, A is a $k_1 \times k_3$ coefficient matrix of the exogenous variables in the observation equation, Z_t is a $k_3 \times 1$ vector of exogenous variables, μ is a $k_2 \times 1$ vector of constants and F is a $k_2 \times k_2$ coefficient matrix of the state equation. The observation error, e_t , and the state error, v_t , are normally distributed with zero mean and covariance matrices R and Q , respectively. In both equations the vector of state variables, β_t , needs to be estimated. In addition, in the observation equation the unknown parameters are the elements of the coefficient matrices H and A and the non-zero elements of matrix R . In the state equation the unknown parameters are the elements of μ , F and Q .

A: State space representations of the models

For the model in equations 4 to 7 with h set to 2 the observation equation has the following matrices:

$$\ln \left(\frac{C_t}{P_t} \right) = \begin{bmatrix} 1 & 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} c_t^M \\ \mu_t^M \\ \nu_t^M \\ c_{t-1}^M \end{bmatrix} + \begin{bmatrix} 1 & -1 & 1 \end{bmatrix} \begin{bmatrix} \ln K_t \\ \ln R_t \\ \ln \left[\mathbb{E}_t \left(\frac{Q_{t+1}}{P_t} \right) \right] \end{bmatrix} + \epsilon_t \quad (12)$$

and the state equation has the following matrices:

$$\begin{bmatrix} c_t^M \\ \mu_t^M \\ \nu_t^M \\ c_{t-1}^M \end{bmatrix} = \begin{bmatrix} \rho_1 & 0 & 0 & \rho_2 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} c_{t-1}^M \\ \mu_{t-1}^M \\ \nu_{t-1}^M \\ c_{t-2}^M \end{bmatrix} + \begin{bmatrix} \varepsilon_t^M \\ \zeta_t^M \\ \zeta_t^M \\ 0 \end{bmatrix} \quad (13)$$

For the model in equation 9 with h^Q set to 2 the observation equation has the following matrices:

$$Q_t = \begin{bmatrix} 1 & 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} c_t^Q \\ \mu_t^Q \\ \nu_t^Q \\ c_{t-1}^Q \end{bmatrix} + \epsilon_t^Q \quad (14)$$

and the state equation has the following matrices:

$$\begin{bmatrix} c_t^Q \\ \mu_t^Q \\ \nu_t^Q \\ c_{t-1}^Q \end{bmatrix} = \begin{bmatrix} \phi_1 & 0 & 0 & \phi_2 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} c_{t-1}^Q \\ \mu_{t-1}^Q \\ \nu_{t-1}^Q \\ c_{t-2}^Q \end{bmatrix} + \begin{bmatrix} \varepsilon_t^Q \\ \zeta_t^Q \\ \zeta_t^Q \\ 0 \end{bmatrix} \quad (15)$$

B: Priors

The conjugate priors distribution for the variance parameters $(\sigma_{\varepsilon^M}^2, \sigma_{\zeta^M}^2, \sigma_{\zeta^M}^2, \sigma_{\varepsilon^Q}^2, \sigma_{\varepsilon^Q}^2, \sigma_{\zeta^Q}^2, \sigma_{\zeta^Q}^2, \sigma_{\varepsilon^Q}^2)$ belong to the inverted gamma distribution family. The random variable X follows an inverted gamma distribution with shape parameter α and scale parameter β , $X \sim IG(\alpha, \beta)$, if:

$$f(x) = \frac{1}{\Gamma(\frac{\alpha}{2})(\frac{2}{\beta})^{\frac{\alpha}{2}}} x^{-\frac{1}{2}(\alpha+2)} e^{-\frac{\beta}{2x}}, \quad x > 0 \quad (16)$$

where $\Gamma(\cdot)$ is the gamma function. The mean (μ) and variance (σ^2) are given by:

$$\mu = \frac{\beta}{\alpha - 2} \quad \alpha > 2, \quad \sigma^2 = \frac{2\mu^2}{\alpha - 4} \quad \alpha > 4 \quad (17)$$

The conjugate priors distribution for the covariance matrices of the state variable innovations (V and R) are inverse Wishart. The random matrix $\mathbf{X}_{p \times p}$ (positive definite) follows an inverse Wishart distribution with scale matrix $\mathbf{\Psi}_{p \times p}$ (positive definite) and degrees of freedom $\vartheta > p - 1$, $\mathbf{X} \sim W^{-1}(\mathbf{\Psi}, \vartheta)$, if:

$$f(\mathbf{x}) = \frac{|\mathbf{\Psi}|^{\frac{\vartheta}{2}}}{2^{\frac{\vartheta p}{2}} \Gamma_p(\frac{\vartheta}{2})} |\mathbf{x}|^{-\frac{(\vartheta+p+1)}{2}} e^{-\frac{1}{2}tr(\mathbf{\Psi}\mathbf{x}^{-1})} \quad (18)$$

where $\Gamma(\cdot)$ is the multivariate gamma function. The mean and variance are given by:

$$\mu = \frac{\mathbf{\Psi}}{\vartheta - p - 1} \quad \vartheta > p + 1 \quad (19)$$

$$Var(x_{ii}) = \frac{2\psi_{ii}^2}{(\vartheta - p - 1)^2(\vartheta - p - 3)} \quad (20)$$

$$Cov(x_{ij}, x_{kl}) = \frac{2\psi_{ij}\psi_{kl} + (\vartheta - p - 1)(\psi_{ik}\psi_{jl} + \psi_{il}\psi_{kj})}{(\vartheta - p)(\vartheta - p - 1)^2(\vartheta - p - 3)} \quad (21)$$

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