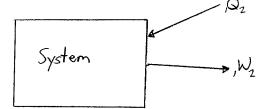
GIVEN: A system of fixed mass at constant pressure and temperature

FIND: Equivalent system form of Eqtn. 2.35 (First Law) which is used to define the heat of reaction.

Assumptions: expansion/contraction of the system boundary is a reversible process, only work done by system is boundary expansion/contraction

APPROACH: Write the first law for the system. Substitute the appropriate expression for constant pressure work and solve for the specific heat transfer.

sketch of system:



first law for a system:

$$_{1}Q_{2} - _{1}W_{2} = m(u_{2} - u_{1})$$

for a system at constant pressure the reversible work can be expressed as

 $_{1}W_{2} = \int PdV = P(V_{2}-V_{1}) = mP(V_{2}-V_{1})$ v = specific

substituting into the first law

$$Q_{2} - mP(v_{2} - v_{1}) = m(u_{2} - u_{1})$$

$$Q_{2} = m[(u_{2} + Pv_{2}) - (u_{1} + Pv_{1})] = m(h_{2} - h_{1})$$

$$Q_{2} = Q_{2}/m = h_{2} - h_{1}$$

if state 1 is the reactants and state 2 is the products then

q=hp-he same form as Egtn 2.35

COMMENTS: Note that the first law for a constant pressure system has

COMMENTS: Note that the first law for a constant pressure system has the same form as for a control volume, This is only true for constant pressure. Also, the internal energies u, and uz are mixture internal energies. Even assuming ideal gas behavior, u, \neq uz at constant temperature if the composition changes. (see Joule's experiment with gases and internal energy)

GIVEN:
$$A/E = h_A/h_E = 18$$
 $T_A = 800 K (preheated)$
 $T_E = 450 K$
 $P = 1atm$
 $h_{f,A} = h_{f,P_F} = 0$

FIND: Tad for P = 1 atm

ASSUMPTIONS: Air = 79%Nz /21% Oz 3 properties as given.

SOLUTION: Write 1st law (mass basis) recognizing that

mp = mp + m=

$$\hat{m}_{A}h_{A}$$
 $\hat{m}_{E}h_{E}$
 $\hat{m}_{E}h_{E}$
 $\hat{m}_{E}h_{E}$
 $\hat{m}_{E}h_{E}$
 $\hat{m}_{E}h_{E}$

mather + mph = (ma+mp) has Divide by mp & substitute properties (hi = 4; +4; (Ti-Tex)):

$$\frac{18\left(1200(800-300)\right) + \left(\frac{1.16\cdot10^{3}}{29} + 3500(450-300)\right)}{= (18+1)\left(1200\left(\frac{1}{400} - 300\right)\right)}$$
Solve for Tad

PROBLEM 2-38 (continued)

$$7.080 \cdot 10^{7} + 4.0525 \cdot 10^{7} = 2.28 \cdot 10^{4} (T_{ad} - 300)$$

$$T_{ad} = 2251 + 300$$

$$T_{ad} = 2551 + 500$$

comments: i) Use of simplified properties focuses attention on energy conservation. ii) The use of a mass-based 1st law simplifies the solution (the = the).

GIVEN: Adiabatic const. - P combustion: (A/F) = 15, J=1, Tref = 300, T= T4 = 600K, simplified properties FIND: a) Tad b) HV@ 600K ASSUMPTIONS: Air is 79% N2, 21% 02 SOLUTION: a) Ho = How or ho = hor Stoichiometry: 12gf + 15 kg4 -> 16 kgpr HR = m_A h_A + m_E h_ = m_A (h_{F,A} + c_{F,A} (TATING)) + M= (1/2 + G) = (TF-Tref)) How = (mA+ME) how = (mA+ME) (how + GIPr (Tad-Tug)) Substitute property values = let m= 1, M= 15: $H_R = 15(0 + 1200(600 - 300)) + 1(2.10^7 + 3500(600 - 300))$ HR = 5.4.106 + 2.105.107 = 2.645.107 J HR = 16 (-1.25.106 + 1500 (Pal-300)) Hp_ = -2.107 + 2.4/04 (Tal-300) Set He=Hpr & Solve for Tal: 2.645,107 = -2.107 + 2.4.104 (Tal-300) Tel = 2235 K

PROBLEM 2-39 (Continued)

b)
$$HV = H_R - H_P$$
, for 1 kg FUEL @ 600K
From part a), $H_R(600) = 2.645 \cdot 10^7 \text{ J}$ (per kg_F) -

 $H_{Pr}(600) = 16 \left(\frac{h_{Pr}^2}{4P_{Pr}} + \frac{h_{Pr}^2}{4P_{Pr}} \left(\frac{1}{4P_{Pr}} - \frac{h_{Pr}^2}{4P_{Pr}} \right) \right)_{T=600}$
 $= 16 \left(-1.25 \cdot 10^6 + 1500 \left(600 - 300 \right) \right)$
 $H_{Pr} = -1.28 \cdot 10^7 \text{ J} \left(\text{per kg}_F \right)$
 $HV = H_R - H_{Pr} = 2.645 \cdot 10^7 - \left(-1.28 \cdot 10^7 \right)$
 $HV = 3.925 \cdot 10^7 \text{ J} \left(\text{per kg}_F \right)$

Comment: This ficticious fuel with simplified properties has a low HV (2 40,000 ki/kg) compared to most real fuels (HV ~ 45,000 kJ/kg, cf. Table 8.1).

GIVEN: Steady-flow reactor with
$$H_2-O_2$$
 @ $D=0.5$, $P=Satm$, $Q/\dot{m}=187$ kJ/kg; zero-K reference state $h_{f,i}^{o}s:h_{f,o}=h_{f,h_2}=0$ $h_{f,i}^{o}s:h_{f,o}=-238,000$ kJ/kmol $h_{f,h_2}^{o}b=-38,600$ kJ/kmol

FIND: a) Mup (W/o dissociation)

- b) Yipr (W/o dissociation)
- c) Tout (w/o dissoc.) for Tin, Hz = 300 K, Tin, oz = 800 K, all Gi = 40 kJ/kmol-K
- d) Ald OH to products & write equations needed to find Tod.

SOLUTION :

a)
$$2H_2 + \frac{1}{2}O_2 \Rightarrow 2H_2O + \times O_2$$

 O -balance; $\frac{2}{2} = 2 + 2x$; $x = \frac{1}{2} - 1 = \frac{1}{2} - 1 = 1$
 $MW_{pr} = \sum N_i MW_i / \sum N_i$
 $= 2(18.016) + 1(31.999) = 22,68 \text{ kg/kmol}$

b)
$$V_{02} = V_{02} \frac{MW_{02}}{MW_{Pr}} = \frac{V_{02}}{N_{Pr}} \frac{MW_{02}}{MW_{Pr}} = \frac{1}{3} \frac{31.999}{22.68}$$

$$= 0.470$$

PROBLEM 2-40 (continued)

c) 1st law:
$$\dot{Q} - \dot{W}^2 = \dot{m} \left(h_{pr} - h_{R} \right)$$
 $\dot{Q}/\dot{m} + h_{R} = h_{pr}$
 $h_{R} = Y_{H_{L}} h_{H_{L}} + Y_{o2} h_{o2}$ or $h_{R} = \frac{h_{L}}{mw_{R}} = \frac{Y_{H_{L}} h_{H_{L}} + Y_{o2} h_{o2}}{Y_{H_{L}} mw_{H_{L}} + Y_{o2} mw_{o2}}$

Reactants
 $H_{Z} = \frac{N}{2} \frac{V}{0.5} + \frac{h}{40(300-0)} = \frac{12,000}{12,000}$
 $0_{Z} = 2 + 0.5 + 0.5(31.949) = 17.008$
 $h_{R} = 0.5(12000) + 0.5(32000) = 22,000$
 $h_{R} = \frac{22,000}{17.0} = 1294$ t_{R}/kg

Products
$$N \propto \overline{h} (= \overline{h} + c_{P}(T-0)) t J/k mol$$

 $H_{2}O$ 2 0.666 (-238,000 + 40 T_{Pr})
 O_{2} 1 0.383 (0 + 40 T_{Pr})

$$h_{Pr} = \frac{2 \chi_{i} h_{i}}{M w_{Pr}} = 0.66 \overline{c} \left(-238,000 + 40 \overline{l}_{Pr}\right) + 33 \overline{d} \left(40 \overline{l}_{Pr}\right)$$

$$\frac{1}{22.68}$$

$$h_{Pr} = -6995.88 + 1.7637 \overline{r}_{Pr} \left(1 = \overline{l} k T/kg\right)$$

$$Returning to 1 to law : Q/m + h_{R} = h_{Pr}$$

$$-187 + 1294 = -6995.88 + 1.7637 \overline{r}_{R}$$

Solving for Tpr:

$$\overline{P}_{L} = 4594 K$$

$$2H_2 + \frac{1}{2}O_2 \rightarrow aH_2O + bO_2 + coH$$

Element conservation: ratio of H-to-Outoms in reactants equals H-to-O ratio in products, i.e.,

i)
$$\frac{\# Hatoms}{\# Oatoms} = \frac{4}{4} = 1 = \frac{2x_{H20} + 1_{OH}}{x_{H20} + 2x_{O2} + x_{OH}}$$

(iii)
$$\frac{\chi_{0H}^{2}(P/p^{0})^{2}}{\chi_{H_{2}O}(P/p^{0})\chi_{0}^{1/2}(P/p^{0})^{1/2}} = \frac{\chi_{0H}}{\chi_{H_{2}O}\chi_{02}^{1/2}}(P/p^{0})^{1/2} = \chi_{p}$$

where
$$K_{p} = \exp(-\Delta G_{+}/R_{u}T)$$

= $\exp\left[-\frac{(2\bar{g}_{0H}(\tau) - \bar{g}_{H_{2}O} - 0.5\bar{g}_{02}(\tau))}{R_{u}T}\right]$

Types. i-ili define the product mixture composition, that it to jobs, & You. Knowing these, the 1st law is formulated as in part c:

iv)
$$\frac{\partial}{\partial m} + h_R = h_R$$

PROBLEM 2-40 (CONTINUES)

The LHS of Egn. is is unchanged from partc. The RHS becomes

$$h_{R} = \frac{\overline{h_{pr}}}{MW_{pr}} = \frac{\chi_{H_{2}0} \overline{h_{H_{2}0}}(T) + \chi_{o_{2}} \overline{h_{o_{2}}(T)} + \chi_{o_{H}} \overline{h_{o_{H}}(T)}}{\chi_{H_{2}0} MW_{H_{2}0} + \chi_{o_{2}} MW_{o_{2}} + \chi_{o_{H}} MW_{o_{H}}}$$

where

$$\bar{h}_{H_2O}(T) = \bar{h}'_{H_2O} + \bar{c}_p(T - \bar{h}_{ef})$$

$$\bar{h}_{OZ}(T) = \bar{h}'_{f,OZ} + \bar{c}_p(T - \bar{h}_{ef})$$

$$\bar{h}_{OH}(T) = \bar{h}'_{f,OH} + \bar{c}_p(T - \bar{h}_{ef})$$

$$\bar{h}_{OH}(T) = \bar{h}'_{f,OH} + \bar{c}_p(T - \bar{h}_{ef})$$

with the above substitutions into Egnir, our egn. set is complete: Egni-ir with unknowns that, to, to, to, to, it.

COMMENTS: Part L shows, in a simple manner, how dissociation of products is coupled to a 1st-law analysis.

GIVEN: The equilibrium reaction $CO_2 \longleftrightarrow CO + \frac{1}{2}O_2$

FIND: Verify that the results of table 2.2 satisfy Eqtns 2.64 and 2.65 for the following conditions: a) $T = 2000 \, K$, $P = 0.1 \, atm$ b) $T = 2500 \, K$, $P = 100 \, atm$ c) $T = 3000 \, K$, $P = 1 \, atm$

ASSUMPTIONS: ideal gas behavior (X; = Pi/P)

APPROACH: Calculate OGT using appendix A and compare with table 2.2. Using OGT, calculate Kp. Compare with the value of Kp calculated using the mole fractions listed in table 2.2.

a) T=2000 K, P=0.1 atm $\Delta G_{r}^{\circ} = \left[\Sigma N_{i} \bar{g}_{f,i}^{\circ} \right]_{p} - \left[\Sigma N_{i} \bar{g}_{f,i}^{\circ} \right]_{R}$

where Ni represents the stoichiometric coefficients of the equilibrium reaction

 $\Delta G_{7}^{\circ} = [Ng_{f}^{\circ}]_{co} + [Ng_{f}^{\circ}]_{o_{z}} - [Ng_{f}^{\circ}]_{co_{z}} = /g_{f_{co}}^{\circ} + \frac{1}{2}g_{f_{o_{z}}} - 1g_{f_{co_{z}}}$ $\Delta G_{7}^{\circ} = 1(-285948) + \frac{1}{2}(0) - 1(-396410) = /10462 \quad \text{KJ} \quad \text{agrees with} \quad \text{table 2.2}$ $K_{p} = \exp\left[-\frac{\Delta G_{r}^{\circ}}{R_{u}T}\right] = \exp\left[\frac{-110462}{(8.315)(2005)}\right] = /.304 \times 10^{-3}$ $K_{p} = \frac{\chi_{co} \chi_{o_{z}}^{\prime 2}}{\chi_{co_{z}}} \left(\frac{P}{P_{o}}\right)^{1/2} = \frac{(0.0315)(0.0158)^{1/2}}{(0.9527)} \left(\frac{0.1 \text{ atm}}{1 \text{ atm}}\right)^{1/2} = /.314 \times 10^{-3}$

2 methods of determining Kp match so the data in table 2.2 satisfy Egtn. 265

b) T = 2500 K, P= latm

 $\Delta G_{r}^{o} = I g_{fco}^{\circ} + \frac{1}{2} g_{foz}^{\circ} - I g_{fcoz}^{\circ} = I(-327245) + \frac{1}{2}(0) - I(-396152) = 68907 \text{ KJ}$ $K_{p} = \exp \left[\frac{-\Delta G_{r}^{\circ}}{R_{u}T} \right] = \exp \left[\frac{-68907}{8.315} (2506) \right] = 0.03634$ $K_{p} = \frac{\chi_{co} \chi_{oz}^{1/2}}{\chi_{coz}} \left(\frac{f}{P_{o}} \right)^{1/2} = \frac{(0.0789)(0.0145)}{(0.9566)} (100)^{1/2} = 0.03638$ (continued)

PROBLEM 2-41 (CONTINUATION)

b (continued):

The value of OGr calculated here matches OGr in table 2.2 so Eqtn. 2.64 is satisfied and the Kp calculated from OGr matches the Kp determined from the mole fractions in table 2.2 so Eqtn. 2.65 is satisfied

c) T= 3000 K, P= 1 atm

$$\Delta G_{\tau}^{\circ} = 19f_{co} + \frac{1}{2}9f_{02} - 19f_{0co_{2}} = 1(-367684) + \frac{1}{2}(0) - 1(-395562) = 27878 \text{ KJ}$$

$$K_{P} = \exp\left[-\frac{\Delta G_{\tau}^{\circ}}{R_{u}T}\right] = \exp\left[-\frac{27878}{(8.315)(3000)}\right] = 0.32707$$

$$K_{P} = \frac{\chi_{co}\chi_{o_{2}}^{\prime/2}}{\chi_{co_{2}}} \left(\frac{P}{P_{o}}\right)^{1/2} = \frac{(0.3581)(0.1790)^{1/2}}{(0.4629)} \left(\frac{1\text{ atm}}{1\text{ atm}}\right)^{1/2} = 0.32730$$

Again, these calculations show that the results in table 2.2 satisfy Egtns. 2.64 and 2.65

GIVEN: A closed vessel containing 1 kmole of Oz when there is no dissociation

FIND: The mole fractions X_0 and X_{02} at the following conditions: a) $T=2500\,\text{K}$, $P=1\,\text{atm}$ b) $T=2500\,\text{K}$, $P=3\,\text{atm}$

Assumptions: Ideal gas, system is in chemical equilibrium

APPROACH: There are two unknowns (χ_0 and χ_{0z}) so 2 equations must be used. The first is the definition of κ_p and the second is $\xi \chi_i = 1$

a) T=2500 K

$$\Delta G_{\tau}^{\circ} = [Ng_{f,\tau}^{\circ}]_{0} - [Ng_{f,\tau}^{\circ}]_{0} = 2(88203) - 0 = 176406 \text{ KJ/Kmole}$$

$$K_{\rho} = \exp\left[\frac{-\Delta G}{R_{u}T}\right] = \exp\left[-\frac{(176406)}{(8.315)(2500)}\right] = 206.3 \times 10^{-6}$$

$$K_p = \frac{\chi_o^2}{\chi_{o_2}} \left(\frac{p_p}{p_o} \right) = 206.3 \times 10^{-6}$$
 FIRST EQUATION

From $\Sigma X_i = 1 = X_0 + X_{02}$ $X_0 = 1 - X_0$ SECOND EQUATION

substituting the second equation into the first and rearranging yields

$$(\frac{P}{P_0})\chi_0^2 + K_p \chi_0 - K_p = 0$$
 quadratic equation

Solving for $X_0 = \frac{-K_p \pm \sqrt{K_p^2 + 4(P/P_0)(K_p)}}{2(P/P_0)}$ Note: Only + yields physically realistic result

 $T=2500K_{p}=1 \text{ atm}: K_{p}=206.3 \times 10^{-6}, P_{p}=1 \longrightarrow X_{o}=0.0143, X_{oz}=1-X_{o}=0.9857$ $T=2500K_{p}=3 \text{ atm}: K_{p}=206.3 \times 10^{-6}, P_{p}=3 \longrightarrow X_{o}=0.00826, X_{oz}=1-X_{o}=0.9917$

COMMENTS: Note how this system follows the principle of Le Châtelier. Increasing the system pressure causes the system to shift towards more Oz, thereby reducing the number of moles in the system (NotNoz)

GIVEN: The equilibrium reaction $O_2 \leftrightarrow 20$ in a closed vessel containing I kmole of inert diluent and I kmole of O_2 with no dissociation

FIND: The mole fractions Xo and Xoz. Compare these results with those found in problem 2-22. Discuss.

Assumptions: ideal gas behavior system is in chemical equilibrium, mert . diluent (Ar) does not play a role in the equilibrium reaction

APPROACH: Calculate OG and Kp. Using the definition of Kp and conservation of elements, solve for the two unknowns Xo and Xoz

conservation of elements:
$$O_z$$
 O Ar

Initial I O I

equilibrium shift $-Z$ $+ZZ$ O

final state $I-Z$ ZZ $I \leftarrow \#OF MOLES$

mole fractions:
$$\chi_{0z} = \frac{Noz}{N_{TOT}} = \frac{1-2}{2+2}$$
, $\chi_{c} = \frac{N_{o}}{N_{TOT}} = \frac{22}{2+2}$

at T = 2500 K: Note: Ar is not part of the equilibrium reaction $\Delta G_{\tau}^{\circ} = \left[Ng_{\tau}^{\circ}\right]_{0} - \left[Ng_{\tau}^{\circ}\right]_{0_{2}} = 2\left[88203\right]_{0} - 1\left[0\right] = 176406 \text{ KT/kmde}$ $K_{p} = \exp\left[-\frac{\Delta G_{\tau}^{\circ}}{R_{u}T}\right] = \exp\left[-\frac{176406}{(8.315)(2500)}\right] = 206.3 \times 10^{-6}$ $K = X_{0}^{2} \left(P\right) = 206.3 \times 10^{-6}$

$$K_{p} = \frac{\chi_{o}^{2}}{\chi_{o_{2}}} \left(\frac{P}{P_{o}}\right) = 206.3 \times 10^{-6}$$

substituting f χ_{o} and $\chi_{o_{z}}$ in terms of z

$$K_{P} = \frac{\left[2^{\frac{1}{2}/(2+\frac{1}{2})}\right]^{2}}{\left[(1-\frac{1}{2})/2+\frac{1}{2}\right]} = 206.6 \times 10^{-6} \text{ for } P = P_{0} = 1 \text{ atm}$$

$$(4+ K_p) Z^2 + K_p Z - 2K_p = 0 \longrightarrow Z = \frac{-K_p \pm \sqrt{k_p^2 - 4(4+K_p)(-2K_p)}}{2(4+K_p)}$$
for physically realistic results
$$Z = -\frac{K_p + \sqrt{k_p^2 - 4(4+K_p)(-2K_p)}}{2(4+K_p)}$$
(continued)

PROBLEM 2-43 (continued)

Solving for
$$\frac{7}{2}$$
: $\frac{7}{2} = 0.0101$

$$\chi_{02} = \frac{1-7}{2+7} = \frac{1-0.0101}{2+0.0101} = 0.492$$

$$\chi_{0} = \frac{27}{2+7} = \frac{2(0.0101)}{2+0.0101} = 0.01$$

$$\chi_{AC} = \frac{1}{2+7} = \frac{1}{2+0.0101} = 0.4974$$

$$\chi_{o_2} = 0.492$$
 $\chi_{o} = 0.01$
 $\chi_{Ar} = 0.4974$

To compare the results of problem 2-22 with the above results, we must look at number of moles instead of mole fractions since there is argon present in this problem (i.e., even with no dissociation of Oz to form O, the mole fractions would be different despite the fact that there would be I kmole of Oz present in both problems)

Problem 2-22

O: $N_0 = \chi_0 N_{TOT} = 0.014$ O₂: $N_{02} = \chi_{02} N_{TOT} = 0.9926$

Problem 2-23

$$N_o = \chi_o N_{tor} = \chi_o (2+2) = 0.01(2.01) = 0.02$$

 $N_{02} = \chi_{02} (2+2) = 0.492(2.01) = 0.989$

COMMENTS: Note that the diluent does not affect ΔGr or the formulation of K_p in terms of nole fractions since it does not participate in the equilibrium reaction. The diluent does, however, affect the system by altering how the mole fractions are defined. For example, the total number of noles in problem 2-22 could be written as 1+2 while in this problem $N_{TOT} = 2+2$ due to the diluent. This result is consistent with Le Châtelier's principle in that teducing the partial pressures (with the diluent) tesults in more dissociation.

GIVEN: At P = 10 ofm, T = 3000K:

Tron = 0.6783, Tro = 0.2144, To= 0.1072

FIND: Kp for CO2 = CO + 1/2 O2

ASSUMPTIONS: ideal gas mixture

SOLUTION: This is astraightforward application of the definition of to (Egn. 2.65):

$$K_{p} = \frac{\left(P_{co}/p^{o}\right)\left(P_{62}/p^{o}\right)^{1/2}}{\left(P_{co2}/p^{o}\right)} = \frac{\gamma_{co}\gamma_{o2}}{\gamma_{co2}}\left(P/p^{o}\right)^{1/2}$$

$$\sqrt{p} = \frac{0.2144 (0.1072)^{1/2}}{0.6783} \left(\frac{10}{1}\right)^{1/2} = 0.1635 (3.1623)$$

 $K_{p} = 0.3273$

(OMMENT: Note the influence of the total pressure on the result. Note also that, since the temperature in given, we could have calculated kp from exp(-16-1/2, a more complicated approach. From Appendix A Tables 1, 2, & 11: 16300 = -367,685+1/20)-(-395,562) = 27,877 RI/Rmol; Kp = exp(-27877/8.315(3000)) = 0.327, The same result as above.

GIVEN: At P=0.8 atm, H_2O , H_2 , O_2 mixture has the composition: $\chi_{H_2O}=0.9$, $\chi_{H_2}=0.03$, ξ $\chi_{O_2}=0.07$.

FIND: for HOZH+LOZ

ASSUMPTIONS: ideal gas mixture

SOLUTION: This is a straightforward application of the definition of to (Egn. 2,65):

$$K_{p} = \frac{(P_{H_{2}}/P^{\circ})(P_{02}/P^{\circ})}{(P_{H_{2}})(P^{\circ})} = \frac{\gamma_{H_{2}}}{\gamma_{H_{2}}} \frac{\gamma_{02}}{\gamma_{H_{2}}} (P/P^{\circ})^{1/2}$$

$$= \frac{0.03(0.07)^{1/2}}{0.9} \left(\frac{0.8}{1}\right)^{1/2} = 0.008819(0.8944)$$

$$K_p = 0.00789$$

Comment: Note how the total pressure enters into this calculation.

GIVEN: Water-gas shift reaction @ T & enthalpies-offormation at T:

$$\frac{h}{h}$$
 $\frac{h}{f}$
 $\frac{h$

FIND: a) Effect of 7 on equilibrium?

ASSOMPTIONS; ideal gas behavior

SOLUTION: a)
$$K_{p}(T) = \frac{\gamma_{(0_{2}} \gamma_{Hz})}{\gamma_{Hz} \gamma_{(0)}} (P/p)^{1+1-1-1}$$

The net exponent of P/p° is zero. There is no effect of P.

5)
$$\Delta H_R = h_{5,002}^2 + h_{5,00}^2 - h_{5,00}^2 - h_{5,00}^2$$

 $= -396,600 + 0 - (-251,700) - (-118,700)$
 $\Delta H_R = -26,200 \implies exothermic © T$
1. Chafolier's law that radicates that the

Le Chatelier's law thus indirates that the teaction will shift to the reactants side with increasing T: 420+ CO = CO2 + HZ

comment: This problem demonstates the application of Lechatelier's Principle.

GIVEN: The reaction $H_2 + \frac{1}{2}O_2 \longrightarrow H_2O$ and and a ratio of moles of elemental H to elemental O equal to one

FIND: The equilibrium composition at T=2000 K and P=1 atm

ASSUMPTIONS: The above reaction is the only reaction involving H #0

APPROACH: Evaluate $\&G_7^2$, determine K_p , and using the definition of K_p and conservation of elements, determine X_{H_2} X_{O_2} $\notin X_{H_2O}$

Evaluation of OGT = 1(9f,T)40 - 1(9f,T)4 - 2(9f,T)0

Using Appendix A $\Delta G_{2000} = 1(-135643) - 1(0) - \frac{1}{2}(0) = -135643$ KT/Kmol

 $K_p = \exp\left[-\frac{667}{RT}\right] = \exp\left[\frac{135643}{(8.315)(2000)}\right] = 3.486 \times 10^3$

In terms of χ_i : $K_P = \frac{\chi_{H_2O}}{\chi_{II} \chi_n^{1/2}} \left(\frac{P}{P_o}\right)^{-\frac{1}{2}}$

Conservation of elements:

$$\frac{\#H}{\#O} = 1 = \frac{2\chi_{H_2O} + 2\chi_{H_2}}{\chi_{H_2O} + 2\chi_{O_2}} \tag{2}$$

and by definition: $\Sigma X_i = 1 = X_{H_2O} + X_{H_2} + X_{O_2}$ (3)

Solving (2) and (3) for $X_{H_2} \neq X_{H_20}$ in terms of X_{02} and substituting into (1):

 $\chi_{H_2} = 3\chi_{o_2-1}$ $\chi_{H_0} = \frac{2 - 4\chi_{o_1}}{3\chi_{o_1-1}(\chi_{o_1})^{1/2}} \left(\frac{P}{P_o}\right)^{-1/2}$ X40= 2-4 X0-

Solving for X_{o_z} by trial #error : $X_{o_z} = 0.3334$ with $P = P_o = 1$ atm $X_{H_2} = 3X_{o_z} - 1 = 0.0003$ $X_{H_2} = 2 - 4X_{o_z} = 0.6662$

Comments :

GIVEN: Equilibrium: 420 = 42+202 @ 2000 K, 12tm FIND: 142, 162, 1420 when #H-atoms is 0.5, 1, = 2

ASSUMPTIONS ; ideal gas behavior

SOLUTION: Apply element conscivation:

$$\#H\text{-atoms} = \frac{2\chi_{420} + 2\chi_{42}}{2\chi_{02} + \chi_{420}}$$

Rearranging,

Z(2/02+ 1/420) - 2/420-2/42, or

Apply equilibrium:

iii)
$$\frac{\chi_{H_2}}{\chi_{H_2}} \frac{\chi_{h_2}}{\chi_{H_2}} \left(\frac{P}{P^0}\right) = \chi_P = \exp\left(-\frac{\Delta G_P^o}{R_u T}\right)$$

Use i) & ii) to eliminate 1/4 & express 1/40 = f(The):

Similarly, use is siis to express the as function of Thos;

Now substitute iv) & o) into iii):

PROBLEM 2-48 (continued)

$$\frac{(Z-2)(P)^{\frac{1}{2}}\sqrt{\frac{1}{2}}}{(Po)^{\frac{1}{2}}\sqrt{\frac{1}{2}}} + \frac{(Z+2)(P)^{\frac{1}{2}}\sqrt{\frac{3}{2}}}{(Z-2)(Po)^{\frac{1}{2}}\sqrt{\frac{3}{2}}} + \frac{2(Z+1)(F)}{(Z-1)(F)}\sqrt{\frac{1}{2}}$$

$$-\frac{2K_{P}}{Z} = 0 = f(O_{2}) \quad \text{vi}$$
To solve the above transcendental egn. for $\chi_{O_{2}}$, we apply the Newton-Raphson iteration method;

vii)
$$\gamma_{o_2}^{\text{new}} = \gamma_{o_2}^{\text{old}} - \frac{f(\gamma_{o_2}^{\text{old}})}{f'(\gamma_{o_2}^{\text{old}})}$$

where The derivative f' (= 4/d1/02) is

viii)
$$f'(\chi_{02}) = \frac{1}{2} \left(\frac{2-2}{2} \sqrt{\frac{p}{p_0}}\right)^{\frac{1}{2}} \chi_{02}^{-\frac{1}{2}} + \frac{3}{2} \left(\frac{2+2}{2} \sqrt{\frac{p}{p_0}}\right)^{\frac{1}{2}} \chi_{02}^{\frac{1}{2}} + \frac{3}{2} \left(\frac{2+2}{2} \sqrt{\frac{p}{p_0}}\right)^{\frac{1}{2}} \chi_{02}^{\frac{1}{2}} + \frac{3}{2} \left(\frac{2+2}{2} \sqrt{\frac{p}{p_0}}\right)^{\frac{1}{2}} \chi_{02}^{\frac{1}{2}} + \frac{3}{2} \left(\frac{2+2}{2} \sqrt{\frac{p}{p_0}}\right)^{\frac{1}{2}} \chi_{02}^{\frac{1}{2}}$$

We evalute $\Delta G_{\tau}^{\circ} = \left[\tilde{g}_{f, k_{2}}^{\circ} + \frac{1}{2} \tilde{f}_{f, \alpha_{2}}^{\circ} - \tilde{g}_{f, k_{2}}^{\circ} \right]_{\tau = 2000}$

 $= 0 + \frac{1}{2}(0) - (-135,643) = + 135,643 \text{ kT/kmol}$ $Kp = exp \left[-\frac{\Delta G_7^{\circ}}{R.T} \right] = exp \left[-\frac{135,643}{8.315(2000)} \right]$

Kp = 2.86857.10-4

Egn Dii) was applied iteratively in a spread sheet to obtain the following results:

PROBLEM 2-48 (continued)

~	Yoz	X42	1420
0.5	0.6000	0,000148	0,39982
1,0	0.3334	0.00033	6.6662
2,0	0.00273	0.00545	0.99182

Comment: As the #H-atoms to #O-atoms
micreases, both the and the increase.

For 2 = 2, the is really unity, i.e.,
nearly all of the # and O atoms, in a
2:1 ratio, are contained in the water.

GIVEN; Equil. react $H_2O \rightleftharpoons H_2 + \frac{1}{2}O_2 \oslash T = 2000 K$ $\frac{f_{mol}(H)}{f_{mol}(O)} = 2 (=2)$

FIND: 142, Noz, 1/20 for a) P=0. Tatm, b) P=1atm, c) P=2atm

ASSUMPTIONS; iteal gas behavior

SOLUTION: The spradsheet developed in problem 2-48 is used here who any changes other than, now, P is railed, while Z is fixed.

Palm	Toz	7/12	1/20
0,5	0,00343	0,00686	6.9897 /
1,0	0,00273	0.00545	0,99182
2,0	0.00217	0,00433	0.99350

Comments: As expected, the dissociation of H2O decreases as the pressure moreages. At 2000K, we expect that other dissociation species should be included in the analysis, in particular, OH, O, and H.

GIVEN: The species H2, O2, OH, O, H and H20

FIND: The solution formulation, indicating the number of unknowns and the equations that will be used to find the unknowns.

ASSUMPTIONS: Ideal gas behavior, system in chemical equilibrium

APPROACH: There are 6 species and consequently 6 unknowns. Therefore there must be 6 equations to find a solution. One equation comes from conservation of elements, one from EX:=1, and the other four from the definition of equilibrium constants Kp

conservation of elements:
$$\frac{\# H \text{ atoms}}{\# O \text{ atoms}} = \frac{2\chi_{H2} + \chi_{OH} + \chi_{H} + 2\chi_{H2O}}{2\chi_{O2} + \chi_{OH} + \chi_{o} + \chi_{H2O}} = 70$$

Summation of
$$X_i$$
: $\Sigma X_i = X_{H_Z} + X_{O_Z} + X_{O_H} + X_{O_H} + X_{H_Z} = 1$ (2)

equilibrium reactions:

$$H_2 + \frac{1}{2}O_2 \longleftrightarrow H_2O \qquad K_{PH_2O} = \exp\left[-\frac{\triangle G_1^o}{R_u T}\right]_{H_2O} = \frac{\chi_{H_2O}}{\chi_{H_2} \chi_{O_2}^{1/2}} \left(\frac{P}{P_o}\right)^{-1/2}$$
3

$$H_Z \iff 2H$$
 $\left(K_P\right)_H = exp\left[-\frac{\Delta G\hat{\tau}}{R_u T}\right]_H = \frac{\chi_H^2}{\chi_{H_Z}}\left(\frac{P}{P_e}\right)$ (4)

$$O_2 \leftrightarrow 20$$
 $(K_P)_o = \exp\left[-\frac{\Delta G_r^o}{R_u T}\right]_o = \frac{\chi_o^2}{\chi_{o_2}} \left(\frac{P}{P_o}\right)$

$$H+O \longleftrightarrow OH$$
 $(K_P)_{OH} = exp\left[-\frac{\Delta G_T^o}{R_u T}\right]_{OH} = \frac{X_{OH}}{X_H X_o} \left(\frac{P}{P_o}\right)^{-1}$

Equations 1-6 can be solved to find the six unknowns:

COMMENTS: Note that other equilibrium reactions involving the species of interest could have been chosen for equations 3-6. For example, the equilibrium reactions $OH+H \iff H_ZO$ or $\frac{1}{2}H_Z+OH \iff H_ZO$ would have been equally valid choices.

GIVEN: An H-O system containing one mole each of elemental hydrogen and oxygen at a temperature of 2000 K and pressure of 1 atm

FIND: The complete equilibrium of the system

APPROACH: Using STANJAN with the appropriate inputs

Computed properties

Independent atom H O	population 1.00000000E+00 1.00000000E+00	element potential -13.7382 -14.9286		
Products at	T = 2000.00 K	P = 1.000E+00	atmospheres	
species	mol fraction in the phase	mol fraction in mixture	mass fraction in mixture	mols*
phase 1: me	olal mass = 22.63	35 kg/kmol		
H	.29482E-04	.29482E-04	.13129E-05	2.21525E-05
HO	.58544E-02	.58544E-02	.43988E-02	4.39892E-03
H2	.33139E-03	.33139E-03	.29515E-04	2.48999E-04
H20	.66217E+00	.66217E+00	.52704E+00	4.97540E-01
0	.38202E-03	.38202E-03	.27003E-03	2.87042E-04
02	.33124E+00	.33124E+00	.46826E+00	2.48887E-01

^{*} Species mols for the atom populations in mols.

```
Mixture properties: molal mass = 22.635 kg/kmol

T = 2000.00 K P = 1.0133E+05 Pa V = 7.2503E+00 m**3/kg

U =-4.7862E+06 J/kg H =-4.0516E+06 J/kg S = 1.1988E+04 J/kg-K

Made 0 (T,P) iterations; 4 equilibrium iterations; v 3.95 IBM-PC
```

COMMENTS: Compare these results with those obtained in problem 2-24 to see the effects of incorporating the additional species H, O, and OH.

GIVEN: propane-air combastion products at 1 atm

FIND! The approximate mole fractions of COZ, CO3 HZO, Hz, H, OH, OZ, O, NZ, NO md N for the following conditions. List The species from highest to lowest mole fraction.

b) \$ = 0.8 , T = Tad

FISSUMPTIONS: The products are in chemical equilibrium

AMROACH: Use HPFLAME rode with Heartants = -103,847 EJ/kmole-fael

5060770N: ·\$=0,8 Td = d=1,2, Ted= K K species 1 Species $\frac{\mathcal{N}}{\mathcal{N}}$ No \mathcal{N}_{2} 0.737 0,69 40 120 0.155 0.152 0.079 002 0.094 (02 0.054 02 0,038 60 H2 OH 0,020 NO 3500 ppm 860 ppm OH 1800 ppm CO 890 ppm Hz 250 ppm Minor species 800 ppm 1-1 ND. 240 ppm 02 250 ppm ppm. 20 ppm 0 176 ppm 1 ppb W 34 ppm 0.14 ppb

COMMENT; Note the relatively large concentration of CO for $\phi = 1.2$ and NO for $\phi = 0.8$.

Problem Title: PROBLEM 2-5% PART A

Data below are as read from the input file. Compare with INPUT.HP. If they do not agree, your input data have not been entered correctly.

CARBON ATOMS	3.0
HYDROGEN ATOMS	8.0
OXYGEN ATOMS	0.0
NITROGEN ATOMS	0.0
EQUIVALENCE RATIO	0.800
TEMPERATURE (K) guess	2000.0
PRESSURE (Pa)	101325.0
ENTHALPY OF REACTANTS (kJ/kmol fuel)	-103847.0

FLAME TEMP. & COMBUSTION PRODUCTS PROPERTIES

Flame Temperature [K] =	2042.03
Mixture Enthalpy [J/kg] =	-0.1151E+06
Mixture Specific Heat, Cp [J/kg-K] =	0.160011E+04
Specific Heat Ratio, Cp/Cv =	1.2282
Mixture Molecular Weight [kg/kmol] =	28.3900
Moles of Fuel per Mole of Products =	0.03146029

The mole fractions of the product species are:

H:	0.00003419	0:	0.00017639	N:	0.00000000
H2:	0.00025351	OH:	0.00180270	co:	0.00088887
NO:	0.00372180	02:	0.03750533	H20:	0.12466922
CO2 ·	0.09349201	N2:	0.73745598		

Problem Title: PROBLEM 2-5% PART B

Data below are as read from the input file. Compare with INPUT.HP. If they do not agree, your input data have not been entered correctly.

CARBON ATOMS	3.0
HYDROGEN ATOMS	8.0
OXYGEN ATOMS	0.0
NITROGEN ATOMS	0.0
EQUIVALENCE RATIO	1.200
TEMPERATURE (K) guess	2000.0
PRESSURE (Pa)	101325.0
ENTHALPY OF REACTANTS (kJ/kmol fuel)	-103847.0

FLAME TEMP. & COMBUSTION PRODUCTS PROPERTIES

Flame Temperature [K] =	2201.09
Mixture Enthalpy [J/kg] =	-0.1685E+06
Mixture Specific Heat, Cp [J/kg-K] =	0.166262E+04
Specific Heat Ratio, Cp/Cv =	1.2304
Mixture Molecular Weight [kg/kmol] =	27.1613
Moles of Fuel per Mole of Products =	0.04407123

The mole fractions of the product species are:

H:	0.00080465	0:	0.00002376	N:	0.00000001
H2:	0.02031565	OH:	0.00085746	co:	0.05358114
NO:	0.00024014	02:	0.00007722	H20:	0.15513821
CO2 ·	0 07863255	мэ.	0 69032921		

PROBLEM 2.53						
	PHI = 0.75	PHI = 0.75	PHI = 0.75	PHI = 1.0	PHI = 1.0	PHI = 1.0
C10H22	P = 1 atm	P = 10 atm	P = 100 atm	P = 1 atm	P = 10 atm	P = 100 atm
T. 1 (1/2)	1973.2	1978.5	1980.8	2276.6	2330.1	2365.6
Tad (K)	-8.38E+04	-8.38E+04	-8.38E+04	-1.10E+05	-1.10E+05	-1.10E+05
h (J/kg)	1514	1462	1441	2287	1941	1728
Cp (J/kg-K)	1.239	1.248	1.252	1.163	1.188	1.210
Cp/Cv	28.67	28.68	28.69	28.37	28.48	28.55
MWmix	0.00962	0.00962	0.00963	0.01248	0.01253	0.01257
NF/Nprod mix	1.43E-05	2.70E-06	4.93E-07	4.69E-04	1.49E-04	4.14E-05
ХН	1.43E-05 1.18E-04	3.89E-05	1.25E-05	3.42E-04	1.11E-04	3.08E-05
X O		1.80E-10	5.87E-11	2.57E-08	1.46E-08	6.70E-09
X N	5.25E-10 1.13E-04	3.73E-05	1.20E-05	3.02E-03	1.75E-03	9.52E-04
X H2		7.28E-04	4.15E-04	0.00320	0.00193	0.00105
X OH	1.26E-03	1.51E-04	4.88E-05	0.01380	0.00850	0.00481
X CO	4.55E-04		3.59E-03	0.00263	0.00222	0.00171
X NO	3.51E-03	3.56E-03	0.04786	0.00203	0.00222	0.00171
X 02	0.04787	0.04784	0.1057	0.00034	0.1351	0.1367
X H2O	0.1051	0.1055		0.1323	0.1331	0.1209
X CO2	0.0958	0.0961	0.0962	0.7267	0.7298	0.7319
X N2	0.7458	0.7461	0.7462	0.7267	0.7236	0.7319
	PHI = 1.25	PHI = 1.25	PHI = 1.25			
C10H22	P = 1 atm	P = 10 atm	P = 100 atm			
Tad (K)	2179.0	2186.2	2188.5			
h (J/kg)	-1.35E+05	-1.35E+05	-1.35E+05			
Cp (J/kg-K)	1604	1525				
Cp/Cv	1.238	1.251	1.255			
MWmix	27.26	27.28	27.28			
NF/Nprod mix	0.0148	0.0148	0.0148			
X H	7.60E-04	2.50E-04				
XO	1.40E-05	1.54E-06				
XN	8.01E-09	2.77E-09				
X H2	0.02331	0.02326				
X OH	6.09E-04	2.04E-04				
X CO	0.06847	0.06844				
X NO	1.54E-04	5.23E-05				
X 02	3.54E-05	3.93E-06				
7 92	0.0 .2 00	0.00= 00				

COMMENTS:

X H2O

X CO2

X N2

1. At lean, stoiciometric, & rich conditions, the effect of increasing P is to suppress dissociation and, as a result, flame temperatures increse slightly. This effect on Tad is greatest at phi = 1, where temperatures are highest. We note that pressure has a negligible influence on the major species [CO2, H2O, N2, O2 (lean), and H2 (rich)], while the minor species mole fractions decrease greatly with pressure.

0.1385

0.0793

0.6888

0.1391

0.0794

0.6893

0.1393

0.0794

0.6894

2. The most significant effect of equivalence ratio is the lower flame temperatures at rich & lean conditions. The CO2 mole fraction exhibits the same behavior as Tad, while the H2O mole fraction falls at lean conditions only, & shows a small increase at the rich condition. For the lean condition, H2 & CO are minor species & O2 a major species; at the rich condition, O2 is a minor species & H2 & CO are major species.

GIVEN: The products of decane (C10Hzz)-air combustion at an equivalence ratio of 1.25

FIND: The mixture composition

Assumptions: ideal gas behavior, only dissociation is the water-gas equilibrium shift, Kp is not a strong function of temperature in temperature range of interest

APPROACH: write the overall combustion equation, determine the A/F ratio, and solve for the species concentrations using conservation of elements and the equilibrium water-gas shift CO+H2O CO2+H2

combustion equation: $C_X H_Y + aO_2 + 3.76aN_2 \rightarrow bCO_2 + CCO + dH_2O + eH_2 + fO_2 + 3.76aN_2$ $a = \frac{X + \frac{Y}{4}}{a} = \frac{10 + \frac{22}{4}}{a} = 17.4$

 $a = \frac{x + \frac{y}{4}}{\phi} = \frac{10 + \frac{22}{4}}{1.25} = 12.4$

Conservation of: b= will solve for using water-gas shift Kp

c c = x-bd = 2a-2b-c = 2a-b-x

H $e = \frac{1}{2} - d = \frac{1}{2} - \frac{1}{2} + \frac{1}{2} + \frac{1}{2}$

F = 0 since combustion is fuel-rich

looking at water-gas equilibrium: CO + H2O ↔ CO2 + H2

$$K_{p} = \frac{\chi_{co_{2}} \chi_{H_{2}}}{\chi_{co} \chi_{H_{2}o}} = \frac{b \cdot e}{c \cdot d} \cdot \left(\frac{1/N_{TOT}}{1/N_{TOT}}\right)^{2} = \frac{b \cdot e}{c \cdot d}$$

$$K_{p} = \frac{b(\frac{1}{2}-a+b+x)}{(x-b)(2a-b-x)}$$

rearranging: $(1-K_p)b^2 + (\frac{1}{2}-2a+2aK_p+x)b + (x^2K_p-2axK_p) = 0$

solving this quadratic equation for b:

$$b = \frac{(2a(K_{p}-1) + \chi + \frac{1}{2}) \pm \sqrt{[2a(K_{p}-1) + \chi + \frac{1}{2}]^{2} - 4(K_{p}-1)K_{p}(2ax-x^{2})}}{2(K_{p}-1)}$$

where only the negative root yields a physically realistic value of b (ie b must be positive)

(continued)

PROBLEM 2-54 (continued)

the preceding equation can be solved by substituting for a, x, y and K_P (which must still be determined

guessing an approximate flame temperature of 2200 K and assuming that Kp doesn't vary much over a few hundred degrees K

at 2200 K=

$$K_p = \exp\left[-\frac{66}{R_nT}\right] = \exp\left[-\frac{30760}{(8.315)(2700)}\right] = 0.19125$$

$$C = \mathcal{K} - b = 10 - 5.361 = 4.638$$

$$d = 2a - b - x = 2(12.4) - 5.361 - 10 = 9.439$$

$$e = \frac{y}{2} - 2a + b + \chi = 11 - 2(12.4) + 5.361 + 10 = 1.561$$

Species	#Moles	X
COZ	5.36	0.079
co	4.64	0.069
H20	9.44	0.140
H2	1.56	0.023
Nz	46.62	0.690
	67.62	1.0

Check:
$$K_p = \frac{\chi_{co}\chi_{H_2}}{\chi_{co}\chi_{H_2o}} = \frac{(0.0793)(0.0231)}{(0.0686)(0.1398)}$$
 $K_p = 0.191$

COMMENTS: From this problem we see that dissociation plays an important role in determining the combustion products, and therefore, adiabatic flame temperature in a fuel-rich process. Compare these results to problems 2-19 and Z-20 where only slight dissociation decreased the adiabatic flame temperature by approximately 130 K.

GIVEN: A natural gas-fired industrial boiler operates with excess air such that the Oz concentration in the flue gases is 2% (vol) after removal of the moisture in the combustion products. The flue gas temperature without air preheat is 700 K.

FIND: a) equivalence ratio of system assuming natural gas is CH4

b) thermal efficiency of the boiler if air and fuel enter at 298 K (no air preheat)

c) With air preheat, the flue gases exit the preheater at 433 K. Determine the thermal efficiency if fuel enters at 298 K and air enters the preheater at 298 K

d) assuming premixed burner operation, estimate the maximum temperature in the combustion space with air prehent (P=1atm)

ASSUMPTIONS: no product dissociation, all energy lost by flue gases in preheater is transfered to air entering boiler, SKE FOPE are neglibible, steady-state

APPROACH: Determine the A/F ratio from element conservation then use conservation of energy to determine the boiler efficiency

a) combustion equation: CHy + aO2 + 3.76aN2 - CO2 + 2H2O + bO2 + 3.76aN2

in products:
$$\chi_{o_2} = 0.02 = \frac{N_{o_2}}{N_{o_2} + N_{H_0} + N_{o_2} + N_{N_2}} = \frac{b}{1 + b + 3.76a}$$

0 atom conservation:
$$b = \alpha - 1 - 1 = \alpha - 2$$

$$CO_2 H_{20}$$

note that the water is still included in the O-atom conservation even though it is not included in the measured Oz mole fraction

substituting b= a-2 into the definition of the Oz mole fraction

$$\chi_{0z} = \frac{\alpha - 2}{1 + (\alpha - 2) + 3.76\alpha} = \frac{\alpha - 2}{4.76\alpha - 1} = 0.02$$

$$\alpha = 2.19 \longrightarrow \alpha = \frac{\chi + \frac{\gamma}{4}}{\phi} \qquad \chi = 1, \ \gamma = 4$$

$$b = \alpha - 2 = 0.19$$

$$A/F)_{molar} = 4.76\alpha = 10.42$$

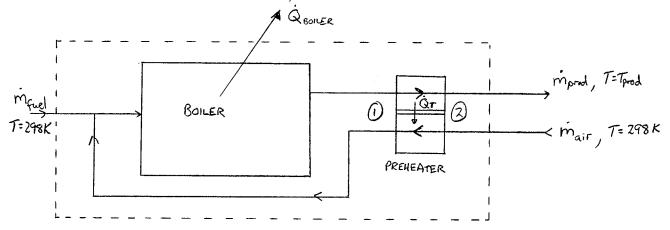
$$\phi = 0.914$$
(continued)

PROBLEM 2-55 (continued)

b) defining the boiler thermal efficiency: $\gamma = \frac{\hat{Q}_{BOILER}}{\hat{Q}_{MAX}}$

where abone is the heat transferred by the boiler and amax represents the maximum possible heat transfer (products at 298 K)

schematic for first law analysis:



9 = Q = - | [ZNihi] prod - huel - A) molar hair

9 = [\(\hat{\times}\frac{\Ni}{Nfuel}\) \(\hat{hi}\)]prod - \(\hat{fuel}\) - \(\hat{F}\))molar \(\hat{hair}\)

For q_{max} $(T_{\text{prod}} = 298 \text{ K})$: $\vec{h} = \vec{h}_f^\circ + (\vec{h} - \vec{h}_f^\circ) = \vec{h}_f^\circ$

 $\frac{\sum_{i}^{N_{i}}}{N_{fuel}} h_{i} = 1 h_{fco_{2}}^{\circ} + 2 h_{fH_{2}0}^{\circ} + b h_{fo_{2}}^{\circ} + 3.76a h_{fN_{2}}^{\circ} \leftarrow from combustion equation$ = 1[-393546] + 2[-241847] + 0 + 0 = -877240 KJ/(knole-fuel)

50, 9 max = -877240 - [-74831] - 10.42 (0) = -802409 KJ/(Knole-fuel)

for no preheat (Tprod = 700 K): h = hf + (h-hf)

 $\frac{\sum \frac{N_i}{\hat{N}_{\text{fuel}}} \hat{h}_i = 1[-393546 + 17749]_{\text{co}_2} + 2[-241847 + 14209] + 0.19[0 + 12503]_{\text{o}_2} + 8.23[0 + 11942]_{N_2} \\
= -730415 \text{ (continued)}$

b(continued):
$$q_{BOILER} = -730415 - [-74831] - 10.42(0) = -655584 k / kmole-fuel$$

$$\eta = \frac{Q_{BOILER}}{Q_{max}} = \frac{q_{BOILER}}{q_{max}} = \frac{-655584}{-802409} = 0.82$$

$$\eta = 0.82$$
without preheat

c) with air preheat
$$(T_{prod} = 433K)$$
: $\bar{h} = \bar{h}_{f}^{\circ} + (\bar{h} - \bar{h}_{f}^{\circ})$
 $q_{RONER} = Z \frac{\dot{N}_{i}}{N_{fud}} \bar{h}_{i} - \bar{h}_{f}^{\circ} - 4 / M_{MAR} \bar{h}_{air}$

$$\sum_{N_{\text{fuel}}}^{N_{\text{fuel}}} = I[-393546 + 5421]_{\text{co}_2} + 2[-241847 + 4609]_{H_{20}} + 0.19[0 + 4043]_{0_2} + 8.23[0 + 3946]_{V_2}$$

$$= -829357 \text{ KI}_{\text{Knole-fuel}}$$

$$9_{\text{BOILER}} = -829357 - \left[-74831\right]_{\text{fuel}} - 10.42 \left(0\right)_{\text{air}} = -754526 \frac{\text{KT}}{\text{kmole-fuel}}$$

$$\eta = \frac{-754526}{-802409} = 0.94 \qquad \boxed{\eta = 0.94} \quad \text{with preheat}$$

d) Estimate the maximum gas temperature in the combustion space with air preheat.

Assume that this temperature is the adiabatic flame temperature and that the flue gas temperature before entering entering the pre-heater is 700 K (i.e., the temperature of the flue gas exiting the boiler remains constant, regardless of whether air pre-heat is used)

first law for the preheater:

per kmole of fuel burned:

PROBLEM 2-55 (continued)

$$ah_{o_2} + 3.76ah_{N_2} = -730415 - [-829357] = 98942 KJ/kmole-fuel)$$
 $H_{air} (KJ/kmole-fuel)$

determine adiabatic flame temperature:

$$H_{p} = H_{R} = H_{fuel} + H_{anr}$$

$$H_{p} = [-74831 + 0] + 98942 \frac{K_{p}}{K_{mole}} + \frac{24111}{K_{mol}} \frac{K_{p}}{K_{mol}} + \frac{1}{1} \frac{K_{p}}{K_{p}} + \frac{1}{1} \frac{K$$

Using appendix A:
$$T(K)$$

$$\begin{array}{ccc}
R(K^{T}/K \text{mole-fuel}) \\
-97329 \\
2300 \\
-50028 \\
2400 \\
-2508
\end{array}$$
Linear interpolation
$$\begin{array}{cccc}
2500 \\
45233
\end{array}$$
For $R = 0$ yields
$$T = 2405 K$$

COMMENTS: Measured combustion product mole fractions are typically based on a "dry" mixture since the product susually condensed out of the mixture before the mixture enters the measuring instruments. This prevents the from condensing in the instruments and damaging them. Also note that the temperature in part d is the upper limit since dissociation is neglected and the combustion process is assumed to be adiabatic.

GIVEN: C8 His products: 1/co2 = 0.06 (wet); 1/co = 0.01 (wet)

FIND: a) \$ 5) xa

ASSUMPTIONS: All of the carbon in the fuel is converted to CD & CO2 and all of the hydrogen to HD. I<1.

SOLUTION: a = x + y/4 = 8 + 18/4 = 12,5

Z[C8H18 + 125 (02+3.76 N2)] -> 6 (02 + 1 CO + dH20 + for + (7)3.76 (125) M2

C-balance: 82 = 6+1

(RHS = 100 kmoles)

2 = 7/8

H-balance, 718 = 2d => d = 63 = 7.875

0-talance: 7 1252 = 2+1+63 + 2f

 $\frac{10.9375}{9} = +10.4375 + 4$

Overall: ZNpr=100 = 6+1+ = +f + = 3,76 12,5 = 100

or f = 85.125 - 41.125 (i)

substitute i) - ii)

(a) $\frac{10.9375}{\phi} = 10.4375 = 85.125 - 41.125$; $\phi = \frac{52.0625}{95.5625} = 0.5448$

b) $f = 85.125 - \frac{41.175}{0.5448} = 9.6386$ 7/62 = f/100 = 0.0964

COMMENT: What is the source of coin a bean product mixture?

Perhaps incomplete mixing or insufficient residence time

to romucut co > coz (See Ch. 5)

GIVEN: CHy/Oz burned to gield CO, COz, HzO, Hz , D=1,5

FIND: a) Mixture composition for T = 1500K b) Mixture composition for T = 2500 K

ASSUMPTIONS; ideal gas mixture

APPROACH: "Water-gas shift" =quilibrium will control the composition to gether with The relative proportions of C, H, &O in The reactant stream.

 $CH_4 + \frac{2}{9} O_2 \rightarrow b CO_2 + CCO + d H_2O + e H_2$ Arbitrarily reference to # H atoms:

i)
$$\frac{\# Catoms}{\# Hatoms} = \frac{1}{4} = \frac{\gamma_{co} + \gamma_{loz}}{2\gamma_{Hzo} + 2\gamma_{Hz}}$$

(i)
$$\frac{\# \text{ Datoms}}{\# \text{ Hatoms}} = \frac{4/\sqrt{5}}{4} = \frac{1}{\sqrt{5}} = \frac{2}{3} = \frac{1}{2} = \frac{2}{2} = \frac{1}{2} =$$

iii)
$$1 = \chi_{co} + \chi_{coz} + \chi_{tz0} + \chi_{tz}$$

Equilibrium; $co + H_{z}0 = coz + H_{z}$
iv) $\chi_{tz}(t) = \frac{\chi_{coz}}{\chi_{tz}} \chi_{tz0}$

a) Simultaneously solve Egns i-iv for kp(T) evaluated at T=1500K. From Table 2.3, Kp(1500) = 0.3887.

PROBLEM 2-57 (Continued)

Alternatively, Epns. 2.72, 2.73, 2.74, 2.75, 2.76 can be employed to solve this problem. (The =0) Using sprendsheet software, we obtain The following results:

T(K)	12	% CO2	% CO	70 to U	98 Hz
	0.3887				
2500	0.1622	9.1	24.3	46.5	20.2

comments: Relatively large amounts of co and the are produced at these conditions. The effect of temperature is not particularly strong.

PROBLEMS 2,58 - 2.62

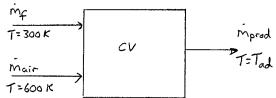
THIS SERIES OF PROBLEMS CAN BE USED AS A SINGLE PROJECT.

GIVEN: A furnace utilizing preheated air and operating at a mass air-fuel ratio of 16. The air is preheated to 600 K and the fuel enters at 300 K.

FIND: the adiabatic flame temperature

Assumptions: The following simplified thermodynamic properties apply $T_{ref} = 300 \text{ K}$ $MW_f = MW_{air} = MW_{prol} = 29 \frac{\text{Kg}/\text{kmole}}{\text{kmole}}$ $C_{P,f} = C_{P,air} = C_{P,prod} = 1200 \text{ J/kg·K}$ $h_{f,air} = h_{f,prod} = 0$ $h_{f,f} = 4 \times 10^7 \text{ J/kg}$

APPROACH: This a first law analysis



for A/F)_{mass} $M_p = H_R$ $M_p = H_R$ $M_{prod} = M_f (1 + A/F)$ $M_{air} = M_f (A/F)$ $M_f = M_f (1)$

 $\dot{H}_P = \dot{H}_R$

 $\dot{m}_{p}h_{p}=\dot{m}_{f}h_{f}+\dot{m}_{air}h_{air}\longrightarrow \dot{m}_{f}(I+A/F)[O+C_{p}(T_{ad}-T_{ref})]_{p}=\dot{m}_{f}(A/F)[O+C_{p}(T_{air}-T_{ref})]_{air}\\ +\dot{m}_{f}[h_{f}^{*}+C_{p}(T_{f}-T_{ref})]_{f}$

 $(1+16)[0+1700(T_{ad}-300)]=(16)[0+1700(600-300)]+(1)[4\times10^{7}+1700(300-300)]$

solving for Tad: Tad = 2543 K

comments: Because of the simplified thermodynamic properties and the fact that implicitly there is no dissociation, preheding the air (AT=300) results in Tad being nearly 300 K higher (DTad = 283 K). If the fuel were preheated too, then DTad = 300 K, exactly.

NOTE! This problem an be used as a small project.

GIVEN: TCH4 = 298 K; Tain = 325 K; Xo = 0,02

FIND: Combinations of 75 FGR & TFOR that result in Tax = 1950 K.

ASSUMPTIONS: FER composition based on no dissociation; natural gas ~ CHy; TER, mad = 1200 K.

APPROACH: i) Use Yor to determine Stoichiometry
ii) Apply 1st law (Egn 2.40) to determine
reg'd enthalpy of FGR
ici) Relate Horn to 8 FGR & TFGR

SOLUTION:

For no dissociation, flue gas composition can be obtained:

 $CH_4 + \frac{2}{3}(O_2 + 3.76N_2) \rightarrow CO_2 + 2H_2O + aO_2 + \frac{2}{3}.76N_2$ O-talance: $2(\frac{2}{9}) = 2 + 2 + 2a$; $a = \frac{2}{9} - 2$ (I) Given $\frac{7}{3}O_2$: $0.02 = \frac{a}{(1 + 2 + c + \frac{2}{3}(3.76))}$ (I) Simultaneous solution of I is II gields:

a = 0.2325 $\phi = 0.8958$

NZOE = NCOZ + NHZO + NOZ + NNZ = /+2+0,2325 + 2(3.76)

PROBLEM 2-64 (continued)

Ntot = 11.627 => FGR composition:

$$f_{02} = \frac{1}{11.627} = 0.0860 \qquad f_{02} = \frac{0.2325}{11.627} = 0.0200$$

Now Nor depends on both the combustion of the fuel and NEGR, i.e.,

$$N_{Pr} = N_{F} \left(\frac{N_{Pr}}{N_{F}} \right) + N_{FOR} \left(\frac{N_{Pr}}{N_{FOR}} \right) \qquad 5 F = CH_{4}$$

We use TPEQUIL to determine NPr/NF:

Output from TPEQUIL

Equil. Calc. for Specified Fuel, Phi, T, & P Using Olikara/Borman Code

Data below are as read from the input file. Compare with INPUT.TP. If they do not agree, your input data have not been entered correctly.

CARBON ATOMS 1.0
HYDROGEN ATOMS 4.0
OXYGEN ATOMS 0.0
NITROGEN ATOMS 0.0
EQUIVALENCE RATIO 0.8958
TEMPERATURE (K) 1950.0
PRESSURE (Pa) 101325.0

CALCULATED COMBUSTION PRODUCTS PROPERTIES

Mixture Enthalpy [J/kg] = -0.5328E+06

Mixture Specific Heat, Cp [J/kg-K] = 0.158621E+04

Specific Heat Ratio, Cp/Cv = 1.2360

Mixture Molecular Weight [kg/kmol] = 27.7295

Moles of Fuel per Mole of Products = 0.08594273 = N_E/N_D

```
PROBLEM 2-64 (continued)
  or Nor/N= = 11.6357
and Npr/NFGR = 11.6357 = 1.0007 N 1
  Substitute I into III & solve for NEGR/NF:
 NFGR = (NA/NF) hpr - hp(1298K) - (NA/NF) hair (325K)

NFGR - (NA/NF) hpr

NFGR - (NA/NF) hpr
                                      See TREQUIL
output
  where
(NPr/N=) har (1950K) = (Mpr/N=) har MWPr
                        = 11.6357 (-532.8 BJ) 27.7295 bg
kmol
                        = -1,71909,105 kI/knol,
  h_= h_eHy (298) = -74,831 & Themoe (Table B.1),
 Thair = 0,21(789)+0.79(783) = 784.3 Emol >
                                              (Tables A. 11 & A.7)
(Npr/NFGR) Top = (1)(-532.8) 27.7295 = -14,774 ET/ tempe
  N_A/N_F = \frac{2(4.76)}{0} = \frac{2(4.76)}{0.8959} = 10,627
  Substituting numerical values from above into I:
\frac{N_{FGR}}{N_{F}} = \frac{-1.71909 \cdot 10^{5} - (-74,831) - D.627(784.3)}{\overline{h}_{FGR} - (-14,774)} = \frac{-105,413}{\overline{h}_{FGR} + 14,774}
                                              (AT)
```

PROBLEM 2-64 (confinued)

To complete our solution, we calculate how for a range of temperatures (330-1200K); solve got to for Morelly; and apply The definition of \$ 7602:

har (TFOR) = ZXi hi (FOR)

For example, at 1200K,

$$\bar{h}_{FGR}(ROOK) = 0.0860(-393,546 + 44,488) + 0.1720(-241,845 + 34,578) + 0.020(0 + 29,775) + 0.7220(0 + 28,118)$$

$$= -44,782 \, bJ/kmol$$

TFOR (K)	hFOR (TFOR) AT/RMOL	MARINE	2 FGR
330	-74,409	1.768	15.7
600	- 65, 858	2.064	127
900	- 55,669	2,578	22,2
1200	- 55,669 - 44,782	3.513	30.2

COMMENT; As expected, less %FOR is required for cooler recycled gases.