



T5 - Band Pass Filter using OPAMP

Integrated Master in Physics Engineering

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June 6th , 2021

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1 Introduction

In this laboratory assignment we seek to build a bandpass filter using an OP-AMP. Particularly we seek to maximize our **merit figure**, M , given by:

$$M = \frac{1}{\text{Cost}(\text{VoltageGainDeviation} + \text{CentralFreqDeviation} + 10^{-6})}$$

where the voltage gain deviation is the absolute value of the difference between the gain at 1000 Hz and 40 dB; and the central frequency deviation is the absolute value of the difference between the central frequency and 1000 Hz. The central frequency, f_c , is given by the geometric mean of the low cut-off frequency and the high cut-off frequency:

$$f_c = \sqrt{f_H f_L}$$

The circuit used was the following:

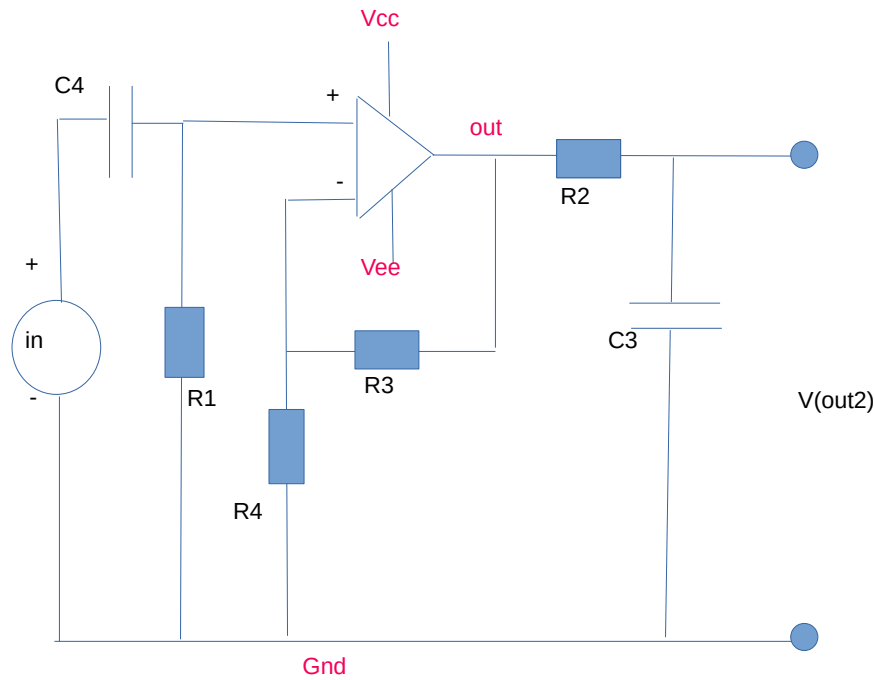


Figure 1: Circuito utilizado

2 Presential Lab

In this lab assigment we were also able to implement this circuit in real life, where we able to measured the gain and the cut-off frequencies. For the circuit configuration, we chose the following components:

R1	R2	R3	R4	C3	C4
1000K Ω	500 Ω	1000K Ω	500 Ω	220nF	220nF

With these components we were able to get a voltage gain of approximately $Gain = 40$ dbs, and cut-off frequencies of 330 Hz and 2.23 KHz , corresponding f_L and f_H , respectively. Using ngpsice, we simulated the same circuit, where we obtained the following results:

Cost	13426.472038661
Central frequency, f_0	847.6288757705225
Central frequency deviation ($diff_{F_0}$)	152.3711242294775
gain at 1000 Hz , G (db)	42.42502
Gain deviation, $Diff_G$	2.4250200000000004
Merit	1.649708859507576e-07
Low Cut off	3.95392e+02
High Cut off	1.81712e+03

3 Theoretical Analysis

3.1 Input and output impedances.

To determine the input and output impedances, we first replace the Op-Amp with its equivalent circuit, as shown in figure (2).

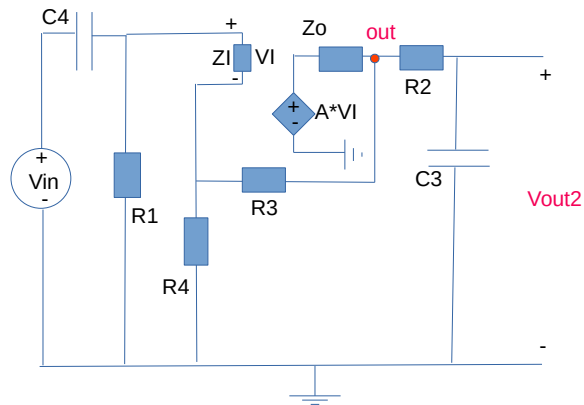


Figure 2: Pass-band circuit, with the amp-pop replaced with its equivalent circuit.

Considering the amp-op configuration is a non-inverting amplifier (and the ideal amp-op model), we get that the output and input impedances, Z_O and Z_I , are 0 and ∞ , respectively, and that the gain A is equal to: $(1 + \frac{R_3}{R_4})$. Therefore we get the following circuit, in figure (3)

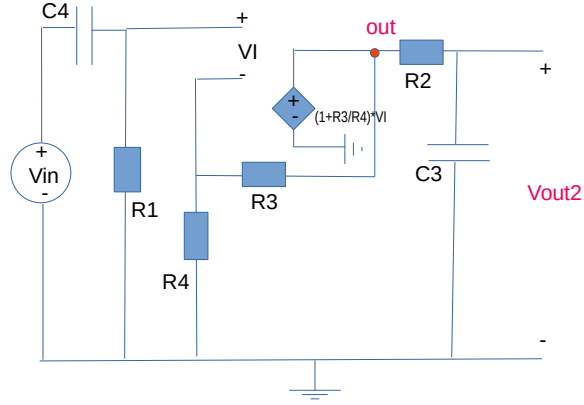


Figure 3: Pass-band circuit, with the amp-pop replaced with its equivalent circuit, using the ideal model approximation.

Finally, we can deduce the expressions for the input and output impedances for the circuit, Z_I and Z_{out} , (as seen by V_{in} and V_{out} , respectively). From the circuit in figure (3), we get that (there is no effect on the first part of the circuit, by V_{out2} , therefore it is not required to short-circuit the output):

$$Z_I(\omega) = Z_{C_4} + R_4 = \frac{1}{j\omega C_4} + R_4 \quad (1)$$

As for the output impedance, we need to short-circuit the input, hence we get the circuit in figure (4), from the V_{out2} terminals:

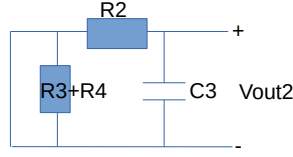


Figure 4: Equivalent circuit seen by the terminals of V_{out2} , when $V_I = 0$.

Therefore we get that:

$$Z_O(\omega) = R_2 || C_3 = \frac{R_2}{j\omega C_3 R_2 + 1} \quad (2)$$

3.2 Transfer function

The transfer function is defined as the ration between the output and the input. In our case, the output is v_0 and the input v_s :

$$T(s) = \frac{v_0}{v_s}$$

after a little algebra, we get to the following expression:

$$T(s) = \frac{R_1 C_1 s}{1 + R_1 C_1 s} \left(1 + \frac{R_3}{R_4}\right) \left(\frac{1}{1 + R_2 C_2 s}\right) \quad (3)$$

where, as usual

$$s = j\omega$$

3.3 Cut-off frequencies

The theoretical cut-off frequencies, f_L and f_H , can be calculated by the Short Circuit Time Constants Method. They are given by¹:

$$f_L = \frac{1}{R_1 C_1} \quad (4)$$

$$f_H = \frac{1}{R_2 C_2} \quad (5)$$

where f_H is the high cut-off frequency and f_L is the low cut-off frequency. Experimentally, the cut off frequencies will be calculated through the following expression:

$$f = \frac{V_{max}}{\sqrt{2}}$$

where f can be either f_H or f_L .

The Results obtained using octave were the following:

Total Cost	13427.69537166100
Central Freq	712.82860548662
Central Frequency difference	287.17139451338
Gain	39.72250000000
Cut off low	218.11200000000
Cut off high	2329.65000000000
Gain Difference	0.27750000000
Merit	0.00000097467

Table 1: Values used as parameters for the circuit studied.

4 Simulation Analysis

The Operating point analysis is the following:

The graphs are the following:

¹If you want to see the deduction in detail, you may visit the following link:
https://ocw.mit.edu/courses/electrical-engineering-and-computer-science/6-012-microelectronic-devices-and-circuits-fall-2009/lecture-notes/MIT6_012F09_lec23.pdf?fbclid=IwAR3ezEOiIWVJOLyNLNp49EwgcpWSC-_IQF06wASvf9cKXiGx2_OzBp1Pnb8

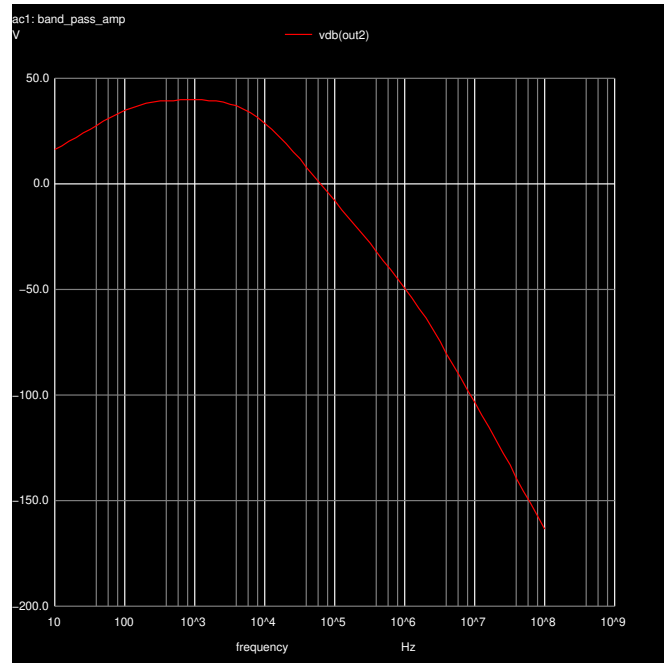


Figure 5: Time analysis

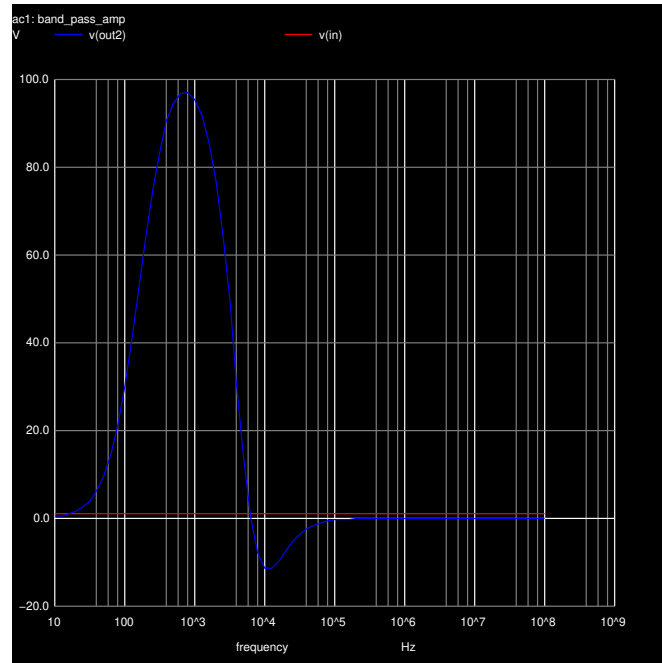


Figure 6: Frequency analysis

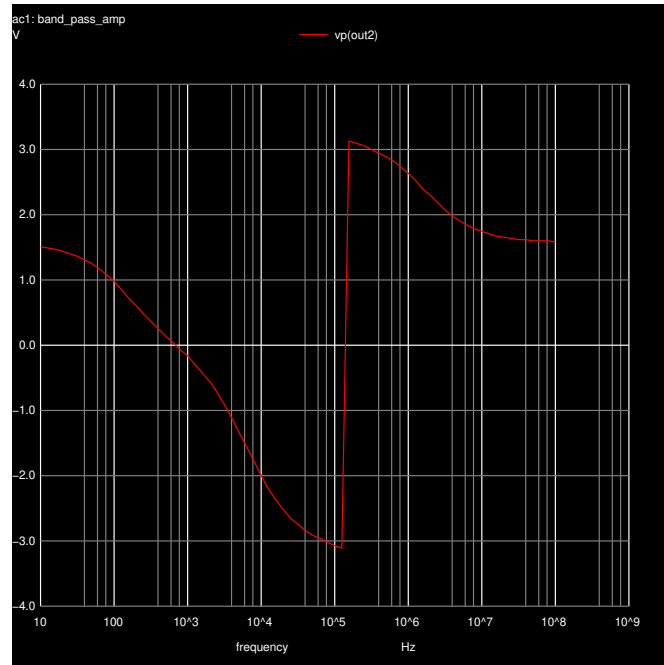


Figure 7: —

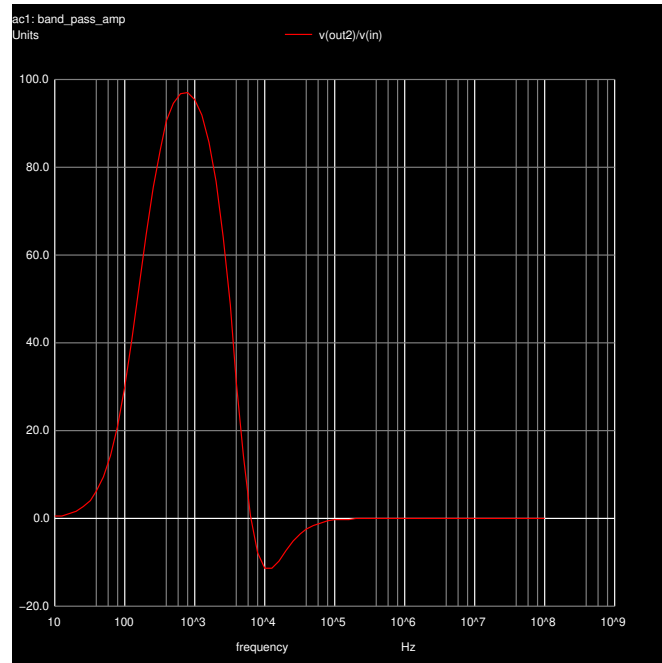


Figure 8: $v(\text{out})/v(\text{in})$

5 Conclusion