

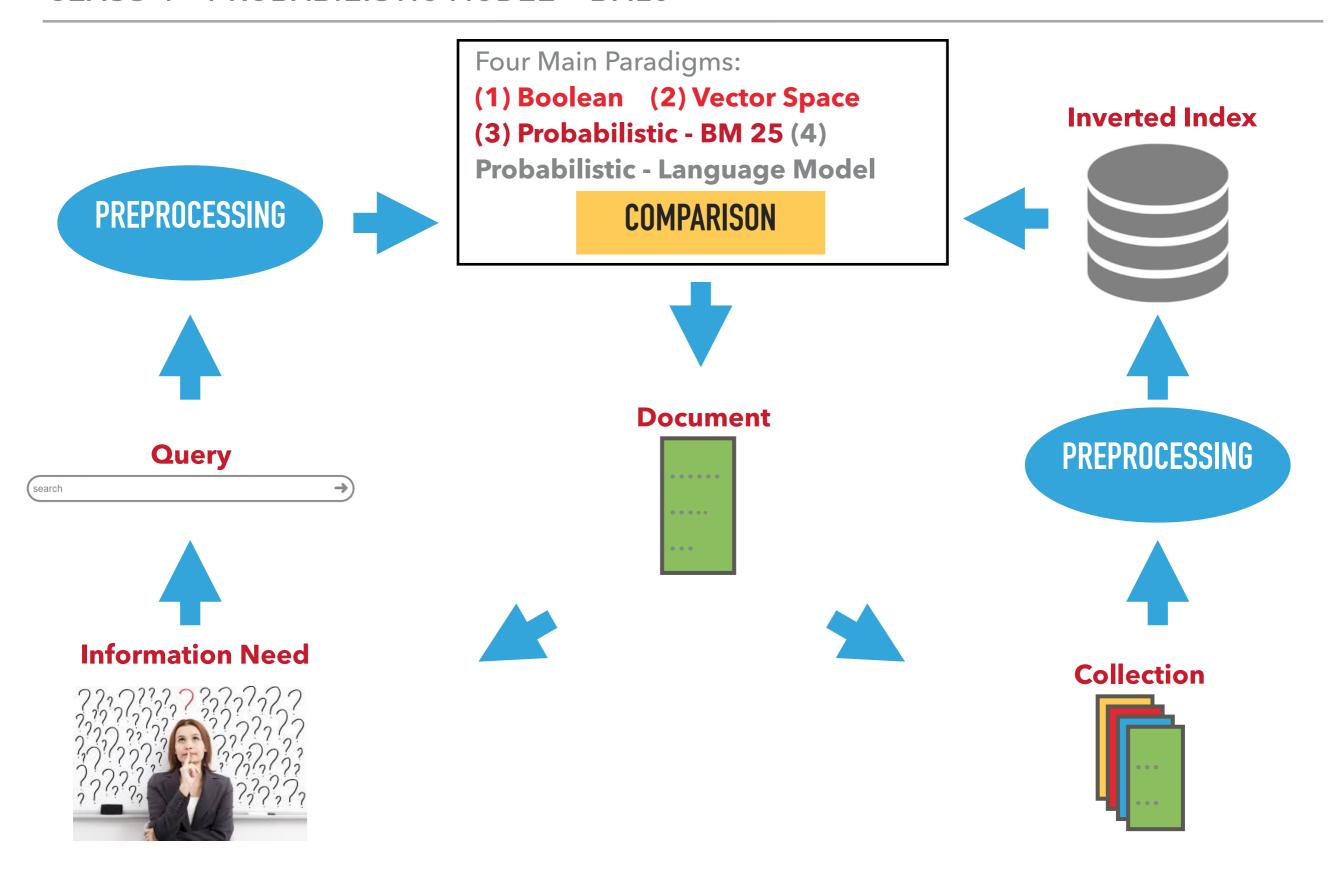
#### 67-300 SEARCH ENGINES

## PROBABILISTIC MODEL -BM25

LECTURER: JOAO PALOTTI (<u>JPALOTTI@ANDREW.CMU.EDU</u>)
22ND MARCH 2016

#### **LECTURE GOALS**

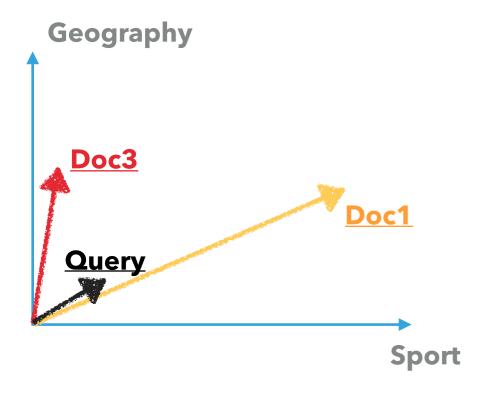
- Notes on Normalization
- Essential concepts in probability
- Probabilistic Framework / Retrieval Status Value
- ▶ BM 25 Formula

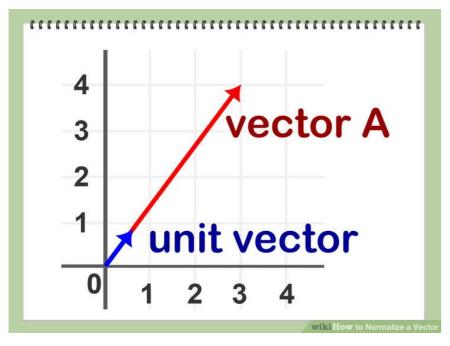


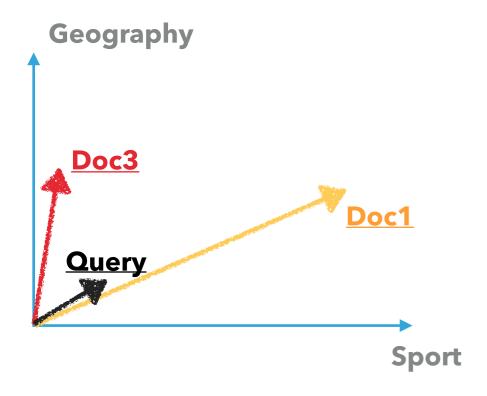
# RECAP VSM

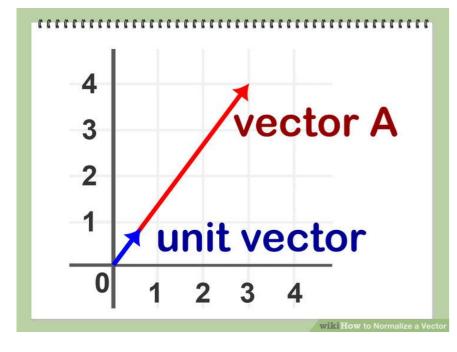
#### RECAP: VECTOR SPACE MODEL RECIPE

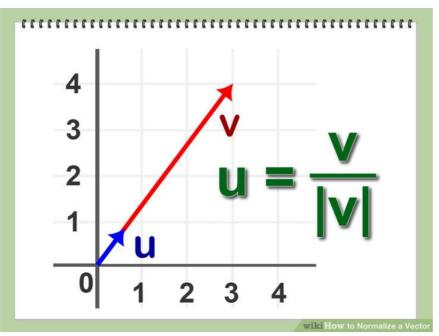
- Represent queries and documents as weighted tf-idf vectors
- Compute the cosine similarity score for the query and each document vector
- Rank documents with respect to the query by cosine similarity score
- Return top K documents (e.g., K = 10) to the user
- Geometric motivation

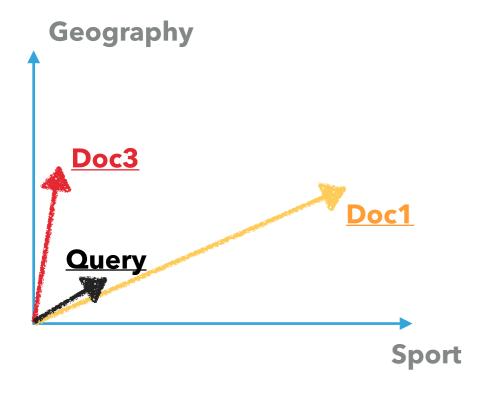


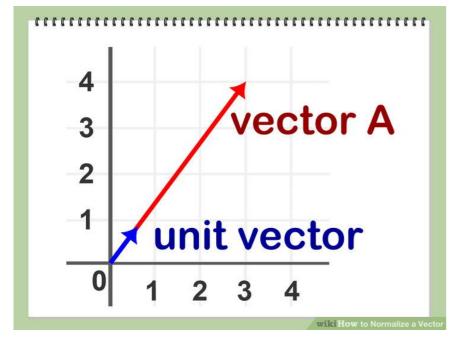


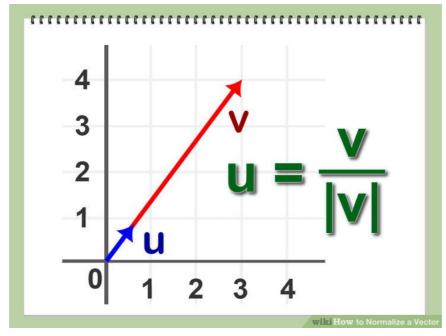


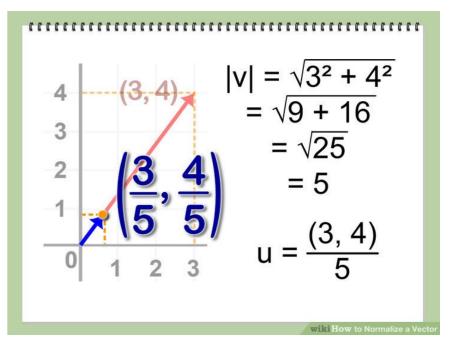


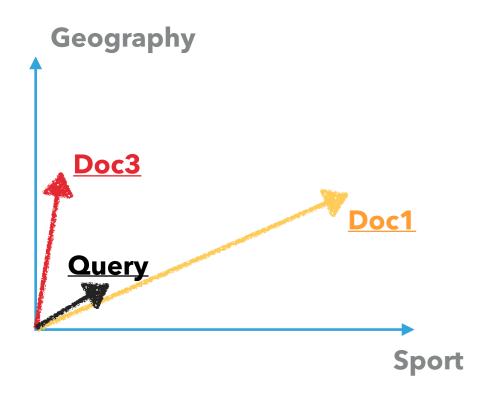




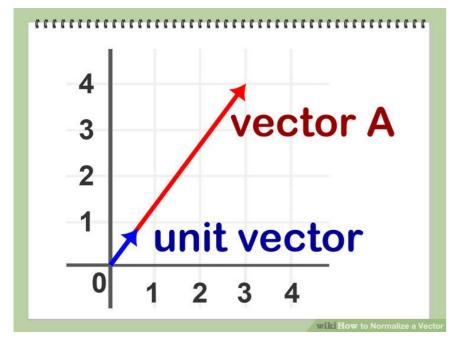


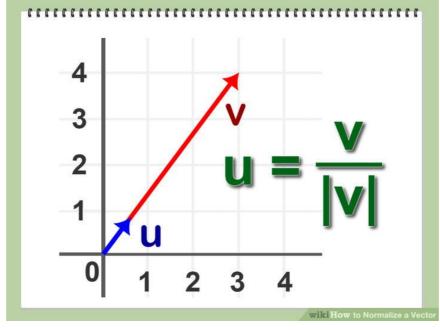


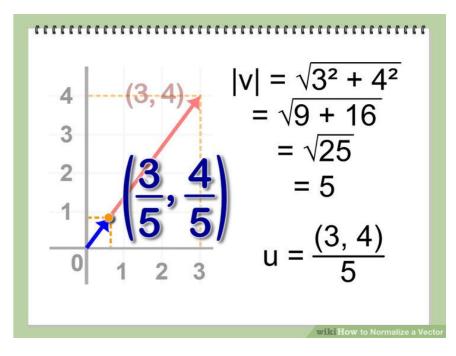


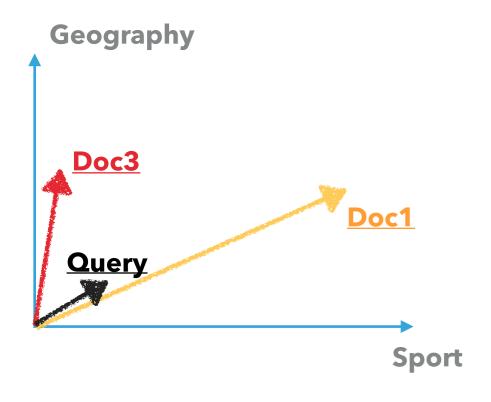


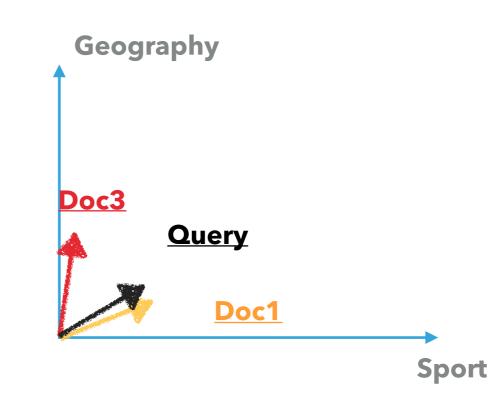
$$|u| = \sqrt{\frac{3}{5} \times \frac{3}{5} + \frac{4}{5} \times \frac{4}{5}} = 1$$

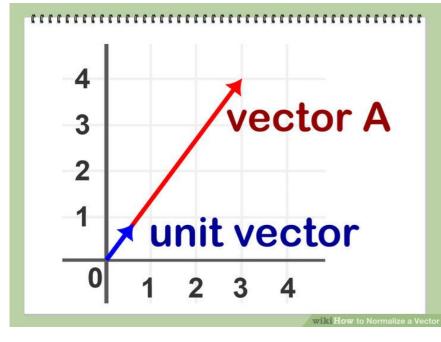


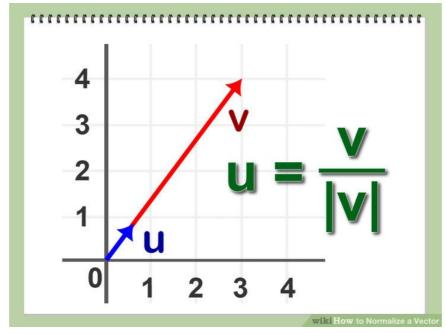


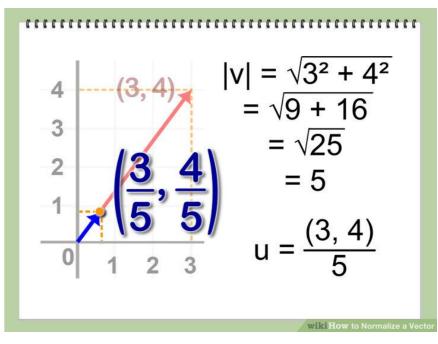










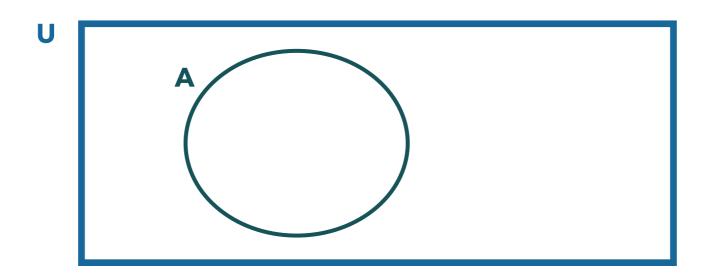


## GLIMPSE OF PROBABILITY

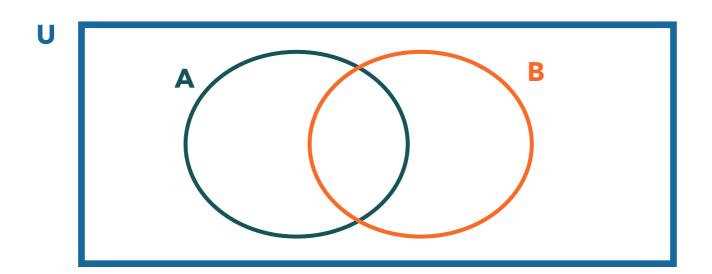
- Random variable A Subset of the space of possible outcomes
- ightharpoonup P(A) Probability of event **A** happening
- $P(A) \leq 1$

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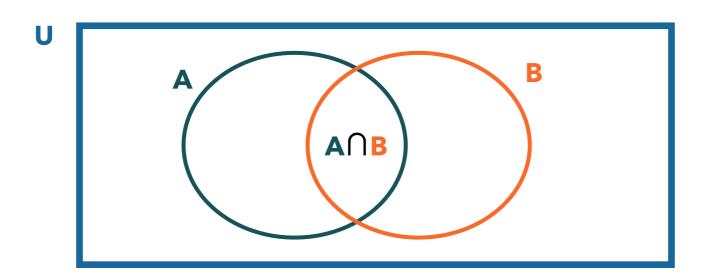
What is  $P(\overline{A})$  ?



- Random variable A Subset of the space of possible outcomes
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- Joint probability:  $P(A, B) = P(A \cap B)$



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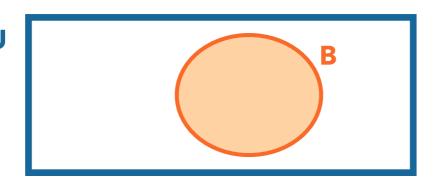


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- Conditional probability: P(A|B)

**Probability of A given B** 

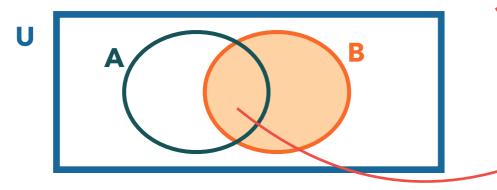
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**Probability of A given B** 



If B happened, what is the probability of A now?

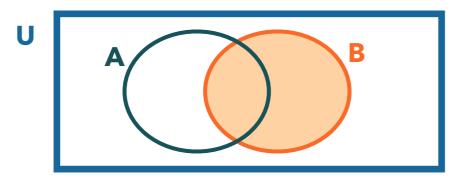
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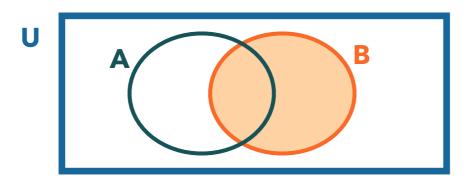
#### **CHAIN RULE**

$$P(A,B) = P(A \cap B) = P(B)P(A|B)$$

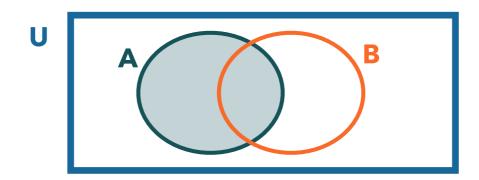


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Posterior probability

**Bayes Theorem:** 

$$P(A|B) = \frac{P(B|A)P(A)}{P(B)}$$

**Prior probability** 

#### OTHER SIMPLE RULES AND DEFINITIONS

Negate one of random variables:

$$P(\overline{A}, B) = P(B|\overline{A})P(\overline{A})$$

Interesting trivial case:

$$P(B) = P(A, B) + P(\overline{A}, B)$$

Odds:

$$O(A) = \frac{P(A)}{P(\overline{A})} = \frac{P(A)}{1 - P(A)}$$

## PROBABILISTIC FRAMEWORK

A RETRIEVAL SYSTEM RESPONSE TO A REQUEST IS A RANKING OF THE DOCUMENTS IN THE COLLECTION IN ORDER OF DECREASING PROBABILITY OF RELEVANCE TO THE USER WHO SUBMITTED THE REQUEST...

## **Probability Ranking Principle (PRP)**

#### RECIPE FOR THE STATISTICAL FRAMEWORK

• Given a request **q**, for each document **d** in the collection, calculate:

$$P(R_{d,q} = 1|d,q)$$

Probability of document d being relevant for a query q, given a document d and a query q

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- Rank documents with respect to their probability of being relevant for the query
- Return top K documents (e.g., K = 10) to the user
- Probabilistic motivation

- x represents a document in the collection (as a vector again)
- R represents the relevant of a document with respect to a query. R = 1, document is relevant. R = 0, document is not relevant
- P(R=1|x)
- Bayes Theorem:

$$P(R = 1|x) = \frac{P(x|R = 1)P(R = 1)}{P(x)}$$

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Prior probability of retrieving a relevant document

$$P(R = 1|x) = \frac{P(x|R = 1)P(R = 1)}{P(x)}$$

probability that if a relevant document is retrieved, it is x

- x represents a document in the collection
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$$P(R=1|x) = \frac{P(x|R=1)P(R=1)}{P(x)} \qquad \blacktriangleright \qquad P(R=0|x) = \frac{P(x|R=0)P(R=0)}{P(x)}$$

$$P(R = 0|x) + P(R = 1|x) = 1$$

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**HOW TO COMPUTE ALL THESE PROBABILITIES?** WHERE ARE THEY COMING FROM?

$$P(R=1|x) = \frac{P(x|R=1)P(R=1)}{P(x)} \qquad \blacktriangleright \qquad P(R=0|x) = \frac{P(x|R=0)P(R=0)}{P(x)}$$

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#### PROXIES FOR PROBABILITY

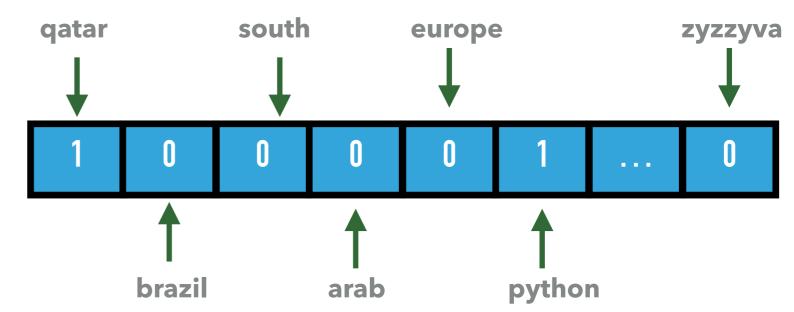
- Binary Independence Model
  - Mathematically beautiful, limited
- ▶ BM25
  - More complex theory, highly useful
- Language Models
  - A linguistic oriented approach

#### BINARY INDEPENDENCE MODEL

$$P(R=1|q,x)$$

- Binary: Boolean
  - binary/Boolean version of the bag of words approach

i love the python language but i am afraid i will find a real python in the desert in qatar



- Independence:
  - ▶ Terms occurs in documents independently

$$P(R=1|q,x)$$

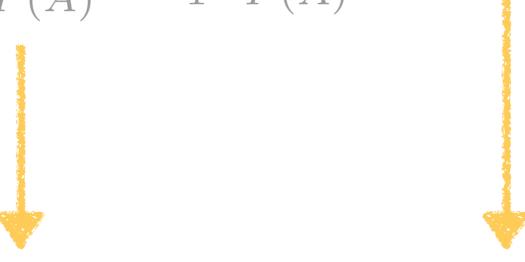
We start by calculating the odds:

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BINARY INDEPENDENCE MODEL 
$$O(R|q,x) = \frac{P(R=1|q,x)}{P(R=0|q,x)}$$

Use Bayes' Theorem:

$$P(A|B) = \frac{P(B|A)P(A)}{P(B)}$$

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$$\frac{P(R=1|q,x)}{P(R=0|q,x)} = \frac{\frac{P(R=1|q)P(x|R=1,q)}{P(x|q)}}{\frac{P(R=0|q)P(x|R=0,q)}{P(x|q)}}$$

NARY INDEPENDENCE MODEL 
$$O(R|q,x) = \frac{P(R=1|q,x)}{P(R=0|q,x)}$$

Use Bayes' Theorem:

$$P(A|B) = \frac{P(B|A)P(A)}{P(B)}$$



$$\frac{P(R=1|q,x)}{P(R=0|q,x)} = \frac{\frac{P(R=1|q)P(x|R=1,q)}{P(x|q)}}{\frac{P(R=0|q)P(x|R=0,q)}{P(x|q)}}$$

$$O(R|q,x) = \frac{P(R=1|q,x)}{P(R=0|q,x)} = \frac{P(R=1|q)}{P(R=0|q)} \times \frac{P(x|R=1,q)}{P(x|R=0,q)}$$

More transformations:

$$O(R|q,x) = \frac{P(R=1|q,x)}{P(R=0|q,x)} = \frac{P(R=1|q)}{P(R=0|q)} \times \frac{P(x|R=1,q)}{P(x|R=0,q)}$$

More transformations: <u>Constant for a query</u>

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**Still needs estimation** 

Use independence assumption:

$$\frac{P(\overrightarrow{x}|R=1,q)}{P(\overrightarrow{x}|R=0,q)} = \prod_{i=1}^{V} \frac{P(x_i|R=1,q)}{P(x_i|R=0,q)}$$

That's where we are so far:  $O(R|q,x) = \prod_{i=1}^v \frac{P(x_i|R=1,q)}{P(x_i|R=0,q)}$ 

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- We can divide it into two:

$$O(R|q,x) = \prod_{x_i=1} \frac{P(x_i = 1|R = 1, q)}{P(x_i = 1|R = 0, q)} \prod_{x_i=0} \frac{P(x_i = 0|R = 1, q)}{P(x_i = 0|R = 0, q)}$$

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 $\triangleright p_i$ : term appearing in a relevant document

$$p_i = P(x_i = 1 | R = 1, q)$$

 $ightharpoonup \mathcal{T}_i$ : term appearing in a non relevant document

$$r_i = P(x_i = 1 | R = 0, q)$$

We can rewrite from:

$$O(R|q,x) = \prod_{x_i=1} \frac{P(x_i = 1|R = 1, q)}{P(x_i = 1|R = 0, q)} \prod_{x_i=0} \frac{P(x_i = 0|R = 1, q)}{P(x_i = 0|R = 0, q)}$$

$$p_i = P(x_i = 1 | R = 1, q)$$
  $r_i = P(x_i = 1 | R = 0, q)$ 

To:

$$O(R|q,x) = \prod_{x_i=1}^{n} \frac{p_i}{r_i} \prod_{x_i=0}^{n} \frac{1-p_i}{1-r_i}$$

Not done yet... 
$$O(R|q,x) = \prod_{x_i=1} \frac{p_i}{r_i} \prod_{x_i=0} \frac{1-p_i}{1-r_i}$$

We assume terms not in the query can be ignored:

$$O(R|q,x) = \prod_{\substack{x_i=1; q_i=1}} \frac{p_i}{r_i} \prod_{\substack{x_i=0; q_i=1}} \frac{1-p_i}{1-r_i}$$

There is still another trick to manipulate this equation...

▶ What we have:  $O(R|q,x) = \prod_{x_i=1; q_i=1} \frac{p_i}{r_i} \prod_{x_i=0; a_i=1} \frac{1-p_i}{1-r_i}$ 

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After adding a small trick here:

$$O(R|q,x) = \prod_{x_i=1;q_i=1} \frac{p_i}{r_i} \prod_{x_i=1;q_i=1} \frac{1-r_i}{1-p_i} \times \frac{1-p_i}{1-r_i} \prod_{x_i=0;q_i=1} \frac{1-p_i}{1-r_i}$$

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And moving things around:

$$O(R|q,x) = \prod_{x_i=1;q_i=1} \frac{p_i \times (1-r_i)}{r_i \times (1-p_i)} \prod_{x_i=1;q_i=1} \frac{1-p_i}{1-r_i} \prod_{x_i=0;q_i=1} \frac{1-p_i}{1-r_i}$$

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- Multiplying fractions is hard for computers, we can use the logarithm to deal with hardware/numeric limitation
- Result is know as **Retrieval Status Value (RSV)**

$$RSV = \log \prod_{x_i=1; q_i=1} \frac{p_i \times (1-r_i)}{r_i \times (1-p_i)} = \sum_{x_i=1; q_i=1} \log \frac{p_i \times (1-r_i)}{r_i \times (1-p_i)}$$



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$$RSV = \log \prod_{x_i=1; q_i=1} \frac{p_i \times (1-r_i)}{r_i \times (1-p_i)} = \sum_{x_i=1; q_i=1} \log \frac{p_i \times (1-r_i)}{r_i \times (1-p_i)}$$

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Docs	Relevant	Non-Rel.	Total
$x_i=1$			n
$x_i = 0$			N - n
Total			N

Docs	Relevant	Non-Rel.	Total
$x_i=1$			n
$x_i = 0$			N - n
Total	S		N

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$x_i=1$	S		n
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Total	S	N-S	N

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$x_i=1$	S	n-s	n
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$$p_i \approx \frac{s}{S}$$

$$r_i pprox rac{n-s}{N-S}$$

Merging everything into...

$$RSV = \log \prod_{x_i=1; q_i=1} \frac{p_i \times (1-r_i)}{r_i \times (1-p_i)} = \sum_{x_i=1; q_i=1} \log \frac{p_i \times (1-r_i)}{r_i \times (1-p_i)}$$

$$p_i \approx \frac{s}{S}$$
  $r_i \approx \frac{n-s}{N-S}$ 

$$c_i = K(N, n, S, s) = \log \frac{\frac{\overline{S} - s}{\overline{S} - s}}{\frac{n - s}{N - n - S + s}}$$

## KEY RESULTS FROM THE THEORY

▶ Given the RSV value, what if p ~ 0?

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$$RSV = \log \sum_{x_i=1; q_i=1} \frac{(1-r_i)}{r_i} \quad \cdots \quad \frac{N-n-S+s}{n-s}$$

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# ESTIMATION OF P IS THE HARDEST PART

- Remember pi is the probability of term i in relevant documents
- ▶ Getting an accurate estimation of pi is hard (but not impossible)
- Proxies:
  - From a set of known relevant documents (pseudo-relevance)
  - A constant value Then we use only IDF
  - proportional to the prob. of occurrence of term i in the collection

# **BOOTSTRAPPING P**<sub>1</sub>

- 1. Assume pi is a constant (rank using only IDF)
- 2. Ask the user/Guess the relevant document set D
- 3. Improve estimation for pi and ri
  - 1. Count distribution of  $x_i$  in D. Adjust  $p_i = |D_i| / |D|$
  - 2. Not retrieved documents counted as not relevant. Adjust  $r_i = (n_i - |D_i|) / (N - |D|)$
- 4. Repeat from 2 until pi and ri converge.

- Best Match 25 results in a series of empirical try-and-error
- Aims to overcome some limitations from BIM, such as the binary part

$$RSV_d = \sum_{t \in q} \log \left[ \frac{N}{df_t} \right] \cdot \frac{(k_1 + 1)t f_{td}}{k_1((1-b) + b \times (L_d/L_{ave})) + t f_{td}}$$

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What if we have b = 0? What if we have b = 1?

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What if we have b = 0? What if we have b = 1? What if we have K1 = 0?
What if we have K1 very high?

We might have large queries and we might want to control for query size as well:

$$RSV_d = \sum_{t \in q} \log \left[ \frac{N}{df_t} \right] \cdot \frac{(k_1 + 1)t f_{td}}{k_1((1 - b) + b \times (L_d/L_{ave})) + t f_{td}} \frac{(k_3 + 1)t f_{tq}}{k_3 + t f_{tq}}$$

- Typical parameters are:
  - ▶ 1.2 < K\_1 < 2; 0 < K\_3 < 1000; b = 0.75
- It is common to use the smoothed version of BM25. We will see what is smoothing next lecture...

# WHAT DID WE SEE? WHAT SHOULD YOU KNOW?

- Essential concepts in probability
- Theoretic justification of ranking by relevance
- Derivation of the Retrieval Status Value (RSV)
- ▶ BM 25

# TODAY'S LECTURE IN THE STANFORD IR BOOK

Chapter 11 - Probabilistic Information Retrieval