

# Estrutura de Dados

Prof. Rafael Nunes

# Algoritmos de Busca e Ordenação

*Search and Sorting Algorithms*

Parte 2

# Ordenação

# Algoritmos de Ordenação Interna

*Continuação*

# Algoritmos de Ordenação Interna

- Complexidade  $O(n^2)$ 
  - Bubble Sort – Método da Bolha
  - Insertion Sort – Inserção direta
  - Selection Sort – Seleção direta
  - Shell Sort – Incrementos Decrescentes
- Complexidade  $O(n \log n)$ 
  - Merge Sort – Método da Intercalação
  - Quick Sort – Método da Troca e Partição
  - Heap Sort – Seleção em Árvore

# Algoritmos de Ordenação Interna

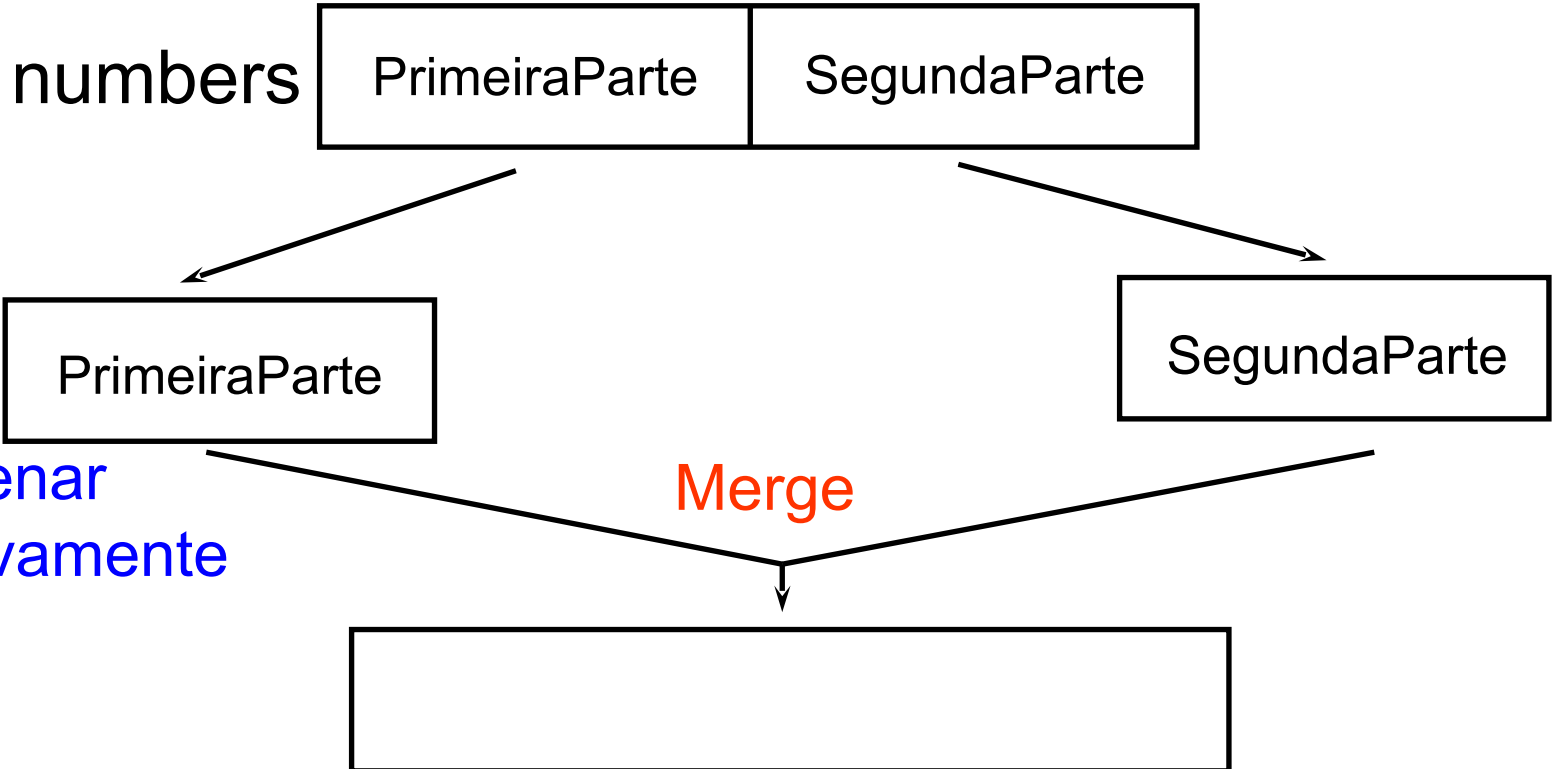
*Complexidade  $O(n \log n)$*

# Merge Sort

*Método da intercalação*

# Merge Sort: Funcionamento

Dividir em  
duas metades



Ordenar  
Recursivamente

Merge

Fim - Ordenado!



# Merge-Sort(numbers, 0, 7)

Divide

A:



# Merge-Sort(numbers, 0, 7)

Merge-Sort(numbers, 0, 3) , divide

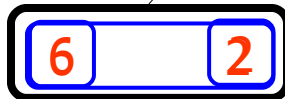
A:



# Merge-Sort(numbers, 0, 7)

Merge-Sort(numbers, 0, 1) , divide

A:



# Merge-Sort(numbers, 0, 7)

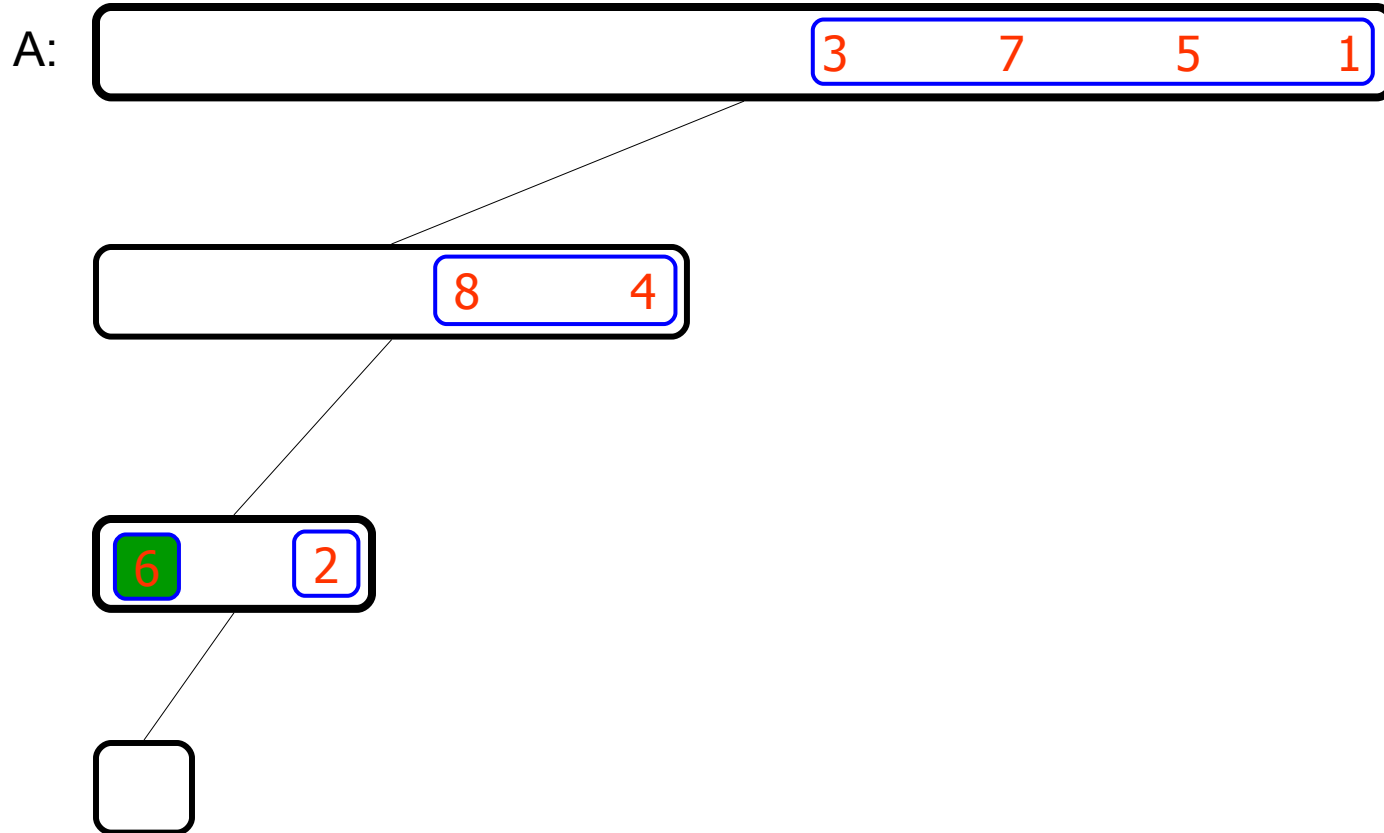
Merge-Sort(numbers, 0, 0) , caso base

A:



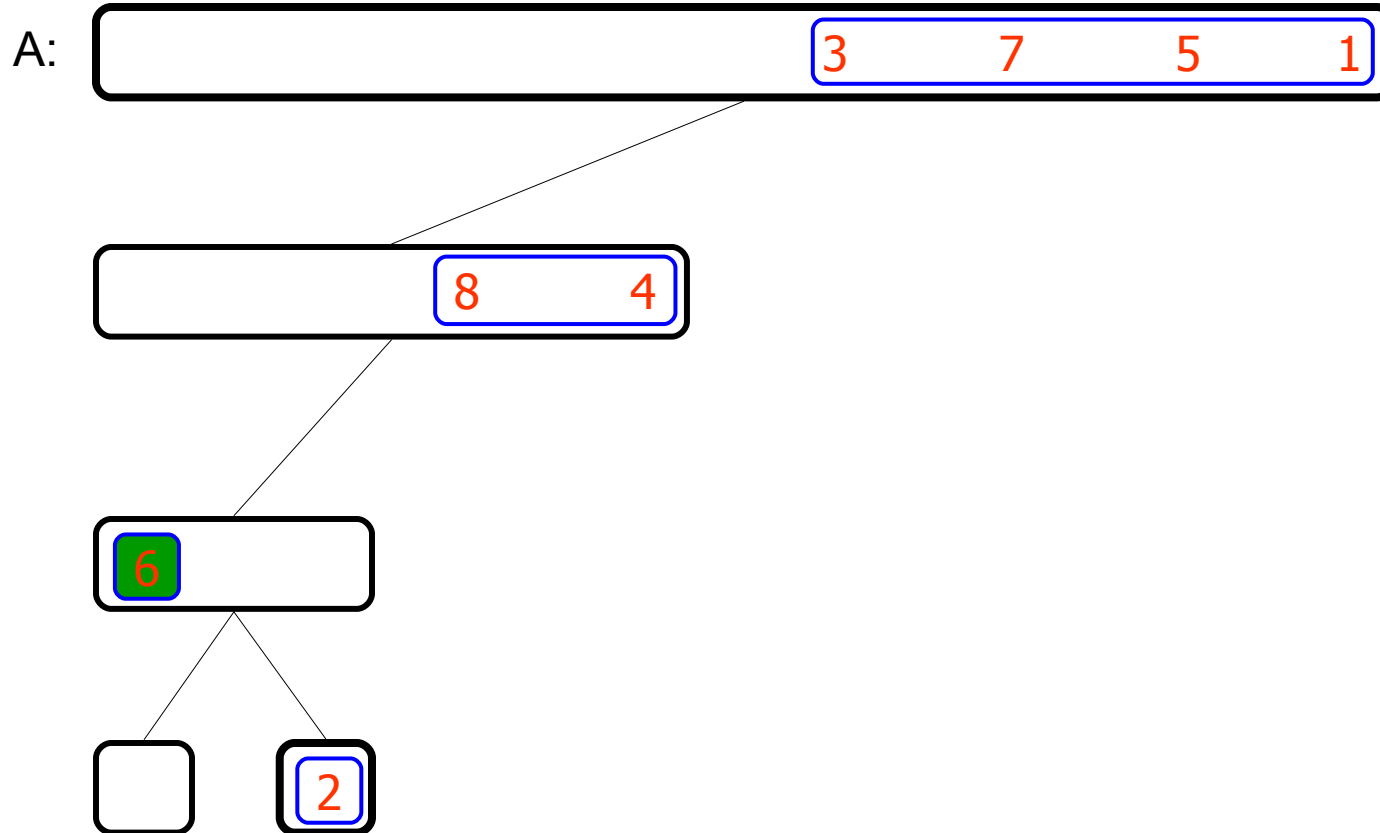
# Merge-Sort(numbers, 0, 7)

Merge-Sort(numbers, 0, 0), retorna



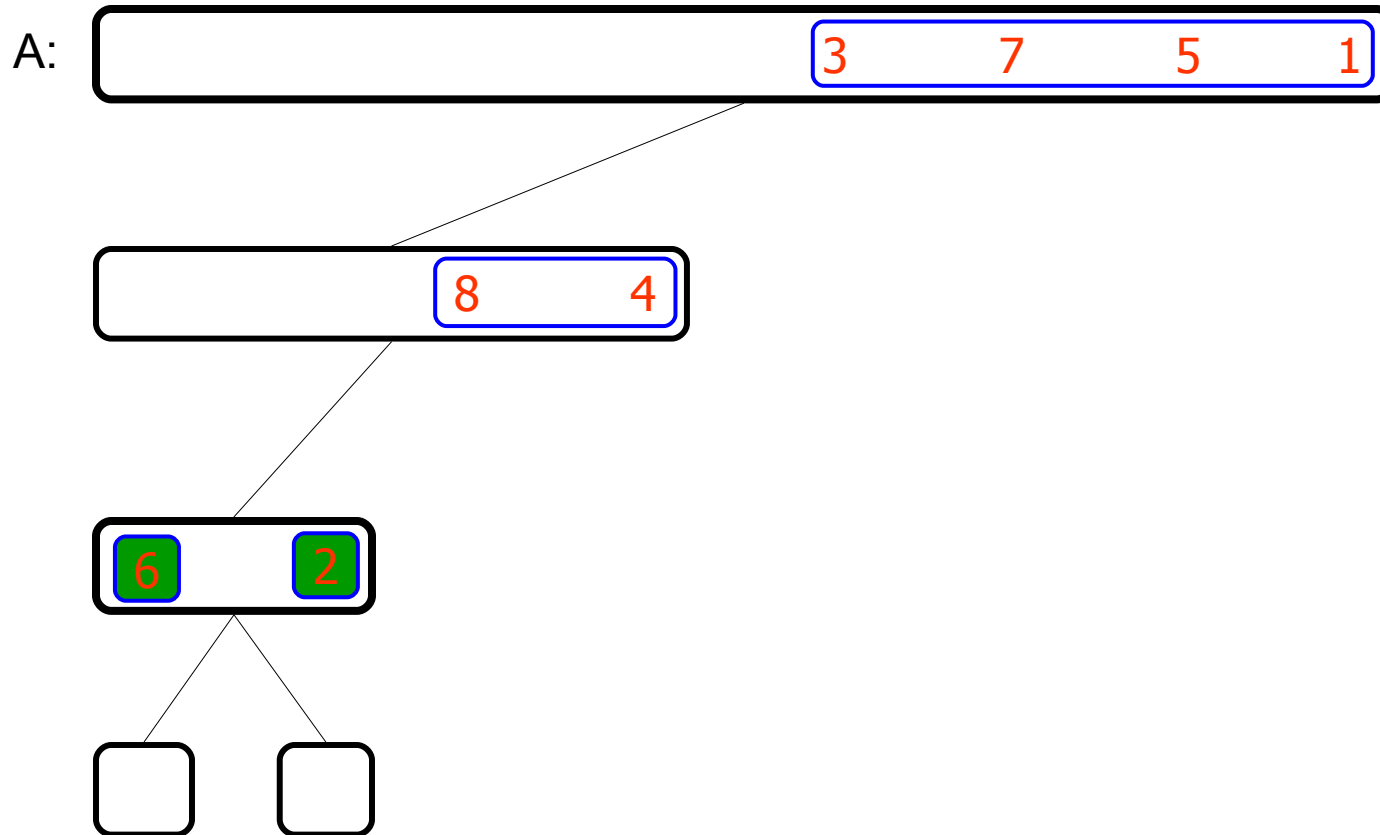
# Merge-Sort(numbers, 0, 7)

Merge-Sort(numbers, 1, 1) , caso base



# Merge-Sort(numbers, 0, 7)

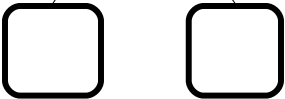
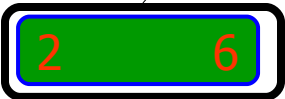
Merge-Sort(numbers, 1, 1), retorna



Merge-Sort(numbers, 0, 7)

Merge(numbers, 0, 0, 1)

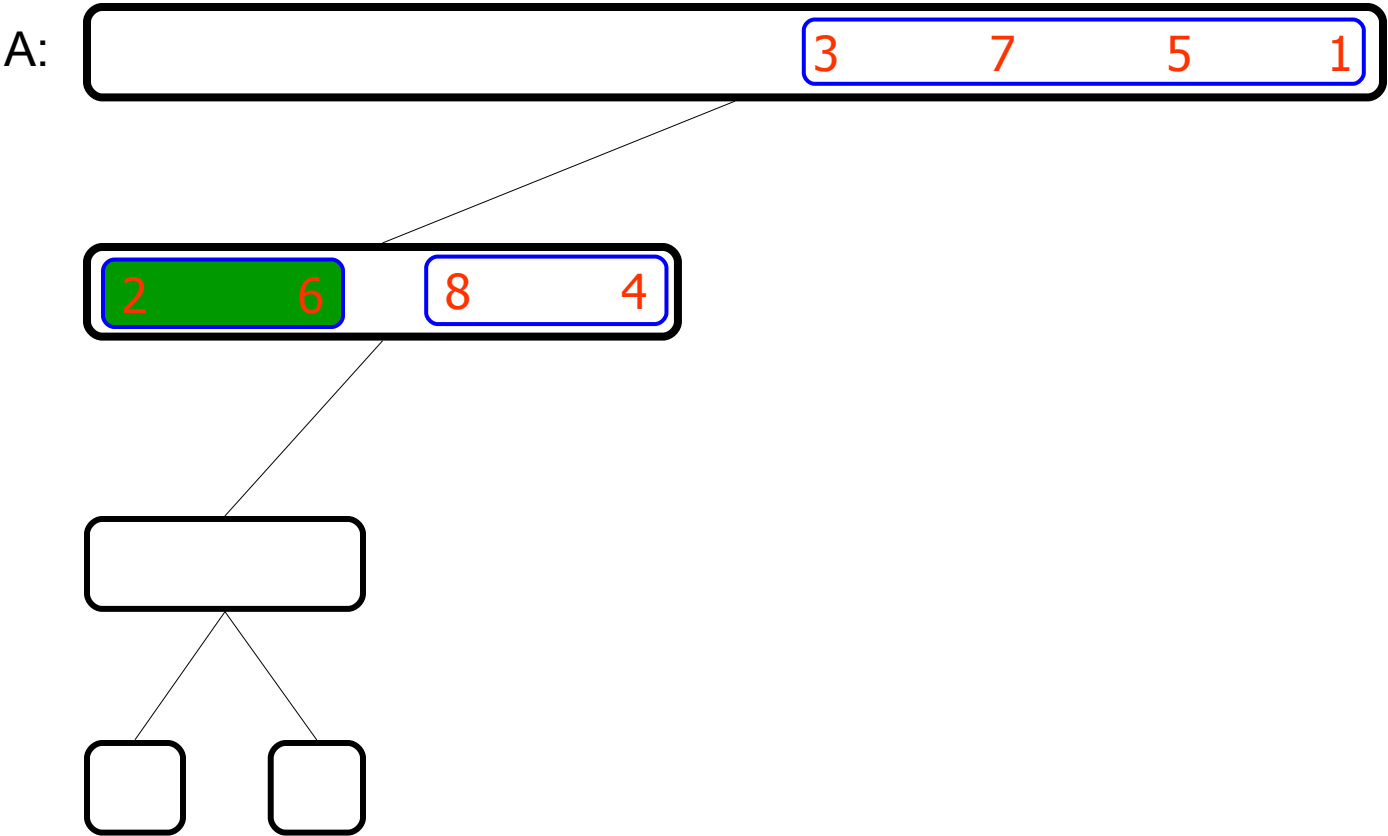
A:





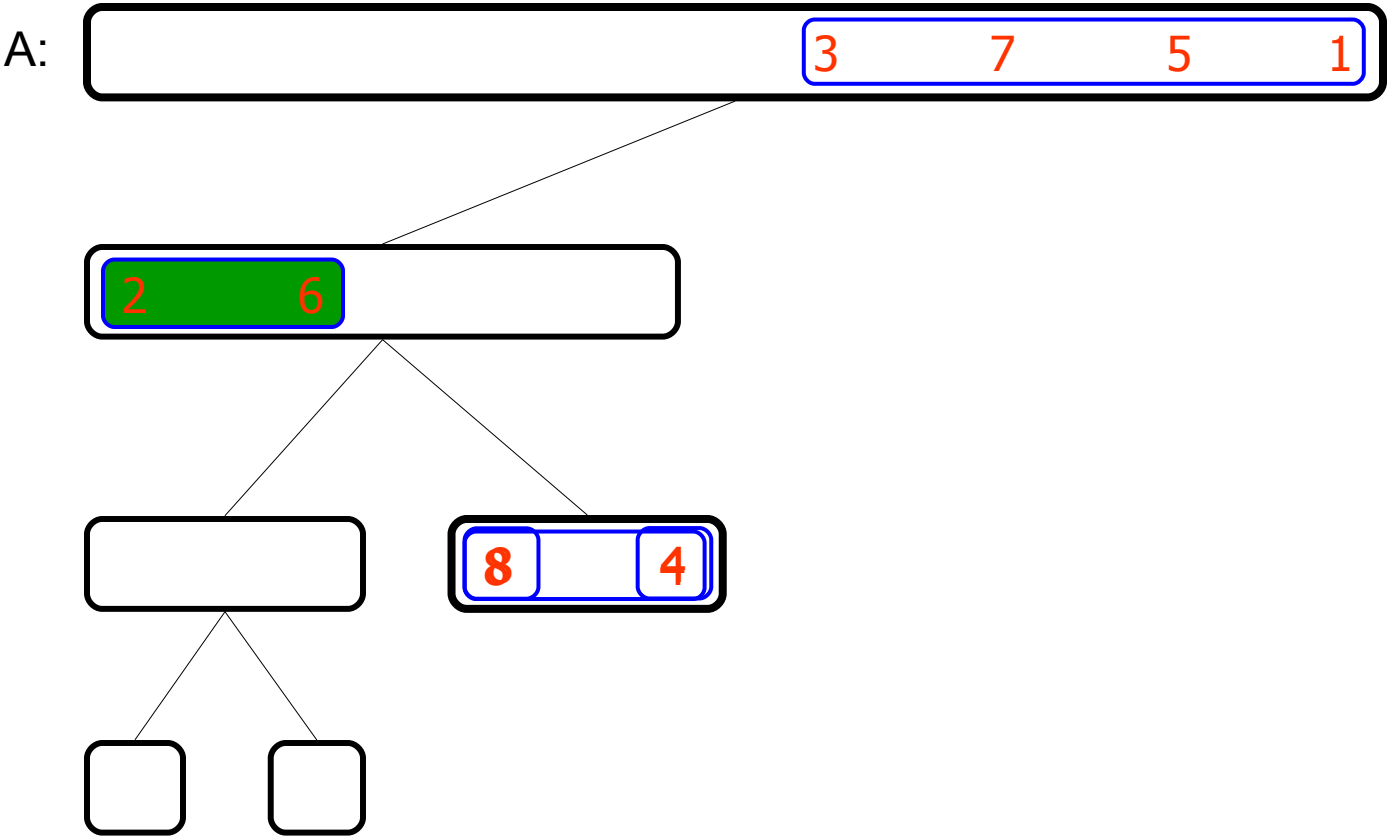
Merge-Sort(numbers, 0, 7)

Merge-Sort(numbers, 0, 1), retorna



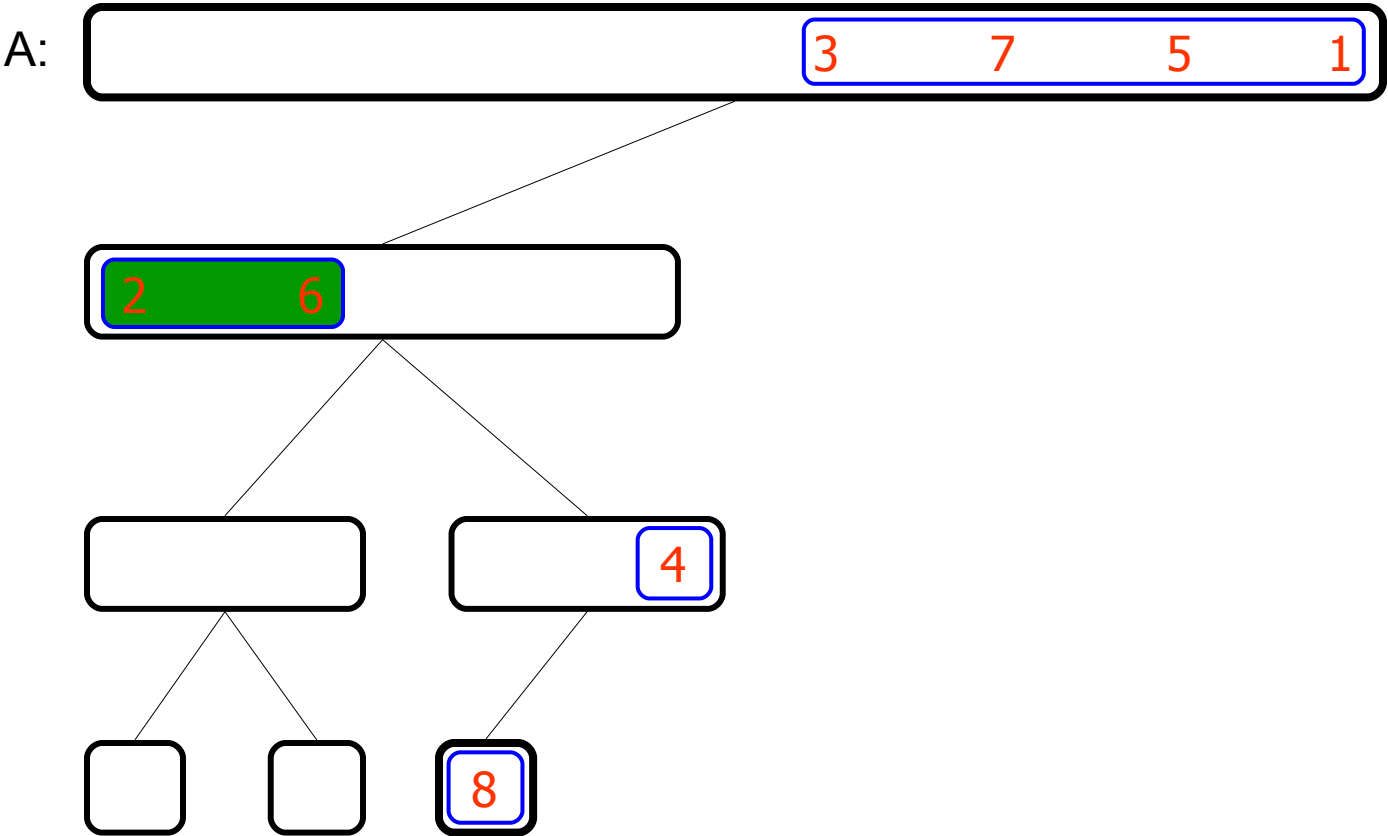
# Merge-Sort(numbers, 0, 7)

Merge-Sort(numbers, 2, 3) , divide



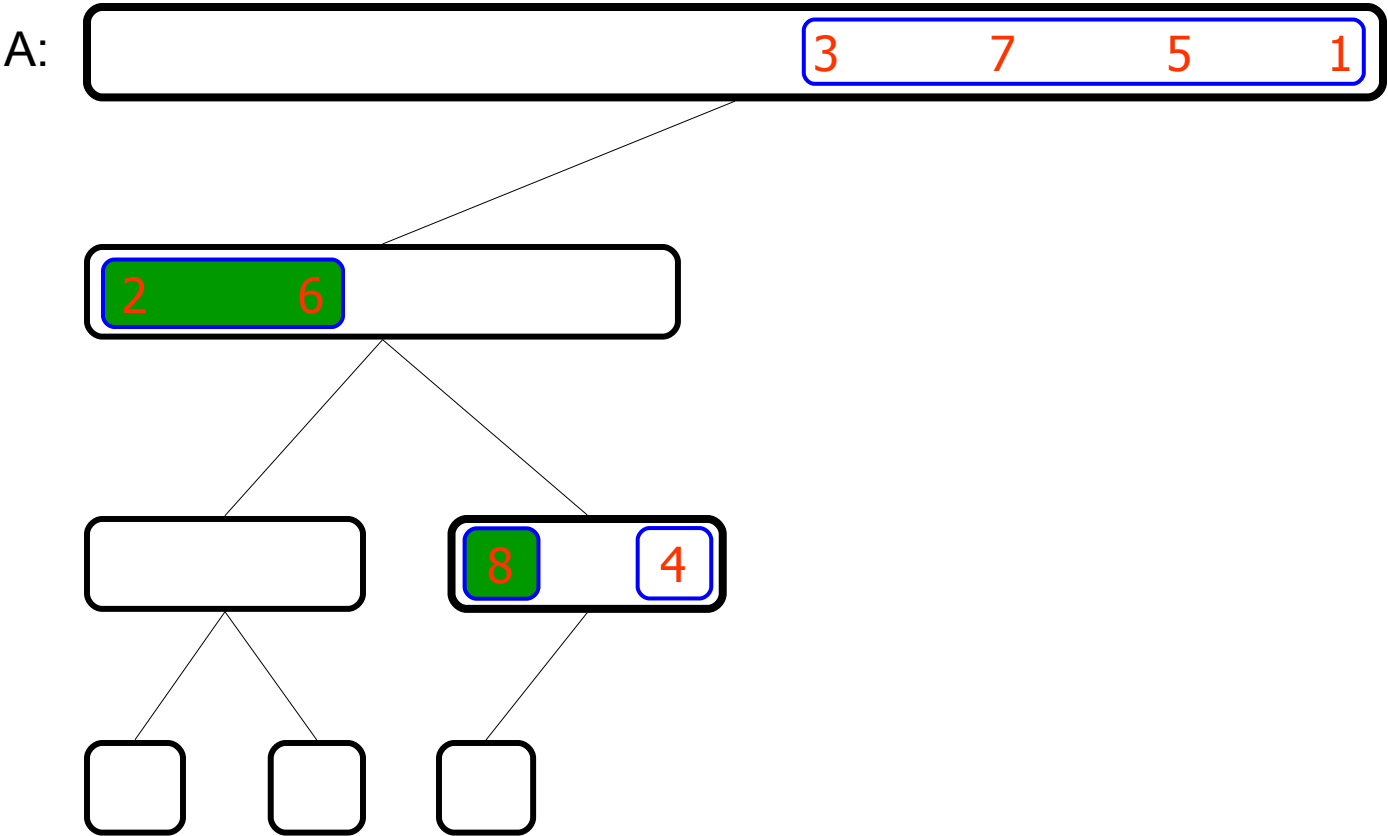
# Merge-Sort(numbers, 0, 7)

Merge-Sort(numbers, 2, 2), caso base



Merge-Sort(numbers, 0, 7)

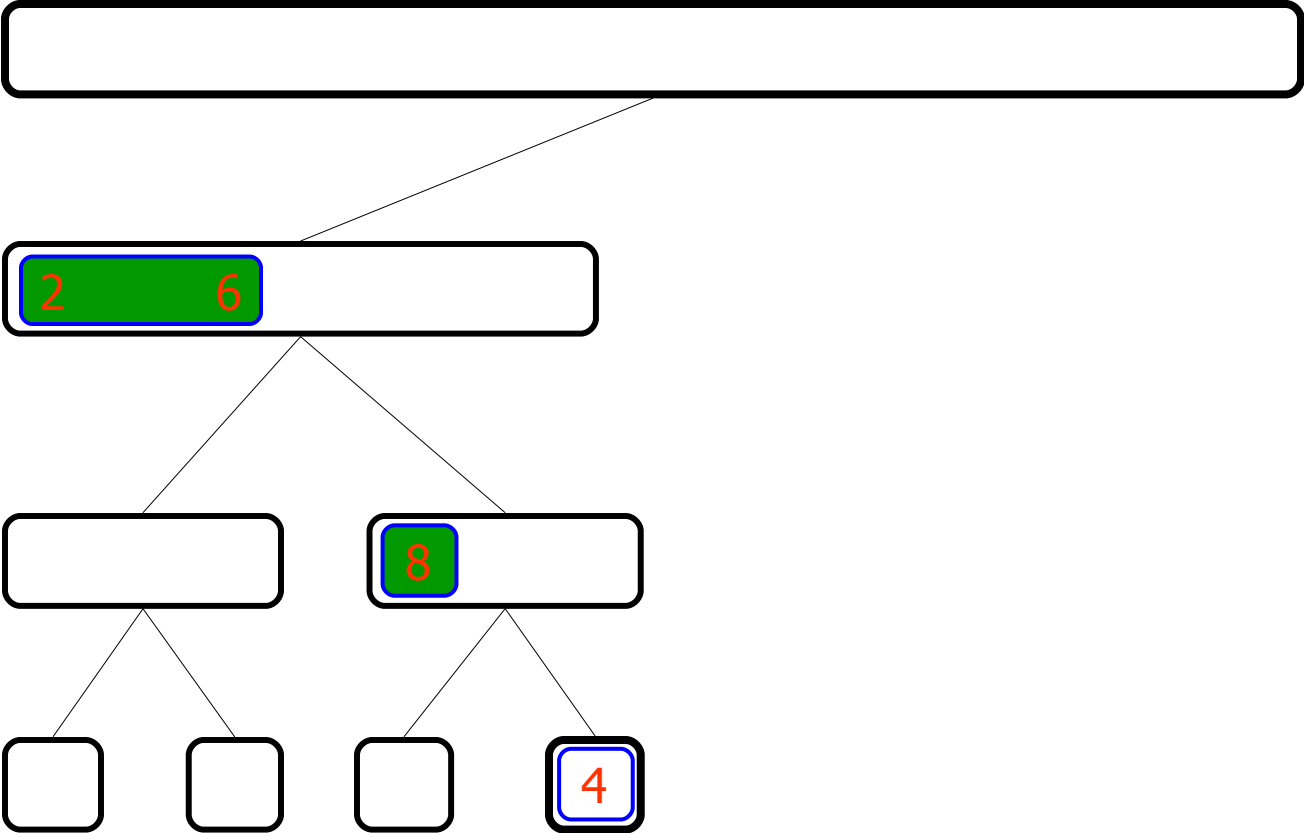
Merge-Sort(numbers, 2, 2), retorna



Merge-Sort(numbers, 0, 7)

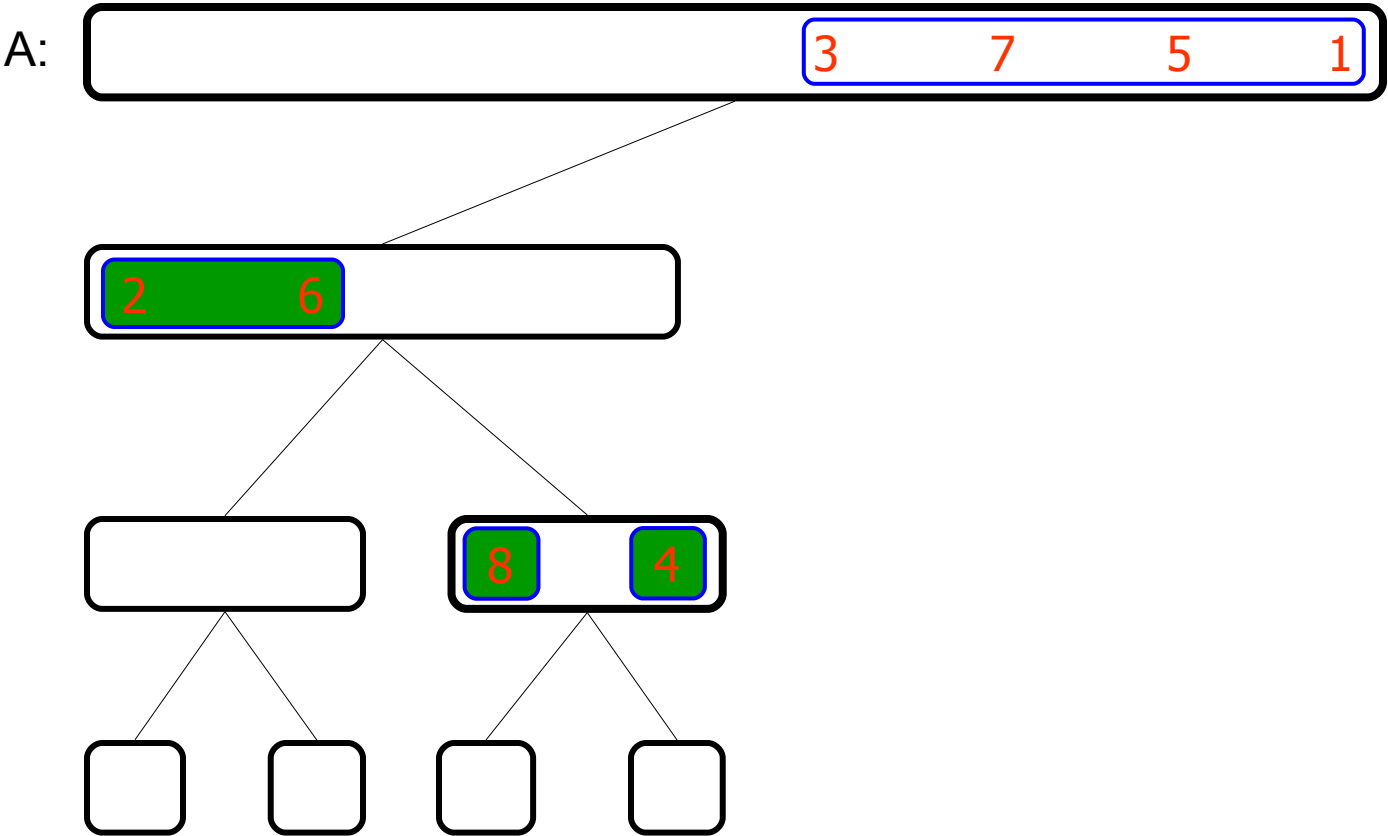
Merge-Sort(numbers, 3, 3), caso base

A:



Merge-Sort(numbers, 0, 7)

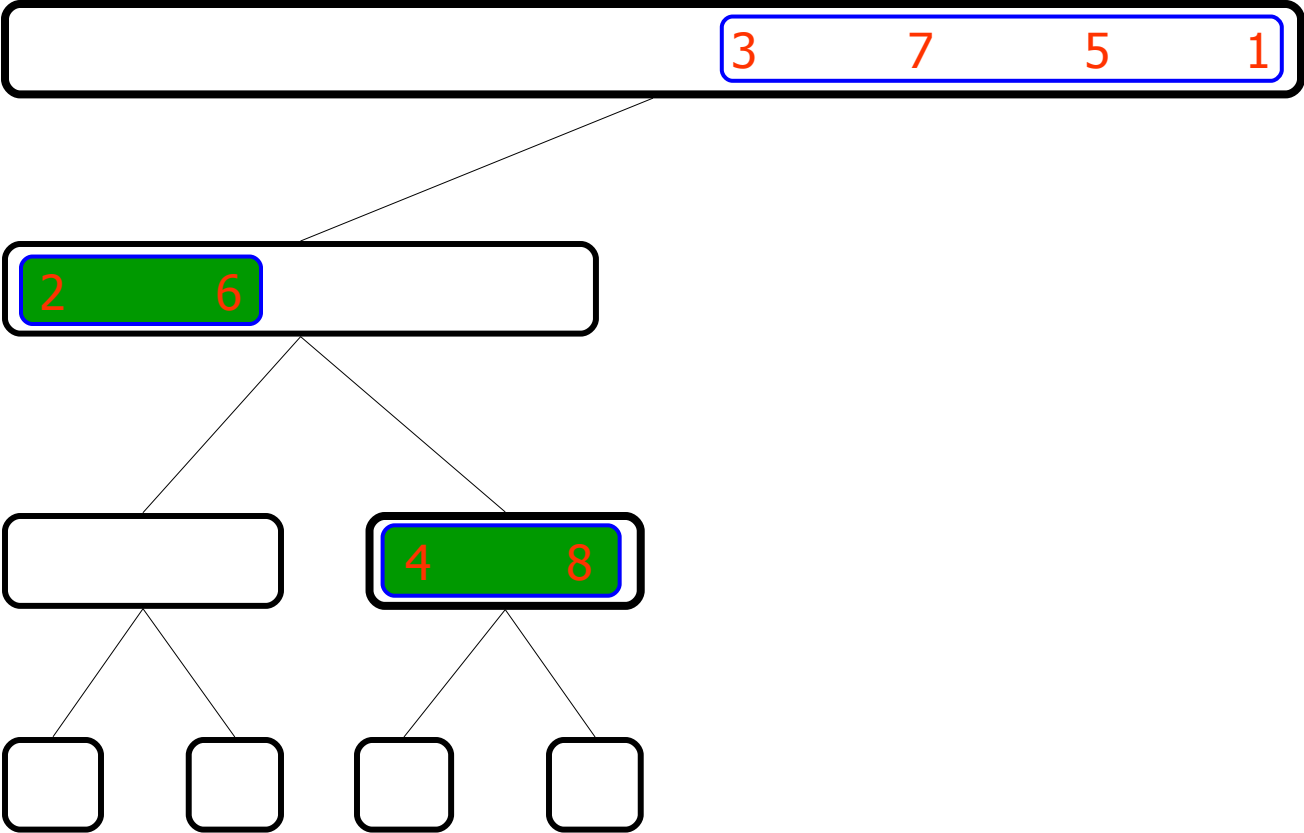
Merge-Sort(numbers, 3, 3), retorna



Merge-Sort(numbers, 0, 7)

Merge(numbers, 2, 2, 3)

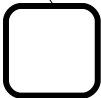
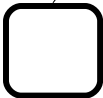
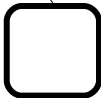
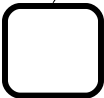
A:



Merge-Sort(numbers, 0, 7)

Merge-Sort(numbers, 2, 3), retorna

A:

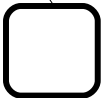
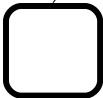
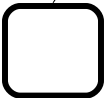




Merge-Sort(numbers, 0, 7)

Merge(numbers, 0, 1, 3)

A:

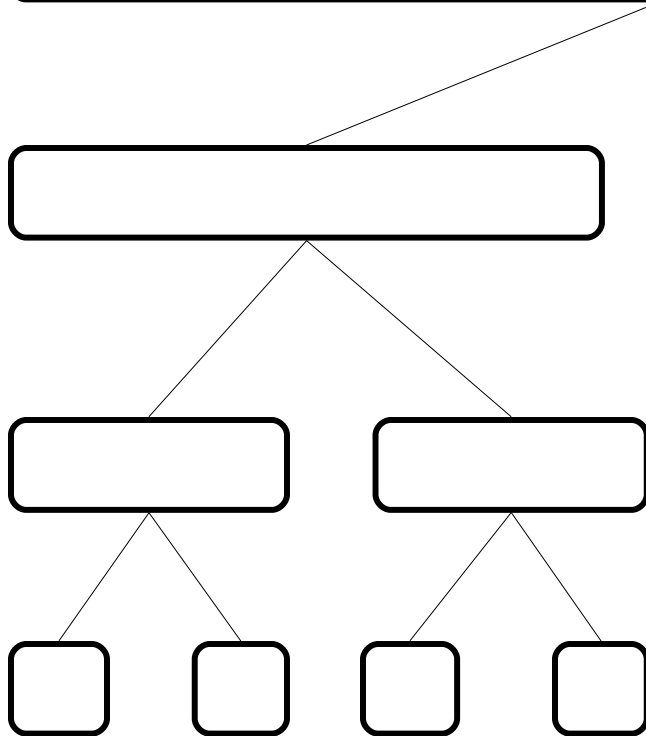


# Merge-Sort(numbers, 0, 7)

Merge-Sort(numbers, 0, 3), retorna

A: 

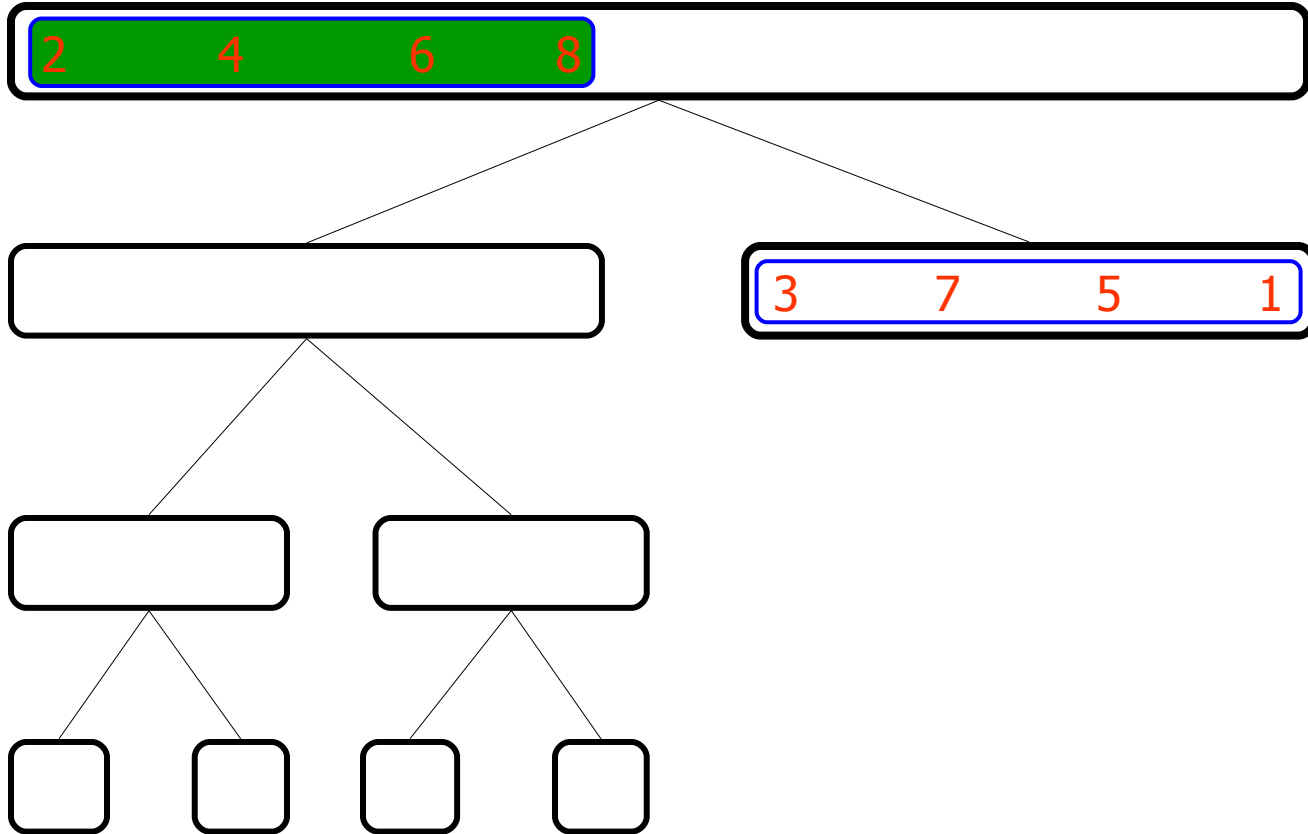
2	4	6	8	3	7	5	1
---	---	---	---	---	---	---	---



# Merge-Sort(numbers, 0, 7)

## Merge-Sort(numbers, 4, 7)

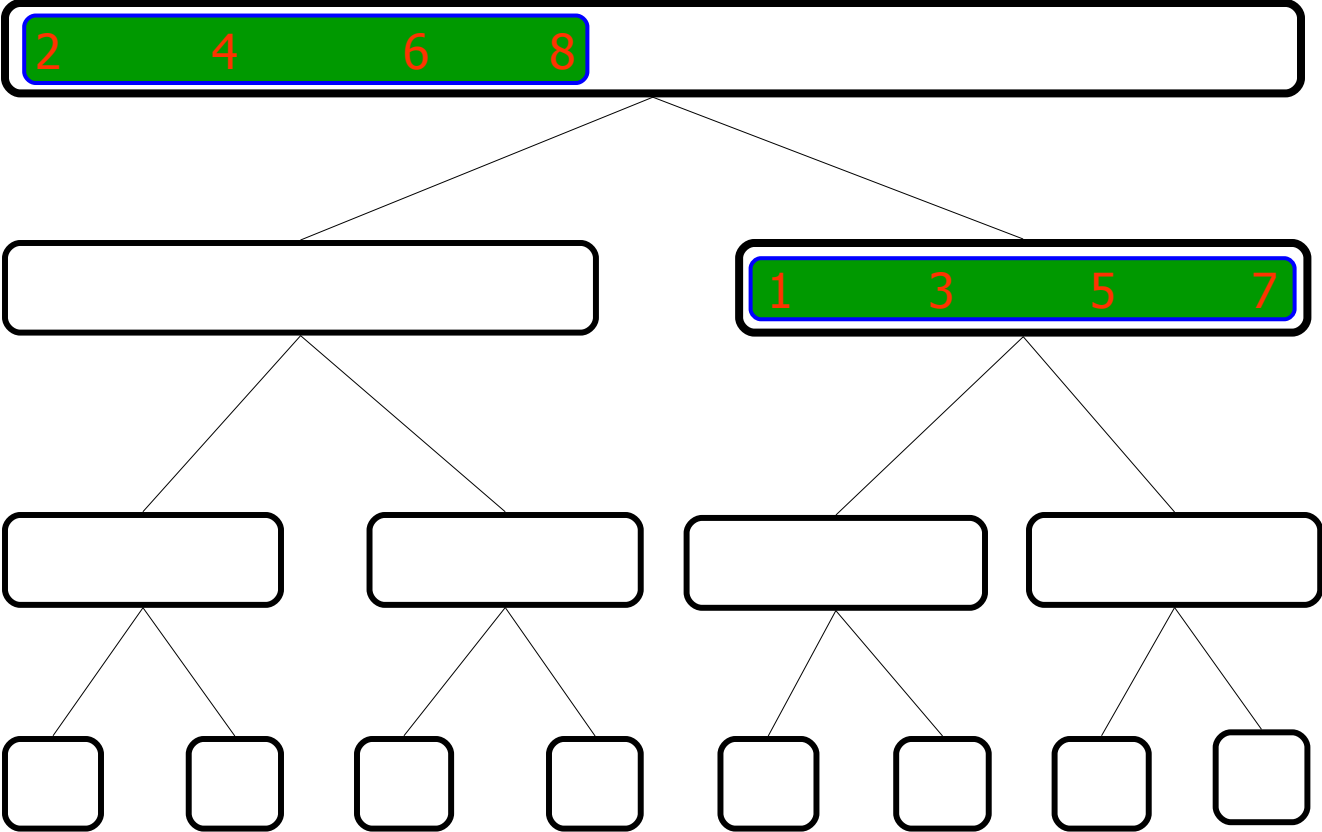
A:



# Merge-Sort(numbers, 0, 7)

Merge (numbers, 4, 5, 7)

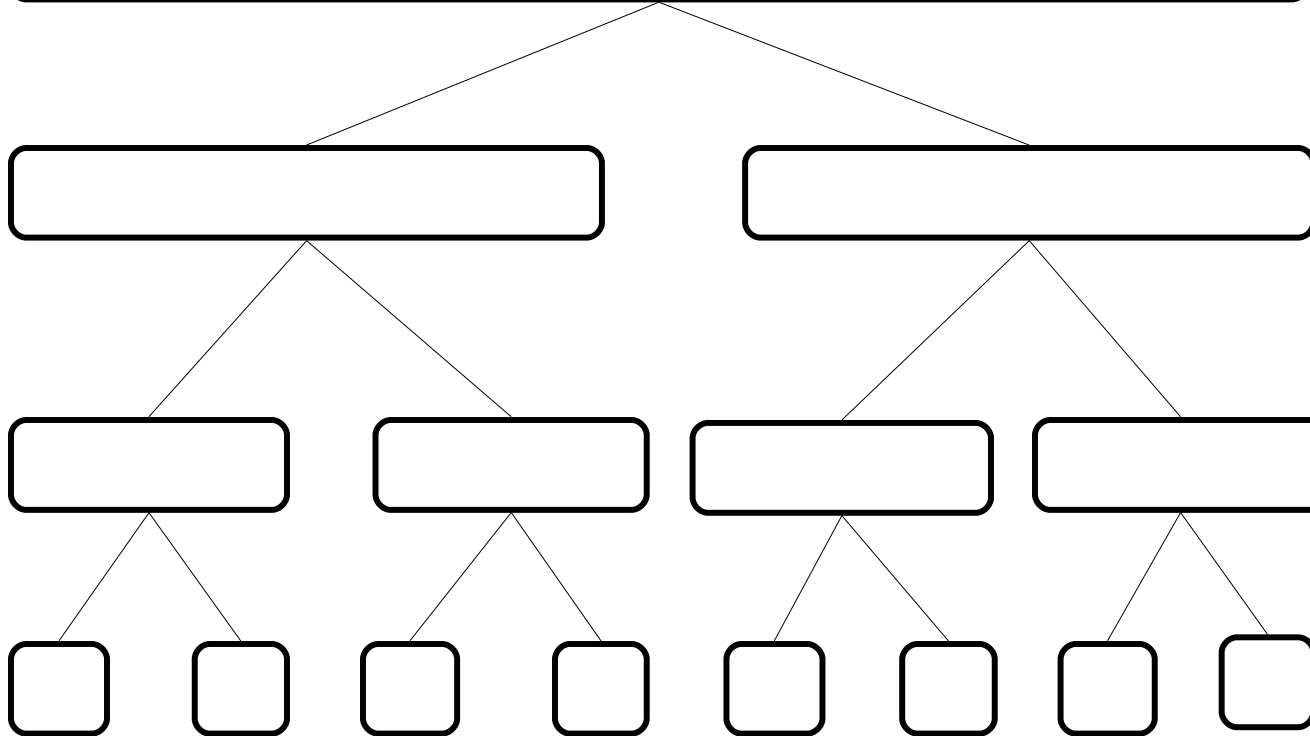
A:



# Merge-Sort(numbers, 0, 7)

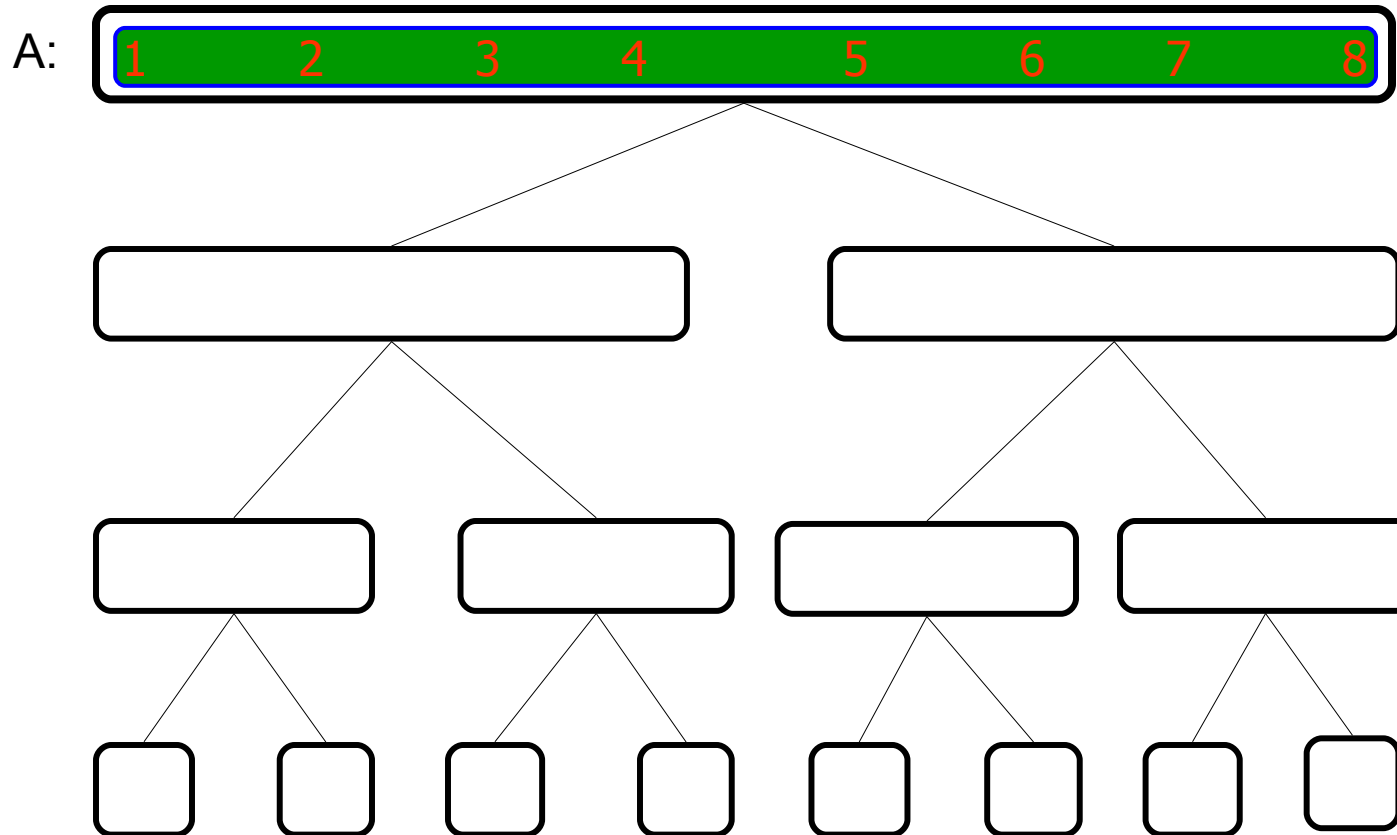
Merge-Sort(numbers, 4, 7), retorna

A:



# Merge-Sort(numbers, 0, 7)

Merge-Sort(numbers, 0, 7), Fim! Ordenado!



# Merge Sort: Algoritmo

Merge-Sort (numbers, esq, dir)

if  $\text{esq} \geq \text{dir}$  (Não faz Nada!)

else

meio  $\leftarrow \lfloor (\text{esq} + \text{dir}) / 2 \rfloor$

Merge-Sort(numbers, esq, meio)

Merge-Sort(numbers, meio+1, dir)

Merge(numbers, esq, meio, dir)



Chamada  
Recursiva

# Quick Sort

*Método da troca e partição*



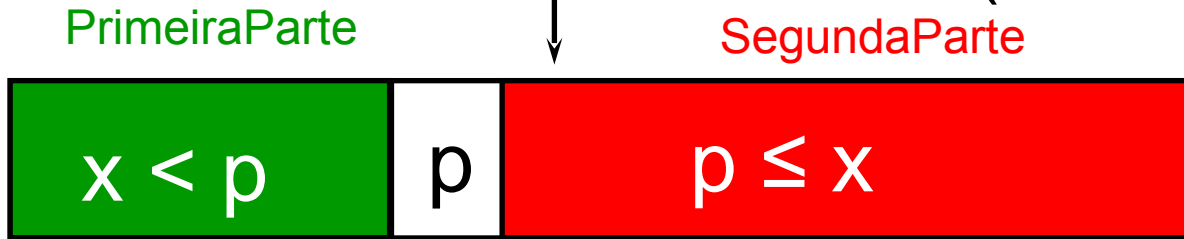
# Quick Sort

numbers:

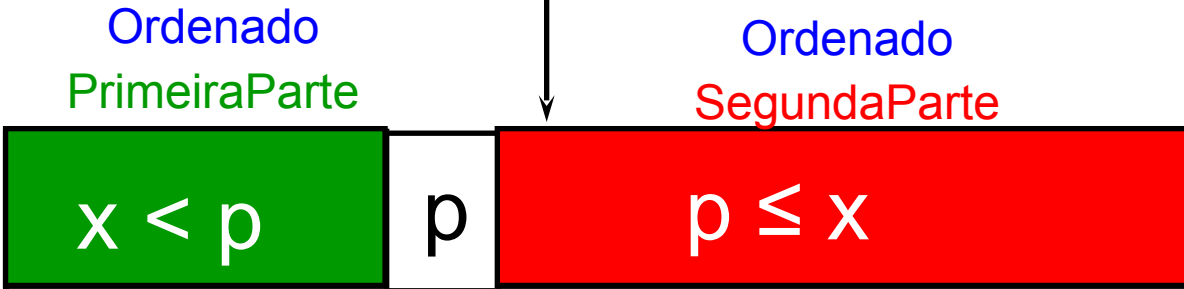
pivô



Particiona (Divide)



Chamada Recursiva



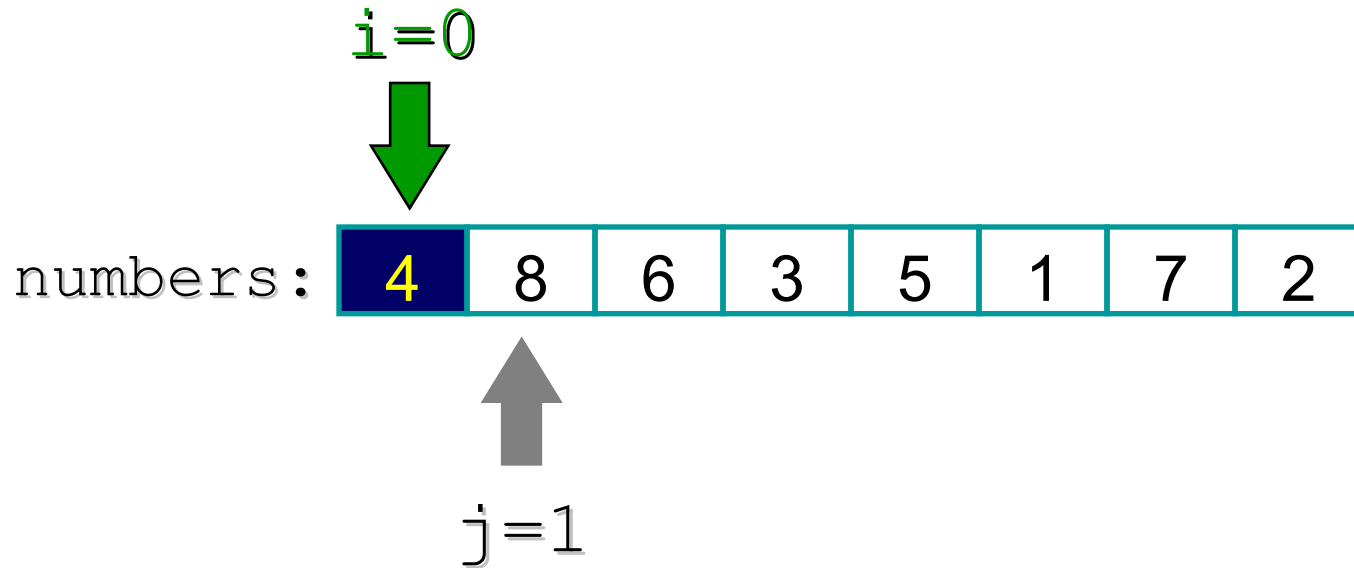
Ordenado

# Exemplo de como Particionar

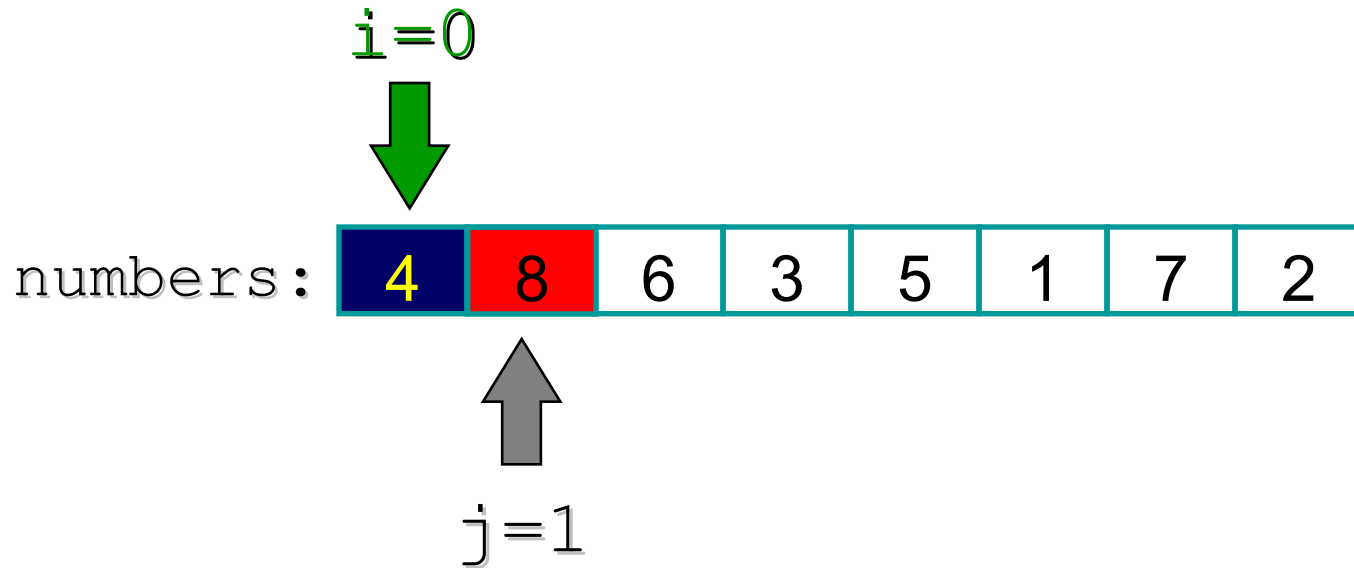
numbers:

4	8	6	3	5	1	7	2
---	---	---	---	---	---	---	---

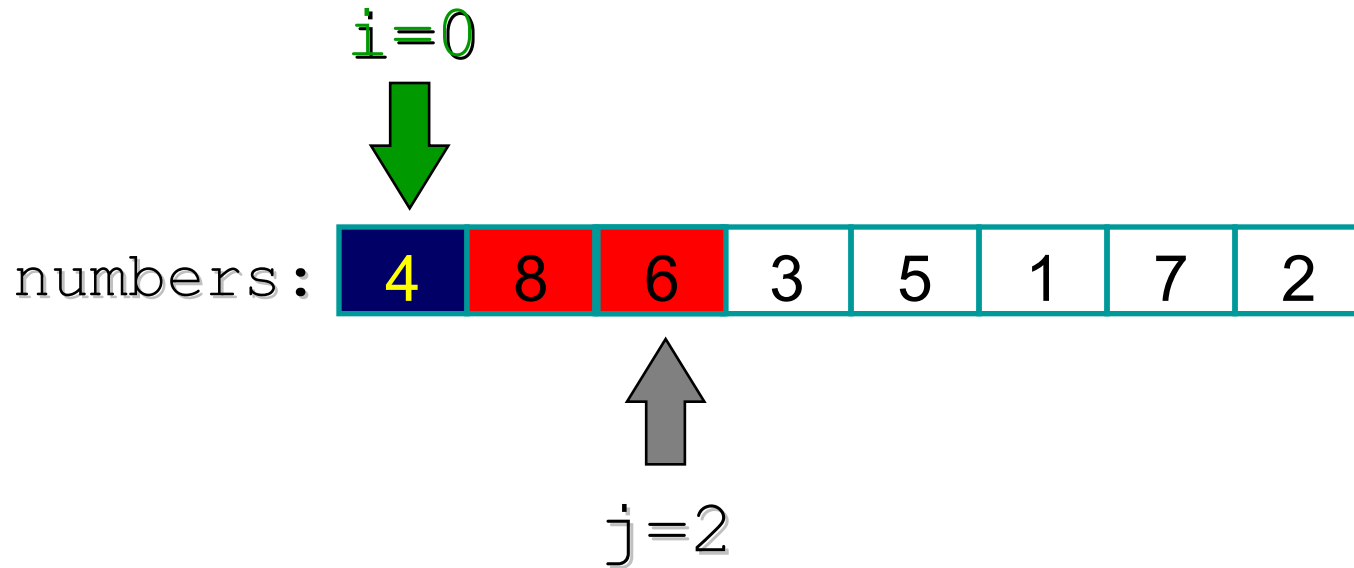
# Exemplo de como Particionar



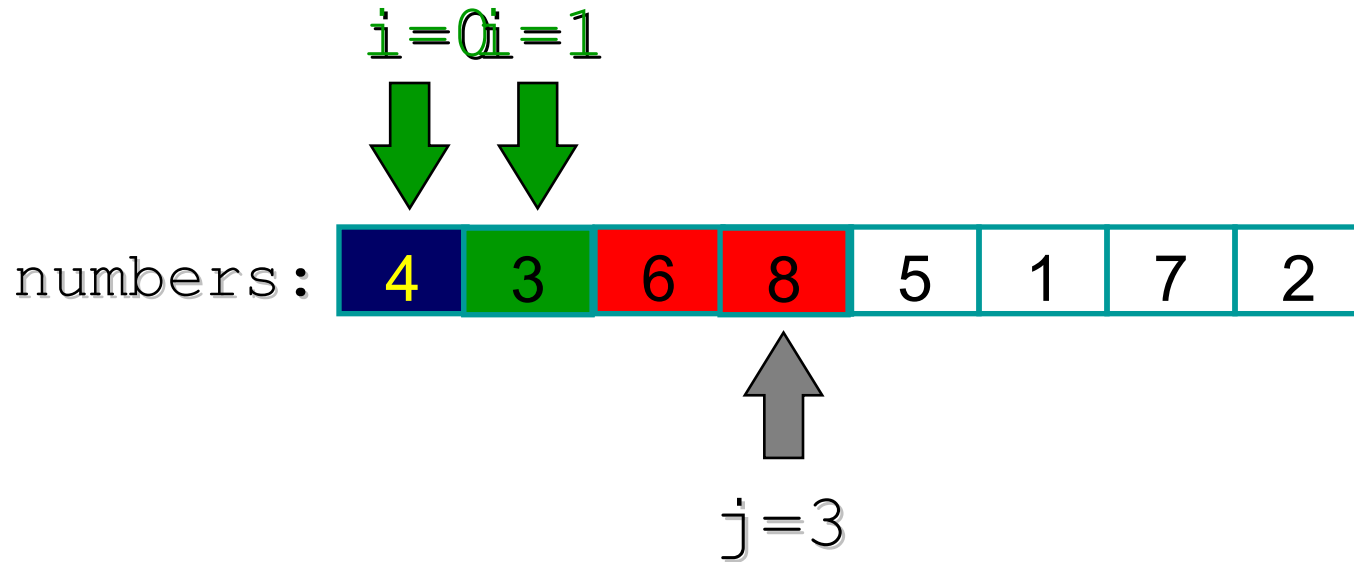
# Exemplo de como Particionar



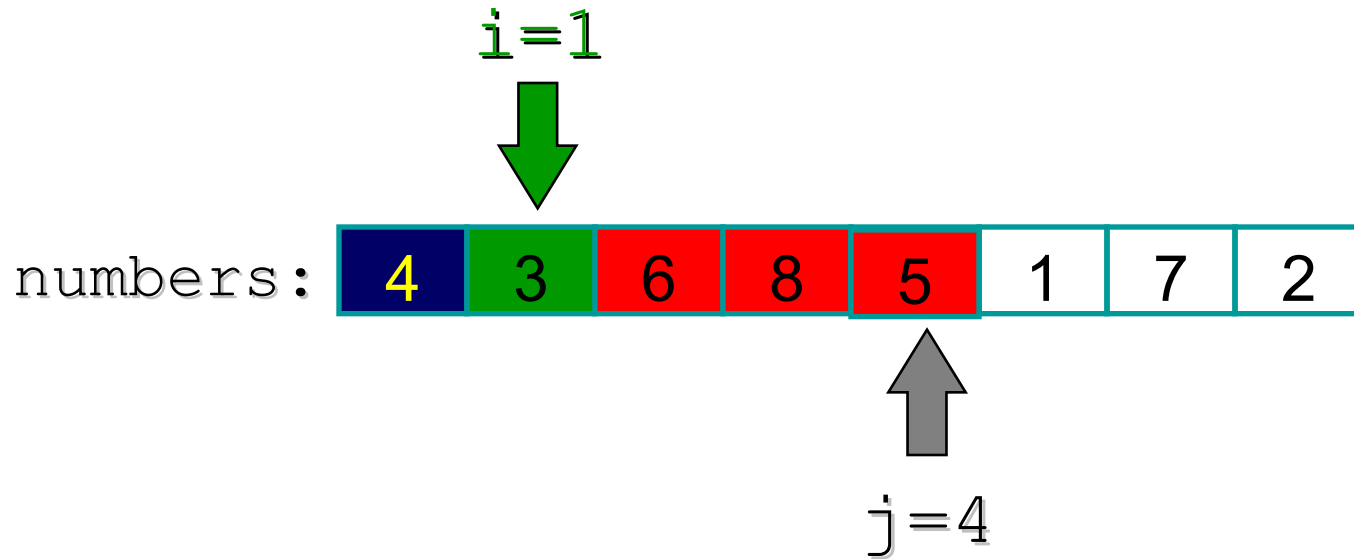
# Exemplo de como Particionar



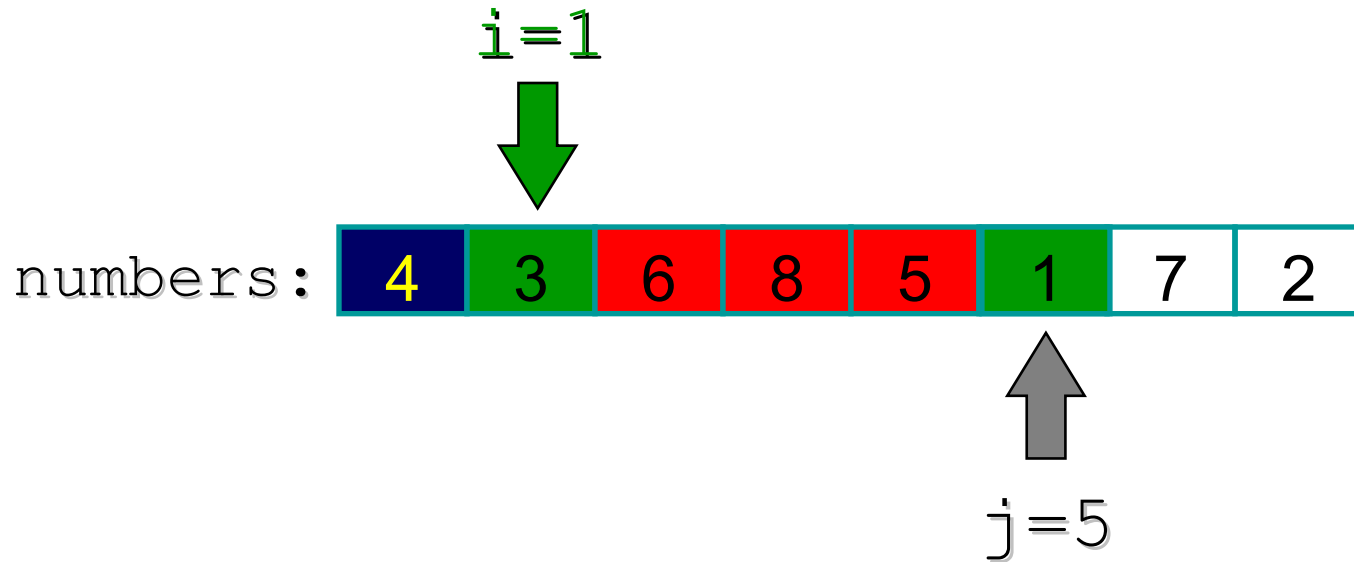
# Exemplo de como Particionar



# Exemplo de como Particionar

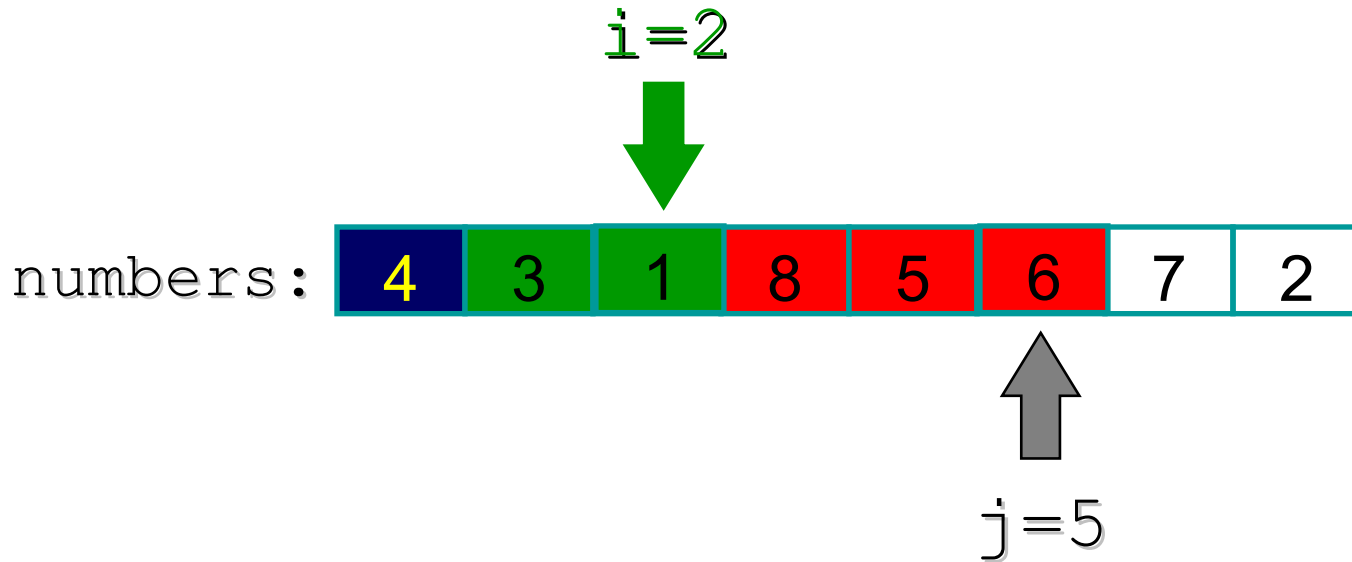


# Exemplo de como Particionar

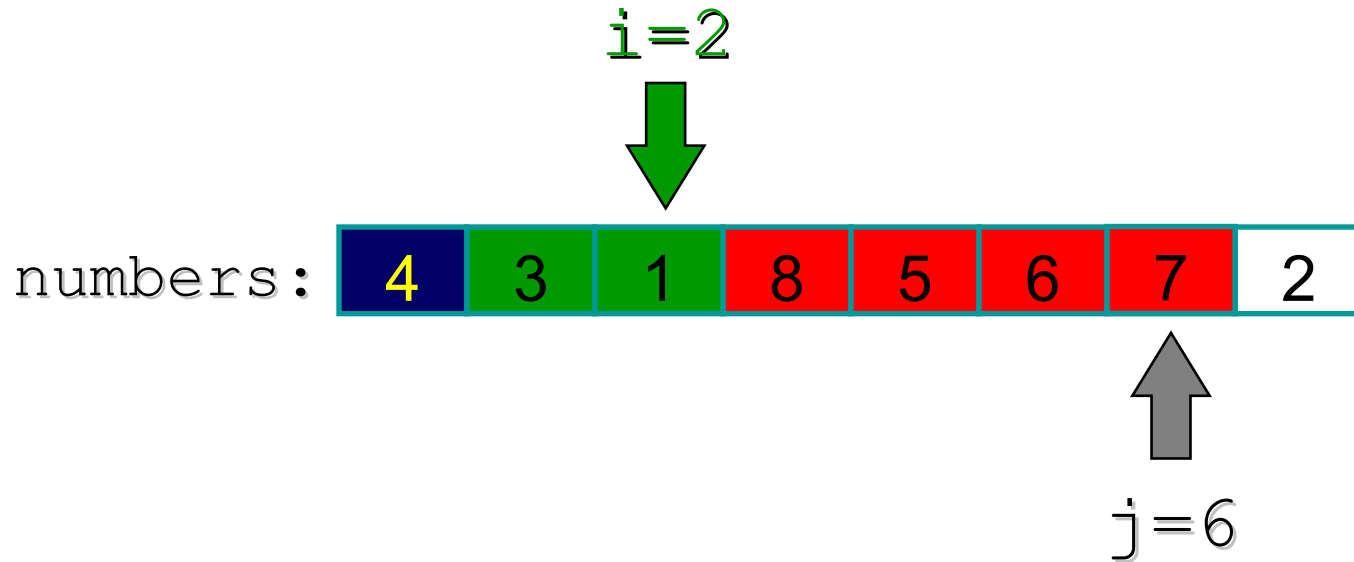




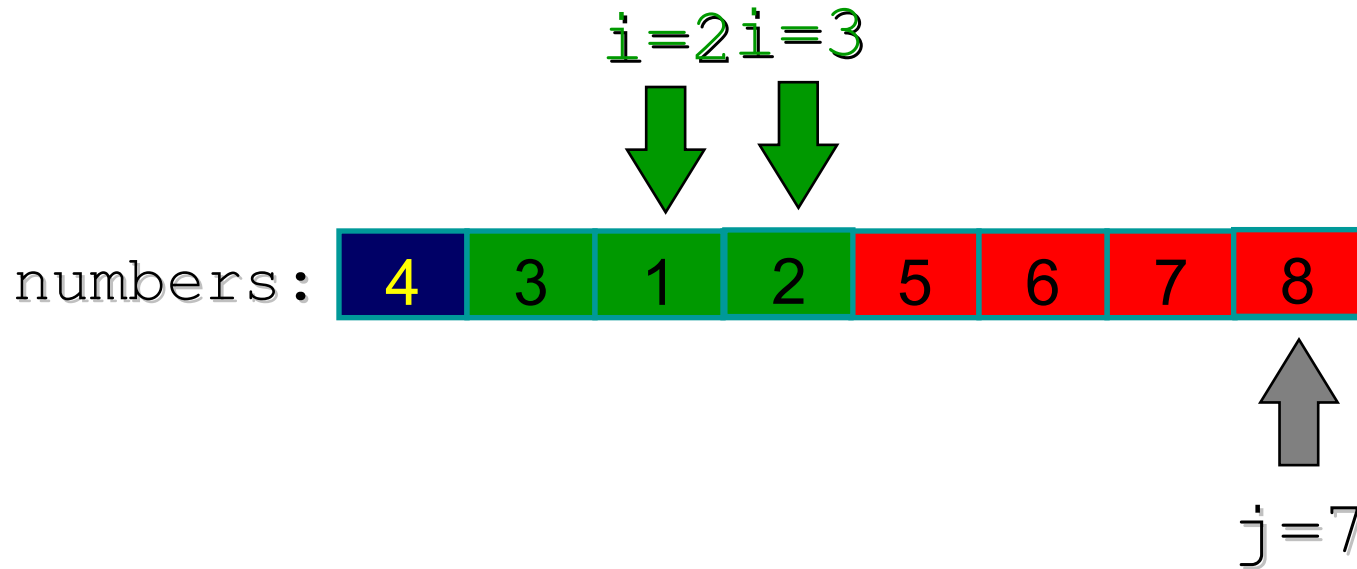
# Exemplo de como Particionar



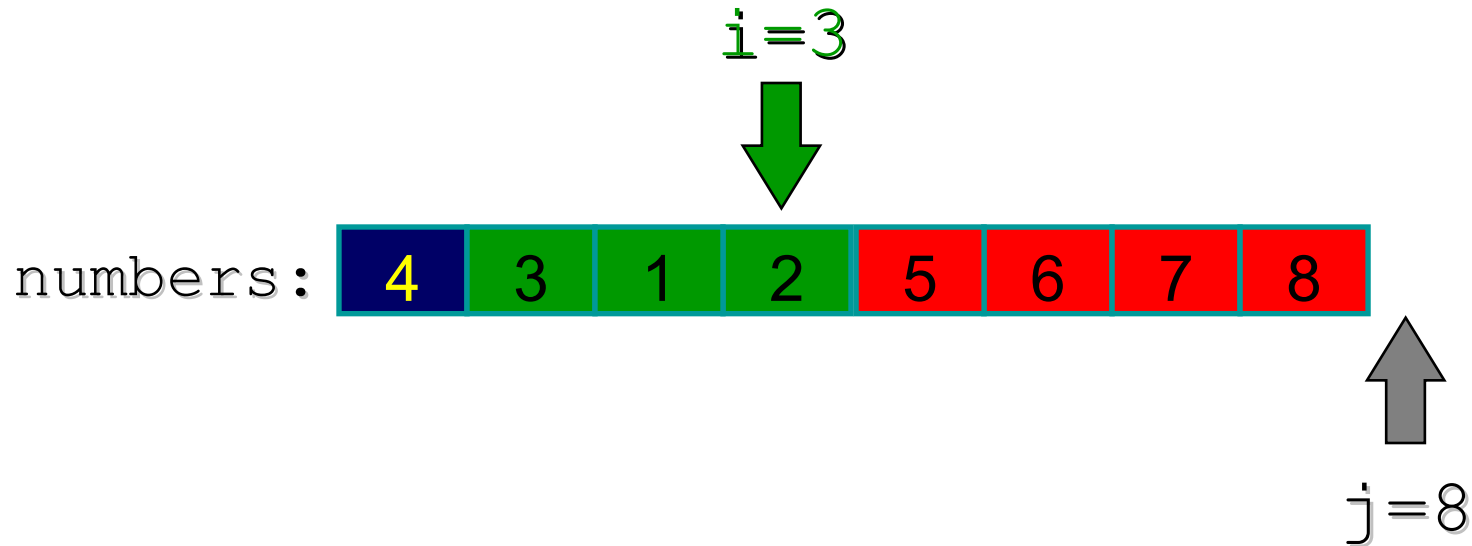
# Exemplo de como Particionar



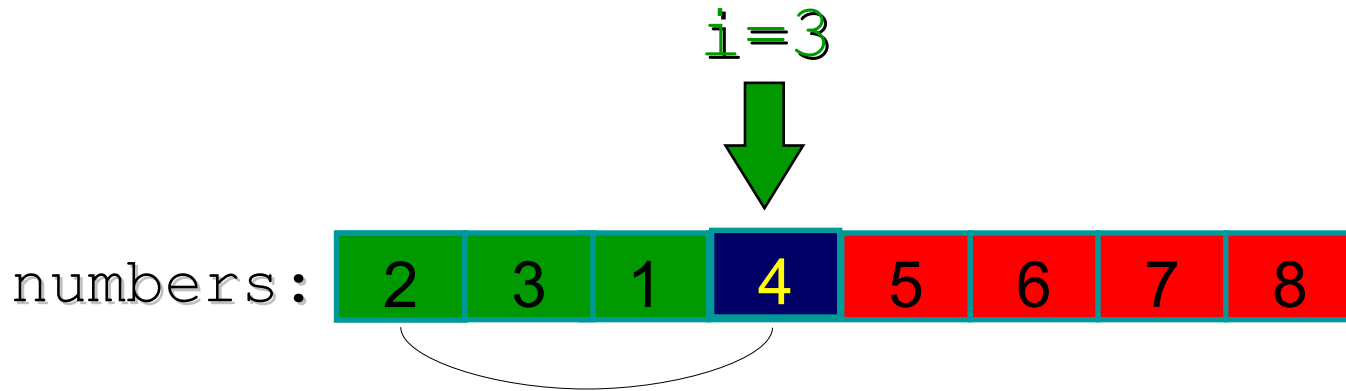
# Exemplo de como Particionar



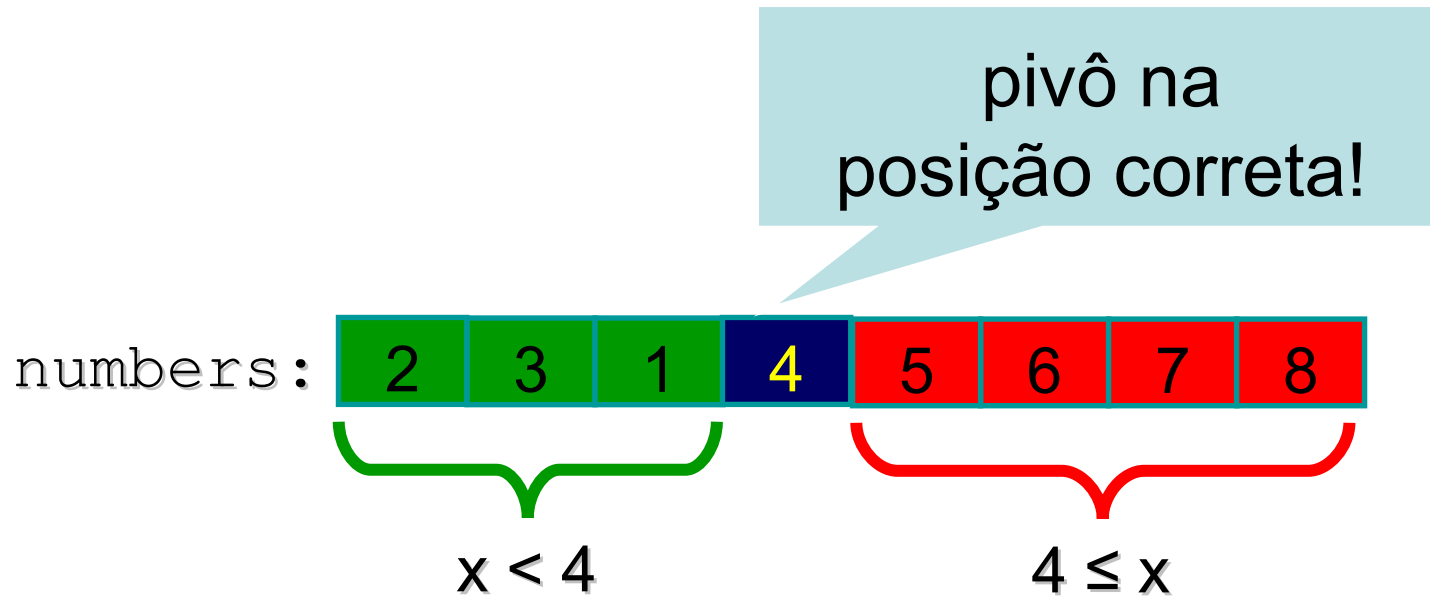
# Exemplo de como Particionar



# Exemplo de como Particionar



# Exemplo de como Particionar



particiona(numbers, esq, dir)

1.      $x \leftarrow \text{numbers}[\text{esq}]$

2.      $i \leftarrow \text{esq}$

3.     for  $j \leftarrow \text{esq}+1$  até dir

4.         if **numbers[j] < x** then

5.              $i \leftarrow i + 1$

6.             troque(numbers[i], numbers[j])

7.         end if

8.     end for j

9.     troque(numbers[i], numbers[esq])

10.    return i

# Quick-Sort(numbers, 0, 7)

Particiona

numbers:

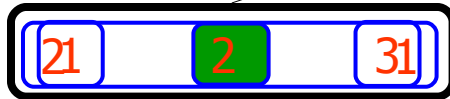




# Quick-Sort(numbers, 0, 7)

Quick-Sort(numbers, 0, 2) , particiona

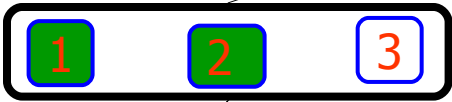
numbers:



# Quick-Sort(numbers, 0, 7)

Quick-Sort(numbers, 0, 0) , return base

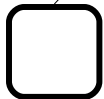
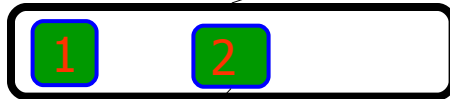
numbers:



# Quick-Sort(numbers, 0, 7)

Quick-Sort(numbers, 1, 1) , caso base

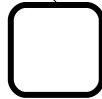
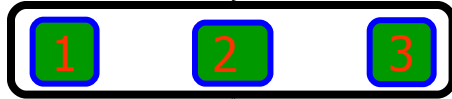
numbers:



# Quick-Sort(numbers, 0, 7)

Quick-Sort(numbers, 0, 2), retorna

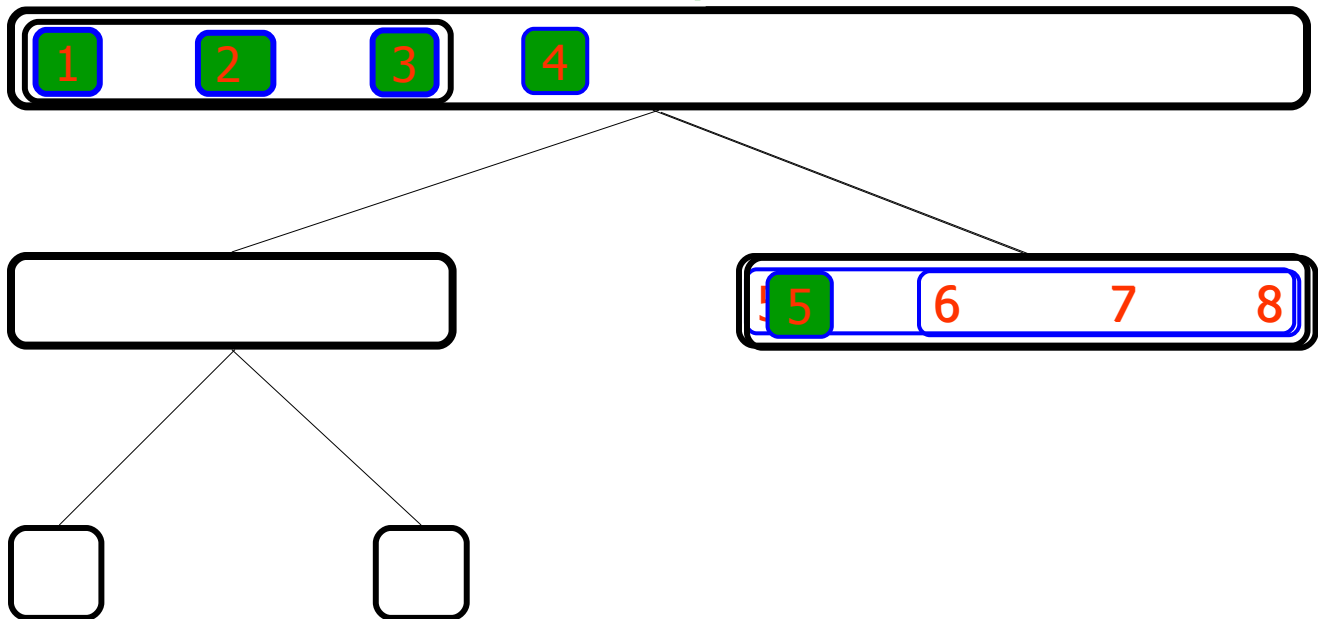
numbers:



# Quick-Sort(numbers, 0, 7)

Quick-Sort(numbers, 4, 7) , particiona

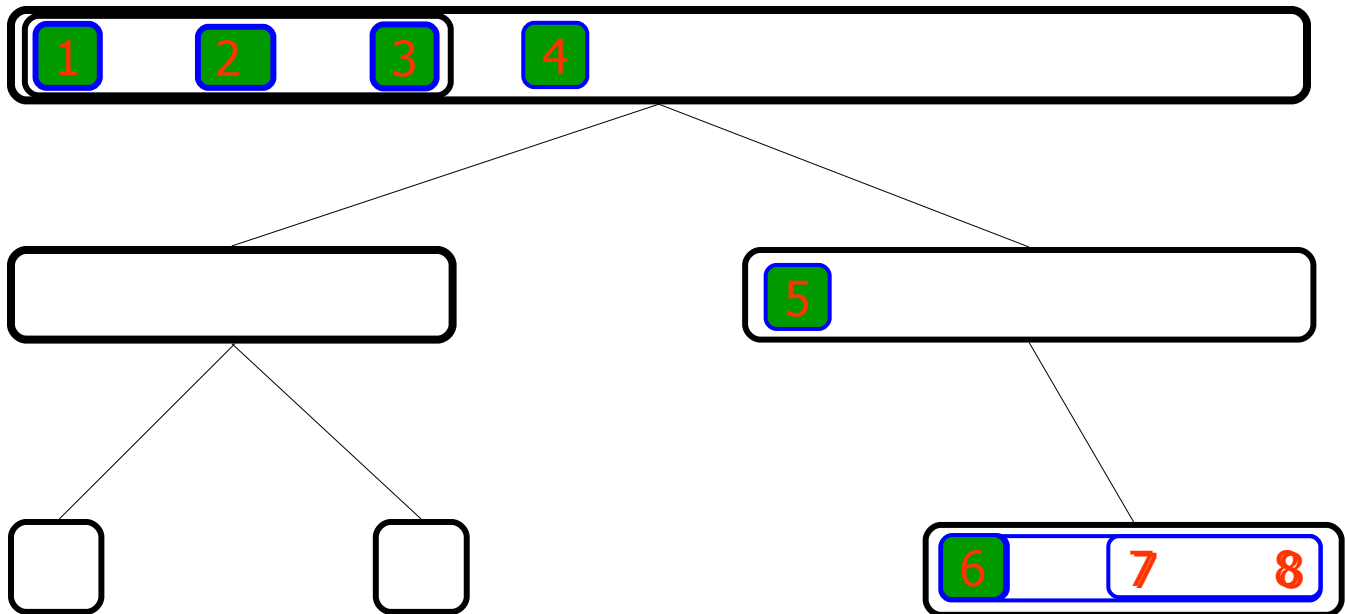
numbers:



# Quick-Sort(numbers, 0, 7)

Quick-Sort(numbers, 5, 7) , particiona

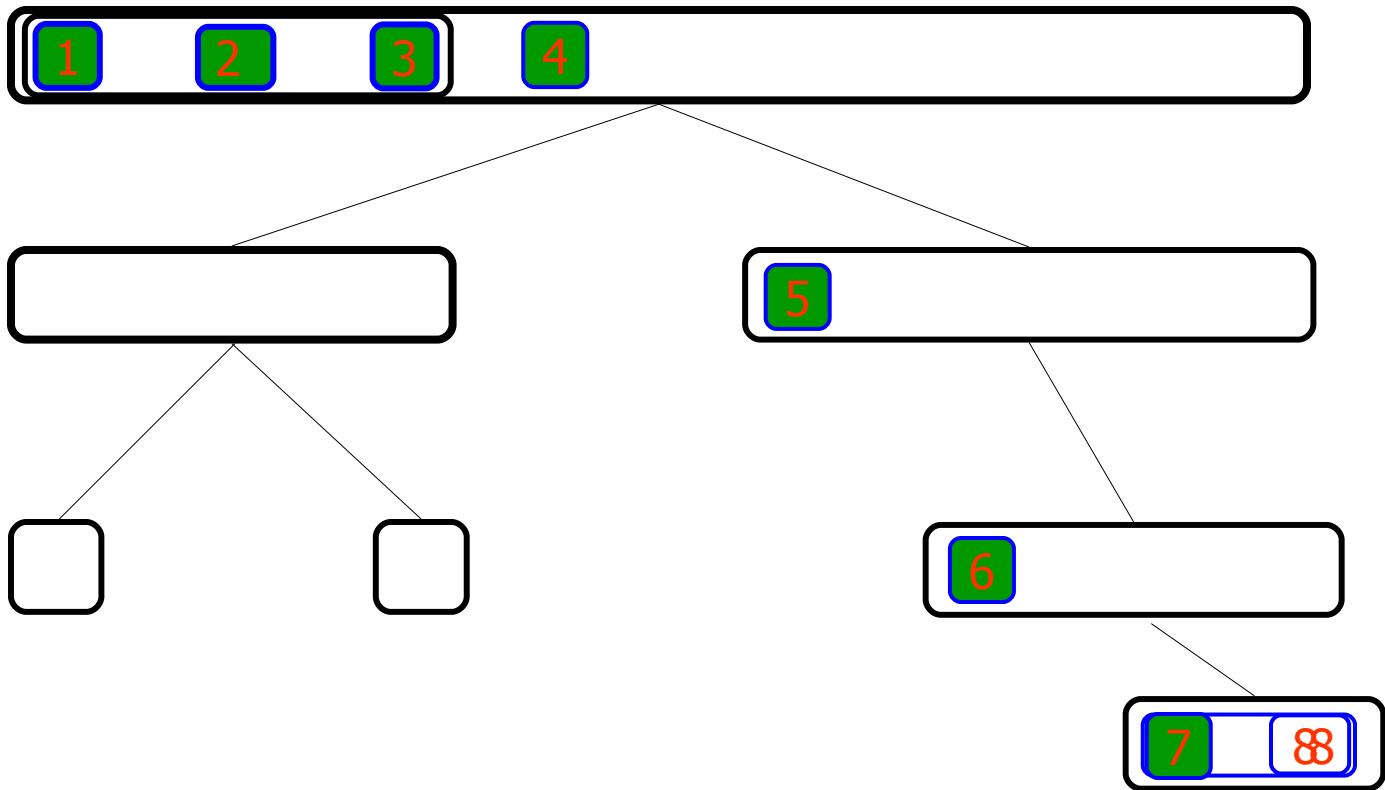
numbers:



# Quick-Sort(numbers, 0, 7)

Quick-Sort(numbers, 6, 7) , particiona

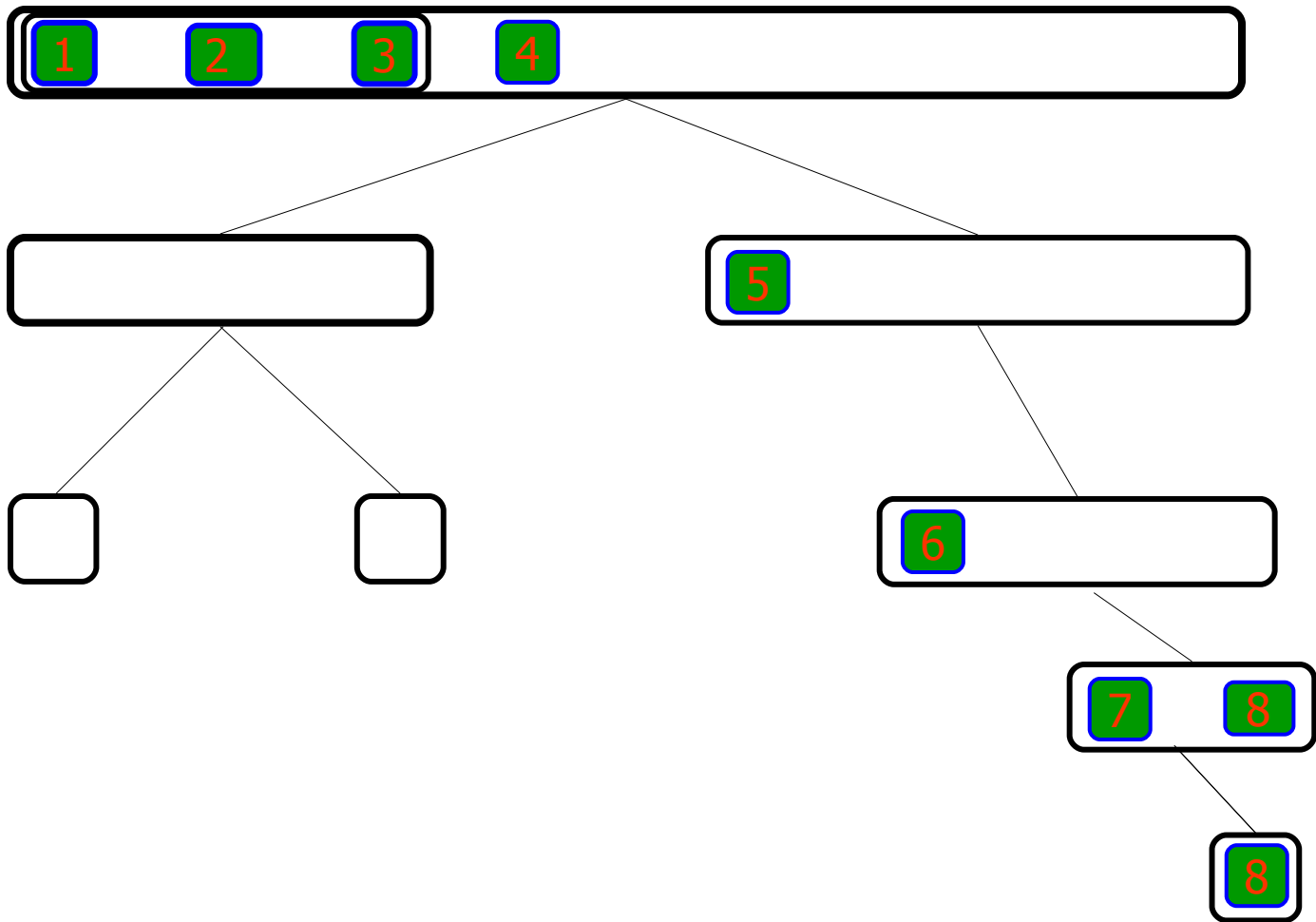
numbers:



# Quick-Sort(numbers, 0, 7)

Quick-Sort(numbers, 7, 7) , recursive base

numbers:

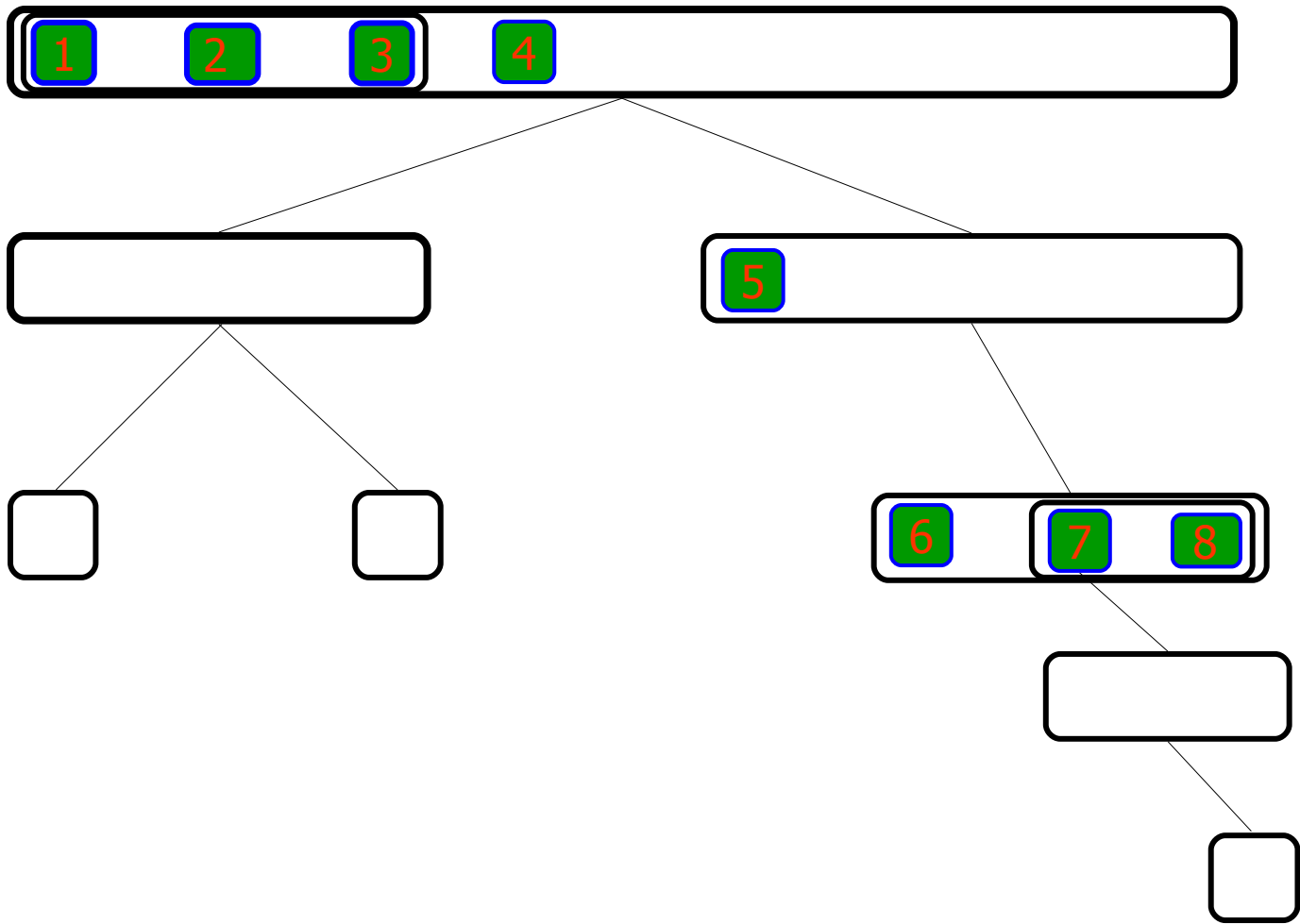




# Quick-Sort(numbers, 0, 7)

Quick-Sort(numbers, 6, 7) , retorna

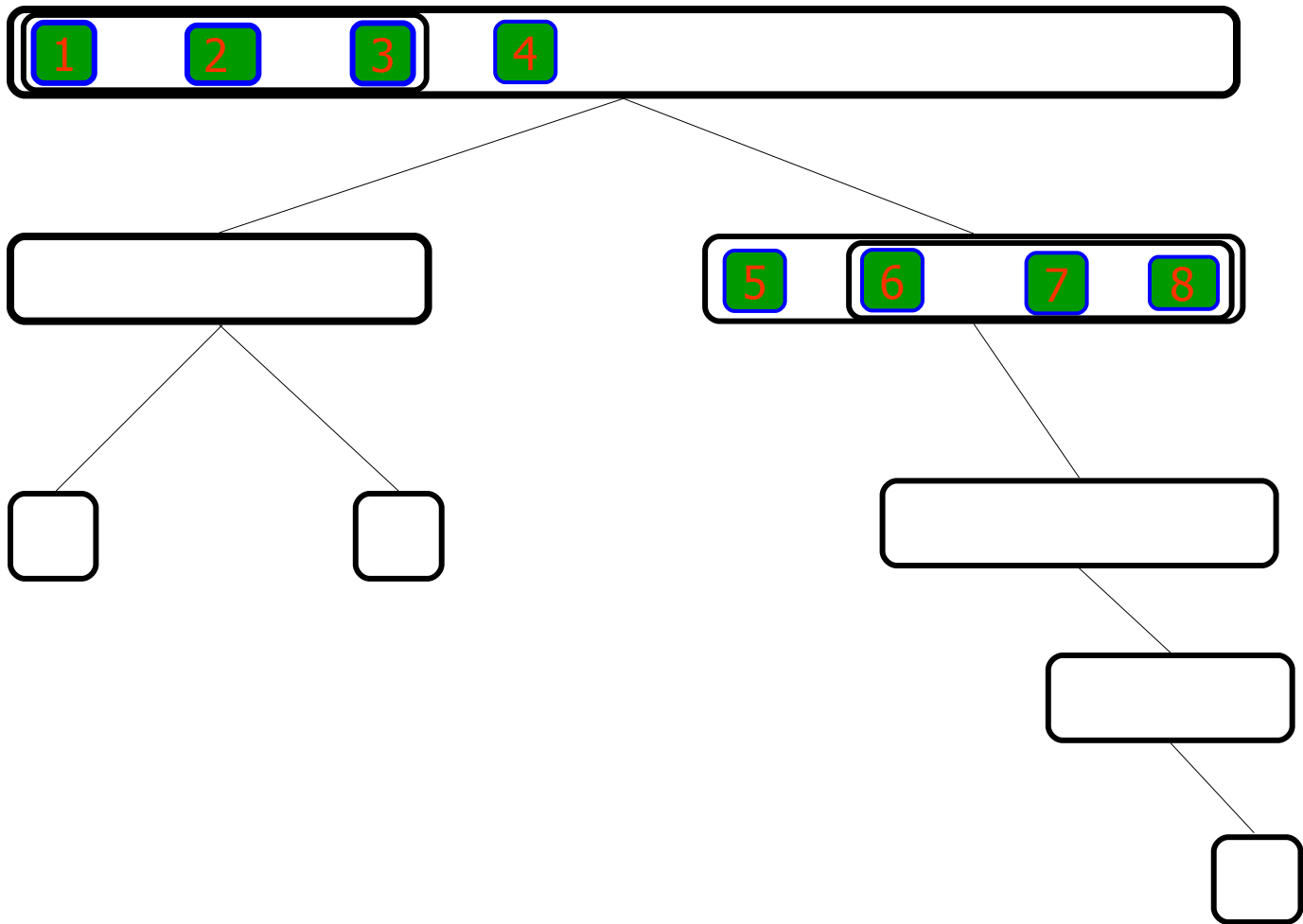
numbers:



# Quick-Sort(numbers, 0, 7)

Quick-Sort(numbers, 5, 7) , retorna

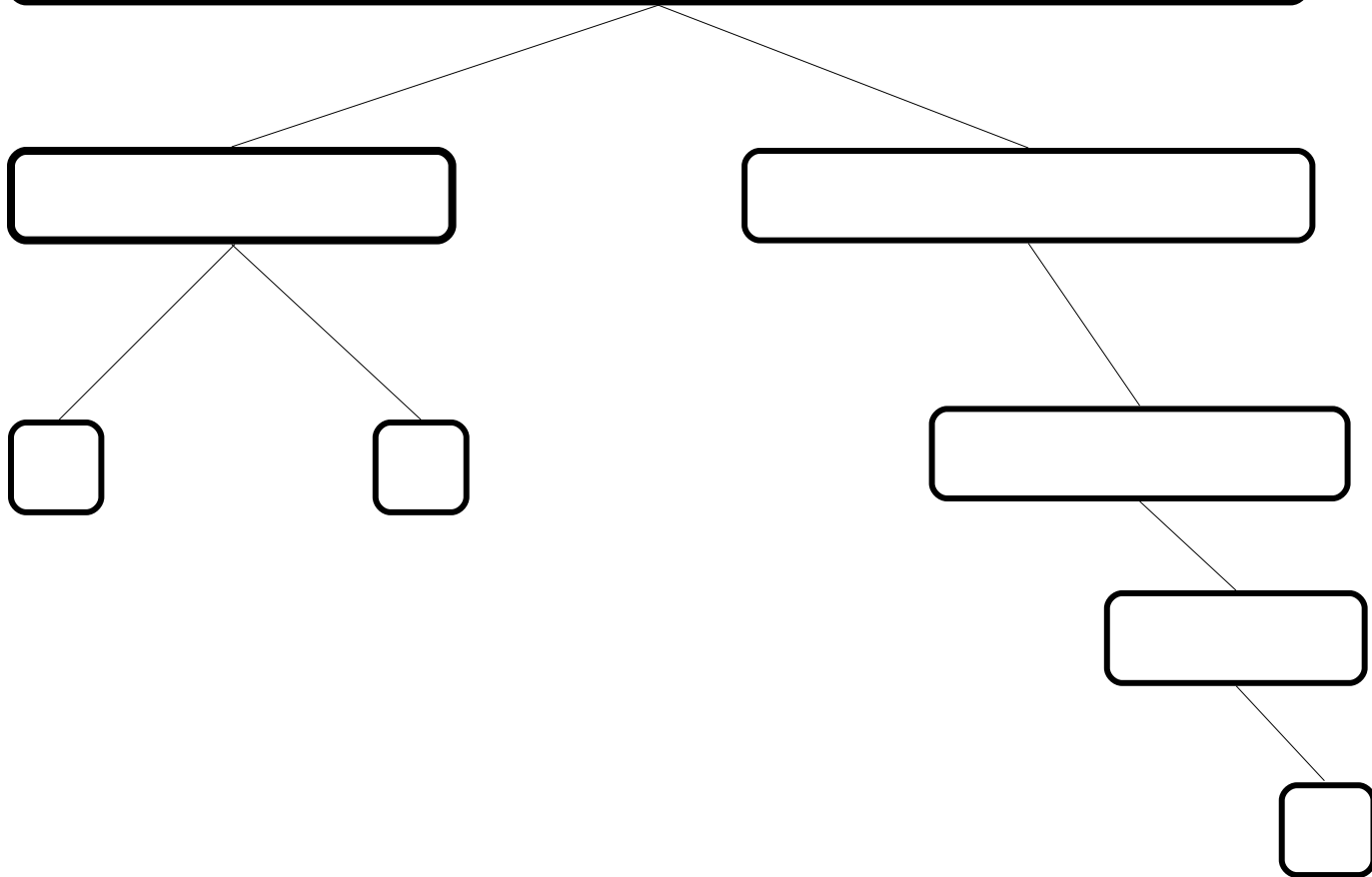
numbers:



# Quick-Sort(numbers, 0, 7)

Quick-Sort(numbers, 4, 7) , retorna

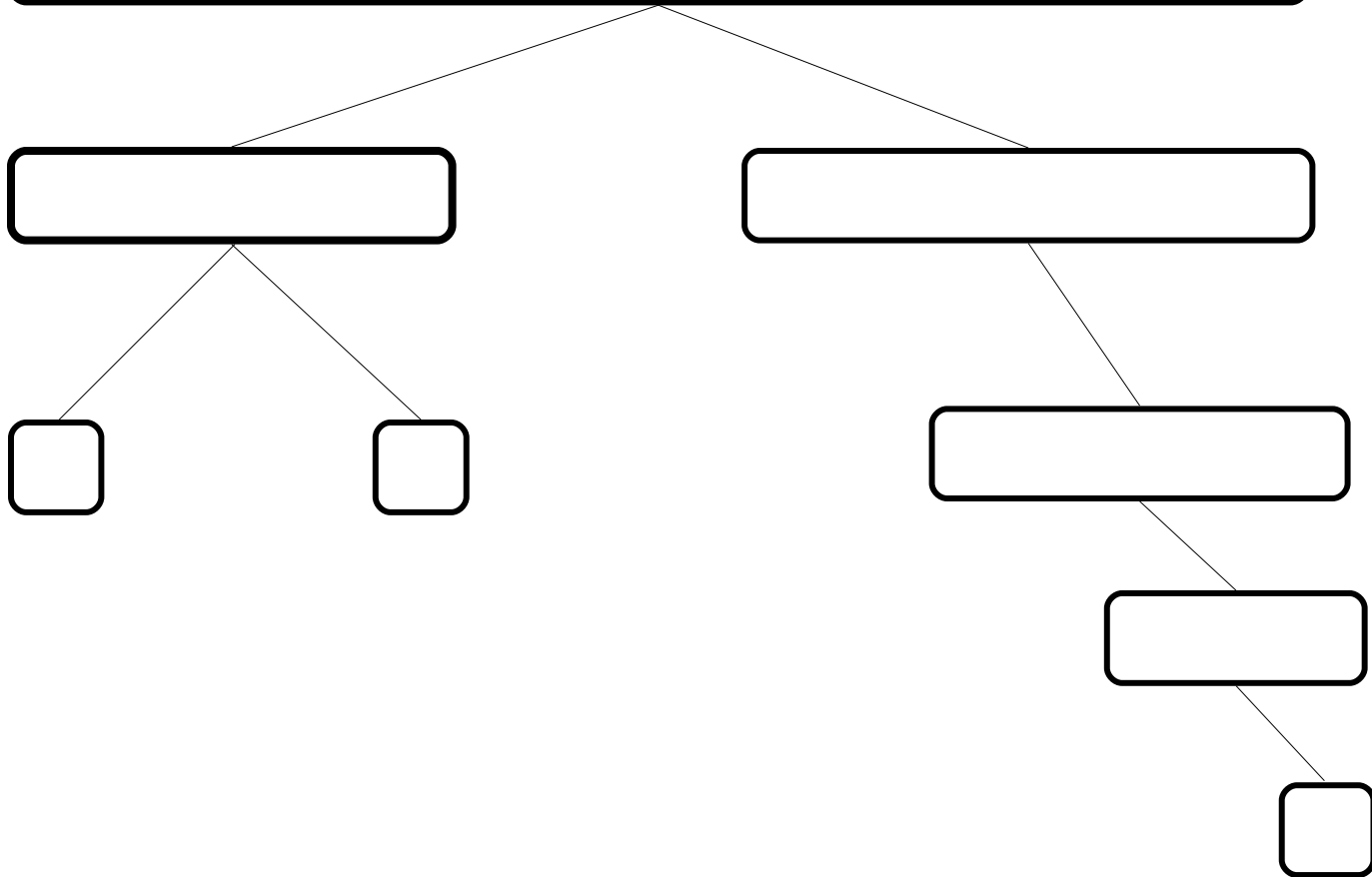
numbers:



# Quick-Sort(numbers, 0, 7)

Quick-Sort(numbers, 0, 7) , Fim! Ordenado!

numbers:



# Quick Sort

```
Quick-Sort(numbers, esq, dir)
```

```
  if      esq  $\geq$  dir (Não faz Nada! – Ordenado!)
```

```
  else
```

```
    pivo  $\leftarrow$  Particiona(numbers, esq, dir)
```

```
    Quick-Sort(numbers, esq, pivo-1 )
```

```
    Quick-Sort(numbers, pivo+1, dir)
```

```
  end if
```

# Heap Sort

*Seleção em árvore*

Até a próxima...