## Exercicio 4.R

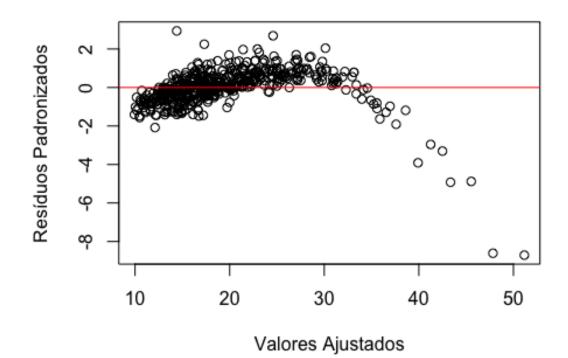
joaopaulodecker

2025-10-14

```
# A - Amostra
base = read.csv2("selecao.csv")
set.seed(07052006)
base1 = base[sample(nrow(base), 500),]
# B - Seleção de variáveis - método backward
mc=lm( y ~ ., data=base1)
backward_model=step(mc, direction = "backward")
## Start: AIC=956.74
## y \sim x1 + x2 + x3 + x4 + x5 + x6 + x7 + x8 + x9 + x10
##
##
## Step: AIC=956.74
## y \sim x1 + x2 + x3 + x4 + x5 + x6 + x7 + x8 + x10
##
##
         Df Sum of Sq
                         RSS
                                 AIC
## <none>
                      3255.4 956.74
## - x2
                13.45 3268.9 956.80
          1
## - x3
                13.49 3268.9 956.81
         1
          1
## - x5
               32.10 3287.5 959.64
## - x1 1
              45.68 3301.1 961.70
## - x6
               54.75 3310.2 963.08
          1
## - x4
          1
               66.66 3322.1 964.87
          1 467.93 3723.4 1021.89
## - x8
## - x10
          1
              878.10 4133.5 1074.14
## - x7
          1 2936.73 6192.2 1276.22
summary(backward_model)
##
## Call:
## lm(formula = y \sim x1 + x2 + x3 + x4 + x5 + x6 + x7 + x8 + x10,
##
      data = base1)
##
## Residuals:
       Min
                 10
                      Median
                                   3Q
                                           Max
                      0.1288
                                        7.2920
## -21.7933 -1.1019
                               1.4379
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.330105 1.755205 -0.188 0.85090
```

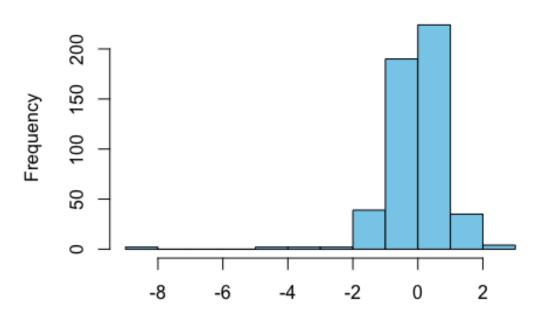
```
## x1
               -0.001888
                           0.000720
                                     -2.622
                                             0.00901 **
## x2
                0.397672
                           0.279450
                                      1.423
                                             0.15536
                                     -1.425
## x3
               -0.001667
                           0.001169
                                             0.15473
                           0.024751
               -0.078398
                                     -3.167
                                             0.00163 **
## x4
                                      2.198
## x5
                0.169575
                           0.077149
                                             0.02841 *
                0.086940
                           0.030286
                                      2.871
                                             0.00427 **
## x6
## x7
                0.725019
                           0.034485
                                     21.024 < 2e-16
## x8
                0.285508
                           0.034020
                                      8.392 5.14e-16
                2.693361
                           0.234277
                                     11.496 < 2e-16 ***
## x10
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 2.578 on 490 degrees of freedom
## Multiple R-squared: 0.8696, Adjusted R-squared: 0.8672
## F-statistic: 363.1 on 9 and 490 DF, p-value: < 2.2e-16
# C - Análise de resíduos
plot(fitted(backward model), rstandard(backward model),
     main = "Gráfico de Resíduos do Modelo Original",
     xlab = "Valores Ajustados",
     ylab = "Resíduos Padronizados")
abline(h = 0, col = "red")
```

#### Gráfico de Resíduos do Modelo Original



```
# Histograma dos resíduos
hist(rstandard(backward_model),
    main = "Histograma dos Resíduos Padronizados",
    xlab = "Resíduo Padronizado",
    col = "skyblue")
```

#### Histograma dos Resíduos Padronizados



Resíduo Padronizado

```
# foi verificada a possibilidade de variáveis quadráticas
# D - backward com variáveis quadráticas
mcq = 1m(y \sim x1 + x2 + x3 + x4 + x5 + x6 + x7 + x8 + x9 + x10 + 
                                               I(x1^2) + I(x2^2) + I(x3^2) + I(x4^2) + I(x5^2) +
                                               I(x6^2) + I(x7^2) + I(x8^2) + I(x9^2) + I(x10^2),
                                       data = base1)
backward_model_quad = step(mcq, direction = "backward")
## Start: AIC=-806.71
## y \sim x1 + x2 + x3 + x4 + x5 + x6 + x7 + x8 + x9 + x10 + I(x1^2) +
                             I(x2^2) + I(x3^2) + I(x4^2) + I(x5^2) + I(x6^2) + I(x7^2) +
##
                              I(x8^2) + I(x9^2) + I(x10^2)
##
##
## Step: AIC=-806.71
## y \sim x1 + x2 + x3 + x4 + x5 + x6 + x7 + x8 + x9 + x10 + I(x1^2) +
```

```
I(x2^2) + I(x3^2) + I(x4^2) + I(x5^2) + I(x6^2) + I(x7^2) +
##
       I(x8^2) + I(x9^2)
##
##
##
## Step: AIC=-806.71
## y \sim x1 + x2 + x3 + x4 + x5 + x6 + x7 + x8 + x10 + I(x1^2) + I(x2^2) +
       I(x3^2) + I(x4^2) + I(x5^2) + I(x6^2) + I(x7^2) + I(x8^2) +
##
       I(x9^2)
##
##
             Df Sum of Sq
                               RSS
                                        AIC
## - x6
              1
                      0.00
                             92.31 -808.71
## - I(x1^2)
                      0.00
                             92.31 -808.71
              1
## - I(x6^2)
              1
                      0.00
                             92.31 -808.70
## - I(x4^2)
              1
                      0.03
                             92.35 -808.53
## - I(x5^2)
                      0.04
                             92.36 -808.47
              1
## - I(x8^2)
              1
                      0.12
                             92.43 -808.08
## - x2
              1
                      0.29
                             92.60 -807.15
## <none>
                             92.31 -806.71
## - I(x2^2)
              1
                      0.48
                             92.79 -806.13
## - x1
              1
                      0.51
                             92.82 -805.98
## - I(x3^2)
                      0.61
                             92.92 -805.41
              1
## - x3
              1
                      0.63
                             92.94 -805.30
## - x5
              1
                      0.83
                             93.15 -804.21
## - I(x7^2)
              1
                      1.31
                             93.62 -801.66
## - x4
              1
                      5.56
                             97.87 -779.46
## - I(x9^2)
              1
                     67.97
                            160.29 -532.83
## - x10
              1
                    361.78 454.09
                                    -12.15
## - x7
                   1262.35 1354.66 534.35
              1
## - x8
              1
                   1417.94 1510.25
                                     588.71
##
## Step: AIC=-808.71
## y \sim x1 + x2 + x3 + x4 + x5 + x7 + x8 + x10 + I(x1^2) + I(x2^2) +
       I(x3^2) + I(x4^2) + I(x5^2) + I(x6^2) + I(x7^2) + I(x8^2) +
##
##
       I(x9^2)
##
             Df Sum of Sq
                               RSS
                                        AIC
##
## - I(x1^2)
                      0.00
                             92.31 -810.71
              1
## - I(x5^2)
              1
                      0.05
                             92.36 -810.46
## - I(x4^2)
                      0.09
              1
                             92.40 -810.23
## - I(x8^2)
              1
                      0.12
                             92.43 -810.08
## - I(x6^2)
              1
                      0.13
                             92.44 -810.03
## - x2
              1
                      0.29
                             92.60 -809.15
## <none>
                             92.31 -808.71
## - I(x2^2)
                             92.79 -808.13
              1
                      0.48
                             92.82 -807.98
## - x1
                      0.51
              1
## - I(x3^2)
              1
                      0.61
                             92.93 -807.39
## - x3
              1
                      0.63
                             92.95 -807.29
## - x5
              1
                      0.84
                             93.16 -806.16
## - I(x7^2)
              1
                      1.31
                             93.63 -803.66
## - x4
              1
                     13.63 105.94 -741.88
```

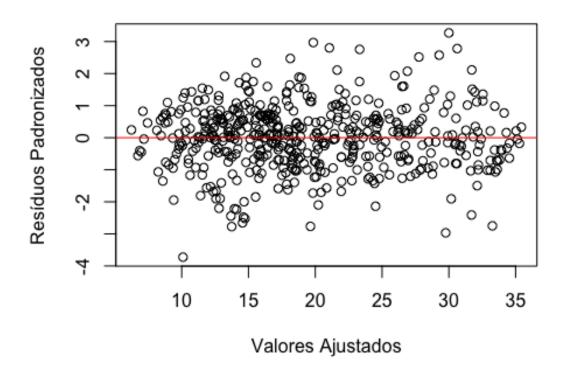
```
## - I(x9^2)
              1
                    68.32 160.63 -533.75
## - x10
              1
                   362.03 454.34
                                    -13.88
## - x7
              1
                  1313.93 1406.24
                                    551.03
## - x8
                  1420.96 1513.28
              1
                                    587.71
##
## Step: AIC=-810.71
## y \sim x1 + x2 + x3 + x4 + x5 + x7 + x8 + x10 + I(x2^2) + I(x3^2) +
       I(x4^2) + I(x5^2) + I(x6^2) + I(x7^2) + I(x8^2) + I(x9^2)
##
##
##
             Df Sum of Sq
                               RSS
                                       AIC
## - I(x5^2)
              1
                      0.05
                             92.36 -812.46
## - I(x4^2)
                             92.40 -812.23
              1
                      0.09
## - I(x8^2)
              1
                      0.12
                             92.43 -812.07
## - I(x6^2)
              1
                      0.13
                             92.44 -812.02
## - x2
              1
                      0.29
                             92.61 -811.13
## <none>
                             92.31 -810.71
## - I(x2^2)
              1
                      0.49
                             92.80 -810.08
## - I(x3^2)
                      0.61
                             92.93 -809.39
              1
                     0.63
## - x3
              1
                             92.95 -809.29
## - x5
              1
                      0.85
                             93.16 -808.15
## - I(x7^2)
                      1.31
                             93.63 -805.65
              1
## - x1
              1
                      2.45
                             94.76 - 799.61
## - x4
                     13.71
                           106.02 -743.47
              1
## - I(x9^2)
              1
                    68.32
                            160.64 -535.73
## - x10
              1
                    362.08 454.40
                                    -15.82
## - x7
              1
                  1314.53 1406.84 549.25
## - x8
              1
                  1421.40 1513.71
                                   585.86
##
## Step: AIC=-812.46
## y \sim x1 + x2 + x3 + x4 + x5 + x7 + x8 + x10 + I(x2^2) + I(x3^2) +
       I(x4^2) + I(x6^2) + I(x7^2) + I(x8^2) + I(x9^2)
##
##
             Df Sum of Sq
##
                               RSS
                                       AIC
## - I(x4^2)
                      0.05
              1
                             92.41 -814.21
## - I(x6^2)
              1
                      0.09
                             92.45 -813.98
## - I(x8^2)
                      0.12
                             92.48 -813.83
              1
## - x2
                      0.31
                             92.67 -812.78
              1
## <none>
                             92.36 -812.46
## - I(x2^2)
              1
                      0.51
                             92.87 -811.73
## - I(x3^2)
              1
                      0.64
                             93.00 -811.00
## - x3
              1
                      0.65
                             93.01 -810.93
## - I(x7^2)
              1
                      1.30
                             93.66 -807.48
## - x1
              1
                      2.44
                             94.80 -801.42
## - x5
                     9.89
                           102.25 -763.59
              1
## - x4
              1
                     16.30
                           108.66 -733.21
## - I(x9^2)
              1
                     69.10
                           161.46 -535.18
## - x10
              1
                   366.83 459.20
                                    -12.57
## - x7
              1
                  1322.39 1414.75
                                    550.05
## - x8
              1
                  1476.36 1568.72
                                    601.70
##
```

```
## Step: AIC=-814.21
## y \sim x1 + x2 + x3 + x4 + x5 + x7 + x8 + x10 + I(x2^2) + I(x3^2) +
       I(x6^2) + I(x7^2) + I(x8^2) + I(x9^2)
##
##
##
             Df Sum of Sq
                               RSS
                                       AIC
## - I(x6^2)
              1
                     0.09
                             92.49 -815.73
## - I(x8^2)
                     0.10
                             92.51 -815.67
              1
## - x2
              1
                     0.33
                             92.73 -814.43
## <none>
                             92.41 -814.21
## - I(x2^2)
                     0.52
                             92.93 -813.38
              1
## - I(x3^2)
              1
                     0.63
                             93.03 -812.82
## - x3
              1
                     0.64
                             93.05 -812.75
## - I(x7^2)
              1
                     1.29
                             93.70 -809.28
## - x1
              1
                     2.63
                             95.04 -802.17
## - x5
              1
                    10.04 102.45 -764.62
## - x4
              1
                    58.99 151.40 - 569.34
## - I(x9^2)
              1
                    69.35
                           161.76 -536.25
## - x10
              1
                   371.34 463.75
                                     -9.64
## - x7
              1
                  1322.36 1414.76
                                   548.05
## - x8
              1
                  1534.69 1627.10 617.97
##
## Step: AIC=-815.73
## y \sim x1 + x2 + x3 + x4 + x5 + x7 + x8 + x10 + I(x2^2) + I(x3^2) +
       I(x7^2) + I(x8^2) + I(x9^2)
##
##
##
             Df Sum of Sq
                               RSS
                                       AIC
                             92.57 -817.34
## - I(x8^2)
              1
                     0.07
## - x2
                             92.82 -815.97
              1
                     0.33
## <none>
                             92.49 -815.73
## - I(x2^2)
                     0.52
                             93.01 -814.94
              1
## - I(x3^2)
                     0.60
                             93.10 -814.48
              1
## - x3
                     0.62
                             93.11 -814.39
              1
## - I(x7^2)
              1
                     1.23
                             93.72 -811.13
## - x1
              1
                     2.64
                             95.13 -803.68
## - x5
              1
                    11.14
                           103.64 - 760.85
## - I(x9^2)
                           163.88 -531.75
              1
                    71.38
## - x4
                   133.38
                           225.87 -371.31
              1
## - x10
              1
                   371.43 463.92
                                   -11.45
                  1333.10 1425.59 549.87
## - x7
              1
## - x8
                  1618.39 1710.88 641.08
##
## Step: AIC=-817.34
## y \sim x1 + x2 + x3 + x4 + x5 + x7 + x8 + x10 + I(x2^2) + I(x3^2) +
##
       I(x7^2) + I(x9^2)
##
##
             Df Sum of Sq
                               RSS
                                       AIC
## - x2
              1
                     0.33
                             92.90 -817.53
## <none>
                             92.57 -817.34
## - I(x2^2) 1
                     0.52
                             93.09 -816.54
## - I(x3^2) 1
                     0.62
                             93.19 -816.01
```

```
## - x3
              1
                     0.63
                            93.20 -815.93
## - x1
              1
                     2.73
                            95.30 -804.79
## - I(x7^2)
              1
                     2.76
                           95.32 -804.67
              1
                    11.48 104.05 -760.87
## - x5
## - x4
              1
                   133.33 225.90 -373.27
## - x10
              1
                   372.04 464.61
                                   -12.71
## - I(x9^2)
                   831.47 924.04
              1
                                  331.07
## - x7
              1
                  1377.09 1469.66
                                  563.09
## - x8
                  1618.39 1710.96 639.10
              1
##
## Step: AIC=-817.53
## y \sim x1 + x3 + x4 + x5 + x7 + x8 + x10 + I(x2^2) + I(x3^2) + I(x7^2) +
##
       I(x9^2)
##
##
             Df Sum of Sq
                              RSS
                                      AIC
## <none>
                            92.90 -817.53
## - I(x2^2)
              1
                     0.39
                            93.29 -817.44
## - I(x3^2)
                            93.50 -816.34
              1
                     0.60
                     0.62
## - x3
              1
                            93.52 -816.20
## - x1
              1
                     2.40
                            95.31 -806.76
## - I(x7^2)
                     2.77
                           95.67 -804.87
              1
## - x5
              1
                    11.52 104.42 -761.10
## - x4
              1
                   133.66 226.56 -373.80
## - x10
              1
                   372.44 465.34
                                  -13.92
## - I(x9^2)
              1
                   832.98 925.88
                                  330.07
## - x7
              1
                  1377.28 1470.18 561.27
## - x8
                  1622.72 1715.63 638.46
              1
summary(backward model quad)
##
## Call:
## lm(formula = y \sim x1 + x3 + x4 + x5 + x7 + x8 + x10 + I(x2^2) +
       I(x3^2) + I(x7^2) + I(x9^2), data = base1)
##
## Residuals:
        Min
                  1Q
                       Median
                                    3Q
                                            Max
## -1.61814 -0.26235 0.01461 0.25871 1.39703
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
                          1.855e-01 -22.428 < 2e-16 ***
## (Intercept) -4.160e+00
## x1
               -4.248e-04 1.195e-04 -3.554 0.000416 ***
## x3
                1.286e-03 7.123e-04
                                       1.806 0.071604 .
## x4
               -7.707e-02 2.909e-03 -26.497 < 2e-16 ***
                                       7.778 4.41e-14 ***
## x5
                9.882e-02 1.270e-02
## x7
                1.435e+00 1.687e-02 85.057
                                             < 2e-16 ***
## x8
                1.336e+00 1.447e-02 92.325
                                             < 2e-16 ***
## x10
                                             < 2e-16 ***
                1.781e+00 4.026e-02 44.231
## I(x2^2)
               -1.571e-02 1.098e-02 -1.430 0.153298
```

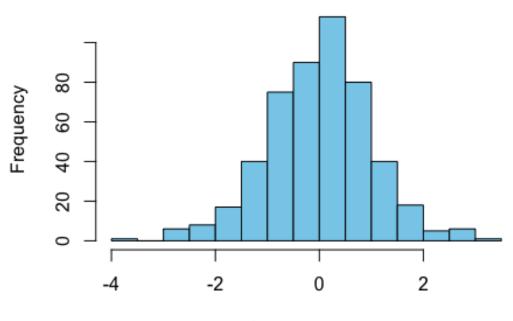
```
## I(x3^2)
              -2.745e-06 1.552e-06 -1.768 0.077638
## I(x7^2)
              -2.657e-03 6.971e-04 -3.811 0.000156 ***
## I(x9^2)
              -1.146e-02 1.733e-04 -66.148 < 2e-16 ***
## ---
## Signif. codes:
                  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.4363 on 488 degrees of freedom
## Multiple R-squared: 0.9963, Adjusted R-squared: 0.9962
## F-statistic: 1.188e+04 on 11 and 488 DF, p-value: < 2.2e-16
# Análise de resíduos
plot(fitted(backward_model_quad), rstandard(backward_model_quad),
    main = "Gráfico de Resíduos do Modelo Original",
    xlab = "Valores Ajustados",
    ylab = "Resíduos Padronizados")
abline(h = 0, col = "red")
```

### Gráfico de Resíduos do Modelo Original



```
# Histograma dos resíduos
hist(rstandard(backward_model_quad),
    main = "Histograma dos Resíduos Padronizados",
    xlab = "Resíduo Padronizado",
    col = "skyblue")
```

# Histograma dos Resíduos Padronizados



Resíduo Padronizado