

Tabular and Feature Space Synthetic Data Generation: A Literature Review

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The generation of synthetic data can be used for anonymization, regularization, oversampling, semi-supervised learning, self-supervised learning and various other tasks. Such broad potential motivated the development of new algorithms, specialized in data generation for specific data formats and Machine Learning (ML) tasks. However, one of the most common data formats used in industry applications, tabular data, is generally overlooked; Literature analyses are nearly non-existent, state-of-the-art methods are spread across domains and ML tasks and there is little to no distinction among the main types of mechanism underlying synthetic data generation algorithms. In this paper, we analyse tabular and feature space synthetic data generation algorithms. Specifically, we propose a unified taxonomy as an extension and generalization of previous taxonomies, review 70 generation algorithms across six ML problems, distinguish the main generation mechanisms identified into six categories, describe each type of generation mechanism, discuss metrics to evaluate the quality of synthetic data and provide recommendations for future research. We expect this study to assist researchers and practitioners identify important gaps in the literature and design better and more informed practices regarding synthetic data.

1 Introduction

Synthetic data is obtained from a generative process based on properties of real data [1]. The generation of synthetic data is essential for various domains and tasks. For example, synthetic data is used as a form of regularizing neural networks (*i.e.*, data augmentation) [CITATION]. One form of anonymizing datasets is via the production of synthetic observations (*i.e.*, synthetic data generation) [CITATION]. In settings where only a small portion of training data is labeled, some techniques generate artificial data using both labeled and unlabeled data with a modified loss function to train neural networks (*i.e.*, semi-supervised learning) [2]. In imbalanced learning contexts, synthetic data can be used to balance the target classes' frequencies and reinforce the learning of minority classes (*i.e.*, oversampling) [3]. Some active learning frameworks use data generation to improve the quality of data selection and classifier training [4]. Other techniques employ data generation to produce deep neural networks without labeled data (*i.e.*, self-supervised learning) [5].

28 The breadth of these techniques span multiple domains, such as facial recognition [6], Land Use/Land
29 Cover mapping [CITATION], medical image processing [CITATION], Natural Language Processing
30 (NLP) [7] or credit card default prediction [8]. According to the domain and data type, the data generation
31 techniques used may vary significantly. Generally speaking, some data generation mechanisms are specific
32 to some domains, data types or tasks. For example, ... Most, if not all, of these techniques are applied
33 on the input or output space.

34 However, there are various data generation techniques that are invariant to the task or data types used.
35 These techniques can be either applied in the feature space [9] or in tabular datasets¹. On one hand,
36 data generation in the feature space uses a generative model to learn a manifold, lower-dimensional
37 abstraction over the input space [11], defined here as the feature space. At this level, any tabular data
38 generation mechanism can be applied and reconstructed into the input space if necessary. On the other
39 hand, synthetic data generation on tabular data can be applied to most problems. Although, the choice
40 of generation mechanism is still dependant on (1) the importance of the relationships found between
41 the different features, (2) the ML task developed and (3) the motivation for the generation of synthetic
42 data. For example, when generating data to address an imbalanced learning problem (*i.e.*, oversampling),
43 the relationships between the different features are not necessarily kept since the goal is to reinforce
44 the learning of the minority class by redefining an ML classifier’s decision boundaries. If the goal is to
45 anonymize a dataset, perform some type of descriptive task, or ensure a consistent model interpretability,
46 these relationships need to be kept.

47 Depending on the context, evaluating the quality of the generated data is a complex task. For example,
48 for image and time series data, perceptually small changes in the original data can lead to large changes
49 in the euclidean distance [1, 12]. The evaluation of generative models typically account primarily for the
50 performance in a specific task, since good performance in one criterion does not imply good performance
51 on another [12]. However, in computationally intensive tasks it is often impracticable to search for the
52 optimal configurations of generative models. To address this limitation, other evaluation methods have
53 been proposed to assist in this evaluation, which can be distinguished into statistical divergence metrics
54 and precision/recall metrics [13]. The relevant performance metrics found in the literature are discussed
55 in Section 6.

56 1.1 Motivation, Scope and Contributions

57 This literature review focuses on generation mechanisms applied to tabular data and the different ML
58 techniques where tabular synthetic data is used. In addition, we focus on the ML perspective of synthetic
59 data, as opposed to the practical perspective. From a practical sense, synthetic data is used as a proxy
60 of real data. It is assumed to be inaccessible, essential and a secondary asset for tasks like education,
61 software development, or systems demonstrations [14].

62 We focus on data generation techniques in the tabular and feature space (*i.e.*, embedded inputs) with
63 a focus on classification and associated ML problems. Related literature reviews are mostly focused on
64 specific algorithmic or domain applications, with little to no emphasis on the core generative process.
65 For this reason, these techniques often appear “sandboxed”, even though there is a significant overlap
66 between them. There are some related reviews published since 2019. Assefa et al. [1] provides a general
67 overview of synthetic data generation for time series data anonymization in the finance sector. Hernandez
68 et al. [15] reviews data generation techniques for tabular health records anonymization. Raghunathan
69 [16] reviews synthetic data anonymization techniques that preserve the statistical properties of a dataset.
70 Nalepa et al. [17] reviews data augmentation techniques for brain-tumor segmentation. Bayer et al. [18]

¹Tabular data is a database structured in tabular form, composed of columns (features) and rows (observations) [10]

Table 1: Related literature reviews published since 2019.

Reference	Data type	ML problem	Domain	Observations
Assefa et al. [1]	—	Differential privacy	Finance	Analysis of applications, motivation and properties of synthetic data for anonymization.
Hernandez et al. [15]	Tabular	Differential privacy	Healthcare	Focus on GANs.
Raghunathan [16]	Tabular	Differential privacy	Statistics	Focus on general definitions such as differential privacy and statistical disclosure control.
Nalepa et al. [17]	Image	Segmentation	Medicine	Analysis of algorithmic applications on a 2018 brain-tumor segmentation challenge.
Bayer et al. [18]	Text	Classification	—	Distinguish 100 methods into 12 groups.
Shorten et al. [19]	Text	Deep Learning	—	General overview of text data augmentation.
Chen et al. [20]	Text	Few-shot Learning	—	Augmentation techniques for machine learning with limited data
Feng et al. [7]	Text	—	—	Overview of augmentation techniques and applications on NLP tasks.
Liu et al. [21]	Text	—	Various	Analysis of industry use cases of data augmentation in NLP. Emphasis on input level data augmentation.
Yi et al. [22]	Image	—	Medicine	Emphasis on GANs.
Wang et al. [23]	Image	Deep Learning	—	Regularization techniques using facial image data. Emphasis on Deep Learning generative models.
Shorten et al. [24]	Image	Deep Learning	—	Emphasis on data augmentation as a regularization technique.
Khosla et al. [25]	Image	—	—	Broad overview of image data augmentation. Emphasis on traditional approaches.
Iwana et al. [26]	Time series	Classification	—	Defined a taxonomy for time series data augmentation.
Wen et al. [27]	Time series	Various	—	Analysis of data augmentation methods for classification, anomaly detection and forecasting.
Zhao et al. [28]	Graph	Various	—	Graph data augmentation for supervised and self-supervised learning.
Khalifa et al. [29]	Image	—	Various	General overview of image data augmentation and relevant domains of application.

distinguishes augmentation techniques for text classification into feature and data space, while providing an extensive overview of augmentation methods within this domain. However, the taxonomy proposed and feature space augmentation methods are not necessarily specific to the domain. Shorten et al. [19], Chen et al. [20], Feng et al. [7] and Liu et al. [21] also review data augmentation techniques for text data. Yi et al. [22] review Generative Adversarial Network architectures for medical imaging. Wang et al. [23] reviews face data augmentation techniques. Shorten et al. [24] and Khosla et al. [25] discuss techniques for image data augmentation. Iwana et al. [26] and Wen et al. [27] also review time series data augmentation techniques. Zhao et al. [28] review data augmentation techniques for graph data. The analysis of related literature reviews ² is shown in Table 1.

²published since 2019, using the search query ("synthetic data generation" OR "oversampling" OR "imbalanced learning" OR "data augmentation") AND ("literature review" OR "survey"). Retrieved on August 11th, 2022. More articles were added later whenever found relevant.

80 The different taxonomies established in the literature follow a similar philosophy, but vary in terminology
81 and are often specific to the technique discussed. Regardless, it is possible to establish a broader taxonomy
82 without giving up on specificity. This study provides a joint overview of the different data generation
83 approaches, domains and ML techniques where data generation is being used, as well as a common
84 taxonomy across domains. It extends the analyses found in these articles and uses the compiled knowledge
85 to identify research gaps. We compare the strengths and weaknesses of the models developed within each
86 of these fields. Finally, we identify possible future research directions to address some of the limitations
87 found. The contributions of this paper are summarized below:

- 88 • Bridge different ML concepts using synthetic data generation in its core (Algorithmic applications +
89 Review of the State-of-the-art).
- 90 • Propose a synthetic data generation/data augmentation taxonomy to resolve the ambiguity in the
91 literature (Data augmentation taxonomy).
- 92 • Characterize all relevant data generation methods using the proposed taxonomy.
- 93 • Discuss the ML techniques in which synthetic data generation/data augmentation is used, beyond
94 regularization and consolidate the current data generation mechanisms across the different techniques
95 (Algorithmic Applications).
- 96 • Bring to light the key challenges of synthetic data generation and put forward possible research
97 directions in the future.

98 1.2 Paper Organization

99 This paper is organized as follows: Section 2 defines and formalizes the different concepts, goals, trade-offs
100 and motivations related to synthetic data generation. Section 3 establishes the taxonomy used to categorize
101 all the methods described in the paper. Section ?? reviews synthetic data generation mechanisms in the
102 feature space. Section ?? reviews synthetic data generation mechanisms in the input space. Section 4
103 describes the applications of synthetic data in ML methods. Section 6 reviews performance evaluation
104 methods of synthetic data generation mechanisms. Section 7 summarizes the main findings and discusses
105 limitations and possible research directions in the state-of-the-art. Section 9 presents the main conclusions
106 drawn from this study.

107 2 Background

108 In this section we define basics concepts, common goals, trade-offs and motivations regarding the generation
109 of synthetic data in ML. We define synthetic data generation as the production of observations using
110 a generative model (regardless of its nature) that resemble naturally occurring observations within
111 a certain domain. It requires access to either a training dataset, a generative process, or a data
112 stream. However, additional requirements might be imposed depending on the ML task being developed.
113 For example, to generate artificial data for regularization purposes in supervised learning (*i.e.*, data
114 augmentation) the training dataset must be annotated [CITATION]. The generation of synthetic data for
115 anonymization purposes assumes synthetic datasets to be different from the original data, while following
116 the same statistical properties [CITATION]. Domain knowledge may also be necessary to encode specific
117 relationships among features into the generative process.

118 2.1 Relevant Learning Problems

119 The breach of sensitive information is an important barrier to the sharing of datasets, especially when it
120 concerns personal information [30]. A common solution for this problem is the generation of synthetic
121 data without identifiable information. Generally speaking, ML tasks that require data with sensitive
122 information are not compromised when using synthetic data. The experiment conducted by Patki et al.
123 [31] using relational datasets showed that in 11 out of 15 comparisons ($\approx 73\%$), practitioners performing
124 predictive modelling tasks using fully synthetic datasets performed the same or better than those using
125 the original dataset. This topic is discussed in Section 4.1.

126 A common problem in the training of deep neural networks are their capacity to generalize [32] (*i.e.*, reduce
127 the difference in classification performance between known and unseen observations). Data augmentation
128 is a common method to address this problem. The generation of synthetic observations increases the
129 range of the possible input space used in the training phase, which reduces the performance difference
130 between known and unseen observations. Although other regularization methods exist, data augmentation
131 is a useful method since it does not affect the choice in the architecture of the ML classifier and does not
132 exclude the usage of other regularization methods. In domains such as computer vision and NLP, data
133 augmentation is also used to improve the robustness of models against adversarial attacks [33, 34]. These
134 topics are discussed into higher detail in Section 4.2.

135 In supervised learning, synthetic data generation is often motivated by the need to balance target class
136 distributions (*i.e.*, oversampling). Since most ML classifiers are designed to perform best with balanced
137 datasets, defining an appropriate decision boundary to distinguish rare classes becomes difficult [35].
138 Although there are other approaches to address imbalanced learning, oversampling techniques are generally
139 easier to implement since they do not involve modifications to the classifier. This topic is discussed into
140 higher detail in Section 4.3.

141 In supervised learning projects where labeled data is not readily available, but can be labeled, an Active
142 Learning (AL) method may be used to improve the labelling process. AL aims to reduce the cost of
143 producing training datasets by finding the most informative observations to label and feed into the
144 classifier [36]. In this case, the generation of synthetic data is particularly useful to reduce the amount of
145 labelled data required for a successful ML project and its costs. A similar motivation applies to the case
146 of few-shot learning: small datasets may be expanded with synthetic data [37]. These topics are discussed
147 in Sections 4.4 and ??.

148 The two other techniques reliant on synthetic data generation is Semi-supervised and Self-supervised
149 learning. The former leverages both labeled and unlabeled data in the training phase, simultaneously.
150 Most of the methods in the literature apply perturbations on the training data as part of the training
151 procedure [38]. Self-supervised learning is a technique used to train neural networks in the absence of
152 labeled data. Both techniques use synthetic data generation as an internal procedure for most of these
153 methods. These techniques are discussed in Sections 4.5 and 4.6.

154 2.2 Problem Formulation

155 The original dataset, $\mathcal{D} = \mathcal{D}_L \cup \mathcal{D}_U$, is a collection of real observations and is distinguished according
156 to whether a target feature exists, $\mathcal{D}_L = ((x_i, y_i))_{i=1}^l$, or not, $\mathcal{D}_U = (x_i)_{i=1}^u$. All three datasets, \mathcal{D} ,
157 \mathcal{D}_L and \mathcal{D}_U consist of ordered collections with lengths $l + u$, l and u , respectively. Synthetic data
158 generation is performed using a generator, $f_{gen}(x; \tau) = \tilde{x}$, where τ defines the generation policy (*i.e.*, its

hyperparameters), $x \in \mathcal{D}$ is an observation and $\tilde{x} \in \mathcal{D}^s$ is a synthetic observation. Analogous to \mathcal{D} , the synthetic dataset, \mathcal{D}^s , is also distinguished according to whether there is an assignment of a target feature, $\mathcal{D}_L^s = ((\tilde{x}_j, \tilde{y}_j))_{j=1}^{l'}$, or not, $\mathcal{D}_U^s = (\tilde{x}_j)_{j=1}^{u'}$.

Depending on the ML task, it may be relevant to establish metrics to measure the quality of \mathcal{D}^s . In this case, a metric $f_{qual}(\mathcal{D}^s, \mathcal{D})$ is used to determine the level of similarity/dissimilarity between \mathcal{D} and \mathcal{D}^s . In addition, a performance metric to estimate the performance of a model on the objective task, f_{per} , may be used to determine the appropriateness of a model with parameters θ , *i.e.*, f_θ . The generator’s goal is to generate \mathcal{D}^s with arbitrary length, given $\mathcal{D} \sim \mathbb{P}$ and $\mathcal{D}^s \sim \mathbb{P}^s$, such that $\mathbb{P}^s \approx \mathbb{P}$, $x_i \neq x_j \forall x_i \in \mathcal{D} \wedge x_j \in \mathcal{D}^s$. $f_{gen}(x; \tau)$ attempts to generate a \mathcal{D}^s that maximizes either f_{per} , f_{qual} , or a combination of both.

3 Data Generation Taxonomy

The taxonomy proposed in this paper is a compilation of different definitions found in the literature, along with other traits that vary among domains and generation techniques. Within image data studies, Shorten et al. [24] and Khalifa et al. [29] divide data augmentation techniques into “basic” or “classical” approaches and deep learning approaches. In both cases, the former refers to domain-specific generation techniques, while the latter may be applied to any type of data. Iwana et al. [26] proposes a time-series data augmentation taxonomy divided in four families: (1) Decomposition, (2) Pattern mixing, (3) Generative models and (4) Decomposition. With exception to generative models, the majority of the methods presented in the remaining families are well established and domain specific. Hernandez et al. [15] defines a taxonomy for synthetic tabular data generation approaches divided in three types of approaches: (1) Classical, (2) Deep learning and (3) Others. Most taxonomies found followed similar definitions with variations in terminology or distinction criteria. In addition, all taxonomies with categories defined as “basic”, “traditional” or “classical” use these to characterize domain-specific transformations.

Within the taxonomies found, none of them consider how a generation mechanism employs \mathcal{D} into the generation process or, if applicable, the training phase. However, it is important to understand whether a generation mechanism randomly selects x and a set of close neighbors, thus considering local information only, or considers the overall dataset or data distribution for the selection of x and/or generation of \tilde{x} . Our proposed taxonomy is depicted in Figure 1. It characterizes data generation mechanisms using four properties:

1. **Architecture.** Defines the broader type of data augmentation. It is based on domain specificity, architecture type or data transformations using a heuristic or random perturbation process. Generation techniques that apply a form of random perturbation, interpolation or geometric transformation to the data with some degree of randomness are considered randomized approaches. Typical, domain-specific data generation techniques are considered traditional architectures. These techniques apply transformations to a data point using *a priori* domain knowledge. Generative models based on neural network architectures are defined as network-based. These architectures attempt to either generate observations in the feature space and/or by producing observations that are difficult to distinguish from the original dataset.
2. **Application level.** Refers to the phase of the ML pipeline where the generative process is included. Generative models are considered internal if they are used alongside the primary ML task, whereas models used prior to the development of the primary ML task are considered external.
3. **Scope.** Considers the usage of the original dataset’s properties. Generative models that consider the

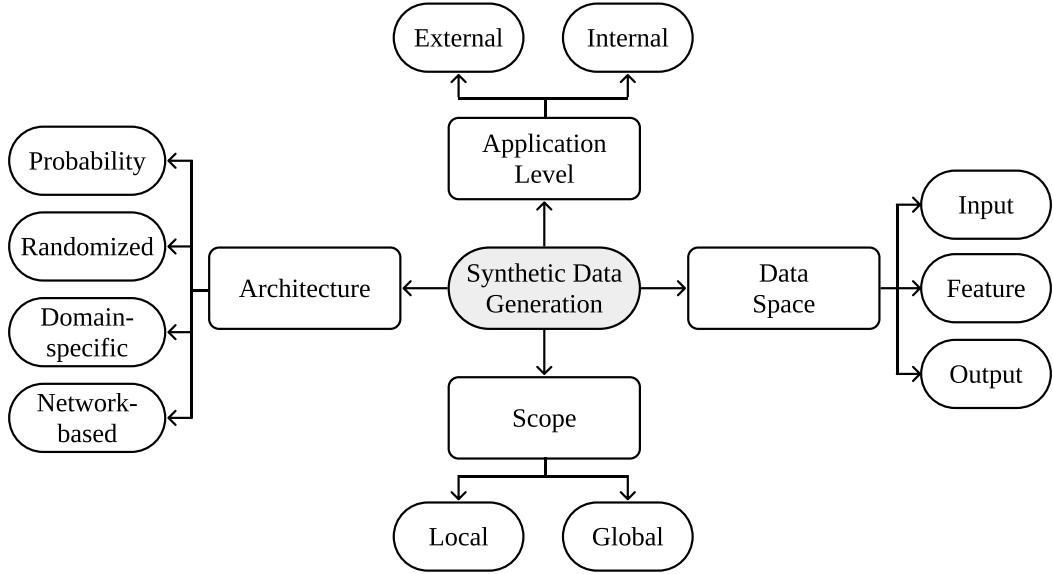


Figure 1: General taxonomy of data generation mechanisms proposed in this paper.

density of the data space, statistical properties of \mathcal{D} , or attempt to replicate specific relationships found in \mathcal{D} are considered to have a global scope, whereas generative models that consider a single observation and/or a set of close neighbors are considered to have a local scope. On the one hand, generative models with a local scope do not account for \mathbb{P}^s but allow for a larger diversity of candidate x^s and higher variance within \mathcal{D}^s . On the other hand, generative models with a global scope have a higher capacity to model \mathbb{P}^s but produce candidate x^s with lower diversity and lower variance within \mathcal{D}^s .

4. Data space. Refers to the type data representation used to apply the generative model. Generation mechanisms can be applied using the raw dataset (*i.e.*, on the input space), an embedded representation of the data (*i.e.*, on the feature space) or based on the target feature (*i.e.*, on the output space). Although some studies discuss the need to generate synthetic data on the input space [30, 31], there are various studies that apply synthetic data generation techniques on a feature space.

Throughout the analysis of the different types of generation mechanisms, all relevant methods were characterized using this taxonomy and listed in Table 2.

Table 2: Summary of the synthetic data generation methods discussed in this work.

Algorithm	ML Problem	Type	Architecture	Level	Data Space	Scope
SDV [31]	Anon.	PDF	Probabilistic	External	Input	Global
MST [39]	DP	Marginal	Probabilistic	External	Input	Global
MWEM [40]	DP	Marginal	Probabilistic	External	Input	Global
MWEM-PGM [41]	DP	PGM	Probabilistic	External	Input	Global
PrivBayes [42]	DP	PGM	Probabilistic	External	Input	Global
DPGAN [43]	DP	GAN	Network	External	Feature	Global
DPCTGAN [44]	DP	GAN	Network	External	Feature	Global
PATE-GAN [45]	DP	GAN	Network	External	Feat. + Out.	Global
PATECTGAN [44]	DP	GAN	Network	External	Feat. + Out.	Global
FEM [46]	DP	Workload	Probabilistic	External	Input	Global

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Table 2: Summary of the synthetic data generation methods discussed in this work.

Algorithm	ML Problem	Type	Architecture	Level	Data Space	Scope
RAP [47]	DP	Workload	Probabilistic	External	Input	Global
PDF [48, 49]	—		Probabilistic	External	Input	Global
Kamino [50]	DP		Probabilistic	External	Input	Global
RON-GAUSS [51]	DP	PDF	Probabilistic	Internal	Feature	Global
HDMM [52]	DP		Probabilistic	External	Input	Global
DualQuery [53]	DP		Probabilistic	External	Input	Global
ROS(E) [54]	Ovs	Bootstrap	Randomized	External	Input	Local
SMOTE [55]	Ovs	Linear	Randomized	External	Input	Local
SMOTENC [55]	Ovs	Linear	Randomized	External	Input	Local
SMOTEN [55]	Ovs	Linear	—	External	Input	Local
Borderline-SMOTE [56]	Ovs	Linear	Randomized	External	Input	Local
G-SMOTE [57]	Ovs	Geometric	Randomized	External	Input	Local
ADASYN [58]	Ovs	Linear	Randomized	External	Input	Local
KernelADASYN [59]	Ovs	PDF	Probabilistic	External	Input	Local
MOKAS [60]	Ovs	Rec. Err.	Network	External	Feature	Global
SOMO [61]	Ovs	Linear	Net.+Rand.	External	Input	Global
G-SOMO [62]	Ovs	Geometric	Net.+Rand.	External	Input	Global
VAE [63]	Ovs					
GMM [64]						
GMM [65]						
Safe-level SMOTE [66]	Ovs	Linear	Randomized	External	Input	Local
LR-SMOTE [67]	Ovs	Linear	Randomized	External	Input	Global
K-means SMOTE [68]	Ovs	Linear	Randomized	External	Input	Global
DBSMOTE [69]	Ovs	Linear	Randomized	External	Input	Local
CGAN [70]	Ovs	GAN	Network	External	Feature	Global
K-means CTGAN [71]	Ovs	GAN	Network	External	Feature	Global
SMOTER [72]	Ovs + Reg	Linear	Randomized	External	Input	Local
G-SMOTER [73]	Ovs + Reg	Linear	Randomized	External	Input	Local
RACOG [74]	Ovs	PGM	Probabilistic	External	Input	Global
wRACOG [74]	Ovs	PGM	Probabilistic	External	Input	Global
RWO [75]	Ovs	RW	Probabilistic	External	Input	Global
PDFOS [76]	Ovs	PDF	Probabilistic	External	Input	Global
Mixup [77]	DA	Linear	Randomized	External	In.+Out.	Local
M-Mixup [78]	DA	Linear	Network	Internal	Feat.+Out.	Global
NL-Mixup [79]	DA	Geometric	Randomized	External	In.+Out.	Local
AE-DA [80]	DA	AE	Network	External	In./Feat.+Out.	Local
MODALS [81]	DA	—	Network	Internal	Feat.	Global
LSI [82]	DA	AE	Network	External	Feat.+Out.	Global
Gibbs [83]	DA	PGM	Probabilistic	External	Input	Global
MedGAN [84]	DA	GAN	Network	External	Feature	Global
GANBLR [85]	DA	PGM	Probabilistic	External	Input	Global
TableGAN [86]	DA	GAN	Network	External	Feature	Global
CTGAN [87]	DA	GAN	Network	External	Feature	Global
TVAE [87]	DA	AE	Network	External	Feature	Global
AE [88]	DA	AE	Network	External	Feature	Global
InfoMixup [4]	AL	Linear	Network	Internal	Feat.+Out.	Global
VAEACGAN [89]	AL	AE	Network	Internal	Feature	Global
AL-G-SMOTE [36]	AL	Geometric	Randomized	Internal	Input	Local
DAE [90]	Semi-SL	AE	Network	Internal	Input	Global
II-model [91]	Semi-SL	PDF	Randomized	Internal	In.+Feat.	Local
Mean Teacher [92]	Semi-SL	PDF	Randomized	Internal	In.+Feat.	Local
ICT [93]	Semi-SL	Linear	Randomized	Internal	Input	Local

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Table 2: Summary of the synthetic data generation methods discussed in this work.

Algorithm	ML Problem	Type	Architecture	Level	Data Space	Scope
Mixmatch [94]	Semi-SL	Linear	Randomized	Internal	Input	Local
SDAT [95]	Semi-SL	AE+PDF	Net.+Prob.	Internal	Feature	Global
MCoM [96]	Semi-SL	Linear	Randomized	Int.+Ext.	Inp.+Feat.	Global
C-Mixup [97]	Semi/Self-SL	AE+Lin.	Net+Rand.	Internal	Feature	Global
VIME [10]	Semi/Self-SL	Mask	Randomized	Internal	Input	Local
SubTab [98]	Self-SL	Mask	Rand.+Prob.	Internal	Input	Local
Scarf [99]	Self-SL	Mask	Randomized	Internal	Input	Local
A-SFS [100]	Self-SL	Mask	Randomized	Internal	Input	Local

4 Algorithmic applications

In this section we discuss the data generation mechanisms for the different contexts where they are applied. We emphasize the constraints in each problem that condition the way generation mechanisms are used.

4.1 Privacy

Synthetic data generation is a technique used to produce synthetic, anonymized versions of datasets [30]. It is considered a good approach to share sensitive data without compromising significantly a given data mining task [101, 86]. Traditional data anonymization techniques, as well as federated learning are two other viable solutions for privacy-preserving data publishing tasks, but contain drawbacks [15]. On the one hand, traditional data anonymization requires domain knowledge, is labor intensive and remains susceptible to disclosure [102]. On the other hand, federated learning is a technically complex task that consists on training ML classifiers on edge devices and aggregating temporarily updated parameters on a centralized server, instead of aggregating the training data [103]. Although it prevents sharing sensitive data, its applicability is dependent on the task. Dataset anonymization via synthetic data generation attempts to balance disclosure risk and data utility in the final synthetic dataset. The goal is to ensure observations are not identifiable and the relevant data mining tasks are not compromised [104, 105].

The generation of synthetic datasets allow a more flexible approach to the successful implementation of ML tasks. To do this, it is important to guarantee that sensitive information in \mathcal{D} is not leaked into \mathcal{D}^s . Differential privacy (DP), a formalization of privacy, offers strict theoretical privacy guarantees [44]. A differentially private generation mechanism produces a synthetic dataset, regulated by the privacy parameter ϵ , with statistically indistinguishable results when using either \mathcal{D} or neighboring datasets $\mathcal{D}' = \mathcal{D} \setminus \{x\}$, for any $x \in \mathcal{D}$. A synthetic data generation model (f_{gen}) guarantees (ϵ, δ) -differential privacy if $\forall S \subseteq \text{Range}(f_{gen})$ all $\mathcal{D}, \mathcal{D}'$ differing on a single entry [40]:

$$Pr[f_{gen}(\mathcal{D}) \in S] \leq e^\epsilon \cdot Pr[f_{gen}(\mathcal{D}') \in S] + \delta \quad (1)$$

In this case, ϵ is a non-negative number defined as the privacy budget. A lower ϵ guarantees a higher level of privacy, but reduces the quality of the produced synthetic data. The generation of DP synthetic data is especially appealing since DP is not affected by post-processing; any ML pipeline may be applied using \mathcal{D}^s without losing differential privacy [106].

240 Despite the formalization and the ability to quantify differential privacy, there are popular synthetic
 241 data-based anonymization approaches that perform this task without DP guarantees. Specifically, the
 242 Synthetic Data Vault (SDV) [31] is a method for database anonymization that uses Gaussian Copula
 243 models for generating data. However, this method allows the usage of other generation mechanisms. A
 244 posterior extension of SDV was proposed to generate data using a CTGAN [87] and to handle sequential
 245 tabular data using a conditional probabilistic auto-regressive neural network [107].

246 The choice of the most appropriate DP synthetic data generation techniques depends on the task to be
 247 developed (if known) and the domain. However, marginal-based algorithms appear to perform well across
 248 various tests [108]. A well-known method for the generation of DP synthetic datasets is the combination
 249 of the Multiplicative Weights update rule with the Exponential Mechanism (MWEM) [40]. The MWEM
 250 mechanism is an active learning-style algorithm that maintains an approximation of \mathcal{D}^s . At each time step,
 251 MWEM selects the worst approximated query (determined by a scoring function) using the Exponential
 252 Mechanism and improves the accuracy of the approximating distribution using the Multiplicative Weights
 253 update rule. A known limitation of this method refers to its scalability. Since this method represents
 254 the approximate data distribution in datacubes, this method becomes infeasible for high-dimensional
 255 problems [41]. This limitation was addressed with the integration of a Probabilistic Graphical Model-based
 256 (PGM) estimation into MWEM (MWEM-PGM) and a subroutine to compute and optimize the clique
 257 marginals of the PGM, along with other existing privacy mechanisms [41]. Besides MWEM, this method
 258 was used to modify and improve the quality of other DP algorithms: PrivBayes [42], HDMM [52] and
 259 DualQuery [53].

260 PrivBayes [42] circumvents the curse of dimensionality by computing a differentially private Bayesian
 261 Network (*i.e.*, a type of PGM). Instead of injecting noise into the dataset, they inject noise into the
 262 lower-dimensional marginals. The high-dimensional matrix mechanism (HDMM) [52] mechanism is
 263 designed to efficiently answer a set of linear queries on high-dimensional data, which are answered using
 264 the Laplace mechanism. The DualQuery algorithm [53] is based on the two-player interactions in MWEM,
 265 and follows a similar synthetic data generation mechanism as the one found in MWEM.

266 FEM [46] follows a similar data generation approach as MWEM. It also uses the exponential mechanism and
 267 replaces the multiplicative weights update rule with the follow-the-perturbed-leader (FTPL) algorithm [109].
 268 The Relaxed Adaptive Projection (RAP) algorithm [47] uses the projection mechanism [110] to answer
 269 queries on the private dataset using a perturbation mechanism and attempts to find the synthetic dataset
 270 that matches the noisy answers as accurately as it can.

271 Kamino [50] introduces denial constraints in the data synthesis process. Kamino builds on top of the
 272 probabilistic database framework (PDF) [48, 49], which uses ordinary databases to model a probability
 273 distribution and integrates denial constraints as parametric factors, out of which the synthetic observations
 274 are sampled. RON-GAUSS [51] combines the random orthonormal (RON) dimensionality reduction
 275 technique and synthetic data sampling using either a Gaussian generative model or a Gaussian mixture
 276 model. The motivation for this model stems from the *Diaconis-Freedman-Meckes* effect [111], which states
 277 that most high-dimensional data projections follow a nearly Gaussian distribution. Since RON-GAUSS
 278 includes a feature extraction step (using RON) and the synthetic data generated is not projected back
 279 into the input space, we consider RON-GAUSS an internal approach to the ML pipeline.

280 The MST mechanism [39] is a marginal estimation-based approach that produces differentially private
 281 data. It uses the Private-PGM mechanism [41] that relies on the PGM approach to generate synthetic
 282 data. PGM models are most commonly used when it is important to maintain the pre-existing statistical
 283 properties and relationships between features [112].

284 Another family of DP synthetic data generation techniques relies on the usage of Generative Adversarial

285 Networks (GAN). DPGAN [43] modifies the original GAN architecture to make it differentially private
 286 by introducing noise to gradients during the learning procedure. This approach was also applied on
 287 a conditional GAN architecture directed towards tabular data (CTGAN) [87], which originated the
 288 DPCTGAN [44]. Another type of GAN-based DP data synthesis method is based on the combination of
 289 a GAN architecture and the Private Aggregation of Teacher Ensembles (PATE) [113] approach. Although
 290 the PATE method generates a DP classifier, it served as the basis for PATE-GAN [45], a DP synthetic
 291 data generation mechanism. PATE-GAN replaces the discriminator component of a GAN with the
 292 PATE mechanism, which guarantees DP over the generated data. The PATE mechanism is used in the
 293 learning phase to train an ensemble of classifiers to distinguish real from synthetic data. In a second step,
 294 the predicted labels are passed (with added noise) to another discriminator, which is used to train the
 295 generator network.

296 4.2 Regularization

297 When there are no underlying problems in the training data, it is sampled from a fixed data source, is labeled,
 298 and balanced, the resulting ML classifier is expected to achieve good generalization performance [114].
 299 However, if one or more of these assumptions does not hold, the ML model becomes prone to overfitting [115].
 300 Regularization techniques are often used to address problems like overfitting, small training dataset, high
 301 dimensionality, outliers, label noise and catastrophic forgetting [116, 117, 118, 119]. They can be divided
 302 into three groups [120]:

- 303 1. Output level modifications. Transforms the labels in the training data.
- 304 2. Algorithmic level modifications. Modifies the classifier’s architecture, loss function or other compo-
 305 nents in the training procedure.
- 306 3. Input level modifications. Modifies the training dataset by expanding it with synthetic data.

307 The last approach, input level modifications, is known as data augmentation. It is used to increase the size
 308 and data variability of data in a training dataset, by producing synthetic observations [121, 122]. Since
 309 it is applied at the data level, it can be used for various types of problems and classifiers [123]. Earlier
 310 definitions of data augmentation refer to methods based on iterative optimization or sampling algorithms
 311 that introduce unobserved data or latent variables [124]. In the current ML literature, data augmentation
 312 techniques mostly refer to the former, while the latter is better known as feature extraction. Although
 313 data augmentation is commonly used and extensively studied in computer vision [24] and natural language
 314 processing [7], research on tabular data augmentation is sparse.

315 Mixup [77] consists of a linear interpolation between two randomly selected observations and their
 316 target feature values, $(x_i, y_i), (x_j, y_j) \in \mathcal{D}_L$, such that given $\lambda \sim \text{Beta}(\alpha, \alpha)$, $x^s = \lambda x_i + (1 - \lambda)x_j$ and
 317 $y^s = \lambda y_i + (1 - \lambda)y_j$, where α is a predetermined hyperparameter. This method was the source to Manifold
 318 Mixup (M-Mixup) [78]. It generates synthetic data in the feature spaces of a neural network classifier’s
 319 hidden layers. Another Mixup-based data augmentation approach, Nonlinear Mixup (NL-Mixup) [79],
 320 applies a nonlinear interpolation policy. In this case, Λ is a set of mixing policies sampled from a beta
 321 distribution applied to each feature. This approach modifies the original mixup approach to generate
 322 data within a hyperrectangle/orthotope: $x^s = \Lambda \odot x_i + (1 - \Lambda) \odot x_j$, where \odot denotes the Hadamard
 323 product.

324 Feng et al. [80] proposed an autoencoder-based data augmentation (AE-DA) approach where the training
 325 of the autoencoder is done for each target class, non-iteratively, which reduces the amount of time required

compared to the batch processing approach. The decoding weights of an autoencoder is scaled and linearly combined with an observation from another class using a coefficient that follows the beta distribution. The latter step varies from typical interpolation-based approaches, since this coefficient is usually drawn from a uniform distribution.

The Modality-Agnostic Automated Data Augmentation in the Latent Space model (MODALS) [81] leverages on the concept discussed by DeVries et al. [9], as well as the Latent Space Interpolation method (LSI) [82] and M-Mixup [78]. However, MODALS introduces a framework for data augmentation internally. It contains a feature extraction step, trained using a combination of adversarial loss, classification loss and triplet loss, where latent space generation mechanisms are applied. The classifier is trained using the original and the synthetic observations generated in the feature space. In this study the authors discuss Difference transform augmentation method. It generates within-class synthetic data by selecting a x^c and two random observations within the same class, x_i, x_j , to compute $x^s = x^c + \lambda(x_i - x_j)$. In addition they also experiment with Gaussian noise and Hard example extrapolation, determined by $x^s = x^c + \lambda(x^c - \mu)$, where μ is the mean of the observations within a given class.

In the model distillation approach proposed in [83] the student model is trained with synthetic data generated with Gibbs sampling. Although Gibbs sampling is infrequently used in recent literature, two oversampling methods using Gibbs sampling appear to achieve state-of-the-art performance [74]. However, probabilistic-based approaches for data augmentation are uncommon; there are some methods proposed for the more specific case of oversampling, but no more related methods for data augmentation were found.

A well-known approach to GAN-based data augmentation is Table-GAN [86]. It utilizes the vanilla GAN approach to the generation of synthetic data. However, vanilla GAN does not allow the controlled generation of synthetic data given conditional attributes such as the target feature values in supervised learning tasks and may be the cause for aggravated categorical feature imbalance. These limitations were addressed with the CTGAN [87] algorithm, which implements the conditional GAN approach to tabular data. Another GAN-based architecture, MedGAN [84], can also be adapted for tabular data and is used as a benchmark in related studies (*e.g.*, [87, 85]). When compared to the remaining GAN-based approaches, MedGAN’s architecture is more complex and is generally outperformed in the experiments reported in the literature. The GANBLR [85] modifies vanilla GAN architectures with a Bayesian network as both generator and discriminator to create synthetic data that is expected to be indistinguishable from real data. This approach benefits from its interpretability and reduced complexity, while maintaining state-of-the-art performance across various evaluation criteria.

Another less popular approach for network-based synthetic data generation are autoencoder architectures. TVAE, proposed in [87] achieved state-of-the-art performance. It consists of the VAE algorithm with an architecture modified for tabular data (*i.e.*, 1-dimensional). However, as discussed by the authors, this method contains limitations since it is difficult to achieve DP with AE-based models since they access the original data during the training procedure, unlike GANs. Delgado et al. [88] studies the impact of data augmentation on supervised learning with small datasets. The authors compare four different AE architectures: Undercomplete, Sparse, Deep and Variational AE. Although any of the tested AE architectures improved classification performance, the deep and variational autoencoders were the best overall performing models.

One problem frequently found in industry settings is the training of ML models on imbalanced datasets. Since most supervised machine learning classifiers are designed to expect classes with similar frequencies, with highly skewed distributions in \mathcal{D}_L , the classifier's predictions tend to be biased towards overrepresented classes [3]. For example, one can predict correctly with over 99% accuracy whether credit card accounts were defrauded using a constant classifier. This issue can be addressed in 3 different ways: resampling, algorithmic modifications and cost-sensitive solutions [125]. Resampling techniques are more general approaches when opposed to algorithmic and cost-sensitive methods. They modify \mathcal{D}_L to ensure balanced class frequencies by removing majority class observations (*i.e.*, undersampling), producing synthetic minority class observations (*i.e.*, oversampling), or a combination of both. However, since undersampling removes observations from \mathcal{D}_L , it has the disadvantage of information loss [126] and lacks effectiveness when compared to oversampling methods [127, 128]. Oversampling can be considered a specific setting of data augmentation.

Oversampling is an appropriate technique when, given a set of n target classes, there is a collection C_{maj} containing the majority class observations and C_{min} containing the minority class observations such that $\mathcal{D}_L = \bigcup_{i=1}^n C_i$. The training dataset \mathcal{D}_L is considered imbalanced if $|C_{maj}| > |C_{min}|$. This imbalance is quantified using the Imbalance Ratio (IR), expressed as $IR = \frac{|C_{maj}|}{|C_{min}|}$. An oversampling algorithm with a standard generation policy will generate a $\mathcal{D}_L^s = \bigcup_{i=1}^n C_i^s$ that guarantees $|C_i \cup C_i^s| = |C_{maj}|, \forall i \in \{1, \dots, n\}$. The model f_θ will be trained using an artificially balanced dataset $\mathcal{D}'_L = \mathcal{D}_L \cup \mathcal{D}_L^s$.

Random Oversampling (ROS) is considered a classical approach to oversampling. It oversamples minority classes by randomly picking samples with replacement. It is a bootstrapping approach that, if generated in a smoothed manner (*i.e.*, by adding perturbations to the synthetic data), is also known as Random Oversampling Examples (ROSE) [54]. However, the random duplication of observations often leads to overfitting [129].

The Synthetic Minority Oversampling Technique (SMOTE) [55] attempts to address the data duplication limitation in ROS with a two stage data generation mechanism:

1. Selection phase. A minority class observation, $x^c \in C_{min}$, and one of its k -nearest neighbors, $x^{nn} \in C_{min}$, are randomly selected.
2. Generation phase. A synthetic observation, x^s , is generated along a line segment between x^c and x^{nn} : $x^s = \alpha x^c + (1 - \alpha)x^{nn}, \alpha \sim \mathcal{U}(0, 1)$.

Although the SMOTE algorithm addresses the limitations in ROS, it brings other problems, which motivated the development of several SMOTE-based variants [57]: (1) it introduces noise when a noisy minority class observations is assigned to x^c or x^{nn} , (2) it introduces noise when x^c and x^{nn} belong to different minority-class clusters, (3) it introduces near duplicate observations when x^c and x^{nn} are too close together and (4) it does not account for within-class imbalance (*i.e.*, different input space regions should assume a different importance according to the concentration of minority class observations).

Borderline-SMOTE [56] modifies SMOTE's selection mechanism. It calculates the k -nearest neighbors for all minority class observations and selects the ones that are going to be used as x^c in the generation phase. An observation is selected based on the number of neighbors belonging to a different class, where the observations with no neighbors belonging to C_{min} and insufficient number of neighbors belonging to C_{maj} are not considered for the generation phase. This approximates the synthetic observations to the

border of the expected decision boundaries. Various other methods were proposed since then to modify selection mechanism, such as K-means SMOTE [68]. This approach addresses within-class imbalance and the generation of noisy synthetic data by generating data within clusters. The data generation is done according to each cluster’s imbalance ratio and dispersion of minority class observations. DBSMOTE [69] also modifies the selection strategy by selecting as x^c the set of core observations in a DBSCAN clustering solution.

The Adaptive Synthetic Sampling approach (ADASYN) [58] uses a comparable approach to Borderline-SMOTE. It calculates the ratio of non-minority class observations within the k -nearest neighbors of each $x \in C_{min}$. The amount of observations to be generated using each $x \in C_{min}$ as x^c is determined according to this ratio; the more non-minority class neighbors an observation contains, the more synthetic observations are generated using it as x^c . The generation phase is done using the linear mechanism in SMOTE. However, this approach tends to aggravate the limitation (1) previously discussed. A second version of this method, KernelADASYN [59], replaces the generation mechanism with a weighted kernel density estimation. The weighing is done according to ADASYN’s ratio and the synthetic data is sampled using the calculated Gaussian Kernel function whose bandwidth is passed as an additional hyperparameter.

Modifications to SMOTE’s generation mechanism are less common and generally attempt to address problem of noisy synthetic data generation. Safe-level SMOTE [66] truncates the line segment between x^c and x^{nn} according to a safe level ratio. Geometric-SMOTE (G-SMOTE) [57] it generates synthetic data within a deformed and truncated hypersphere to also avoid the generation of near-duplicate synthetic data. It also introduces a modification of the selection strategy to combine the selection of majority class observations as x^{nn} to avoid the introduction of noisy synthetic data.

LR-SMOTE [67] modifies both the selection and generation mechanisms. The set of observations to use as x^c contains the misclassified minority class observations using a SVM classifier, out of which the potentially noisy observations are removed. The k-means clustering method is used to find the closest observations to the cluster centroids, which are used as x^c . The observations with a higher number of majority class neighbors are more likely to be selected as x^{nn} . Although the generation mechanism synthesizes observations as a linear combination between x^c and x^{nn} , it restricts or expands this range by setting $\alpha \sim \mathcal{U}(0, M)$, where M is a ratio between the average euclidean distance of each cluster’s minority class observations to x^c and the euclidean distance between x^c and x^{nn} .

The Minority Oversampling Kernel Adaptive Subspaces algorithm (MOKAS) [60] adopts a different approach when compared to SMOTE-based mechanisms. It uses the adaptive subspace self-organizing map (ASSOM) [130] algorithm to learn sub-spaces (*i.e.*, different feature spaces for each unit in the SOM), out of which synthetic data is generated. The synthetic data is generated using a lower dimensional representation of the input data to ensure the reconstructed data is different from the original observations. Overall, the usage of SOMs for oversampling is uncommon. Another two examples of this approach, SOMO [61] and G-SOMO [62] use a similar approach as K-means SMOTE. In the case of G-SOMO, instead of using SMOTE’s generation mechanism, it uses G-SMOTE’s instead.

Oversampling via VAE [63]

Oversampling via GMM [64, 65]

Another set of network-based methods that fully replace SMOTE-based mechanisms are GAN-based architectures. One example of this approach is CGAN [70]. It uses an adversarial training approach to generate data that approximates the original data distribution and indistinguishable from the original dataset (according to the adversarial classifier). A more recent GAN-based oversampler, K-means

CTGAN [71] uses a K-means clustering method as an additional attribute to train the CTGAN. In this case, cluster labels allow the reduction of within-class imbalance. These types of approaches benefit from learning the overall per-class distribution, instead of using local information only. However, GANs require more computational power to train, their performance is sensitive to the initialization and are prone to the “mode collapse” problem.

Statistical-based oversampling approaches are less common. Some methods, such as RACOG and wRACOG [74] are based on Gibbs sampling, PDFOS [76] is based on probability density function estimations and RWO [75] uses a random walk algorithm.

Although oversampling for classification problems using continuous features appears as a relatively well explored problem, there is a general lack of research on oversampling using nominal features or mixed data types (*i.e.*, using both nominal and continuous features) and regression problems. SMOTENC [55] introduces a SMOTE adaptation for mixed data types. It calculates the nearest neighbors of x^c by including in the euclidean distance metric the median of the standard deviations of the continuous features for every nominal feature values that are different between x^c and x^m . The generation is done using the normal SMOTE procedure for the continuous features and the nominal features are determined with their modes within x^c ’s nearest neighbors. The SMOTEN [55] is an oversampling algorithm for nominal features only. It uses the nearest neighbor approach proposed in Cost et al. [131] and generates x^s using the modes of the features in x^c ’s nearest neighbors. Solutions to oversampling in regression problems are generally also based on SMOTE, such as SMOTER [72] and G-SMOTER [73].

4.4 Active Learning

AL is an informed approach to data collection and labeling. In classification problems, when $|\mathcal{D}_U| \gg |\mathcal{D}_L|$ and it is possible to label data according to a given budget, AL methods will search for the most informative unlabeled observations. Once labeled and included into the training set, these observations are expected to improve the performance of the classifier to a greater extent when compared to randomly selecting observations. AL is an iterative process where, at each iteration, an acquisition function $f_{acq}(x, f_\theta) : \mathcal{D}_U \rightarrow \mathbb{R}$ computes a classification uncertainty score for each unlabeled observation. f_{acq} provides the selection criteria based on the uncertainty scores, f_θ and the labeling budget [4].

One way to improve an AL process is via the generation of synthetic data. In this case, synthetic data is expected to improve classification with a better definition of the classifier’s decision boundaries. This allows the allocation of the data collection budget over a larger area of the input space. However, research focused on this topic is both recent and limited [CITATION]. These methods can be divided into AL with pipelined data augmentation approaches and AL with within-acquisition data augmentation. Pipelined data augmentation is the more intuitive approach, where at each training phase data augmentation is done to improve the quality of the classifier and is independent from f_{acq} . In Fonseca et al. [36], the pipelined approach in tabular data achieves a superior performance compared to the traditional AL framework using the G-SMOTE algorithm and the oversampling generation policy. Other methods, although developed and tested on image data, could also be adapted for tabular data: in the Bayesian Generative Active Deep Learning framework [89] the authors propose VAEACGAN, which uses a VAE architecture along with an auxiliary-classifier generative adversarial network (ACGAN) [132] to generate synthetic data.

The Look-Ahead Data Acquisition via augmentation algorithm [4] proposes an acquisition function that considers the classification uncertainty of synthetic data generated using a given unlabeled observation, instead of only estimating classification uncertainty of the unlabeled observation itself. This approach considers both the utility of the augmented data and the utility of the unlabeled observation. This

goal is achieved with the data augmentation method InfoMixup, which uses M-Mixup [78] along with the distillation of the generated synthetic data using f_{acq} . The authors additionally propose InfoSTN, although the original Spatial Transform Networks (STN) [133] were originally designed for image data augmentation.

4.5 Semi-supervised Learning

Semi-supervised learning (Semi-SL) techniques modify the learning phase of ML algorithms to leverage both labeled and unlabeled data. This approach is used when $|\mathcal{D}_U| \gg |\mathcal{D}_L|$ (similarly to AL settings), but additional labeled data is impossible or difficult to acquire. In recent years the research developed in this area directs much of its focus to neural network-based models and generative learning [38]. Overall, Semi-SL can be distinguished between transductive and inductive methods. In this section, we will focus on synthetic data generation mechanisms in inductive, perturbation-based Semi-SL algorithms applicable to tabular or feature space data.

Ladder networks [90] is semi-supervised learning architecture that learns a manifold feature space using a Denoising Autoencoder (DAE). The synthetic data is generated during the learning phase; random noise introduced into the input data and the DAE learns to predict the original observation. Although this method was developed for image data, DAE networks can be adapted for tabular data [134].

The Π -model uses labeled and unlabeled data jointly in the training phase [91]. Besides minimizing cross-entropy, they add to the loss function the squared difference between two input level transformations (Gaussian noise and other image-specific methods) in the network’s output layer (with dropout). In this case, the perturbations are applied both in the input space (via Gaussian noise) and feature space (via dropout). This model served as the source for the Mean Teacher algorithm [92], which used the same types of augmentation. The Interpolation Consistency Training (ICT) [93] method combined the mean teacher and the Mixup approach, where synthetic observations are generated using only the unlabeled observations and their predicted label using the teacher model. In Mixmatch [94], the Mixup method is used by randomly selecting any pair of observations and their true labels (if it’s a labeled observation) or predicted label (if it’s unlabeled).

The development of Semi-SL algorithms specifically adapted for tabular data is limited. The Semi-SL data augmentation for tabular data (SDAT) algorithm [95] uses an autoencoder to generate synthetic data in the feature space with Gaussian perturbations. The Contrastive Mixup (C-Mixup) [97] algorithm generates synthetic data using the Mixup mechanism with observation pairs within the same target label. The Mixup Contrastive Mixup algorithm (MCoM) [96] proposes the triplet Mixup method using three observations where $x^s = \lambda_i x_i + \lambda_j x_j + (1 - \lambda_i - \lambda_j) x_k$, where $\lambda_i, \lambda_j \sim \mathcal{U}(0, \alpha)$, $\alpha \in (0, 0.5]$ and x_i, x_j and x_k belong to the same target class. The same algorithm also uses the M-Mixup method as part of the feature space learning phase.

4.6 Self-supervised Learning

Self-supervised learning (Self-SL), although closely related to Semi-SL, assumes \mathcal{D}_L to be either empty or very small. These models focus on representation learning using \mathcal{D}_U using secondary learning tasks, which can be adapted to almost all types of downstream tasks [135]. This family of techniques allow the usage of raw, unlabeled data, which is generally cheaper to acquire when compared to processed, curated and labeled data. Although not all Self-SL methods rely on data augmentation (*i.e.*, STab [136]), the

majority of state-of-the-art tabular Self-SL methods use data augmentation as a central concept for the training phase.

The value imputation and mask estimation method (VIME) [10] is a Semi-SL and Self-SL approach that introduces Masking, a tabular data augmentation method. It is motivated by the need to generate corrupted, difficult to distinguish synthetic data in a computationally efficient way for Self-SL training. They replace with probability p_m feature values in x_i with another randomly selected value of each corresponding feature. To do this, the authors use a binomial mask vector $m = [m_1, \dots, m_d]^\top \in \{0, 1\}^d$, $m_j \sim \text{Bern}(p_m)$, observation x_i and the noise vector ϵ (*i.e.*, the vector of possible replacement values). A synthetic observation is produced as $x^s = (1 - m) \odot x_i + m \odot \epsilon$. A subsequent study proposed the SubTab [98] framework present a multi-view approach; analogous to cropping in image data or feature bagging in ensemble learning. In addition the authors propose an extension of the masking approach proposed in VIME by introducing noise using different approaches: Gaussian noise, swap-noise (*i.e.*, the approach proposed in VIME) and zero-out noise (*i.e.*, randomly replace a feature value by zero).

The Self-supervised contrastive learning using random feature corruption method (Scarf) [99] uses a similar synthetic data generation approach as VIME. Scarf differs from VIME by using contrastive loss instead of the denoising auto-encoder loss used in VIME, but this topic is out of the scope of this paper. A-SFS [100] is a Self-SL algorithm designed for feature extraction. It achieved higher performance compared to equivalent state-of-the-art augmentation-free approaches such as Tabnet [137] and uses the masking generation mechanism described in VIME.

5 Generation mechanisms

In this section we provide a general description of the synthetic data generation mechanisms found in the learning problems in Section 4. Table 3 summarizes the assumptions and usage of the generation mechanisms across the selected works and learning problems.

Table 3: Analysis of synthetic data generation mechanisms.

Type	Mechanism	Smoothness	Manifold	Priv.	Reg.	Ovs.	AL	Semi-SL	Self-SL
Perturbation	Random	✓	✓	×	×	✓	×	×	×
	Laplace	✓	✓	✓	×	×	×	×	×
	Gaussian	✓	✓	✓	✓	×	×	✓	✓
	Swap-noise	×	×	×	×	×	×	✓	✓
	Zero-out noise	×	×	×	×	×	×	×	✓
PDF	Gaussian Gen.	×	✓	✓	×	✓	×	×	×
	Gaussian Mix.	×	✓	✓	×	✓	×	×	×
	KDE	×	✓	×	×	✓	×	×	×
PGM	Bayesian Net.	×	×	✓	✓	×	×	×	×
	Gibbs	×	×	×	✓	✓	×	×	×
	Random Walk	×	×	×	×	✓	×	×	×
Linear	Between-class Int.	×	✓	×	✓	×	✓	✓	×
	Within-class Int.	✓	✓	×	✓	✓	✓	✓	×
	Extrapolation	✓	✓	×	✓	✓	×	×	×
	Inter.+Extra.	✓	✓	×	×	✓	×	×	×
	Difference Transf.	✓	✓	×	✓	×	×	×	×

Continued on next page

Table 3: Analysis of synthetic data generation mechanisms.

Type	Mechanism	Smoothness	Manifold	Priv.	Reg.	Ovs.	AL	Semi-SL	Self-SL
	Hard Extra.	✓	✓	×	✓	×	×	×	×
Geometric	Hypersphere	✓	✓	×	×	✓	✓	×	×
	Triangular	✓	✓	×	×	×	×	✓	×
	Hyperrectangle	×	✓	×	✓	×	×	×	×
Neural nets.	GAN	×	×	✓	✓	✓	✓	×	×
	AE	×	×	×	✓	✓	✓	✓	×
Others	Exponential M.	×	×	✓	×	×	×	×	×
	Reconstruction err.	×	×	×	×	✓	×	×	×

We focus on 2 key conditions for the data generation process, smoothness and manifold space. The smoothness condition requires that if two observations x_i, x_j are close, then it's expected that y_i, y_j have the same value. The manifold condition requires synthetic data generation to occur within locally euclidean topological spaces. Therefore, a generation mechanism with the smoothness requirement also requires a manifold, while the opposite is not necessarily true.

In the remaining subsections we will describe the main synthetic data generation mechanisms found in the literature, based on the studies discussed in Section 4.

5.1 Perturbation Mechanisms

The general perturbation-based synthetic data generation mechanism is defined as $x^s = x_i + \epsilon$, where ϵ is the noise vector sampled from a certain distribution. The random perturbation mechanism can be thought of as the non-informed equivalent of PGMs and PDFs. It samples $|\epsilon|$ values from a uniform distribution, i.e., $e_i \sim \mathcal{U}(\cdot, \cdot), \forall e_i \in \epsilon$, while the minimum and maximum values depend on the context and level of perturbation desired, typically centered around zero.

Laplace (commonly used in DP algorithms) and Gaussian perturbations sample ϵ with $e_i \sim \text{Lap}(\cdot, \cdot)$ and $e_i \sim \mathcal{N}(\cdot, \cdot)$, respectively. Within the applications found, in the presence of categorical features, these methods tend to use n-way marginals (also known as conjunctions or contingency tables [53]) to ensure the generated data contains variability in the categorical features and the distribution of categorical feature values follows some given constraint. Although various other distributions could be used to apply perturbations, the literature found primarily focuses on introducing noise via random, Laplace and Gaussian distributions.

Masking modifies the original perturbation based approach by introducing a binomial mask vector, $m = [m_1, \dots, m_d]^\top \in \{0, 1\}^d, m_i \sim \text{Bern}(p_m)$ and the generation mechanism is defined as $x^s = (1 - m) \odot x_i + m \odot \epsilon$ [10]. The ϵ variable is defined according to the perturbation used. The Gaussian approach generates the noise vector as $\epsilon = x_i + \epsilon'$, where $e'_i \sim \mathcal{N}(\cdot, \cdot), \forall e'_i \in \epsilon'$. The swap-noise approach shuffles the feature values from all observations to form ϵ , while the zero-out noise approach sets all ϵ values to zero. Intuitively, the masking technique modifies an observation's feature values with probability p_m , instead of adding perturbations over the entire observation. Figure 2 shows a visual depiction of the masking technique.

ID	A	B	C			
1	0.27	0.77	0.99	<div style="display: flex; align-items: center;"><div style="margin-right: 10px;"><div style="border-left: 1px solid black; height: 100px; position: relative;"><div style="position: absolute; top: 0; left: -10px;">Swap-noise</div><div style="position: absolute; top: 30px; left: -10px;">Zero-out</div><div style="position: absolute; top: 60px; left: -10px;">Gaussian</div></div><div style="margin-left: 10px;">$\epsilon = \begin{bmatrix} 0.53 & 0.77 & 0.10 \end{bmatrix}$ $\epsilon = \begin{bmatrix} 0 & 0 & 0 \end{bmatrix}$ $\epsilon = \begin{bmatrix} 0.89 & 0.23 & 0.48 \\ -0.13 & +0.09 & +0.01 \end{bmatrix}$</div><div style="margin-left: 10px;">$\longrightarrow x^s = \begin{bmatrix} 0.89 & 0.77 & 0.10 \end{bmatrix}$ $\longrightarrow x^s = \begin{bmatrix} 0.89 & 0 & 0 \end{bmatrix}$ $\longrightarrow x^s = \begin{bmatrix} 0.89 & 0.32 & 0.49 \end{bmatrix}$</div></div></div>		
2	0.89	0.23	0.48			
3	0.53	0.66	0.31			
4	0.12	0.91	0.65			
5	0.64	0.01	0.10			
				$x_2 = \begin{bmatrix} 0.89 & 0.23 & 0.48 \end{bmatrix}$	$m = \begin{bmatrix} 0 & 1 & 1 \end{bmatrix}$	

Figure 2: Examples of synthetic observations generated with different masking approaches.

5.2 Probability Density Function Mechanisms

The Gaussian generative model, despite unfrequently used when compared to the remaining Probability Density Function mechanisms discussed in this subsection, is an essential building block for these mechanisms. In particular, we describe the multivariate gaussian approach, which follows near-Gaussian distribution assumptions. However, in high-dimensional data, it is possible to motivate this approach via the *Diaconis-Freedman-Meckes* effect [111], which states that high-dimensional data projections generally follow a nearly Gaussian distribution. The Gaussian generative model produces synthetic data from a Gaussian distribution $x^s \sim \mathcal{N}(\mu, \Sigma)$, where $\mu \in \mathbb{R}^d$ is a vector with the features' means and $\Sigma \in \mathbb{R}^{d \times d}$ is the covariance matrix. It follows the following density function [51]:

$$f(x) = \frac{1}{\sqrt{(2\pi)^d \det(\Sigma)}} \exp \left(-\frac{1}{2} (x - \mu)^T \Sigma^{-1} (x - \mu) \right) \quad (2)$$

Consequently, to define a Gaussian generative model it is only necessary to estimate the dataset's mean and covariance matrix.

A Gaussian mixture model (GMM) comprises several Gaussians that aim to represent normally distributed subpopulations within a dataset. Its training procedure allows the model to iteratively learn the subpopulations using the Expectation Maximization algorithm. A GMM becomes more appropriate than the Gaussian generative model when the data is expected to have more than one higher-density regions, leading to a poor fit of unimodal Gaussian models.

Kernel Density Estimation (KDE) methods use a kernel function to estimate the density of the dataset's distribution at each region of the input/feature space. Despite the various kernel options, the Gaussian kernel is commonly used for synthetic data generation [59]. The general kernel estimator is defined as follows:

$$\hat{p}(x) = \frac{1}{N + h} \sum_{i=1}^N K \left(\frac{x - x_i}{h} \right) \quad (3)$$

Where $N = |\mathcal{D}|$, h is a smoothing parameter known as bandwidth and K is the kernel function. The Gaussian kernel is defined as follows:

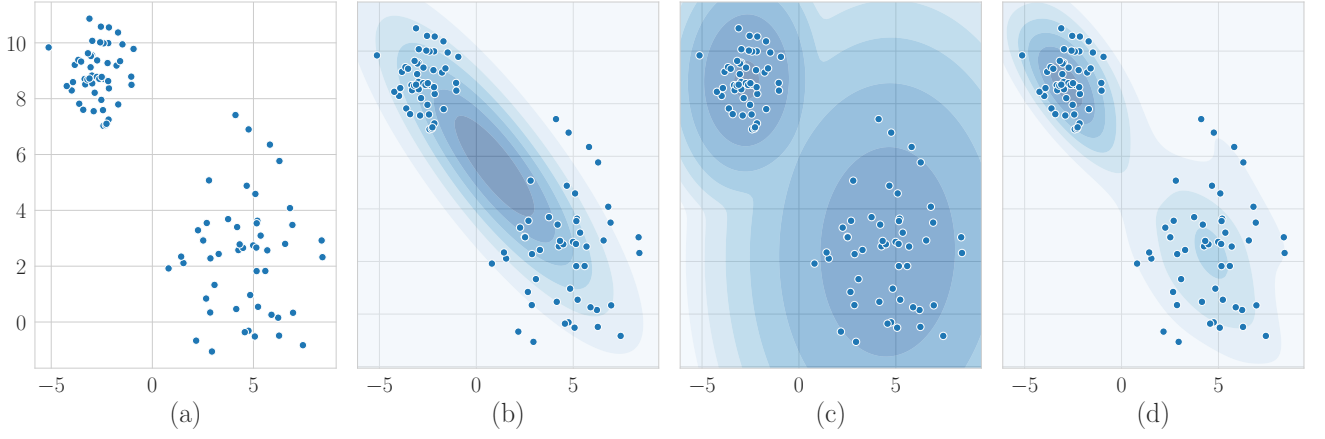


Figure 3: Examples of PDF mechanisms fitted to a mock dataset. Legend: (a) Original dataset, (b) Gaussian generative model, (c) Gaussian Mixture Model and (d) Gaussian Kernel Density Estimation.

$$G_i(x) = K\left(\frac{x - x_i}{h}\right) = \frac{1}{(\sqrt{2\pi}h)^d} \exp\left(-\frac{1}{2} \frac{(x - x_i)^T (x - x_i)}{h^2}\right) \quad (4)$$

Therefore, the Gaussian KDE approach can also be expressed as $\hat{p}(x) = \frac{1}{N+h} \sum_{i=1}^N G_i(x)$, while the data is sampled from the estimated probability distribution. Figure 3 shows a visualization of the PDF mechanisms discussed, applied to a mock dataset.

5.3 Probabilistic Graphical Models

A Bayesian network can be thought of as a collection of conditional distributions. It represents the joint probability distribution over the cross-product of the feature domains in \mathcal{D} . It is a directed acyclic graph that represents \mathcal{D} 's features as nodes and their conditional dependencies as directed edges. The set of features pointing directly to feature $v \in V, d = |V|$ via a single edge are known as the parent variables, $pa(v)$. A Bayesian network calculates $p(x)$ as the product of the individual density functions, based on the conditional probabilities of the parent variables:

$$p(x) = \prod_{v \in V} p(x_v | x_{pa(v)}) \quad (5)$$

Although this method requires the construction of a directed acyclic graph, there is research on ML approaches for the learning of these structures [138]. Bayesian networks can be used for synthetic data generation when the relationship between variables is known (or can be learned) and when the data is high dimensional, making the sampling process non-trivial.

Random walk algorithms comprise the general process of iterating through a set of random steps. Although uncommon, random walk approaches may be used to sample data. The random walk approach described in Zhang et al. [75] uses the Gaussian noise mechanism over minority class observations to create synthetic

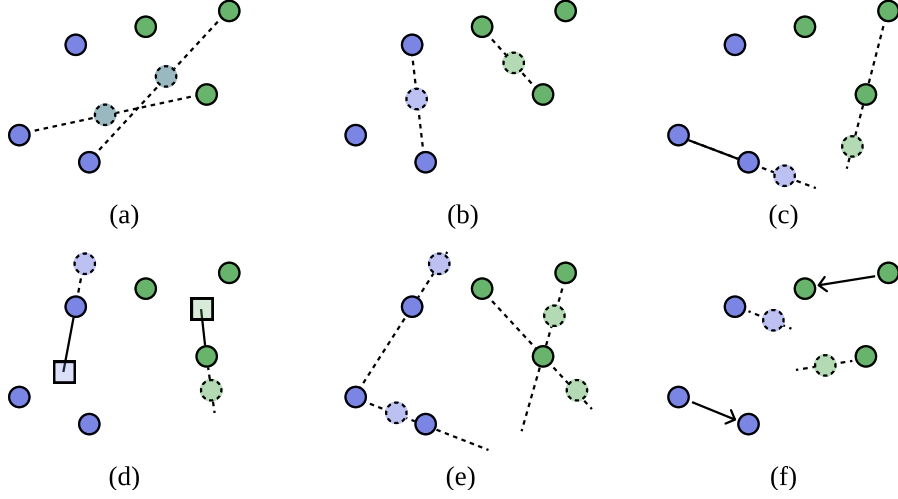


Figure 4: Examples of linear transformation mechanisms. Legend: (a) Between-class interpolation, (b) Within-class interpolation, (c) Observation-based extrapolation, (d) Mean-based extrapolation, (e) Combination of interpolation and extrapolation and (f) Difference transform.

observations. The Gibbs sampling mechanism also performs a random walk by iterating through sampled feature values.

Gibbs sampling is a Markov Chain Monte Carlo algorithm that iteratively samples a synthetic observation’s feature values. It is a suitable method to sample synthetic data from a Bayesian network. The process starts with an initial observation selected from \mathcal{D} , x_0 and is used to begin the sampling process. In its original format, the sampling of each feature value v in x_i^s is conditioned by x_{i-1}^s and the feature values already sampled from x_i^s , such that $x_{i,v}^s \sim p(x_{i,v}^s | x_{i,1}^s, \dots, x_{i,v-1}^s, x_{i-1,v+1}^s, \dots, x_{i-1,d}^s)$. Therefore, Gibbs sampling is a special case of the Metropolis-Hastings algorithm.

5.4 Linear Transformations

Linear interpolation mechanisms can be split into two subgroups: between and within-class interpolation. Both mechanisms follow a similar approach; they use a scaling factor λ , typically sampled from either $\mathcal{U}(0, 1)$ or $\text{Beta}(\alpha, \alpha)$:

$$x^s = \lambda x_i + (1 - \lambda)x_j = x_j + \lambda(x_i - x_j) \quad (6)$$

The within-class interpolation mechanism selects two observations from the same class, while the between-class interpolation mechanism selects two observations from different classes and also interpolates the one-hot encoded target classes y_i and y_j . However, the approach to select observations might vary according to the ML task and data generation algorithm. For example, most SMOTE-based methods select a center observation and a random observation within its k -nearest neighbors belonging to the same class, while the Mixup method selects two random observations, regardless of their class membership.

The observation-based linear extrapolation mechanism modifies Equation 6 such that $x^s = x_i + \lambda(x_i - x_j)$, while the mean-based extrapolation mechanism uses the mean of a class’ observations, μ^c and a randomly selected observation to generate $x^s = x_i^c + \lambda(x_i^c - \mu^c)$. The combination of both interpolation and

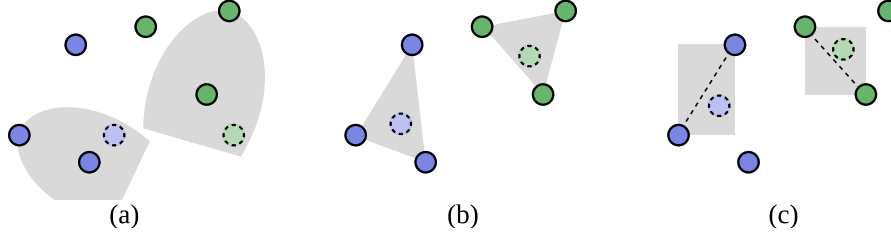


Figure 5: Examples of geometric transformation mechanisms. Legend: (a) hypersphere mechanism, (b) triangular mechanism and (c) hyperrectangle mechanism.

extrapolation mechanisms was found in the literature. This mechanism can be achieved using Equation 6 and modifying λ 's range to either decreasing its minimum value below zero or increasing its maximum value above one.

The difference transform mechanism uses two observations to compute a translation vector (multiplied by the scaling factor λ) and apply it on a third observation:

$$x^s = x_i + \lambda(x_j - x_k) \quad (7)$$

Although there are various linear transformation mechanisms in the literature, the majority of the relevant studies found applied linear interpolation mechanisms. Within-class interpolation was frequently found in oversampling methods, while between-class interpolation was found most often in regularization methods. A depiction of the linear transformation mechanisms found in the literature are presented in Figure 4.

5.5 Geometric Transformations

Overall, geometric transformation mechanisms were not frequently found in the literature. They are primarily used to develop Mixup or SMOTE-based variants. Figure 5 shows a visual example of the related mechanisms.

The hypersphere mechanism generates data within a distorted, n-dimensional hyperspheroid. It is formed using an observation to define the center of the geometry and another to define its edge. It is defined with two hyperparameters, the deformation factor, $\alpha_{def} \in [0, 1]$, and the truncation factor, $\alpha_{trunc} \in [-1, 1]$. The deformation factor deforms the hypersphere into an elliptic shape, where $\alpha_{def} = 1$ applies no deformation and $\alpha_{def} = 0$ creates a line segment. The truncation factor limits the generation area of the hyperspheroid within a subset of the hypersphere, where $\alpha_{trunc} = 0$ applies no truncation, $\alpha_{trunc} = 1$ uses the half of the area between the two selected observations and $\alpha_{trunc} = -1$ uses the opposing area. In Figure 5a, the two generation areas were formed using approximately $\alpha_{trunc} = \alpha_{def} = 0.5$.

The triangular mechanism selects three observations to generate $x^s = \lambda_i x_i + \lambda_j x_j + (1 - \lambda_i - \lambda_j) x_k$, where $\lambda_i, \lambda_j \sim \mathcal{U}(0, \alpha)$, $\alpha \in (0, 0.5]$. The hyperrectangle mechanism uses an approach similar similar to Equation 6. However, the scaling factor is changed into a scaling vector, $\Lambda = [\lambda_1, \dots, \lambda_d] \in [0, 1]^d$, $\lambda_i \sim \text{Beta}(\alpha, \alpha)$, where α is a hyperparameter used to define the Beta distribution. A synthetic observation is generated with $x^s = \Lambda \odot x_i + (1 - \Lambda) \odot x_j$, where \odot denotes the Hadamard product. This operation originates a generation area like the ones presented in Figure 5c.

5.6 Neural Networks

Generative Adversarial Network (GAN) architectures are structured as a minimax two-player game composed of two models, a generator and a discriminator. Both models are trained simultaneously throughout the learning phase to learn to generate data with similar statistical properties when compared to the original data. The generative model captures the data distribution, while the discriminator estimates the probability of an observation coming from the training data. The goal of the generator model is to produce synthetic observations that are capable of fooling the discriminator, making it impossible for the discriminator to distinguish real from synthetic observations. Although they were originally developed in an unsupervised learning setting [139], subsequent contributions proposed GANs for semi-SL, supervised learning and reinforcement learning.

An autoencoder (AE) is a type of neural network architecture that learns manifold representations of an input space. These models are typically trained by regenerating the input and are designed with a bottleneck in the hidden layers that corresponds to the learned feature space. It contains two parts, an encoder and a decoder. The encoder transforms the input data into lower-dimensional representations (*i.e.*, the feature space), while the decoder projects these representations into the original input space. Since it was first proposed [140], many variants were developed for multiple purposes. However, based on the literature found for synthetic data generation, the variational AE architecture appears to be the most popular approach.

6 Evaluating the Quality of Synthetic Data

The vast majority of synthetic data generation models are evaluated on a ML utility basis. There is a general lack of research on the development of metrics to evaluate the quality of synthetic data beyond common metrics such as Overall Accuracy (OA) or F1-score. One motivation to do this is the ability to anticipate the quality of the data after training a ML classifier, which may be an expensive and time-consuming task. This is a challenging problem, since the usefulness of synthetic data generators depend on the assumptions imposed according to the dataset, domain and ML problem [141]. This section focuses on the main evaluation approaches found in the literature, as well as recently proposed methods. For a more comprehensive analysis of performance metrics for synthetic data evaluation, the reader is referred to [142] and [12].

The GANBLR model [85] was evaluated on three aspects: (1) ML utility, (2) Statistical similarity, and (3) Interpretability. In Xu et al. [87], the authors evaluate the CTGAN and TVAE models using a likelihood fitness metric (to measure statistical similarity) and ML efficacy (*i.e.*, utility). Hittmeir et al. [143] evaluate synthetic data generators using a 2-step approach: Similarity comparison and data utility. According to Alaa et al. [13], the evaluation of generative models should quantify three key aspects of synthetic data:

1. Fidelity **TODO: DEFINE**
2. Diversity
3. Generalization

The effective evaluation of synthetic data generation methods is a complex task. A good performance with respect to one evaluation method does not necessarily imply a good performance on the primary ML

task, results from different evaluation methods seem to be independent and evaluating the models directly onto the target application is generally recommended [12]. Each evaluation procedure must be carefully implemented and adapted according to the use case.

6.1 Quantitative approaches

The Kullback-Leibler (KL) divergence (and equivalently the log-likelihood) is a common approach to evaluate generative models [12]. Other commonly used metrics, like Parzen window estimates, appear to be a generally poor quality estimation method and are not recommended for most applications Theis et al. [12]. KL divergence is defined as follows:

$$D_{KL}(P||Q) = \sum_{x \in \mathcal{X}} P(x) \log \frac{P(x)}{Q(x)} \quad (8)$$

Where \mathcal{X} is a probability space, P and Q are probability distributions based on \mathcal{D} and \mathcal{D}^s , respectively. KL divergence is a non symmetric measurement that represents how a reference/true probability distribution (P) differs from another (Q). A D_{KL} close to zero means Q is similar to P . However, metrics like the KL divergence or the log-likelihood are generally difficult to interpret, does not scale well for high dimensional data and fails to highlight model failures [13]. Another related metric, used in [144], is the Jensen-Shannon (JS) divergence. It consists of a symmetrized and smoothed variation adaptation of the KL divergence. Having $M = \frac{P+Q}{2}$, it is calculated as:

$$D_{JS}(P||Q) = \frac{D_{KL}(P||M) + D_{KL}(Q||M)}{2} \quad (9)$$

The Wasserstein Distance is another commonly used metric to estimate the distance between two distribution functions. It was also used to develop GAN variants since it improves the stability in the training of GANs [145, 146].

The propensity score was considered an appropriate performance metric to measure the utility of masked data [147]. This metric is estimated via the training of a classifier (typically a logistic regression) on a dataset merged with both the original and synthetic data and labeled information regarding the source of each observation (synthetic or original), to predict the likelihood of an observation to be synthetic. Therefore, this approach guarantees observation-level insights regarding the faithfulness of each observation. Woo et al. [147] suggest a summarization of this metric by computing:

$$U_p = \frac{1}{N} \sum_{i=1}^N (\hat{p}_i - c)^2 \quad (10)$$

Where $N = |\mathcal{D} \cup \mathcal{D}^s|$, $c = \frac{|\mathcal{D}^s|}{N}$ and \hat{p}_i is the estimated propensity score for unit i . This metric is also defined as the propensity Mean Squared Error (pMSE) [141]. When a synthetic dataset is relatively similar to the original dataset, U_p will be closer to zero. Furthermore, if the synthetic data is indistinguishable from the real data, the expected pMSE value is given by [148]:

$$E(pMSE) = \frac{(k-1)(1-c)^2c}{N} \quad (11)$$

Where k is the number of parameters in the logistic regression model (including bias). When the synthetic dataset is easily distinguishable from the original dataset, U_p will be close to $(1-c)^2$. Dankar et al. [30], established a generally consistent, weak negative correlation between U_p and OA.

Chundawat et al. [141] proposed TabSynDex to address the lack of uniformity of synthetic data evaluation, which can also be used as a loss function to train network-based models. It is a single metric evaluation approach bounded within $[0, 1]$ that consists of a combination between (1) the relative errors of basic statistics (mean, median and standard deviation), (2) the relative errors of correlation matrices, (3) a pMSE-based index, (4) a support coverage-based metric for histogram comparison and (5) the performance difference in a ML efficacy-based metric between models trained on real and synthetic data.

The three-dimensional metric proposed by Alaa et al. [13] presents an alternative evaluation approach. It combines three metrics (α -Precision, β -Recall and Authenticity) for various application domains. It extends the Precision and Recall metrics defined in [149] into α -Precision and β -Recall, which are used to quantify fidelity and diversity. Finally, the authenticity metric is estimated using a classifier that is trained based on the distance (denoted as d) between x^s and its nearest neighbor in \mathcal{D} , x_{i^*} ; if $d(x^s, x_{i^*})$ is smaller than the distance between x_{i^*} and its nearest neighbor in $\mathcal{D} \setminus \{x_{i^*}\}$, x^s will likely be considered unauthentic. This approach provides a three fold perspective over the quality of \mathcal{D}^s and allows a sample-level analysis of the generator’s performance. Furthermore, there is a relative trade-off between the two metrics used to audit the generator and the synthetic data; a higher α -Precision score will generally correspond to a lower Authenticity score and vice versa.

A less common evaluation approach is to attempt to replicate the results of studies using synthetic data [150, 151, 152]. Another method is the computation of the average distance among synthetic observations and their nearest neighbors within the original dataset [143]. The Confidence Interval Overlap and Average Percentage Overlap metrics may be used to evaluate synthetic data specifically for regression problems [153, 154].

6.2 Qualitative approaches

One of the approaches found in the literature is the comparison of the features’ distributions with synthetic data and the original data using histogram plots [143]. This comparison can be complemented with the quantification of these distribution differences [150]. Another evaluation method is the comparison of correlation matrices via heat map plots [143].

Another way to assess the quality of synthetic data is the subjective assessment by domain experts [150]. The goal of such test is to understand whether domain experts are able to distinguish synthetic from real data, which could be quantified with classification performance metrics. A low classification performance implies synthetic data that is difficult to distinguish from real data.

772 7 Discussion

773 The generation of tabular and feature space synthetic data has applications in multiple ML tasks
774 and domains. Specifically, we found six areas that were shown to benefit from synthetic data: data
775 privacy, regularization, oversampling, active learning, semi-supervised learning and self-supervised learning.
776 Synthetic data may be used either as an accessory task to improve a ML model’s performance over a
777 primary task (*e.g.*, regularization and oversampling), an intermediate task (*e.g.*, feature extraction), or
778 as a final product itself (*e.g.*, data anonymization). The analysis of data generation algorithms for each
779 relevant learning problem led to the proposal of a general purpose taxonomy primarily focused on the
780 underlying mechanisms used for data generation. We characterized every algorithm discussed in this work
781 into four categories: (1) architecture, (2) application level, (3) data space and (4) scope. The successful
782 implementation of synthetic data generation generally requires a few considerations:

- 783 1. Ensuring the dataset’s features are comprised within similar, fixed boundaries. For example, any
784 method using a neighbors-based approach will rely on distance measurements (typically the euclidean
785 distance), which is sensitive to the scale of the data and a nearest-neighbors estimation may vary
786 depending on whether the data was scaled *a priori*. This can be achieved with data scaling.
- 787 2. Various generation mechanisms require a manifold. There are two approaches to address non-
788 manifold input data: (1) Adopt methods sensitive to the presence of non-metric features, or (2)
789 project the input data into a manifold (*i.e.*, a feature space).
- 790 3. The smoothness assumption is prevalent in linear and perturbation-based data generation mechanisms.
791 If a classification problem has low class separation and difficult to solve, the choice in the design
792 of the generator algorithm is also difficult. Generally, generation algorithm with a global scope
793 might adapt better to classification problems with low separability. On the other hand, problems
794 with higher separability might require a definition of more uniform decision boundaries to prevent
795 overfitting, which can be achieved with generation algorithms with a local scope.
- 796 4. Considering the trade-off between performance and computational power. It is generally understood
797 that computationally-intensive approaches tend to produce synthetic data with higher quality. When
798 trained properly, neural network mechanisms typically lead to synthetic data that is more difficult
799 to distinguish compared to the remaining approaches. Geometric mechanisms have also achieved
800 good results but often require a careful tuning of their hyperparameters. Linear and perturbation
801 mechanisms do not require much training and use less hyperparameters, but have been know for
802 often producing low diversity synthetic data (*vis a vis* the original dataset).

803 This work focused primarily on the mechanisms used to generate synthetic observations; preprocessing,
804 learning phase design, feature space learning and ML task-specific contributions were secondary objectives
805 for analysis. Consequently, understanding of how the constraints within each task condition the choice
806 and design of the synthetic data generator is a subject of future work.

807 Throughout the analysis of the literature, we identified six types of generation mechanisms and discuss more
808 specific methods used in classical and state-of-the-art techniques. Techniques for data privacy via synthetic
809 data rely primarily on perturbation mechanisms, PDFs, PGMs and Neural networks. Regularization
810 approaches frequently employ Linear mechanisms. Other less commonly used mechanisms are PGMs,
811 Neural network approaches, geometric and perturbation mechanisms. Various Oversampling algorithms
812 have been proposed using each of the mechanisms found. However, the most prevalent mechanisms used
813 were linear-based. AL methods rarely employ synthetic data. The few studies found employ primarily
814 linear and geometric mechanisms, and a minority used AE models for feature space augmentation. Most

815 Semi-SL methods used perturbation and linear mechanisms, while geometric mechanisms are rarely used.
816 All tabular Self-SL methods used perturbation mechanisms.

817 Designing an approach to measure the quality of synthetic data depends on the target ML problem.
818 A wholistic evaluation approach for synthetic data should consider the analysis of (1) ML utility, (2)
819 Statistical similarity, (3) interpretability. The analysis of statistical similarity can be further divided into
820 (1) fidelity, (2) diversity and (3) generalization. However, balancing the analysis between these three
821 perspectives is not a straightforward task. For example, duplicating a dataset to form a synthetic dataset
822 will result into the best possible fidelity and diversity, but bad generalization. Overall, there is a paucity
823 of research into the development of comprehensive analyses of synthetic data, as well as understanding
824 the balance between the different types of analyses.

825 8 Future Work

826 As discussed throughout our analysis, it appears the synthetic data generation research is generally
827 sandboxed across ML problems and domains, even though all of these areas integrate synthetic data in its
828 core. Given the breadth and complexity of input-level and feature-level data generation mechanisms, it is
829 increasingly important to find an *a priori* approach to efficiently determine appropriate data generation
830 policies and techniques. However, the complexity of this task is determined by various factors: different data
831 types, ML problems, model architectures, computational resources, performance metrics and contextual
832 constraints. Auto-augmentation and meta learning aim to address this challenge and are still subject to
833 active research.

834 It is generally understood that, if learned properly, the feature space is expected to be convex and isotropic.
835 In that case, using linear generation techniques in the feature space would produce synthetic data without
836 introducing noise [81]. However, it is unclear which types of model/architectures and training procedures
837 contribute to the learning of a good feature space according to the context. Furthermore, we found a
838 limited amount of research on tabular data augmentation using auto-encoder architectures. Although
839 there are studies performing data augmentation on tabular data in various domains [88], defining the
840 architecture and learning phase of an AE is not an intuitive task. Generally, autoencoders are used to
841 learn a manifold for more complex data types. As long as the method used to generate the feature space
842 is appropriate, the methods discussed in this study could be used in the feature space regardless of the
843 type of data.

844 The quality of synthetic data generation in high-dimensional scenarios appears as a prevailing limitation
845 in various applications, especially within linear and geometric mechanisms. This limitation can be
846 addressed with dimensionality reduction techniques, as well as feature space learning. However, research
847 on generation in the feature space is greatly focused on GAN architectures, which require significant
848 computational power. Other methods to learn manifold embeddings could be explored to address this
849 limitation.

850 It remains an open question which generation mechanisms, or types of mechanisms, create better synthetic
851 data [81]. Although there is no one-size-fits-all solution, a general set of rules of thumb could be devised,
852 such as understanding how certain characteristics of a problem will affect the choice of the generation policy,
853 which types of mechanisms are more appropriate for different types of dataset, ML model architecture,
854 domains and target ML problem, or the trade-offs between the different types of generation mechanism. A
855 better understanding of the relationship between recently proposed methods for evaluating synthetic data
856 (as discussed in Section 6) and the performance on the target ML problem might contribute to answer

857 this question. Furthermore, determining the use cases, quality and general performance of data generation
858 on the input, feature and output space should be further developed. Finally, it is still unclear why synthetic
859 data generation works for each of the ML tasks discussed. Research on this topic lacks depth and fails to
860 address the theoretical underpinnings [7, 155].

861 The evaluation of anonymization techniques lack standardized, objective and reliable performance metrics
862 and benchmark datasets to allow an easier comparison across classifiers to evaluate key aspects of data
863 anonymization (resemblance, utility, privacy and performance). These datasets should contain mixed data
864 types (*i.e.*, a combination of categorical, ordinal, continuous and discrete features) and the metrics should
865 evaluate the performance of different data mining tasks along with the anonymization reliability. This
866 problem appears to be universal across domains. For example, Hernandez et al. [15] observed the lack of
867 a universal method or metric to report the performance synthetic data generation algorithms for tabular
868 health records. Therefore, in order to facilitate the usage of these techniques in industry domains, these
869 benchmarks must also be realistic. Rosenblatt et al. [44] attempts to address this problem by proposing a
870 standardized evaluation methodology using standard datasets and real-world industry applications.

871 Unlike data privacy solutions, studies on data augmentation techniques generally do not consider the
872 similarity/dissimilarity of synthetic data. The study of quality metrics for supervised learning may reduce
873 computational overhead and experimentation time. Only one study related to the relationship of quality
874 metrics and performance in the primary ML task was found in [30], which was done only for the pMSE
875 metric.

876 Neural network mechanisms typically involve a higher computational cost compared to the remaining types
877 of mechanisms. This problem is further aggravated with their inconsistent performance, since different
878 initializations may result in very different performances. This problem may be observed in [70]. More
879 generally, feature space representations of training data raises the challenge of interpreting representations;
880 the ability to interpret feature space representations could guide the design of data generation techniques.

881 In non-tabular data domains, a common approach for data augmentation is the combination of several
882 data augmentation methods to increase the diversification of synthetic data. This is true for both text
883 classification [18] and image classification [5]. However, for tabular data, no studies were found that
884 discuss the potential of ensembles of generation mechanisms on tabular data, *i.e.*, understanding how
885 selecting with different probabilities different generation mechanisms to generate synthetic data would
886 affect the performance of the primary ML task. The formalization and analysis carried out in this work,
887 regarding the different types of synthetic data generation mechanisms and quality metrics for feature and
888 tabular synthetic data at an observation level, may facilitate this work.

889 Various oversampling methods have been proposed to address imbalanced learning limitations. However,
890 there is still a major limitation in the literature regarding the oversampling of datasets with mixed data
891 types or with exclusively non metric features at the input space. In addition, the research on oversampling
892 using PDFs or PGMs is scarce.

893 To the best of our knowledge, research on few-shot learning for tabular data is scarce. Few-shot learning
894 research using synthetic data generation techniques has been extensively developed using image [156, 157]
895 and text data [158], but they are rarely adapted or tested for tabular data. One of the few studies found
896 achieved a good performance in both few-shot and zero-shot learning through the adaptation of a Large
897 Language model for tabular data [159].

898 Oversampling does not seem to be a relevant source of bias in behavioral research and does not appear to
899 have an appreciably different effect on results for directly versus indirectly oversampled variables [160].
900 However, most oversampling methods do not account for the training dataset’s distribution, which is

901 especially important for features with sensitive information (*e.g.*, gender or ethnicity). Therefore, the
902 application of oversampling methods on user data may further increase the bias in classification between
903 gender or ethnicity groups.

904 Finally, various synthetic data generation algorithms are research-based, and might not be usable or
905 feasible to be implemented by practitioners [18]. One way to address this problem is to publish the code
906 developed, and ideally make them available as open source libraries for out-of-the-box usage.

907 9 Conclusions

908 This literature review analyses various synthetic data generation-based algorithms for tabular data, with
909 a focus on external level applications. Since synthetic data generation is a crucial step for various ML
910 applications and domains, it is essential to understand and compare which techniques and types of
911 algorithms are used for each of these problems. The usage of synthetic data may be an effective approach
912 to prepare better datasets for a wide range of applications and/or preserve user privacy. Our work proposes
913 a taxonomy based on four key characteristics of generation algorithms, which was used to characterize
914 70 data generation algorithms across six ML problems. This analysis resulted in the categorization
915 and description of the generation mechanisms underlying each of the selected algorithms into six main
916 categories.

917 Despite the extensive research developed on various different methods for synthetic data generation, there
918 are still open questions regarding the theoretical underpinnings of synthetic data adoption for each of the
919 techniques, as well as limitations in the different types of generation mechanisms and evaluation procedures.
920 However, the empirical work presented in the literature show significant performance improvements and
921 promising research directions for future work.

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