

Geometric SMOTE for Imbalanced Datasets with Nominal and Continuous Features

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This is an abstract.

1. Introduction

Synthetic Minority Oversampling Technique (SMOTE) [1].

2. Related Work

This study focuses on multiclass classification problems. A classification problem contains n classes, having C_{maj} as the set of majority class observations (*i.e.*, observations belonging to the most common target class) and C_{min} as the set of minority class observations (*i.e.*, observations belonging to the least common target class). Typically, an oversampling algorithm will generate synthetic data in order to ensure $|C'_{min}| = |C_{maj}| = |C_i|, i \in \{1, \dots, n\}$.

Since the proposal of SMOTE, several other methods were built upon SMOTE to improve the quality of the data generated. The process of generating synthetic data using SMOTE-based algorithms can be divided into two distinct phases [CITATION]:

1. Data selection. A synthetic observation, x^s , is generated based on two existing observations. A SMOTE-based algorithm employs a given heuristic to select a non-majority class observation as the center observation, x^c , and one of its nearest neighbors, x^{nn} , selected randomly. For the case of SMOTE, x^c is randomly selected from each non-majority class.
2. Data generation. Once x^c and x^{nn} have been selected, x^s is generated based on a transformation between the two selected observations. In the case of SMOTE, this transformation is a linear interpolation between the two observations: $x^s = \alpha x^c + (1 - \alpha)x^{nn}, \alpha \sim \mathcal{U}(0, 1)$.

Modifications to the SMOTE algorithm can be distinguished according to the phase where the modifications were applied. This distinction is especially relevant for the case of oversampling on datasets with mixed data types, since it raises the challenge of computing meaningful distances and k-nearest neighbors among observations. For example, State-of-the-art oversampling methods, such as Borderline-SMOTE [2], ADASYN [3], K-means SMOTE [4] and LR-SMOTE [5] modify the data selection mechanism and show promising results in imbalanced learning [6]. However, all of these algorithms select x^c using procedures that include calculating each observation’s k-nearest neighbors or clustering methods, none of which is prepared to handle categorical data.

Modifications to SMOTE’s generation mechanism are less common. A few oversampling methods, such as Safe-level SMOTE [7] and Geometric-SMOTE [8] achieve such modifications and have shown promising results [9]. However, these methods are also unable to handle datasets with categorical data. This limitation is especially true for methods combining modifications in the selection and generation mechanisms, as is the case of the Geometric Self-Organizing Maps Oversampling algorithm [10]. Other methods attempt to replace the SMOTE data generation mechanism altogether using different Generative Adversarial Networks (GAN) architectures [11, 12, 13]. However, these models are not only computationally expensive to train but also sensitive to the training initialization, ensuring a balanced training of the two networks involved is difficult, and tuning their hyperparameters is often challenging or unfeasible [14].

As discussed in Section 1, research on resampling methods with mixed data types is scarce. The original paper proposing SMOTE also proposed SMOTE for Nominal and Continuous (SMOTENC), an adaptation of SMOTE to handle datasets with nominal and continuous features [1]. To determine the k-nearest neighbors of x^c , the nominal features encoded by multiplying the one-hot encoded categorical features by the median of the standard deviations of the continuous features. Once x^c and x^{nn} have been determined, the values of the continuous features in x^s are generated using the SMOTE generation mechanism, while the categorical features are given the most common values occurring in the k-nearest neighbors.

Alternatively to SMOTE-based methods, some non-informed over and undersampling methods may also be used for datasets with nominal and continuous features, specifically Random Oversampling (ROS) and Random Undersampling (RUS). These methods consist in randomly duplicating minority class observations (in the case of ROS), which can lead to overfitting [15, 16], or randomly removing majority class observations (in the case of RUS), which may lead to underfitting [17].

Only two oversampling algorithms capable of handling nominal and continuous features were found. Recently, a new SMOTE-based oversampling method for datasets with mixed data types, SMOTENC [18], was proposed. This method modifies the encoding mechanism for categorical features used in the SMOTENC algorithm to account for categorical features’ change of association with minority classes. The Multivariate Normal Distribution-based Oversampling for Numerical and Categorical features (MNDO-NC) [19] uses the original MNDO method [20] along with the SMOTENC encoding mechanism to find the values of the categorical features for the synthetic observation. However, the results reported in the paper showed that MNDO-NC was consistently outperformed by SMOTENC, which led us to discard this approach from further consideration.

3. Motivation

- There is no method available in the literature that addresses mixed data types while modifying the generation mechanism

- SMOTENC increases the possibility of near duplicates. This phenomenon was already visible with the original SMOTE oversampler. The generation of synthetic observations containing categorical features populated by majority voting further amplifies this effect. Therefore, increasing the diversity of the synthetic data generated becomes particularly relevant.
- The selection mechanism of Geometric-SMOTE has shown effective results in reducing the generation of noisy observations. This mechanism is not present in any of the relevant oversamplers discussed.

4. Proposed Method

We propose G-SMOTENC to handle both nominal and continuous features. This is an extension of the original G-SMOTE oversampler, which affects both its selection and generation mechanisms. Due to the novelty of the work, these modifications are based on the SMOTENC mechanism. However, this method can be extended with further modifications to the categorical data encoding and selection mechanisms in future work. The G-SMOTENC algorithm aims to address the limitations described in Section 3.

Similarly to G-SMOTE being an extension of SMOTE, G-SMOTENC is also an extension of SMOTENC since any method or ML pipeline using the SMOTENC generation mechanism can replace it by G-SMOTENC without any further modifications. The proposed method is described in pseudo-code in Algorithm 1. The functions *SelectionMechanism* and *GenerationMechanism* are described in Algorithms 2 and 3, respectively.

Algorithm 1: G-SMOTENC.

Given: Dataset with binary target classes C_{min} and C_{maj}
Input: $C_{maj}, C_{min}, \alpha_{sel}, \alpha_{trunc}, \alpha_{def}$
Output: C^{gen}
begin
 $N \leftarrow |C_{maj}| - |C_{min}|$
 $C^{gen} \leftarrow \emptyset$
 while $|C^{gen}| < N$ **do**
 $x^c, x^{nn}, X^{nn} \leftarrow \text{SelectionMechanism}(C_{maj}, C_{min}, \alpha_{sel})$
 $x^{gen} \leftarrow \text{GenerationMechanism}(x^c, x^{nn}, X^{nn}, \alpha_{trunc}, \alpha_{def})$
 $C^{gen} \leftarrow C^{gen} \cup \{x^{gen}\}$
end

4.1. Selection Mechanism

The data selection mechanism is preceded by the numerical encoding of the categorical features. It mixes the selection mechanisms of SMOTENC and G-SMOTENC, as shown in Algorithm 2.

The selection mechanism uses the minority, majority and combined mechanisms (introduced by G-SMOTE). However, the nominal features in the minority and majority class observations, C_{maj} and C_{min} are first encoded using a one-hot encoding approach and replacing the constant 1 with the median of the standard deviations of the continuous features in C_{min} divided by 2. The nearest-neighbors (X^{nn}) of x^c are determined based on α_{sel} , which are passed on to the generation mechanism to determine the nominal features' values of x^{gen} in the generation mechanism. Simultaneously, x^{nn} is randomly selected from X^{nn} and will be used to generate x^{gen} 's continuous features' values.

Algorithm 2: G-SMOTENC's selection mechanism.

Input: $C_{maj}, C_{min}, \alpha_{sel}$ **Output:** x^c, x^{nn}, X^{nn} **Function** $CatEncoder(C_{maj}, C_{min})$: $S \leftarrow$ Standard deviations of the continuous features in C_{min} $\sigma_{med} \leftarrow median(S)$ **forall** $i \in \{maj, min\}$ **do****forall** $f \in C_i^T$ **do****if** f is categorical **then** $f' \leftarrow OneHotEncode(f) \times \sigma_{med}/2$ $C'_i \leftarrow (C_i^T \setminus f)^T$ $C'_i \leftarrow (C_i^T \cup f')^T$ **return** C'_{maj}, C'_{min} **Function** $Surface(\alpha_{sel}, x^c, C_{maj}, C_{min})$:**if** $\alpha_{sel} = minority$ **then** $x^{nn} \in C_{min,k}$ // One of the k -nearest neighbors of x^c from C_{min} $X^{nn} \leftarrow C_{min,k}$ **if** $\alpha_{sel} = majority$ **then** $x^{nn} \in C_{maj,1}$ // Nearest neighbor of x^c from C_{min} $X^{nn} \leftarrow C_{maj,1}$ **if** $\alpha_{sel} = combined$ **then** $x_{min}^{nn} \in C_{min,k}$ $x_{maj}^{nn} \in C_{maj,1}$ $x^{nn} \leftarrow argmin(\|x_{min}^{nn} - x^c\|, \|x_{maj}^{nn} - x^c\|)$ $X^{nn} \leftarrow C_{min,k} \cup C_{maj,1}$ **return** x^{nn}, X^{nn} // X^{nn} is the set of k -nearest neighbors**begin** $C'_{maj}, C'_{min} \leftarrow CatEncoder(C_{maj}, C_{min})$ $x^c \in C'_{min}$ // Randomly select x^c from C'_{min} $x^{nn}, X^{nn} \leftarrow Surface(\alpha_{sel}, x^c, C'_{maj}, C'_{min})$ Reverse encoding of nominal features in x^c, x^{nn} and X^{nn}

4.2. Generation Mechanism

G-SMOTENC's generation mechanism is shown in Algorithm 3. It divides the generation of x^{gen} into two parts: (1) generation of continuous feature values and (2) generation of nominal feature values. At this stage, the nominal features from x^c and x^{nn} are discarded. Afterwards, the continuous features are generated using G-SMOTE's generation mechanism; within a hypersphere formed using the truncation and deformation hyperparameters (α_{trunc} and α_{def} , respectively). Finally, the nominal feature values are generated by the mode of each feature within the observations in X^{nn} .

In total, G-SMOTENC contains 3 hyperparameters: the selection strategy (α_{sel}), the truncation factor (α_{trunc}) and the deformation factor (α_{def}). Figure 1 depicts the effect of those hyperparameters in the data selection and generation phases. For an in-depth definition of the hyperparameters mentioned the reader may follow reference [8].

Algorithm 3: G-SMOTENC's generation mechanism.

Input: $x^c, x^{nn}, X^{nn}, \alpha_{trunc}, \alpha_{def}$ **Output:** x^s **Function** *Hyperball*():

- $v_i \sim \mathcal{N}(0, 1)$
- $r \sim \mathcal{U}(0, 1)$
- $x^{gen} \leftarrow r^{1/p} \frac{(v_1, \dots, v_p)}{\|(v_1, \dots, v_p)\|}$
- return** x^{gen}

Function *Vectors*(x^c, x^{nn}, x^{gen}):

- $e// \leftarrow \frac{x^{nn} - x^c}{\|x^{nn} - x^c\|}$
- $x// \leftarrow (x^{gen} \cdot e//)e//$
- $x^\perp \leftarrow x^{gen} - x//$
- return** $x//, x^\perp$

Function *Truncate*($x^c, x^{nn}, x^{gen}, x//, \alpha_{trunc}$):

- if** $|\alpha_{trunc} - x//| > 1$ **then**
 - $x^{gen} \leftarrow x^{gen} - 2x//$
- return** x^{gen}

Function *Deform*($x^{gen}, x^\perp, \alpha_{def}$):

- return** $x^{gen} - \alpha_{def}x^\perp$

Function *Translate*(x^c, x^{gen}, R):

- return** $x^c + Rx^{gen}$

Function *GenNominal*(X^{nn}):

- $x_{nom}^{gen} = \emptyset$
- forall** $f \in (X^{nn})^T$ **do**
 - if** f *is categorical* **then**
 - $x_{nom}^{gen} \cup \{mode(f)\}$ // Ties are decided with random selection
- return** x_{nom}^{gen}

begin

- Discard nominal features from x^c and x^{nn}
- $x^{gen} \leftarrow Hyperball()$
- $x//, x^\perp \leftarrow Vectors(x^c, x^{nn}, x^{gen})$
- $x^{gen} \leftarrow Truncate(x^c, x^{nn}, x^{gen}, x//, \alpha_{trunc})$
- $x^{gen} \leftarrow Deform(x^{gen}, x^\perp, \alpha_{def})$
- $x^{gen} \leftarrow Translate(x^c, x^{gen}, \|x_{cont}^{nn} - x^c\|)$
- $x_{nom}^{gen} \leftarrow GenNominal(X^{nn})$
- $x^{gen} \leftarrow x^{gen} \cup x_{nom}^{gen}$

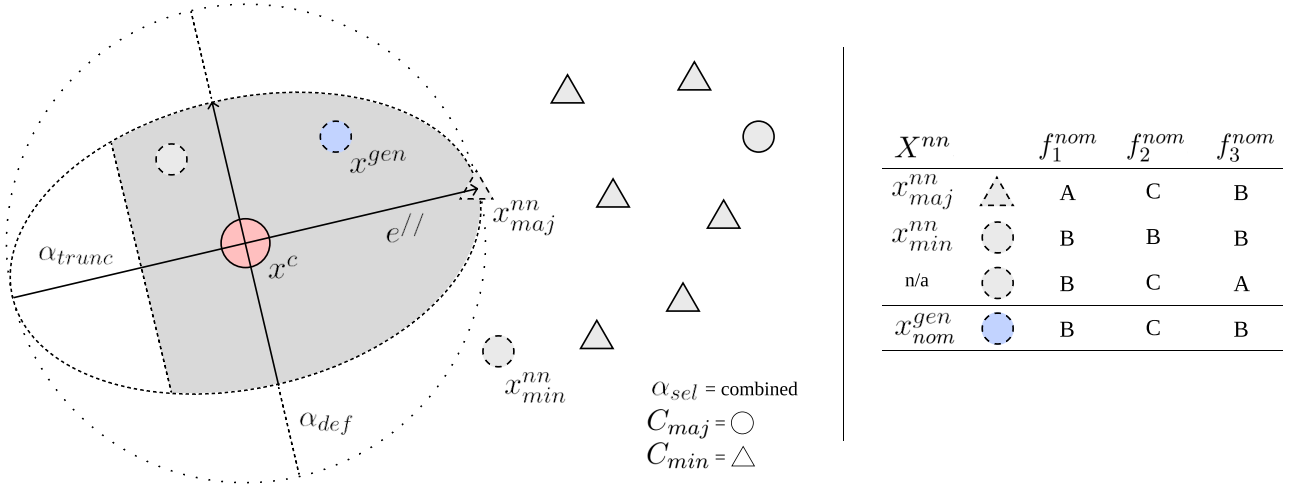


Figure 1: A visual depiction of G-SMOTENC. In this example, α_{trunc} is approximately 0.5 and α_{def} is approximately 0.4.

5. Methodology

This section describes how the evaluation of G-SMOTENC was performed. We describe the datasets used in the experiment, their source and preprocessing steps carried out in Section 5.1. We describe the resampling and classifications methods used for comparing the performance of G-SMOTENC with other relevant oversampling and undersampling methods in Section 5.2. The performance metrics used are defined in Section 5.3. Finally, the experimental procedure is described in Section 5.4.

5.1. Experimental Data

The datasets used in this experiment were extracted from the [UC Irvine Machine Learning Repository](#). All of the datasets are publicly available and cover a range of different domains. The selection of datasets was done to ensure that all datasets are imbalanced and contained non-metric features (*i.e.*, whether ordinal, nominal or binary). These datasets will be used to show how the performance of different classifiers varies according to the used over/undersampling method.

At an initial stage, all datasets were preprocessed manually with minimal manipulations, to avoid the application of preprocessing methods beyond the scope of this paper. This step was conducted to remove features and/or observations with missing values and identifying the non-metric features. The second stage of our preprocessing was done systematically. The resulting datasets are shown in Table 1.

Table 1: Description of the datasets collected after data preprocessing. The sampling strategy is similar across datasets. Legend: (IR) Imbalance Ratio

Dataset	Metric	Non-Metric	Obs.	Min. Obs.	Maj. Obs.	IR	Classes
Abalone	1	7	4139	15	689	45.93	18
Adult	8	6	5000	1268	3732	2.94	2
Adult (10)	8	6	5000	451	4549	10.09	2
Annealing	4	6	790	34	608	17.88	4
Census	24	7	5000	337	4663	13.84	2
Contraceptive	4	5	1473	333	629	1.89	3
Contraceptive (10)	4	5	1036	62	629	10.15	3
Contraceptive (20)	4	5	990	31	629	20.29	3
Contraceptive (31)	4	5	973	20	629	31.45	3
Contraceptive (41)	4	5	966	15	629	41.93	3
Coverttype	2	10	5000	20	2449	122.45	7
Credit Approval	9	6	653	296	357	1.21	2
German Credit	13	7	1000	300	700	2.33	2
German Credit (10)	13	7	770	70	700	10.00	2
German Credit (20)	13	7	735	35	700	20.00	2
German Credit (30)	13	7	723	23	700	30.43	2
German Credit (41)	13	7	717	17	700	41.18	2
Heart Disease	5	5	740	22	357	16.23	5
Heart Disease (21)	5	5	735	17	357	21.00	5

The second part of the data preprocessing pipeline starts with the generation of artificially imbalanced datasets with different Imbalance Ratios ($IR = \frac{|C_{maj}|}{|C_{min}|}$). For each original dataset, we create its more imbalanced versions at intervals of 10, while ensuring that $|C_{min}| \geq 15$. The sampling strategy was determined for class $n \in \{1, \dots, n, \dots, m\}$ as a linear interpolation using $|C_{maj}|$ and $|C'_{min}| = \frac{|C_{maj}|}{IR_{new}}$, as shown in equation 1.

$$|C_i|^{imb} = \min\left(\frac{|C'_{min}| - |C_{maj}|}{n - 1} \cdot |C_i| + |C_{max}|, |C_i|\right) \quad (1)$$

The new, artificially imbalanced dataset, is formed by sampling observations without replacement from each C_i such that $C'_i \subseteq C_i, |C'_i| = |C_i|^{imb}$. The artificially imbalanced datasets are marked with its imbalance ratio as a suffix in Table 1.

The datasets (both original and artificially imbalanced versions) are then filtered to ensure all datasets have a minimum of 500 observations. The remaining datasets whose number of observations is larger than 5000 are randomly sampled to match this number of observations. Afterwards, for each remaining dataset we remove all observations from target classes whose frequency is lower than 15 observations. Finally, the continuous and discrete features are scaled to the range $[0, 1]$ to ensure a common range between all features.

5.2. Machine Learning Algorithms

Table 2: Hyperparameter definition for the classifiers and resamplers used in the experiment.

Classifier	Parameter	Values
DT	min. samples split	2
	criterion	gini
	max depth	3, 6
LR	maximum iterations	10000
	multi-class	One-vs-All
	solver	saga
	penalty	None, L1, L2
KNN	# neighbors	3, 5
	weights	uniform
	metric	euclidean
RF	min. samples split	2
	# estimators	50, 100
	Max depth	3, 6
	criterion	gini
Resampler	Parameter	Values
SMOTENC	# neighbors	3, 5
SMOTE-ENC	# neighbors	3, 5
G-SMOTENC	# neighbors	3, 5
	deformation factor	0.0, 0.25, 0.5, 0.75, 1.0
	truncation factor	-1.0, -0.5, 0.0, 0.5, 1.0
	selection strategy	“combined”, “minority”, “majority”
RUS	replacement	False
ROS	(no applicable parameters)	

The choice of classifiers used in the experimental procedure were based on their type (tree-based, nearest neighbors-based, linear model and ensemble-based), popularity and consistency in performance. We used Decision Tree (DT), a K-Nearest Neighbors (KNN) classifier, a Logistic Regression (LR) and a Random Forest (RF).

Given the lack of existing oversamplers that address imbalanced learning problems with mixed data types, the amount of benchmark methods used is also limited. We used the well known methods and one state-of-the-art oversampling method that are compatible with this type of datasets: SMOTENC, RUS, ROS and SMOTE-ENC. Table 2 shows the hyperparameters used for the parameter search described in Section 5.4.

5.3. Performance Metrics

Although the typical performance metrics, *e.g.*, Overall Accuracy (OA), are intuitive to interpret, they are often inappropriate to measure a classifier’s performance in an imbalanced learning context [CITATION]. For example, to estimate an event that occurs in 1% of the dataset, a constant classifier would obtain an OA of 0.99 and still be unusable. However, this metric is still reported in some of our results to maintain a metric that is easier to interpret.

More recent surveys have found the Geometric-mean ($G\text{-mean} = \sqrt{\text{Sensitivity} \times \text{Specificity}}$), F1-score

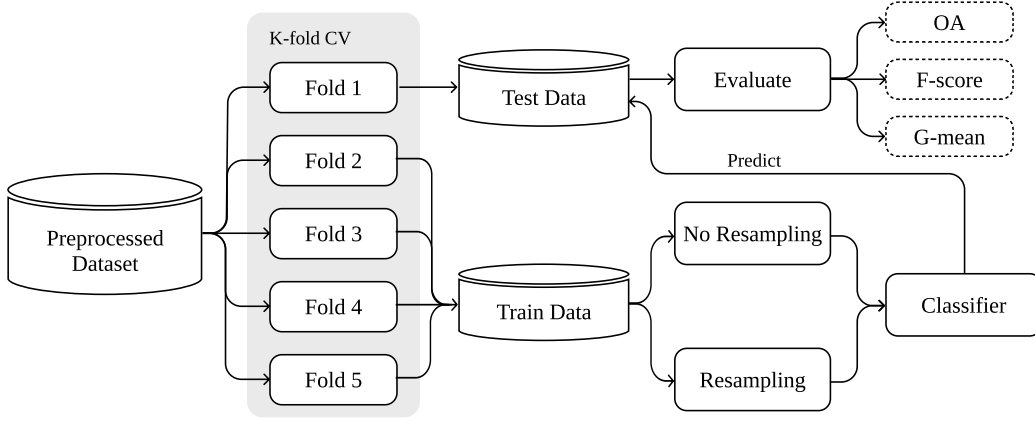


Figure 2: Experimental procedure used in this study.

($F\text{-score} = 2 \times \frac{\text{Precision} \times \text{Recall}}{\text{Precision} + \text{Recall}}$), $\text{Sensitivity} = \frac{TP}{FN+TP}$ and $\text{Specificity} = \frac{TN}{TN+FP}$ to be commonly used performance metrics in imbalanced learning contexts [21]. These metrics are calculated as a function of the number of False/True Positives (FP and TP) and False/True Negatives (FN and TN), having $\text{Precision} = \frac{TP}{TP+FP}$ and $\text{Recall} = \frac{TP}{TP+FN}$. This finding is consistent with other well-known recommendations on the usage of performance metrics [22]. This led us to adopt, along with OA, both F-score and G-mean as the main performance metrics for this study.

5.4. Experimental Procedure

The experimental procedure was applied similarly to all combinations of resamplers, classifiers and hyperparameter combinations across all datasets. The evaluation of the models' performance was tested using a 5-fold Cross Validation (CV) approach. The mean performance in the test set is calculated over the 5 folds and 3 different runs of the experimental procedure for each combination resampling/classifier hyperparameters. For each dataset, results of the hyperparameters that optimize the performance of a resampler/classifier are selected. These results were then used for analysis and are shown in Table 7 (see Appendix). Figure 2 shows a diagram of the experimental procedure described.

A CV run consists of a stratified partitioning (*i.e.*, each partition contains the same relative frequencies of target labels) of the dataset into five parts. A given resampler/classifier combination with a specific set of hyperparameters is fit and tested five times, using one of the partitions as a test set and the remaining ones as training set. The estimated performance consists of the average classification performance across the five different test sets.

5.5. Software Implementation

The algorithmic implementation of G-SMOTENC was written using the Python programming language and is available in the open-source package [ML-Research](#) [23], along with other utilities used to produce the experiment and outputs used in Section 6. In addition, the packages [Scikit-Learn](#) [24], [Imbalanced-Learn](#) [25] and [Research-Learn](#) were also used in the experimental procedure to get the implementations

of the classifiers, benchmark over/undersamplers and run the experimental procedure. The original SMOTE-ENC implementation was retrieved from the [authors' GitHub repository](#). The Latex code, Python scripts (including data pulling and preprocessing, experiment setup and results' analysis), as well as the datasets used are available in this [GitHub repository](#).

6. Results and Discussion

In this section we present the experimental results. We focus on the comparison of classification performance using oversamplers whose generation mechanism is compatible with datasets containing both continuous and categorical features.

The analysis of our experimental results were developed in two stages: (1) analysis of mean ranking and absolute performance and (2) statistical analysis. In Section 6.3 we discuss the main insights extracted by analysing the results reported in Sections 6.1 and 6.2.

6.1. Results

Table 3 presents the mean rankings of cross validation scores across the different combinations of oversamplers, metrics and classifiers. These results were calculated by assigning a ranking score for each oversampler from 1 (best) to 4 (worst) for each dataset, metric and classifier, based on the results reported in Table 7 (see Appendix).

Table 3: Mean rankings over the different datasets, folds and runs used in the experiment.

Classifier	Metric	G-SMOTENC	NONE	SMOTENC	ROS	RUS	SMOTE-ENC
DT	OA	1.66 \pm 0.13	1.61 \pm 0.27	3.58 \pm 0.20	4.68 \pm 0.15	5.42 \pm 0.27	4.05 \pm 0.23
DT	F-Score	1.32 \pm 0.11	3.84 \pm 0.40	3.13 \pm 0.20	4.32 \pm 0.19	5.47 \pm 0.23	2.92 \pm 0.34
DT	G-Mean	1.68 \pm 0.24	5.84 \pm 0.09	2.82 \pm 0.21	2.95 \pm 0.32	4.26 \pm 0.32	3.45 \pm 0.30
KNN	OA	2.50 \pm 0.17	1.37 \pm 0.28	4.21 \pm 0.25	3.34 \pm 0.35	5.68 \pm 0.22	3.89 \pm 0.15
KNN	F-Score	1.37 \pm 0.16	3.95 \pm 0.35	3.11 \pm 0.29	3.47 \pm 0.36	5.53 \pm 0.23	3.58 \pm 0.23
KNN	G-Mean	1.74 \pm 0.17	5.84 \pm 0.12	2.89 \pm 0.23	3.76 \pm 0.33	3.00 \pm 0.45	3.76 \pm 0.23
LR	OA	2.74 \pm 0.19	1.37 \pm 0.28	3.08 \pm 0.21	4.34 \pm 0.30	5.74 \pm 0.17	3.74 \pm 0.28
LR	F-Score	2.11 \pm 0.24	4.53 \pm 0.35	2.37 \pm 0.28	3.47 \pm 0.32	5.21 \pm 0.27	3.32 \pm 0.38
LR	G-Mean	2.13 \pm 0.26	6.00 \pm 0.00	3.61 \pm 0.21	2.11 \pm 0.23	3.32 \pm 0.40	3.84 \pm 0.28
RF	OA	1.82 \pm 0.11	1.24 \pm 0.09	3.97 \pm 0.16	4.32 \pm 0.21	5.92 \pm 0.06	3.74 \pm 0.22
RF	F-Score	1.32 \pm 0.13	5.05 \pm 0.31	3.16 \pm 0.22	3.05 \pm 0.31	5.37 \pm 0.14	3.05 \pm 0.27
RF	G-Mean	1.68 \pm 0.22	5.79 \pm 0.21	3.26 \pm 0.28	2.47 \pm 0.30	3.89 \pm 0.35	3.89 \pm 0.19

Table 4 presents the mean cross validation scores. With exception to the OA metric, G-SMOTENC either outperformed or matched the the remaining oversamplers.

Table 4: Mean scores over the different datasets, folds and runs used in the experiment

Classifier	Metric	G-SMOTENC	NONE	SMOTENC	ROS	RUS	SMOTE-ENC
DT	OA	0.74 ± 0.05	0.75 ± 0.04	0.68 ± 0.04	0.66 ± 0.04	0.58 ± 0.04	0.65 ± 0.04
DT	F-Score	0.56 ± 0.04	0.52 ± 0.04	0.54 ± 0.04	0.52 ± 0.04	0.48 ± 0.04	0.51 ± 0.04
DT	G-Mean	0.69 ± 0.03	0.60 ± 0.02	0.68 ± 0.03	0.67 ± 0.03	0.65 ± 0.03	0.66 ± 0.03
KNN	OA	0.69 ± 0.04	0.73 ± 0.05	0.67 ± 0.04	0.69 ± 0.05	0.57 ± 0.04	0.68 ± 0.05
KNN	F-Score	0.53 ± 0.04	0.50 ± 0.04	0.52 ± 0.04	0.52 ± 0.04	0.46 ± 0.04	0.51 ± 0.04
KNN	G-Mean	0.66 ± 0.03	0.58 ± 0.03	0.64 ± 0.03	0.62 ± 0.03	0.65 ± 0.03	0.63 ± 0.03
LR	OA	0.68 ± 0.05	0.75 ± 0.04	0.68 ± 0.05	0.66 ± 0.05	0.58 ± 0.04	0.67 ± 0.04
LR	F-Score	0.54 ± 0.04	0.52 ± 0.04	0.54 ± 0.04	0.53 ± 0.04	0.48 ± 0.04	0.52 ± 0.04
LR	G-Mean	0.69 ± 0.02	0.60 ± 0.03	0.68 ± 0.02	0.69 ± 0.03	0.67 ± 0.03	0.67 ± 0.03
RF	OA	0.74 ± 0.04	0.76 ± 0.04	0.69 ± 0.04	0.69 ± 0.04	0.59 ± 0.04	0.68 ± 0.05
RF	F-Score	0.57 ± 0.04	0.48 ± 0.04	0.55 ± 0.04	0.55 ± 0.04	0.49 ± 0.04	0.53 ± 0.04
RF	G-Mean	0.70 ± 0.02	0.57 ± 0.02	0.68 ± 0.03	0.69 ± 0.03	0.68 ± 0.03	0.68 ± 0.02

6.2. Statistical Analysis

To conduct an appropriate statistical analysis in an experiment with multiple datasets, it is necessary to use methods that account for the multiple comparison problem. Based on the recommendations found in [26], we applied the Friedman test along with the Holm-Bonferroni test for a post-hoc analysis.

In Section 5.3 we explained that OA, although easily interpretable, is not an appropriate performance metric for imbalanced learning problems. Therefore, the statistical analysis was developed using the two imbalance-appropriate metrics used in the study: F-Score and G-Mean. The statistical analysis started with the assessment of a statistically significant difference in performance across resampling methods using a Friedman test [27]. The results of this test are shown in Table 5. The null hypothesis is rejected in all cases.

Table 5: Results for Friedman test. Statistical significance is tested at a level of $\alpha = 0.05$. The null hypothesis is that there is no difference in the classification outcome across resamplers.

Classifier	Metric	p-value	Significance
DT	F-Score	2.2e-10	True
DT	G-Mean	1.2e-10	True
KNN	F-Score	2.3e-09	True
KNN	G-Mean	9.4e-10	True
LR	F-Score	2.1e-07	True
LR	G-Mean	9.7e-11	True
RF	F-Score	8.5e-12	True
RF	G-Mean	2.0e-10	True

We performed a Holm-Bonferroni test to understand whether the difference in performance of G-SMOTENC is statistically significant to the remaining resampling methods. The results of this test are shown in Table 6. The null hypothesis was rejected in 27 out of 32 tests.

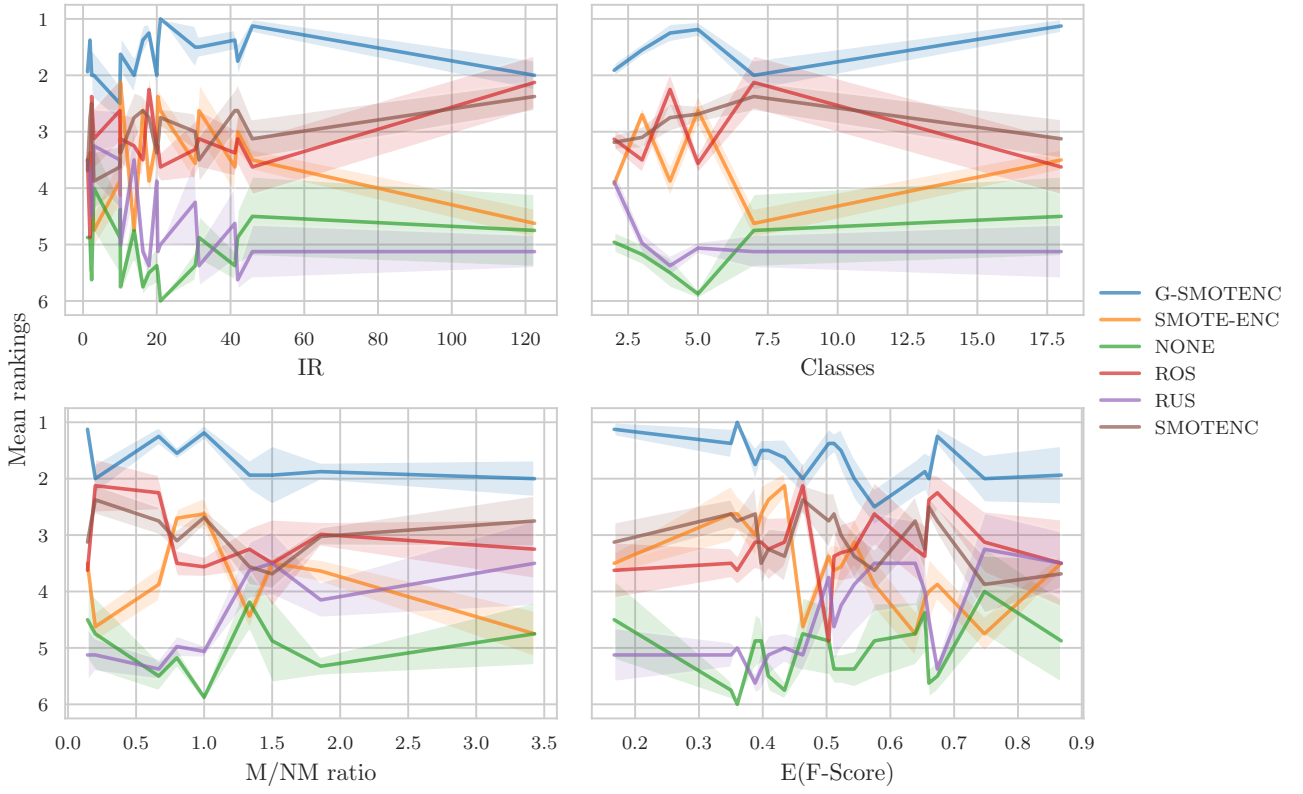


Figure 3: Average ranking of oversamplers over different characteristics of the datasets used in the experiment. Legend: IR — Imbalance Ratio, Classes — Number of classes in the dataset, M/NM ratio — ratio between the number of metric and non-metric features, E(F-Score) — Mean F-Score of dataset across all combinations of classifiers and oversamplers.

Table 6: Adjusted p-values using the Holm-Bonferroni test. Statistical significance is tested at a level of $\alpha = 0.05$. The null hypothesis is that the benchmark methods perform similarly compared to the control method (G-SMOTENC).

Classifier	Metric	MySMOTENC	NONE	RAND-OVER	RAND-UNDER	SMOTENC
DT	F-Score	1.0e-01	1.5e-04	7.3e-06	1.2e-06	1.5e-04
DT	G-Mean	2.3e-02	5.6e-07	2.8e-02	3.9e-04	2.7e-03
KNN	F-Score	5.9e-06	6.4e-04	7.2e-04	6.4e-04	2.2e-04
KNN	G-Mean	3.5e-03	1.6e-05	6.5e-03	2.0e-01	9.6e-03
LR	F-Score	5.6e-02	4.0e-03	9.2e-03	3.6e-04	6.1e-01
LR	G-Mean	4.7e-03	1.6e-07	8.6e-01	2.4e-01	4.0e-04
RF	F-Score	8.0e-03	1.7e-06	8.0e-03	1.7e-06	2.4e-04
RF	G-Mean	1.7e-03	3.8e-06	2.5e-01	2.3e-02	8.8e-03

6.3. Discussion

The results reported in Section 6.1 show that...

The results from this experiment expose some well-known limitations of SMOTE which become par-

ticularly evident with SMOTENC. Specifically, the loss of data variability and in some occasions the near-duplication of observations reveal that the performance of SMOTENC is comparable to ROS' performance.

7. Conclusion

This is a conclusion.

Future work should focus on more sophisticated encoding mechanisms for the categorical features.

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A. Appendix

Table 7: Wide optimal results

Dataset	Classifier	Metric	G-SMOTENC	NONE	SMOTENC	ROS	RUS	SMOTE-EL
Abalone	DT	OA	0.221	0.256	0.190	0.203	0.207	0.191
Abalone	DT	F-Score	0.168	0.170	0.156	0.154	0.132	0.158
Abalone	DT	G-Mean	0.460	0.413	0.445	0.457	0.421	0.443
Abalone	KNN	OA	0.215	0.237	0.186	0.197	0.188	0.191
Abalone	KNN	F-Score	0.167	0.157	0.150	0.151	0.140	0.153
Abalone	KNN	G-Mean	0.429	0.391	0.409	0.397	0.421	0.409
Abalone	LR	OA	0.235	0.272	0.228	0.229	0.195	0.228
Abalone	LR	F-Score	0.189	0.180	0.186	0.179	0.166	0.182
Abalone	LR	G-Mean	0.473	0.415	0.466	0.456	0.441	0.464
Abalone	RF	OA	0.237	0.276	0.221	0.224	0.197	0.225
Abalone	RF	F-Score	0.194	0.174	0.180	0.184	0.162	0.180
Abalone	RF	G-Mean	0.486	0.416	0.461	0.465	0.448	0.458
Adult	DT	OA	0.830	0.835	0.785	0.800	0.785	0.781
Adult	DT	F-Score	0.767	0.763	0.754	0.755	0.744	0.749
Adult	DT	G-Mean	0.809	0.747	0.808	0.806	0.801	0.799
Adult	KNN	OA	0.786	0.805	0.781	0.763	0.761	0.767
Adult	KNN	F-Score	0.738	0.732	0.735	0.718	0.728	0.720
Adult	KNN	G-Mean	0.766	0.724	0.762	0.757	0.780	0.752
Adult	LR	OA	0.803	0.839	0.803	0.804	0.801	0.799
Adult	LR	F-Score	0.768	0.773	0.767	0.771	0.769	0.764
Adult	LR	G-Mean	0.813	0.758	0.805	0.815	0.815	0.805
Adult	RF	OA	0.820	0.832	0.757	0.755	0.753	0.761
Adult	RF	F-Score	0.769	0.739	0.727	0.729	0.728	0.732
Adult	RF	G-Mean	0.796	0.711	0.787	0.797	0.797	0.793
Adult (10)	DT	OA	0.930	0.928	0.822	0.789	0.775	0.819
Adult (10)	DT	F-Score	0.711	0.708	0.656	0.641	0.630	0.644
Adult (10)	DT	G-Mean	0.812	0.663	0.807	0.815	0.808	0.788
Adult (10)	KNN	OA	0.864	0.909	0.854	0.851	0.745	0.853
Adult (10)	KNN	F-Score	0.667	0.652	0.658	0.648	0.602	0.652

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Table 7: Wide optimal results

Dataset	Classifier	Metric	G-SMOTENC	NONE	SMOTENC	ROS	RUS	SMOTE-E
Adult (10)	KNN	G-Mean	0.745	0.629	0.747	0.722	0.783	0.712
Adult (10)	LR	OA	0.836	0.925	0.837	0.815	0.791	0.831
Adult (10)	LR	F-Score	0.666	0.705	0.667	0.663	0.647	0.665
Adult (10)	LR	G-Mean	0.804	0.663	0.787	0.811	0.814	0.783
Adult (10)	RF	OA	0.899	0.924	0.773	0.763	0.743	0.781
Adult (10)	RF	F-Score	0.718	0.615	0.620	0.624	0.610	0.626
Adult (10)	RF	G-Mean	0.809	0.579	0.786	0.806	0.806	0.786
Annealing	DT	OA	0.824	0.843	0.742	0.733	0.694	0.720
Annealing	DT	F-Score	0.736	0.643	0.732	0.724	0.683	0.718
Annealing	DT	G-Mean	0.914	0.738	0.909	0.906	0.880	0.901
Annealing	KNN	OA	0.849	0.847	0.829	0.854	0.508	0.830
Annealing	KNN	F-Score	0.780	0.724	0.747	0.783	0.476	0.741
Annealing	KNN	G-Mean	0.901	0.781	0.867	0.909	0.814	0.856
Annealing	LR	OA	0.572	0.814	0.573	0.566	0.510	0.552
Annealing	LR	F-Score	0.620	0.540	0.617	0.615	0.496	0.499
Annealing	LR	G-Mean	0.851	0.663	0.843	0.848	0.811	0.821
Annealing	RF	OA	0.868	0.868	0.729	0.733	0.637	0.759
Annealing	RF	F-Score	0.800	0.644	0.730	0.736	0.641	0.743
Annealing	RF	G-Mean	0.917	0.727	0.904	0.910	0.873	0.887
Census	DT	OA	0.942	0.943	0.894	0.844	0.795	0.293
Census	DT	F-Score	0.733	0.731	0.693	0.652	0.617	0.258
Census	DT	G-Mean	0.813	0.698	0.800	0.814	0.817	0.621
Census	KNN	OA	0.874	0.933	0.867	0.878	0.731	0.871
Census	KNN	F-Score	0.652	0.648	0.655	0.640	0.567	0.641
Census	KNN	G-Mean	0.767	0.620	0.768	0.733	0.794	0.740
Census	LR	OA	0.940	0.949	0.938	0.940	0.815	0.828
Census	LR	F-Score	0.760	0.743	0.760	0.762	0.639	0.630
Census	LR	G-Mean	0.807	0.707	0.782	0.801	0.837	0.794
Census	RF	OA	0.876	0.933	0.819	0.740	0.714	0.799
Census	RF	F-Score	0.679	0.483	0.636	0.580	0.562	0.614
Census	RF	G-Mean	0.827	0.500	0.818	0.822	0.814	0.810
Contraceptive	DT	OA	0.563	0.538	0.537	0.512	0.525	0.528
Contraceptive	DT	F-Score	0.549	0.518	0.529	0.507	0.520	0.521
Contraceptive	DT	G-Mean	0.661	0.630	0.646	0.630	0.641	0.638
Contraceptive	KNN	OA	0.465	0.478	0.455	0.435	0.468	0.461
Contraceptive	KNN	F-Score	0.460	0.462	0.450	0.432	0.461	0.455
Contraceptive	KNN	G-Mean	0.588	0.580	0.579	0.566	0.590	0.583
Contraceptive	LR	OA	0.515	0.514	0.514	0.510	0.510	0.513
Contraceptive	LR	F-Score	0.512	0.492	0.509	0.505	0.506	0.508
Contraceptive	LR	G-Mean	0.635	0.604	0.631	0.628	0.627	0.630
Contraceptive	RF	OA	0.553	0.557	0.540	0.534	0.526	0.536
Contraceptive	RF	F-Score	0.545	0.524	0.535	0.529	0.522	0.530
Contraceptive	RF	G-Mean	0.659	0.634	0.653	0.649	0.643	0.649
Contraceptive (10)	DT	OA	0.645	0.645	0.568	0.528	0.487	0.592
Contraceptive (10)	DT	F-Score	0.479	0.452	0.478	0.454	0.414	0.490
Contraceptive (10)	DT	G-Mean	0.644	0.584	0.648	0.637	0.610	0.648
Contraceptive (10)	KNN	OA	0.524	0.570	0.508	0.495	0.451	0.512
Contraceptive (10)	KNN	F-Score	0.419	0.404	0.410	0.404	0.368	0.413

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Table 7: Wide optimal results

Dataset	Classifier	Metric	G-SMOTENC	NONE	SMOTENC	ROS	RUS	SMOTE-E
Contraceptive (10)	KNN	G-Mean	0.576	0.529	0.561	0.569	0.561	0.563
Contraceptive (10)	LR	OA	0.516	0.622	0.506	0.489	0.476	0.503
Contraceptive (10)	LR	F-Score	0.431	0.375	0.426	0.425	0.411	0.431
Contraceptive (10)	LR	G-Mean	0.619	0.526	0.609	0.624	0.618	0.621
Contraceptive (10)	RF	OA	0.648	0.651	0.569	0.550	0.494	0.573
Contraceptive (10)	RF	F-Score	0.500	0.387	0.473	0.471	0.425	0.480
Contraceptive (10)	RF	G-Mean	0.656	0.542	0.639	0.650	0.625	0.646
Contraceptive (20)	DT	OA	0.671	0.659	0.612	0.556	0.456	0.620
Contraceptive (20)	DT	F-Score	0.475	0.430	0.459	0.428	0.371	0.470
Contraceptive (20)	DT	G-Mean	0.643	0.570	0.626	0.632	0.605	0.645
Contraceptive (20)	KNN	OA	0.556	0.600	0.529	0.541	0.442	0.543
Contraceptive (20)	KNN	F-Score	0.399	0.375	0.384	0.389	0.345	0.395
Contraceptive (20)	KNN	G-Mean	0.565	0.519	0.544	0.537	0.549	0.556
Contraceptive (20)	LR	OA	0.506	0.641	0.508	0.486	0.440	0.514
Contraceptive (20)	LR	F-Score	0.397	0.375	0.397	0.389	0.358	0.393
Contraceptive (20)	LR	G-Mean	0.608	0.523	0.604	0.613	0.585	0.597
Contraceptive (20)	RF	OA	0.668	0.674	0.588	0.562	0.475	0.605
Contraceptive (20)	RF	F-Score	0.473	0.384	0.450	0.436	0.389	0.454
Contraceptive (20)	RF	G-Mean	0.659	0.535	0.641	0.670	0.633	0.642
Contraceptive (31)	DT	OA	0.667	0.670	0.608	0.604	0.440	0.644
Contraceptive (31)	DT	F-Score	0.454	0.441	0.438	0.453	0.346	0.454
Contraceptive (31)	DT	G-Mean	0.642	0.577	0.605	0.655	0.592	0.629
Contraceptive (31)	KNN	OA	0.563	0.633	0.545	0.550	0.405	0.548
Contraceptive (31)	KNN	F-Score	0.403	0.385	0.384	0.378	0.298	0.387
Contraceptive (31)	KNN	G-Mean	0.574	0.527	0.544	0.531	0.511	0.555
Contraceptive (31)	LR	OA	0.500	0.656	0.508	0.483	0.423	0.516
Contraceptive (31)	LR	F-Score	0.379	0.376	0.379	0.374	0.336	0.379
Contraceptive (31)	LR	G-Mean	0.597	0.523	0.579	0.585	0.580	0.574
Contraceptive (31)	RF	OA	0.681	0.683	0.608	0.583	0.442	0.616
Contraceptive (31)	RF	F-Score	0.450	0.378	0.434	0.435	0.349	0.452
Contraceptive (31)	RF	G-Mean	0.647	0.531	0.630	0.640	0.600	0.626
Contraceptive (41)	DT	OA	0.651	0.666	0.588	0.566	0.433	0.589
Contraceptive (41)	DT	F-Score	0.459	0.426	0.408	0.409	0.336	0.416
Contraceptive (41)	DT	G-Mean	0.622	0.573	0.579	0.589	0.555	0.589
Contraceptive (41)	KNN	OA	0.563	0.611	0.546	0.538	0.395	0.541
Contraceptive (41)	KNN	F-Score	0.393	0.373	0.381	0.370	0.289	0.373
Contraceptive (41)	KNN	G-Mean	0.542	0.515	0.550	0.526	0.515	0.531
Contraceptive (41)	LR	OA	0.525	0.658	0.524	0.504	0.435	0.530
Contraceptive (41)	LR	F-Score	0.389	0.375	0.393	0.387	0.336	0.393
Contraceptive (41)	LR	G-Mean	0.606	0.520	0.604	0.627	0.569	0.600
Contraceptive (41)	RF	OA	0.665	0.681	0.598	0.588	0.415	0.596
Contraceptive (41)	RF	F-Score	0.444	0.378	0.418	0.429	0.323	0.416
Contraceptive (41)	RF	G-Mean	0.612	0.528	0.616	0.616	0.566	0.608
Covertime	DT	OA	0.580	0.705	0.587	0.567	0.450	0.552
Covertime	DT	F-Score	0.484	0.490	0.481	0.475	0.361	0.474
Covertime	DT	G-Mean	0.769	0.671	0.758	0.758	0.700	0.751
Covertime	KNN	OA	0.690	0.700	0.683	0.699	0.454	0.636
Covertime	KNN	F-Score	0.532	0.457	0.535	0.561	0.367	0.484

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Table 7: Wide optimal results

Dataset	Classifier	Metric	G-SMOTENC	NONE	SMOTENC	ROS	RUS	SMOTE-E
Covertypes	KNN	G-Mean	0.745	0.642	0.753	0.763	0.691	0.744
Covertypes	LR	OA	0.637	0.721	0.640	0.611	0.472	0.617
Covertypes	LR	F-Score	0.516	0.507	0.526	0.492	0.353	0.429
Covertypes	LR	G-Mean	0.792	0.678	0.786	0.790	0.697	0.725
Covertypes	RF	OA	0.598	0.704	0.583	0.587	0.485	0.338
Covertypes	RF	F-Score	0.517	0.360	0.507	0.519	0.394	0.284
Covertypes	RF	G-Mean	0.800	0.572	0.799	0.804	0.737	0.691
Credit Approval	DT	OA	0.867	0.847	0.862	0.861	0.865	0.862
Credit Approval	DT	F-Score	0.867	0.845	0.862	0.861	0.865	0.862
Credit Approval	DT	G-Mean	0.874	0.848	0.869	0.867	0.872	0.869
Credit Approval	KNN	OA	0.870	0.865	0.868	0.870	0.865	0.867
Credit Approval	KNN	F-Score	0.869	0.864	0.867	0.869	0.864	0.866
Credit Approval	KNN	G-Mean	0.871	0.865	0.868	0.871	0.866	0.867
Credit Approval	LR	OA	0.873	0.868	0.871	0.874	0.873	0.873
Credit Approval	LR	F-Score	0.873	0.868	0.871	0.874	0.873	0.873
Credit Approval	LR	G-Mean	0.877	0.873	0.877	0.879	0.878	0.878
Credit Approval	RF	OA	0.876	0.877	0.871	0.868	0.868	0.873
Credit Approval	RF	F-Score	0.876	0.877	0.871	0.868	0.868	0.872
Credit Approval	RF	G-Mean	0.879	0.879	0.876	0.872	0.873	0.875
German Credit	DT	OA	0.704	0.713	0.702	0.660	0.644	0.701
German Credit	DT	F-Score	0.662	0.608	0.654	0.633	0.623	0.664
German Credit	DT	G-Mean	0.681	0.608	0.667	0.663	0.660	0.678
German Credit	KNN	OA	0.681	0.718	0.682	0.670	0.641	0.657
German Credit	KNN	F-Score	0.653	0.628	0.650	0.636	0.616	0.626
German Credit	KNN	G-Mean	0.675	0.621	0.668	0.656	0.642	0.646
German Credit	LR	OA	0.727	0.751	0.729	0.724	0.712	0.713
German Credit	LR	F-Score	0.695	0.681	0.697	0.697	0.686	0.676
German Credit	LR	G-Mean	0.722	0.672	0.713	0.720	0.713	0.696
German Credit	RF	OA	0.760	0.741	0.739	0.737	0.700	0.726
German Credit	RF	F-Score	0.701	0.580	0.702	0.709	0.680	0.688
German Credit	RF	G-Mean	0.715	0.588	0.716	0.730	0.719	0.699
German Credit (10)	DT	OA	0.909	0.906	0.804	0.713	0.696	0.752
German Credit (10)	DT	F-Score	0.575	0.539	0.572	0.526	0.511	0.539
German Credit (10)	DT	G-Mean	0.628	0.535	0.629	0.644	0.631	0.593
German Credit (10)	KNN	OA	0.787	0.913	0.757	0.835	0.684	0.795
German Credit (10)	KNN	F-Score	0.578	0.581	0.558	0.573	0.528	0.560
German Credit (10)	KNN	G-Mean	0.662	0.559	0.643	0.588	0.667	0.597
German Credit (10)	LR	OA	0.839	0.904	0.831	0.799	0.682	0.829
German Credit (10)	LR	F-Score	0.619	0.596	0.610	0.620	0.550	0.620
German Credit (10)	LR	G-Mean	0.683	0.578	0.675	0.716	0.722	0.681
German Credit (10)	RF	OA	0.910	0.909	0.865	0.877	0.696	0.860
German Credit (10)	RF	F-Score	0.624	0.476	0.614	0.661	0.557	0.610
German Credit (10)	RF	G-Mean	0.653	0.500	0.646	0.709	0.729	0.628
German Credit (20)	DT	OA	0.952	0.952	0.875	0.795	0.668	0.880
German Credit (20)	DT	F-Score	0.573	0.525	0.559	0.522	0.457	0.579
German Credit (20)	DT	G-Mean	0.666	0.529	0.679	0.690	0.629	0.674
German Credit (20)	KNN	OA	0.856	0.952	0.826	0.905	0.679	0.872
German Credit (20)	KNN	F-Score	0.561	0.535	0.528	0.556	0.491	0.538

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Table 7: Wide optimal results

Dataset	Classifier	Metric	G-SMOTENC	NONE	SMOTENC	ROS	RUS	SMOTE-E
German Credit (20)	KNN	G-Mean	0.692	0.527	0.635	0.570	0.709	0.601
German Credit (20)	LR	OA	0.913	0.952	0.910	0.838	0.680	0.891
German Credit (20)	LR	F-Score	0.596	0.534	0.593	0.553	0.473	0.568
German Credit (20)	LR	G-Mean	0.651	0.531	0.627	0.661	0.682	0.616
German Credit (20)	RF	OA	0.954	0.952	0.920	0.931	0.709	0.920
German Credit (20)	RF	F-Score	0.597	0.488	0.574	0.572	0.493	0.576
German Credit (20)	RF	G-Mean	0.681	0.500	0.625	0.674	0.691	0.639
German Credit (30)	DT	OA	0.968	0.963	0.885	0.856	0.628	0.888
German Credit (30)	DT	F-Score	0.558	0.509	0.526	0.506	0.413	0.528
German Credit (30)	DT	G-Mean	0.686	0.509	0.631	0.602	0.565	0.609
German Credit (30)	KNN	OA	0.902	0.968	0.849	0.935	0.697	0.900
German Credit (30)	KNN	F-Score	0.530	0.492	0.512	0.519	0.473	0.507
German Credit (30)	KNN	G-Mean	0.681	0.500	0.588	0.536	0.705	0.536
German Credit (30)	LR	OA	0.921	0.967	0.918	0.877	0.611	0.920
German Credit (30)	LR	F-Score	0.578	0.516	0.577	0.537	0.421	0.571
German Credit (30)	LR	G-Mean	0.649	0.510	0.650	0.661	0.660	0.608
German Credit (30)	RF	OA	0.968	0.968	0.942	0.954	0.705	0.947
German Credit (30)	RF	F-Score	0.592	0.492	0.563	0.589	0.474	0.560
German Credit (30)	RF	G-Mean	0.689	0.500	0.601	0.606	0.679	0.618
German Credit (41)	DT	OA	0.976	0.971	0.916	0.905	0.635	0.898
German Credit (41)	DT	F-Score	0.563	0.493	0.544	0.502	0.408	0.552
German Credit (41)	DT	G-Mean	0.636	0.497	0.615	0.520	0.524	0.626
German Credit (41)	KNN	OA	0.929	0.976	0.876	0.944	0.674	0.920
German Credit (41)	KNN	F-Score	0.524	0.494	0.500	0.502	0.440	0.493
German Credit (41)	KNN	G-Mean	0.593	0.500	0.558	0.516	0.630	0.504
German Credit (41)	LR	OA	0.940	0.976	0.943	0.927	0.641	0.932
German Credit (41)	LR	F-Score	0.546	0.494	0.552	0.515	0.420	0.516
German Credit (41)	LR	G-Mean	0.602	0.500	0.592	0.598	0.597	0.521
German Credit (41)	RF	OA	0.976	0.976	0.961	0.969	0.636	0.962
German Credit (41)	RF	F-Score	0.598	0.494	0.566	0.591	0.413	0.561
German Credit (41)	RF	G-Mean	0.621	0.500	0.622	0.614	0.572	0.616
Heart Disease	DT	OA	0.532	0.566	0.509	0.473	0.430	0.509
Heart Disease	DT	F-Score	0.371	0.322	0.342	0.331	0.295	0.339
Heart Disease	DT	G-Mean	0.588	0.534	0.563	0.545	0.515	0.548
Heart Disease	KNN	OA	0.538	0.564	0.535	0.534	0.504	0.528
Heart Disease	KNN	F-Score	0.363	0.287	0.360	0.352	0.341	0.348
Heart Disease	KNN	G-Mean	0.571	0.509	0.571	0.560	0.557	0.557
Heart Disease	LR	OA	0.558	0.584	0.557	0.536	0.480	0.562
Heart Disease	LR	F-Score	0.397	0.329	0.395	0.374	0.333	0.400
Heart Disease	LR	G-Mean	0.601	0.539	0.601	0.603	0.567	0.610
Heart Disease	RF	OA	0.553	0.601	0.546	0.539	0.480	0.555
Heart Disease	RF	F-Score	0.385	0.314	0.366	0.360	0.326	0.378
Heart Disease	RF	G-Mean	0.600	0.531	0.580	0.569	0.566	0.582
Heart Disease (21)	DT	OA	0.532	0.566	0.512	0.486	0.431	0.510
Heart Disease (21)	DT	F-Score	0.376	0.296	0.341	0.336	0.311	0.342
Heart Disease (21)	DT	G-Mean	0.598	0.509	0.558	0.562	0.538	0.551
Heart Disease (21)	KNN	OA	0.561	0.569	0.543	0.541	0.491	0.550
Heart Disease (21)	KNN	F-Score	0.385	0.312	0.365	0.363	0.334	0.365

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Table 7: Wide optimal results

Dataset	Classifier	Metric	G-SMOTENC	NONE	SMOTENC	ROS	RUS	SMOTE-E
Heart Disease (21)	KNN	G-Mean	0.589	0.520	0.570	0.566	0.546	0.570
Heart Disease (21)	LR	OA	0.573	0.592	0.565	0.547	0.525	0.561
Heart Disease (21)	LR	F-Score	0.408	0.331	0.405	0.387	0.343	0.405
Heart Disease (21)	LR	G-Mean	0.638	0.540	0.610	0.602	0.583	0.627
Heart Disease (21)	RF	OA	0.577	0.608	0.565	0.561	0.517	0.561
Heart Disease (21)	RF	F-Score	0.417	0.323	0.390	0.383	0.337	0.386
Heart Disease (21)	RF	G-Mean	0.621	0.536	0.596	0.593	0.567	0.590