

Π -Ware: An Embedded Hardware Description Language using Dependent Types

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Background

Hardware Design

Functional Hardware

DTP

Research

Question

Question

Method

DTP / Agda

Big picture

Agda syntax

Π -Ware

Syntax

Semantics

Proofs



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Table of Contents

Background

- Hardware Design
- Functional Hardware
- DTP

Research Question

- Question
- Method

DTP / Agda

- Big picture
- Agda syntax

Π -Ware

- Syntax
- Semantics
- Proofs

Background

- Hardware Design
- Functional Hardware
- DTP

Research Question

- Question
- Method

DTP / Agda

- Big picture
- Agda syntax

Π -Ware

- Syntax
- Semantics
- Proofs



Hardware design is hard(er)

- ▶ Strict(er) correctness requirements
 - You can't simply *update* a full-custom chip after production
 - Intel FDIV
 - Expensive verification / validation (up to 50% of development costs)
- ▶ Low-level details (more) important
 - Layout / area
 - Power consumption / fault tolerance



Hardware design is growing

- ▶ Moore's law will still apply for some time
 - We can keep packing more transistors into same silicon area
- ▶ **But** optimizations in CPUs display diminishing returns
 - Thus, more algorithms *directly* in hardware

Background

Hardware Design

Functional Hardware

DTP

Research Question

Question

Method

DTP / Agda

Big picture

Agda syntax

Π -Ware

Syntax

Semantics

Proofs



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Hardware Description Languages

- ▶ All started in the 1980s
- ▶ *De facto* industry standards: VHDL and Verilog
- ▶ Were intended for *simulation*, not modelling or synthesis
 - *Unsynthesizable* constructs
 - Widely variable tool support

Background

Hardware Design

Functional Hardware

DTP

Research Question

Question

Method

DTP / Agda

Big picture

Agda syntax

Π -Ware

Syntax

Semantics

Proofs



Universiteit Utrecht

Functional Programming

- ▶ Easier to *reason* about program properties
- ▶ Inherently *parallel* and *stateless* semantics
 - In contrast to imperative programming

Background

Hardware Design

Functional Hardware

DTP

Research Question

Question

Method

DTP / Agda

Big picture

Agda syntax

Π-Ware

Syntax

Semantics

Proofs



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Functional Hardware Description

- ▶ A functional program describes a circuit
- ▶ Several *functional* Hardware Description Languages (HDLs) during the 1980s
 - For example, μ FP [Sheeran, 1984]
- ▶ Later, *embedded* hardware Domain-Specific Languages (DSLs)
 - For example, Lava (Haskell) [Bjesse et al., 1998]

Background

Hardware Design

Functional Hardware

DTP

Research Question

Question

Method

DTP / Agda

Big picture

Agda syntax

П-Ware

Syntax

Semantics

Proofs



Universiteit Utrecht

Embedded DSLs for Hardware

- ▶ Lava

Background

Hardware Design

Functional Hardware

DTP

Research

Question

Question

Method

DTP / Agda

Big picture

Agda syntax

Π-Ware

Syntax

Semantics

Proofs



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Dependently-Typed Programming

Dependently-Typed Programming (DTP) är en
programmationstechnik...

Background

Hardware Design

Functional Hardware

DTP

Research Question

Question

Method

DTP / Agda

Big picture

Agda syntax

Π -Ware

Syntax

Semantics

Proofs



Universiteit Utrecht

Research Question

“What are the improvements that DTP can bring to hardware design?”

Background

- Hardware Design
- Functional Hardware
- DTP

Research Question

- Question
- Method

DTP / Agda

- Big picture
- Agda syntax

Π -Ware

- Syntax
- Semantics
- Proofs



Methodology

- ▶ Develop a hardware DSL, *embedded* in a dependently-typed language (Agda)
 - Called **Π -Ware**
 - allowing simulation, synthesis and verification

Background

Hardware Design
Functional Hardware
DTP

Research Question

Question
Method

DTP / Agda

Big picture
Agda syntax

Π -Ware

Syntax
Semantics
Proofs



Dependently-Typed Programming

- ▶ Types can depend on values
 - `Vec`
- ▶ Types of arguments can depend on *values of previous arguments*
 - `take`

Background

Hardware Design
Functional Hardware
DTP

Research Question

Question
Method

DTP / Agda

Big picture
Agda syntax

Π -Ware

Syntax
Semantics
Proofs



Dependently-Typed Programming

- ▶ Dependent pattern matching
 - Example with `Vec` pattern forcing size pattern
- ▶ Programming language / Theorem prover
 - Types as propositions, terms as proofs [Wadler, 2014]
 - Example: `≤` and `3 ≤ 4`.

Background

Hardware Design

Functional Hardware

DTP

Research Question

Question

Method

DTP / Agda

Big picture

Agda syntax

Π-Ware

Syntax

Semantics

Proofs



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Agda syntax for Haskell programmers

- ▶ Liberal identifier lexing (Unicode **everywhere**)
 - $a \equiv b + c$ is a valid identifier, $a \equiv b + c$ an expression
- ▶ *Mixfix* notation
 - $_[_]\!:=_$ is the array update function: `arr [# 3] := true.`

Background

Hardware Design
Functional Hardware
DTP

Research Question

Question
Method

DTP / Agda

Big picture
Agda syntax

Π -Ware

Syntax
Semantics
Proofs



Universiteit Utrecht

Agda syntax for Haskell programmers

- ▶ Implicit arguments
- ▶ “For all” sugar: $\forall n$ is equivalent to $(n : _)$
 - Where $_$ means: guess this type (based on other args)
 - Example: $\forall n \rightarrow \text{zero} \leq n$

Background

Hardware Design
Functional Hardware
DTP

Research Question

Question
Method

DTP / Agda

Big picture
Agda syntax

Π -Ware

Syntax
Semantics
Proofs



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Low-level circuits

- ▶ \mathbb{C}'
- ▶ “Untyped”

Background

Hardware Design
Functional Hardware
DTP

Research Question

Question
Method

DTP / Agda

Big picture
Agda syntax

Π -Ware

Syntax
Semantics
Proofs



Atoms

- ▶ `PiWare.Atom.Atomic`
- ▶ `Bool`, `std_logic`, etc.
- ▶ Example: `PiWare.Atom.Bool`

Background

Hardware Design
Functional Hardware
DTP

Research Question

Question
Method

DTP / Agda

Big picture
Agda syntax

Π -Ware

Syntax
Semantics
Proofs



Gates

- ▶ `PiWare.Gates.Gates`
- ▶ Examples:
 - `{NOT, AND, OR}` (`BoolTrio`)
 - `{NAND}`
 - Arithmetic, Crypto, etc.
- ▶ Example: `PiWare.Gates.BoolTrio`

Background

Hardware Design
Functional Hardware
DTP

Research Question

Question
Method

DTP / Agda

Big picture
Agda syntax

Π -Ware

Syntax
Semantics
Proofs



High-level circuits

- ▶ \mathbb{C}
- ▶ “Typed”

Background

- Hardware Design
- Functional Hardware
- DTP

Research Question

Question
Method

DTP / Agda

- Big picture
- Agda syntax

Π-Ware

- Syntax
- Semantics
- Proofs



Synthesizable

- ▶ $\Downarrow W \Uparrow$ (pronounced Synthesizable)

- $W\ n = \text{Vec}\ \alpha\ n$

- ▶ Example: $\Downarrow W \Uparrow\ (\alpha \times \beta)$

Background

Hardware Design
Functional Hardware
DTP

Research Question

Question
Method

DTP / Agda

Big picture
Agda syntax

Π -Ware

Syntax
Semantics
Proofs



Synthesis

- ▶ Work-in-progress
- ▶ Atom and Gates with VHDL *abstract syntax*

Background

Hardware Design
Functional Hardware
DTP

Research Question

Question
Method

DTP / Agda

Big picture
Agda syntax

Π -Ware

Syntax
Semantics
Proofs



Simulation

- ▶ Combinational
- ▶ Sequential

Background

- Hardware Design
- Functional Hardware
- DTP

Research Question

Question
Method

DTP / Agda

- Big picture
- Agda syntax

Π-Ware

Syntax
Semantics
Proofs



Examples

► AndN

Background

Hardware Design

Functional Hardware

DTP

Research Question

Question

Method

DTP / Agda

Big picture

Agda syntax

Π-Ware

Syntax

Semantics

Proofs



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Problems

- ▶ Definition of $\llbracket _ \rrbracket$ blocks reduction

Background

- Hardware Design
- Functional Hardware
- DTP

Research Question

Question

Method

DTP / Agda

- Big picture
- Agda syntax

Π-Ware

Syntax

Semantics

Proofs



Universiteit Utrecht

Conclusion

Lorem ipsum...

Background

- Hardware Design
- Functional Hardware
- DTP

Research Question

- Question
- Method

DTP / Agda

- Big picture
- Agda syntax

Π -Ware

- Syntax
- Semantics

Proofs



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Future work

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Background

- Hardware Design
- Functional Hardware
- DTP

Research Question

- Question
- Method

DTP / Agda

- Big picture
- Agda syntax

Π -Ware

- Syntax
- Semantics

Proofs



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Thank you!

Questions?



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Background

Hardware Design

Functional Hardware

DTP

Research

Question

Question

Method

DTP / Agda

Big picture

Agda syntax

Π -Ware

Syntax

Semantics

Proofs



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