### C. The Bottom of a Graph

Time limit: 0.254s Memory limit: 1536 MB

We will use the following (standard) definitions from graph theory. Let  $\,V\,$  be a nonempty and finite set, its elements being called vertices (or nodes). Let  $\,E\,$  be a subset of the Cartesian product  $\,V\times V\,$ , its elements being called edges. Then  $\,G=(V,E)\,$  is called a directed graph.

Let n be a positive integer, and let  $p=(e_1,...,e_n)$  be a sequence of length n of edges  $e_i \in E$  such that  $e_i=(v_i,v_{i+1})$  for a sequence of vertices  $(v_1,...,v_{n+1})$ . Then p is called a path from vertex  $v_1$  to vertex  $v_{n+1}$  in G and we say that  $v_{n+1}$  is reachable from  $v_1$ , writing  $(v_1 \rightarrow v_{n+1})$ .

Here are some new definitions. A node v in a graph G=(V,E) is called a sink, if for every node w in G that is reachable from v, v is also reachable from w. The bottom of a graph is the subset of all nodes that are sinks, i.e., bottom $(G)=\{v\in V|\forall w\in V:(v\to w)\Rightarrow(w\to v)\}$ . You have to calculate the bottom of certain graphs.

## **Input Specification**

The input contains several test cases, each of which corresponds to a directed graph G. Each test case starts with an integer number v, denoting the number of vertices of G=(V,E), where the vertices will be identified by the integer numbers in the set  $V=\{1,...,v\}$ . You may assume that 1 <= v <= 5000. That is followed by a non-negative integer e and, thereafter, e pairs of vertex identifiers  $v_1, w_1, ..., v_e, w_e$  with the meaning that  $(v_i, w_i) \in E$ . There are no edges other than specified by these pairs. The last test case is followed by a zero.

## **Output Specification**

For each test case output the bottom of the specified graph on a single line. To this end, print the numbers of all nodes that are sinks in sorted order separated by a single space character. If the bottom is empty, print an empty line.

# Sample Input

```
3 3
1 3 2 3 3 1
2 1
1 2
0
```

### Sample Output

```
1 3
2
```

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