

1.

(a) TRUE

(b) FALSE

(c) FALSE

(d) TRUE

(e) TRUE

2. (a)  $\bar{V} = V_{\text{rms}} \angle \theta_v$

$$= \frac{\sqrt{2} \cdot 100}{\sqrt{2}} = 100 \angle 0^\circ \text{ V}$$

$$\bar{I} = I_{\text{rms}} \angle \theta_i$$

$$= \frac{\sqrt{2}}{\sqrt{2}} = 1 \angle -60^\circ \text{ A}$$

(b) • Active Power

$$P = |\bar{S}| \cos(\phi)$$

$$= 100 \cos(60^\circ)$$

$$\boxed{P = 50 \text{ var}}$$

$$\phi = \theta_v - \theta_i$$

$$|\bar{S}| = V_{\text{rms}} I_{\text{rms}} = 100$$

$$0 - (-60^\circ) = 60^\circ$$

• Apparent Power = 100 var

$$\boxed{S = 100 \text{ var}}$$

• Reactive power

$$Q = |\bar{S}| \sin(\phi)$$

$$= 100 \sin(60^\circ)$$

$$\boxed{Q = 86.6 \text{ var}}$$

(c) Power factor =  $\cos(\phi)$

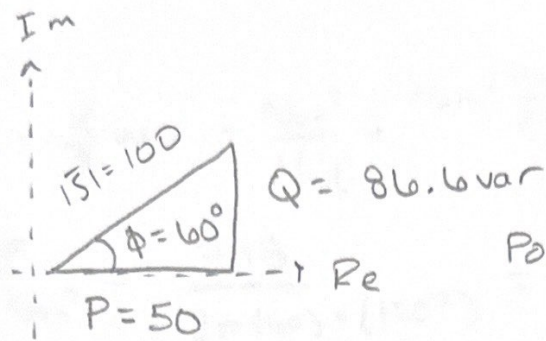
$$= \cos(60^\circ) = 0.5$$

$$\frac{\sin(60^\circ)}{0.866} = \frac{Q}{86.6}$$

$$\text{Power Factor} = 0.5$$

Since  $\sin(\phi)$  and  $Q$  are Positive, the Current is Lagging.

2. (d)



Power factor = 0.5

$$(e) \quad \vec{Z} = \frac{\vec{V}}{\vec{I}} = \frac{100 \angle 0^\circ}{1 \angle -60^\circ} = 100 \angle 60^\circ$$

$$\vec{Z} = R + jX$$

$$R = 100 \cos(60^\circ)$$

$$X = 100 \sin(60^\circ)$$

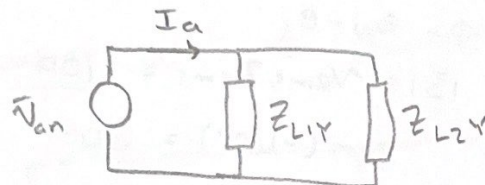
$$\vec{Z} = 50 + j86.6$$

$$R = 50$$

$$X = 86.6$$

The network is  
INDUCTIVE

3. (a)



$$\Delta-Y: Z_{L1} = \frac{9 \angle 30^\circ \Omega}{3}$$

$$Z_{L1Y} = 3 \angle 30^\circ \Omega$$

$$Z_{L2} = \frac{18 \angle 30^\circ \Omega}{3} = 6 \angle 30^\circ \Omega$$

$$Z_{L2Y} = 6 \angle 30^\circ \Omega$$

$$(b) \quad V_{LL} = 207.85 \text{ V} \quad \vec{Z} = 9 \angle 60^\circ \Omega$$

$$V_{an} = \frac{207.85 \text{ V} \angle 0^\circ}{\sqrt{3}} = 120 \angle 0^\circ \rightarrow I_a = \frac{120 \angle 0^\circ}{9 \angle 60^\circ} = 13.3 \angle -60^\circ$$

$$V_{bn} = 120 \angle -120^\circ$$

$$V_{cn} = 120 \angle 120^\circ$$

$$\begin{aligned} I_a &= 13.3 \angle -60^\circ \\ I_b &= 13.3 \angle -180^\circ \\ I_c &= 13.3 \angle 60^\circ \end{aligned}$$

(c)

$$S_{\text{tot}} = 3 \cdot V_{an} I_a^*$$

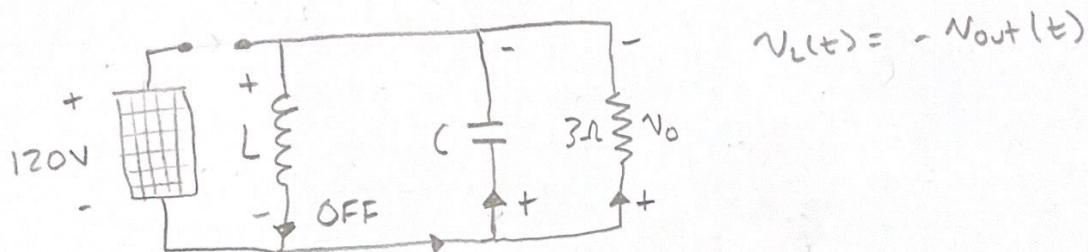
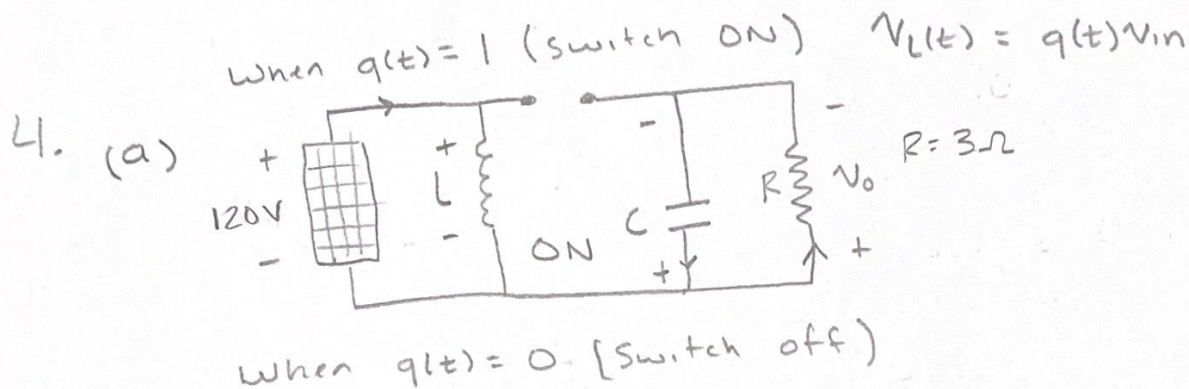
$$= 3 \times (120 \angle 0^\circ) (13.3 \angle 60^\circ)$$

$$S_{\text{TOT}} = 1596 \angle 60^\circ \text{ Var}$$



3. (d)  $PF=1$   
 $Q_{cap} = \frac{X}{3} W_{ur} = \frac{V_{an}^2}{1/\omega L} + V_{an} = \frac{\omega L}{\sqrt{3}}$

$$C = \frac{Q_{cap}}{2\pi f V_{an}^2} = \frac{798}{2\pi (60) \times (120^2)} = \boxed{1.47 \times 10^{-4} F}$$



(b) THIS IS A BUCK-BOOST CONVERTER.

When  $q(t)=1$ ,  $V_L(t) = V_{in} = V_m$   $V_L = \frac{D}{1-D} V_m$   
 when  $q(t)=0$ ,  $V_L(t) = -V_{out}(t) = -V_L$

(c)  $R_L = 3\Omega$ ,  $V_m = 120V$ ,  $I_m = 10A$

$V = IR$   
 $= (10A)(3\Omega)$   
 $V = 30V$

$P_m = 1200W$

$\rightarrow 30 = \frac{D}{1-D} (120)$

To achieve max Power,  
 $D$  should be  $> 0.5$

$30 - 30D = \frac{120D}{1-D}$   
 $30 = 150D$

~~$D = 0.2$~~