

1. A 10 W USB power supply is designed to power a 10 W USB device at the end of a 1 meter cable (copper AWG20). Hint: For simplicity assume power can be converted to current using the nominal USB voltage of 5 V.

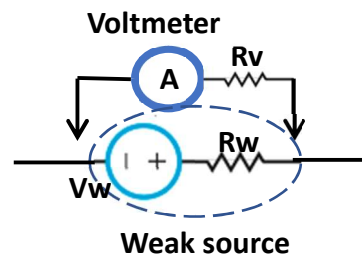
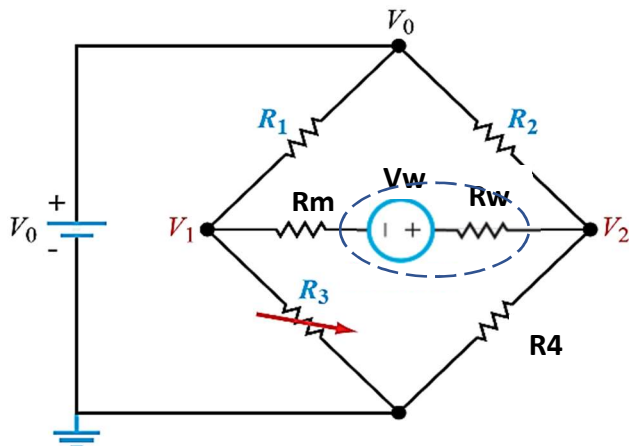
- What is  $V_{th}$  and  $R_{th}$  of the USB supply?
- Assume a 10 meter cable is used. What is the maximum power of the USB device that can be driven?
- If the 10 W supply is connected to a 20 W device, what is the voltage supplied to the load? Is it within USB specifications?

2. Consider a USB battery designed to drive a 2.5 W device. Assume the fully charged (100 %) battery has a  $V_{th100} = 5.25$  V and a fully discharged (0 %) battery has a  $V_{th0} = 4.90$  V.

- What is  $R_{th}$  for the battery?
- If the battery has a capacity of 100 A-hr, how long can the battery power the device?
- Batteries can be damaged if overcharged. Design a simple circuit to prevent this, using diodes.
- Approximately how many diodes are needed assuming  $V_F = 0.66$  V?

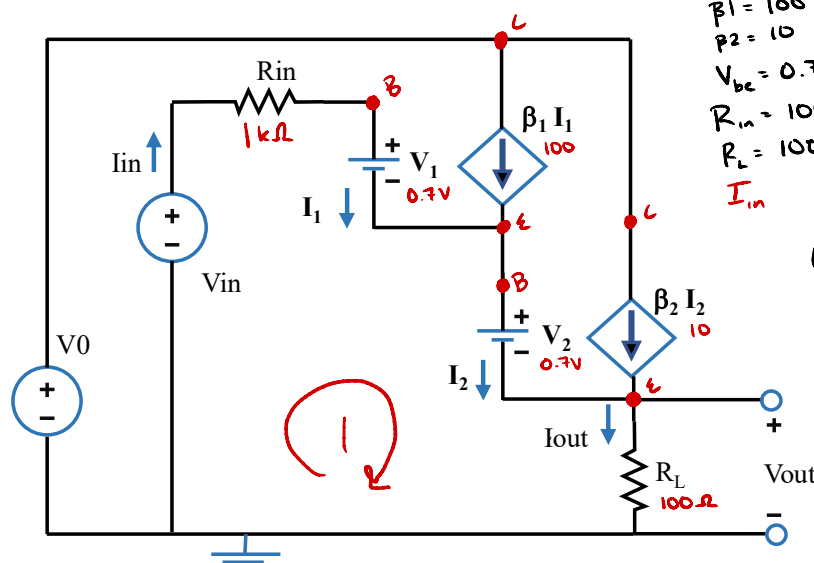
3. A Wheatstone bridge, with resistors  $R_1 = R_2 = R_4 = R$  and variable  $R_3 \sim R$ , is used to measure the Thevenin voltage  $V_w$  of a weak voltage source (defined as having a large  $R_w$ ) by monitoring current through a monitor resistor  $R_m$  in series with the weak source. In short, the variable resistor is adjusted to minimize this current (close to zero as possible), and then a second voltmeter is used to measure ( $V_2 - V_1$ ). Assume the Wheatstone bridge is powered by a 100 V power supply with Thevenin resistance much smaller than  $R$ . Take  $R = 10$  k $\Omega$ . Assume the weak-source has Thevenin voltage and resistance given by  $V_w = 1$  V and  $R_w = 100$  M $\Omega$ .

- Assume that the voltage across the monitor resistor  $R_m$  can be set exactly to zero. What is the approximate percent error if ( $V_2 - V_1$ ) is taken as  $V_w$ ?
- Assume the voltage across  $R_m$  is measured by a voltmeter that can go down to  $V_{m1} = 0.1$  mV. What is the approximate percent error in the voltage measurement if  $R_m = 1$  M $\Omega$ ?
- Using the model of a voltmeter shown, (ie ammeter in series with large resistor  $R_v$ ) what is the error if a voltmeter with resistance  $R_v = 10$   $\Omega$ W is used to measure the voltage of the weak-source directly? Hint: You can neglect the ammeter resistance.
- Now use the same voltmeter with resistance  $R_v = 10$   $\Omega$ W to measure the voltage ( $V_2 - V_1$ ) when the voltage across  $R_m$  has been minimized. What is the percent error in this case? Hint: A rough estimate will do.
- If the voltmeter used to measure the voltage across  $R_m$  has resistance  $R_{v1} = 1$  M $\Omega$ , what is the percent error in this case? Hint:  $R_m = 1$  M $\Omega$  as above.



4. The circuit shown below has two dependent sources. For simplicity assume  $V_1=V_2=0.7\text{ V}$ . Take  $\beta_1 = 100$  and  $\beta_2 = 10$ . Choose  $R_{in} = 1\text{ k}\Omega$  and  $R_L = 100\ \Omega$ . Assume  $V_{in} > V_1+V_2$ .

- What is the voltage gain of the circuit? ( $A_v = V_{out}/V_{in}$ )
- What is the current gain for the circuit? ( $A_i = I_{out}/I_{in}$ )
- What are the limiting voltage and current gains in the limit of large beta.
- For an input voltage of  $V_{in} = 5\text{ V}$  and supply voltage  $V_0 = 10\text{ V}$ , what is the power dissipated in each resistor?
- What is the power supplied by each source?



**Values**  
 $\beta_1 = 100$   
 $\beta_2 = 10$   
 $V_{be} = 0.7\text{ V}$   
 $R_{in} = 1000$   
 $R_L = 100$   
 $I_{in}$

**EQUATION**

$$I_{in} = I_1$$

$$I_2 = (1 + \beta_1) I_1$$

$$\frac{V_{out}}{R_L} = (\beta_2 + 1)(\beta_1 + 1) I_1$$

$$V_{in} = I_2 R_{in} + V_1 + V_2 + R_L (\beta_2 + 1) (\beta_1 + 1) I_1$$

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$$(b) A_i = \frac{I_{out}}{I_{in}} \quad V_{OUT} = 0.99 \times V_{IN} - 1.3875$$

$$\frac{V_{out}}{R_L} = \beta_1 I_1 + \beta_2 I_2$$

$$(c) \beta_1, \beta_2 \gg 1 \quad C = 0$$

$$V_{out} = \frac{(1 + \beta_1)(1 + \beta_2)}{(1 + \beta_2)(1 + \beta_2)} = 1$$

$$(d) V_{in} = 5\text{ V} \quad V_0 = 10\text{ V}$$

$$(e) V_{in}: P = V_{in} I_{in} = \frac{5^2}{1000} = \frac{25}{1000}\text{ W} = 25\text{ mW}$$

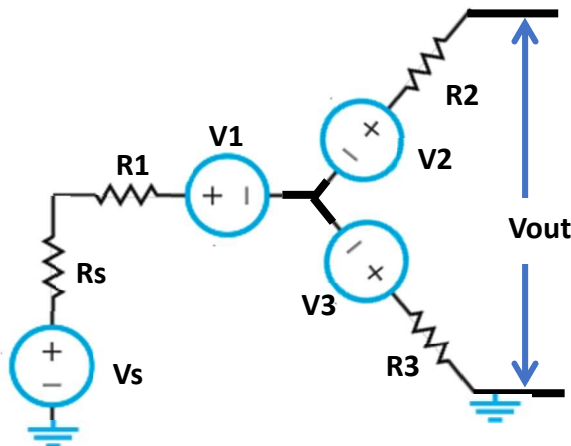
$$V_0 = P = V I = \frac{25}{1000}\text{ W} = 25\text{ mW}$$

$$P_{in} I_{in} = \frac{5}{1000} \quad P = I^2 R = 0.025\text{ W}$$

$$P = I^2 R = (555)^2 \cdot 100 = 3000\text{ W}$$

5. The circuit shown includes Wye power source. Assume the output is loaded with a resistor  $R_L$ . For simplicity assume  $R_1=R_2=R_3=R$ . Also assume  $V_s=10$ ,  $R_s=100$ ,  $V=1$ ,  $R=100$ ,  $R_L=10$  where voltages are in Volts and resistances are in Ohms.

- If  $V_1=V_2=V_3=V=100$  what are the node voltages?
- If  $V_1=V_2=V_3=V=100$  what are the mesh currents?
- What is the Thevenin voltage at the output?
- What is the Thevenin resistance at the output?
- What is the Thevenin voltage at the output if  $V_1=0$ ,  $V_2=V$ ,  $V_3=-V$ ,  $V=100$



$$(A) V_1 + V_2 + V_3 = 100$$

$$100 - 10 = 90\text{ V} = 90\text{ V}$$

$$\text{NODE 2} = 100\text{ V}$$

$$\text{NODE 3} = 0\text{ V}$$

$$(B) I_1 = \frac{V_s}{R_s + R_1} - \frac{V_1}{R_1 + R_4} + \frac{V_3}{R_s} = 0.05\text{ A Hah}$$

$$I_2 = \frac{V_2}{R_2 + R_1} - \frac{V_2}{R_3} = -0.09\text{ A For 2}$$

$$(C) V_{th} = V_{RL} = V_s \cdot \frac{R}{R_{eq}} = 10\text{ V} - \frac{10}{300} = 0.633\text{ V}$$

$$V_{th} = 0.633\text{ V}$$

Extra credit. A 120 W, 12 V battery has the voltage-charge characteristics shown below. Assume a full charge is 10 kW-hr.

- (a) Design a charging circuit to prevent overcharging.
- (b) What is the maximum current that can be supplied to the battery by this charger circuit.
- (c) How long would it take to charge the battery at this current?
- (d) How does state-of-charge depend on time?

