



$R_1$  variable is over the range  $0 \leq R_1 \leq 10\text{ k}\Omega$

Find largest value of  $R_2$  that allows output voltage to vary over range  $1.5\text{ V} \leq V_2 \leq 5.0\text{ V}$

$$V_2 = V_1 \frac{R_2}{R_1 + R_2} \quad 10\text{ k pot, so } R_1 + R_2 = 10\text{ k}\Omega$$

①

$$V_2 = V_1 \frac{R_2}{R_1 + R_2} \rightarrow (1.5\text{ V}) = (9.0\text{ V}) \frac{R_2}{10\text{ k}\Omega + R_2} \rightarrow \left(\frac{1}{6}\right)\text{ V} = \frac{R_2}{10\text{ k}\Omega + R_2}$$

$$5\text{ V} = 9\text{ V} \left( \frac{2\text{ k}\Omega}{R_1 + 10\text{ k}\Omega} \right)$$

$$\rightarrow \left(\frac{1}{6}\right)(10\text{ k}\Omega + R_2) = R_2$$

$$\rightarrow \frac{5}{3} + \frac{1}{6}R_2 = R_2 \rightarrow \frac{5}{3} = \frac{5}{6}R_2 \quad \underline{R_2 = 2\text{ k}\Omega}$$

$$\rightarrow \boxed{1.6\text{ k}\Omega \leq R_1 \leq 10\text{ k}\Omega}$$

②

$$V_2 = V_1 \frac{R_2}{R_1 + R_2} \rightarrow 5\text{ V} = 9\text{ V} \left( \frac{10\text{ k}\Omega}{R_1 + 10\text{ k}\Omega} \right) \rightarrow \underline{R_1 = 8\text{ k}\Omega}$$

$$= \frac{9R_2}{8\text{ k}\Omega + R_2} \rightarrow 1.6\text{ k}\Omega \rightarrow \boxed{1.5\text{ k}\Omega \leq R_2 \leq 10\text{ k}\Omega}$$

$$\frac{9R_2}{8}$$

③

Minimum output

$$1.5\text{ V} = (9\text{ V}) \frac{R_2}{10\text{ k}\Omega} \rightarrow \frac{1.5\text{ V}}{9\text{ V}} = \frac{R_2}{10\text{ k}\Omega} \rightarrow 10\text{ k}\Omega \left( \frac{1}{6} \right) = \left( \frac{R_2}{10\text{ k}\Omega} \right) 10\text{ k}\Omega$$

$$\underline{R_2 = 1.667}$$

Maximum Output

$$5\text{ V} = (9\text{ V}) \frac{R_2}{10\text{ k}\Omega} \rightarrow \frac{5\text{ V}}{9\text{ V}} = \frac{R_2}{10\text{ k}\Omega} \rightarrow 10\text{ k}\Omega \left( \frac{5}{9} \right) = \underline{R_2 = 5.556}$$

So,

$$\boxed{1.667 \leq R_2 \leq 5.556}$$