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Submitted in part fulfilment for the degree of MEng.

Tracing and Debugging in GP2

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Number of words = 3577, as counted by wc -w.
This includes the body of the report only.

Abstract

The University of York has developed a graph programming language, GP2 (Graph Programs 2), which has a small IDE. In this project, new features are designed, implemented, and evaluated which allow users to step through a GP2 program in the IDE.

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1.1 Motivation

Introduce the project, explain why the project needs doing

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Discuss the ethical considerations for the project, which there may not be any at all, if no humans are involved.

2 Literature Review

2.1 Programming by Graph Transformation

2.1.1 Graph Programming

Graph programming involves a series of transformations applied to a graph. The problem being solved must be redefined in terms of a start graph and an algorithm represented by graph transformations. The final graph at the end of the algorithm gives the solution to the problem.

Historically, programming by graph transformation required using a programming language such as C or Java, implementing data structures to represent graphs, and directly making modifications to the graph in the program. However, recently some attempts have been made to create tools for graph programming which abstract away the representation of the graphs, allowing the programmer to focus on the program itself.

Some of these tools include GROOVE [1], AGG [2], GrGen [3], and, most recently, GP2 [4]. All of these are domain-specific languages for graph programming which also provide a graphical interface to describe graphs and transformations.

These kinds of tools take a representation of a graph program, as defined in their graphical editor, and transform this into a runnable program. This can be implemented in a number of languages, including Java (in the case of AGG and GROOVE), C# .NET (GrGen), or C (GP2). This program can then be executed to find the output graph generated by the algorithm.

2.1.2 The GP2 Language

GP2 (Graph Programs 2) is a programming language developed at the University of York [4, 5], an updated implementation of the original language, GP [6]. It is designed for writing programs at a high level, to perform graph transformations without having to implement data structures to represent the graphs in more traditional lower level languages such as C.

```
link
```


where not edge(1, 2)

Figure 2.1: A rule in GP2

Programming in GP2 consists of an input graph, known as the *host graph*, a set of *rules*, and a *program* which defines the order in which to apply the rules. Running a GP2 program on a host graph produces a new graph as a result, called the *output graph*.

Rules

Rules are the basic building blocks of a GP2 program and are defined by a left-hand-side (LHS), a right-hand-side (RHS), and optionally a conditional clause. A rule can be thought of as the definition of a transformation; a subgraph matching the LHS of the rule is transformed to resemble the RHS. An example of a GP2 rule is shown in Figure 2.1.

The conditional clause is used to specify additional constraints on the subgraph matching the LHS. Any match has to both match the LHS and conform to the constraints defined by the conditional clause.

In a compiled program, a rule is split into two phases. The *match* phase searches the current graph for a subgraph which matches the LHS of the rule. This must be an *injective match*, meaning that each item in the LHS must be matched with exactly one item in the host graph.

In this implementation of GP2, rule matches are chosen determinstically due to the impracticality of generating all non-deterministic possibilities, which is what GP1 did. If no match is found for the LHS, the rule is considered *failed*. If a match is found, the program moves on to the second phase, the *application*.

A rule specifies a number of *interface nodes*, nodes which are present in both the LHS and the RHS. These interface nodes can be seen in Figure 2.1; they are the nodes with small numeric labels. During the application phase, any nodes in the LHS which are *not* interface nodes will be deleted. Similarly, any non-interface nodes which appear in the RHS will be created. At the end of the application phase, the subgraph
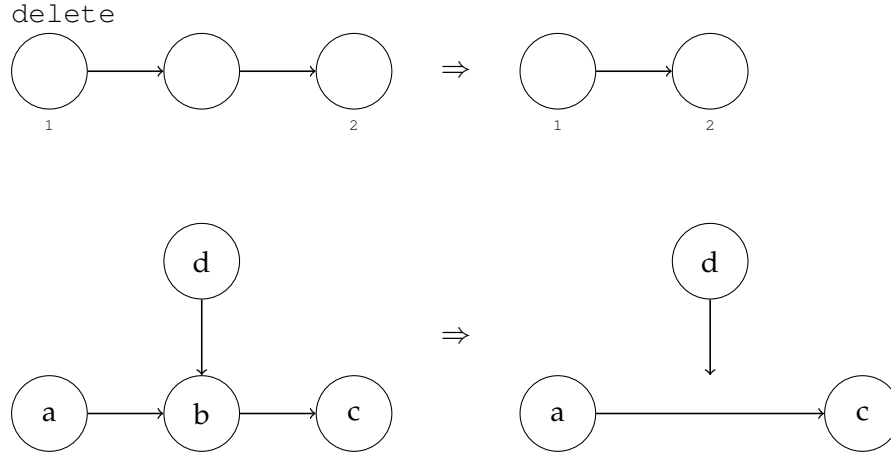
Figure 2.2: Attempting to apply a rule when the match violates the dangling condition

will match the RHS of the rule definition. The new graph created by the application of this rule, an *intermediate graph*, is then used as the input to the next part of the program.

In the example in Figure 2.1, the program will search for a subgraph containing two nodes without an edge connecting them. If a match is found, it will be transformed to resemble the RHS by adding an edge between the nodes.

The Dangling Condition

There is an additional condition which determines whether a rule can be matched, the *dangling condition*. This condition states that if a rule causes a node to be deleted, the rule must also delete all edges incident to that node. In other words, all non-interface nodes in a rule match must have no incoming or outgoing edges which are not also part of the match.

Figure 2.2 shows the result of attempting to apply a rule where the match violates the dangling condition. Since node b is not an interface node, it is deleted during the application of the delete rule. However, the rule does not specify that the edge from b to d should be deleted. This leaves a *dangling edge* from node d with no target. The dangling condition is used to ensure that rules result in no dangling edges.

Programs

A GP2 program defines the order in which to apply rules using 8 simple control structures:

SEQUENCE Two subprograms separated by a semicolon "P; Q" are applied one after the other.

RULE SET Rules in curly braces "{R$_1$, R$_2$, R$_3$}" define a set, where exactly one rule from the set is executed, unless no rule in the set can be matched. The implementation of GP2 selects a rule deterministically, though the the specification allows non-determinism.

IF-THEN-ELSE In the statement "if C then P else Q", the sub-program C is executed, and the result, i.e. success or failure, is recorded, before reverting any changes caused by C. Then, if C succeeded, P is executed on the original graph. If it failed, then Q is executed on the original graph. Note that by taking a copy first, any changes made by C are reverted before executing either P or Q.

TRY-THEN-ELSE Similar to IF-THEN-ELSE, but C is only reverted if it fails. Thus any changes made by C are *not* reverted before executing P, but they *are* reverted before executing Q.

AS-LONG-AS-POSSIBLE A subprogram followed by an exclamation point "P!" is matched and applied repeatedly until it fails. When P fails, it does not transition the program to the fail state.

PROCEDURE Similar to a C preprocessor macro, a procedure is simply a named subprogram where any reference to the procedure name can be replaced with the definition of the procedure.

SKIP A no-op which always succeeds, and does not affect the graph. Invoked using the keyword "skip".

FAIL A no-op which always fails and does not affect the graph. This is the same as attempting to execute a rule for which there are no matches. Invoked using the keyword "fail".

For GP2, a subprogram is either a single rule, referenced by its name, or one of the above control structures. Therefore it is possible to nest control structures to create more complex programs.

In general, execution of a program continues until either all statements are executed, or until a statement results in an attempt to apply a rule which has no matches in the graph. The exceptions to this are As-Long-As-Possible statements, and the conditional statements in If-Then-Else and Try-Then-Else structures. In these cases, a failure to match a rule does not halt execution of the program.

Figure 2.3 shows an example GP2 program, an adapted version of the program used as a case study in Bak's thesis on GP2 [5, p.126]. It is a simple program which determines whether a graph is *2-colourable*, that is, its nodes can be coloured using two different colours without two nodes of the same colour being connected by an edge.

This program consists of four rules and uses many of the constructs outlined previously, including Try-Then-Else, If-Then-Else, Rule Sets, As-Long-As-Possible and Procedures.

It also takes advantage of another feature of GP2, the ability to *colour* a node. The colour of a node is a property which can be set by a rule, or the host graph can contain coloured nodes. The colour is taken into account when searching for a rule match; for example, in this program, `joined_reds` will only match when both the nodes' colours are red.

An example execution of the 2-colouring program is shown in Figure 2.4. Starting with an uncoloured graph, the algorithm picks a node and colours it red using the `init` rule. It then traverses the graph colouring nodes in alternating colours using the `colour_blue` and `colour_red` rules, by defining them as a Rule Set in a Procedure and executing it As-Long-As-Possible. When no more uncoloured nodes are present in the graph, the `Colour` procedure will be unable to match any further rules, so it will end.

To check whether the produced colouring is valid, the entire `Main` procedure is wrapped in a Try-Then-Else statement. After executing `Colour`, the `Invalid` procedure runs. This procedure uses the two remaining rules, `joined_reds` and `joined_blues`, to see if any adjacent nodes are the same colour. If they are, one of these rules will match, triggering the conditional statement `fail` from the If-Then-Else statement. This in turn causes the outer `try` to fail, reverting all changes made to the graph and returning the uncoloured input graph.

However, if `Invalid` fails to match either of the rules, it must mean that no two same-coloured nodes are connected via an edge. This means that it is a valid colouring. The `fail` statement is not executed, meaning the `try` succeeds. The changes to the graph are kept, and the modified graph is returned as the result of the program.

```
Main = try (init; Colour!; if Invalid then fail)
Colour = {colour_blue, colour_red}
Invalid = {joined_reds, joined_blues}
```

init

joined_reds
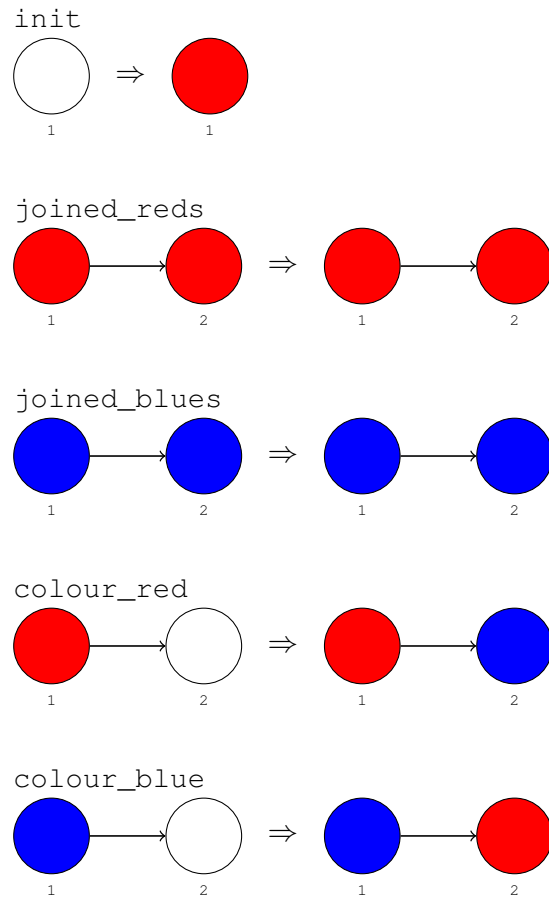

joined_blues

colour_red

colour_blue

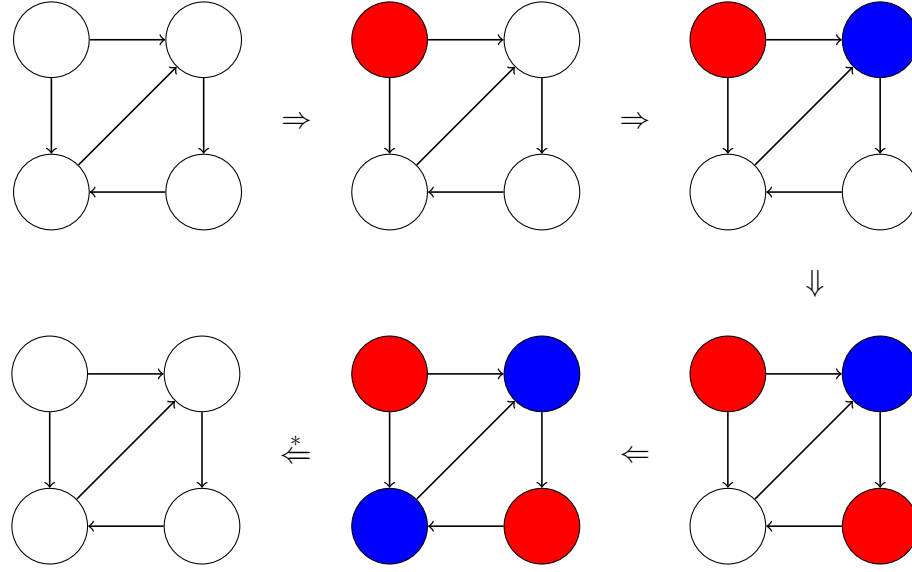Figure 2.3: Definition of 2-colouring in GP2

Figure 2.4: Example execution of 2-colouring

In the example execution in Figure 2.4, the host graph is not 2-colourable. When the rules in `Colour` can no longer be matched, `joined_blues` inside `Invalid` will match with the nodes in the bottom-left and top-right of the graph. Because this rule was successfully applied (even though it has no effect on the graph), the IF-THEN-ELSE causes the program to enter the fail state. This in turn means that the TRY-THEN-ELSE surrounding the program fails, and all the changes made to the input graph are reversed. The output graph is therefore identical to the input graph.

Labels

Nodes and edges in a graph defined in GP2 can also have *labels*. Each node or edge can either have one label or it can be unlabelled. A graph is *partially labelled* if some of the nodes and edges have labels, and it is *totally labelled* if every node and edge has a label.

Labels can be used cosmetically, without affecting the execution of the program, or they can be included in rules to have the program read and modify labels.

GP2 has a type hierarchy for labels, shown in Figure 2.5. Labels can be of any of these five types. An `atom` consists of a single entity, either an

```
                        list
                         ∪I
                        atom

            ↙                      ↘

        int                            string

                                        ∪I

                                        char
```
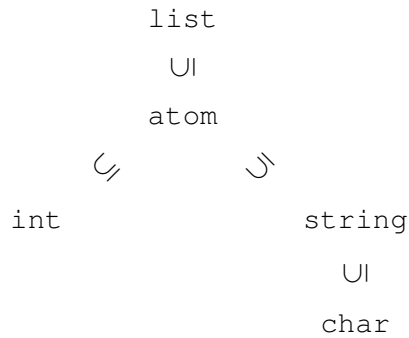
Figure 2.5: GP2's type hierarchy for labels

```
swap(x, y:  int)

    ⎛ x ⎞ ──────▶ ⎛ y ⎞        ⇒        ⎛ y ⎞ ──────▶ ⎛ x ⎞
    1             2                     1             2

where x > y
```

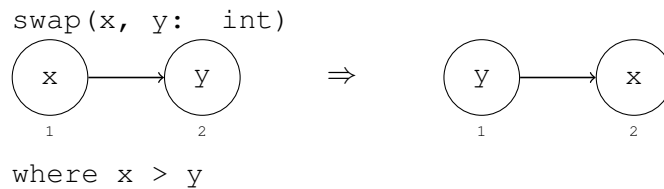Figure 2.6: A GP2 rule which uses labels

int or a string. A list is a collection of atoms concatenated together; the concatenation is shown using a colon (:).

When matching a rule involving labels, GP2 finds a variable assignment which matches the values of the labels in the graph. The values in this assignment are identical when used in the RHS of the rule. When using labels in a rule, the type of each label must be specified so that GP2 can find an assignment for each one.

The rule in Figure 2.6 will only match a pair of nodes where the labels are both integers, and the value of the source node's label is greater than the value of the target node's label. This rule demonstrates both that labels can be used as conditions in the program, and also that a rule can modify labels. It also shows that labels act like variables when used in a rule, since the values of x and y are re-used in the RHS.

2.2 Tracing and Debugging

2.2.1 Debugging in Imperative Languages

When programming in a high level imperative language, such as C or Java, the programmer will more often than not have access to a *debugger*. In [7], Sammet says that a program in a high level language without debugger support may be "harder to debug than an assembly language which the programmer understands", since the programmer has to interpret the compiled code, rather than reading the source code they wrote.

Most language interpreters and Integrated Development Environments (IDEs) have a debugger built in [8], and standalone debuggers are also available for some languages. For C, this may be `gdb` [9], while for Java, it might be `jdb` [10].

A debugger is intended to allow the programmer to pause their program during execution, so that they can inspect the contents of variables and other memory locations. It also allows them to run their program step-by-step to see its execution flow; they may wish to check that a function is called at the expected point during execution, for instance.

Some debuggers also include more advanced features to make debugging easier and to give the programmer more insight into their program. Breakpoints are a common feature which allow the programmer to specify a line of source code and have the program execute normally until the breakpoint is reached, at which point execution will pause, or *break*.

Because GP2 has a rule-based structure, unlike imperative programming languages, it is not clear what a "line of code" represents in a GP2 program. The textual part of a GP2 program can indeed have lines, but since a single line in a GP2 program can be complex and use many rules, this is too high-level to consider a "line of code" as a debugger does. In an imperative language, a single line of code may only perform one or two actions, so inspecting each line individually shows the flow of the program. In GP2, running a line of the textual program could result in tens or hundreds of rules being applied if As-Long-As-Possible is used, for example. It may be inappropriate to focus on how debuggers are implemented for imperative languages when considering GP2.

IDEs

A debugger is often available from within the Integrated Development Environment (IDE) for a language. For example, the Visual Studio IDE

for C, C++, and C# includes the Visual Studio Debugger [11]. One of the most prevalent Java IDEs, Eclipse, integrates with `jdb` [12].

When an IDE integrates with a debugger, it can provide additional functionality by allowing the programmer to interact with the source code and the debugger visually in the same environment. Visual Studio and Eclipse both allow breakpoints to be set directly on a line of source code in the editor, for instance. IDEs often allow the programmer to trace program execution through the source code, by highlighting each line of code as the programmer steps through in the debugger.

It may be useful to use some of these ideas for GP2. For instance, when stepping through a GP2 program, it would be helpful to highlight the current statement or rule being executed, to give the user context.

Edit-and-Continue

Edit-and-continue is an even more advanced feature which requires specific compiler support, and is usually only available in IDEs, since they have access to both the compiler and the debugger. It allows the programmer to pause execution of the program, edit the source code, recompile the program, and continue execution from the previous paused state, without having to restart the program from the beginning. Edit-and-continue is useful for reducing the time taken to find and fix bugs, since fixes can be implemented and tested without having to stop and restart the program's execution.

It is unclear whether edit-and-continue would be a good addition to GP2. On one hand, it can speed up debugging because the programmer does not have to start the program again from the beginning. On the other hand, because GP2 is such a high level language, it may not make sense to resume a program that has been edited. There is a high chance that the modifications would affect the algorithm enough that the current state would not be reached if the program was restarted from the beginning.

Reverse Debugging

`gdb` supports what is called *reverse debugging* [13]. This allows program execution to actually be reversed, running the program backwards to reach an earlier state. This can come in useful to look for non-deterministic bugs which do not always occur; the program can be run until the bug occurs, then executed in reverse to look for the cause.

This ability comes with a trade-off, however; running with reverse debugging enabled reduces the performance of the running program. It can only be used in specific cases and cannot be enabled all the time, since the program would run much slower and possibly exhibit time-related bugs. Reverse debugging is also only available for `gdb` running on Linux.

`gdb`'s implementation of reverse debugging involves recording the machine state after each instruction exectuion, including the values stored in memory and registers. To reverse an instruction, the state from the previous instruction is simply restored, making it appear as if the reversed instruction was never executed. This implementation allows powerful interaction with the program; it can reverse a single instruction at a time, or it can be run backwards until a breakpoint is reached. In theory, although `gdb` does not support this, this system could allow a form of "checkpointing" where execution can be skipped directly back to an arbitrary point by simply restoring the state from that point.

Reverse debugging may be a useful feature for GP2, because it would allow a programmer to step backwards through the execution of a GP2 program to inspect the intermediate graph before and after a rule application, to see what changed. This method is more akin to tracing than traditional debugging, since the debugger is storing a history of everything that occurs during execution.

While the implementation of reverse debugging in `gdb` is limited to the Linux platform, this is because its implementation requires monitoring calls to the kernel and system APIs. This is irrelevant to GP2, because it would only need to trace rule matches and applications, both of which are implemented inside GP2 itself.

2.2.2 Tracing in Functional Languages

The syntax and execution of a GP2 program is very similar to that of a functional programming language. For example, a function in Haskell is similar to a rule or set of rules in GP2; the function defines left-hand-sides and right-hand-sides, and executing it with an argument looks for a LHS which matches the argument, and returns the RHS. This similarity to the matching and application of rules in GP2 suggests that it would be appropriate to consider it like a functional language when implementing debugging or tracing.

Because of the nature of functional languages, it is rare to see traditional debuggers like those used with imperative languages [14]. Lazy evaluation, where the value of a statement is only calculated when it is

required, means that pausing execution on a line of code may not reveal the value of a statement on that line, because it will not be evaluated until later in the program.

To avoid this problem, functional programmers will often use tracing instead. This is where additional code is added to the program which simply outputs information about what the program is doing, either to the console or to a file on disk. The progammer then reads this information back once the program has finished, to see what steps the program took and identify where it differed from the expected execution.

Tracing can be done in primitive ways, by manually adding `print` statements to the code, but there are also more sophisticated tools available. For Haskell, for instance, a handful of different tracing tools are available [15]. Two of them, Freja and Hat, are modified Haskell compilers which add automatic tracing functionality to the compiled program. When the program runs, trace information is stored in the program heap, which can then be accessed at the end of execution. The other tool, Hood, is a Haskell library which is used by importing it and adding `observe` annotations to the code, which preserve lazy evaluation and output information about the program as it runs. The programmer would then inspect the output from the annotations to trace through the program.

The benefit of compiler based tools like Freja and Hat is the programmer does not need to think about where to put tracing code, since all code is traced automatically in the compiled program. However, storing a full trace of an entire program takes up space either in memory or on disk; the advantage of a manual tool like Hood is the programmer can reduce the number of trace points to reduce the trace size.

2.2.3 Debugging Other Graph Programming Tools

Each of the three other graph programming tools mentioned in subsection 2.1.1 have their own debugging or tracing tools.

AGG

Of the three tools, AGG has the simplest debugging tools. It allows the user to select a rule in their graph grammar and then look through all the matches for that rule, by showing them on the current graph.

A unique feature of AGG is that it also allows the user to manually create a match; by selecting nodes and edges first in the LHS of the rule, and then in the graph, the user creates a mapping between the rule and

the current graph to create a match. The tool will alert the user if they attempt to select a mapping which is not a true match.

When a match has been chosen, either automatically or manually, the rule can then be applied by clicking a `Transformation Step` button in the editor. After a rule has been applied, an `Undo Step` button becomes available which reverts the changes made by the most recent rule application.

GROOVE

GROOVE also allows the user to inspect all possible rule matches for the current graph. In the list of rules shown in the editor, the possible matches for each are shown underneath each rule. These matches can be clicked to highlight them on the graph, and double-clicking applies the rule, updating the graph.

Similar to AGG, it is possible to undo a single rule application. However, GROOVE also keeps a history of all previous graph states. In the "State Space Explorer", the tool shows a transition diagram containing all the previously visited graph states, with the transitions representing the rule applied to reach a given state. In this view, the user can select a previous state and jump back to it, allowing the user to undo multiple rule applications at once, or even undoing previous rule applications and re-applying other rules, in one step.

GrGen

GrGen's debugger is different in that it is controlled using a command-line style interface, rather than using buttons in the editor UI. It provides a command to apply a single rule, similar to the other two tools.

However, when applying a rule, GrGen can show more detail. It can show the steps required to apply a rule: the match, the modification to the graph, and the result. It shows each of these stages individually, highlighting the relevant areas on the graph at each stage.

Another unique feature of GrGen's debugger is that it allows the user to tell the program to run until the end of the current loop. GrGen supports a loop structure similar to GP2's As-Long-As-Possible, and the debugger's `step out` command will continue to execute until the current loop ends, giving control back to the user.

Finally, GrGren also supports a feature similar to breakpoints. It allows the user to specify a condition, and when that condition is met, execution

will pause. One type of condition which can be specified is a certain modification to the graph, such as pausing execution when a specific node is deleted from the graph.

2.2.4 Previous Work on Debugging in GP2

There has been some previous work to add debugging facilities to GP2 [16]. This work was focused on modifying the compiler to support stepping through a program.

With the new compiler, command line arguments were added to allow the user to specify how big a "step" should be, and how many steps to execute before stopping. This allows GP2 to approximate breakpoints by picking an appropriate step size and count in order to finish execution at the point the programmer is interested in.

However, there are some problems with this method. For one, once the specified number of steps have been executed, the program terminates completely and outputs the current graph. This means that if the programmer wishes to step through the program one rule at a time, for example, they must run the compiler multiple times and increase the number of steps by one each time, wasting time by re-executing earlier steps at each iteration.

Another problem is that, although the compiler was modified, the graphical editor remains unchanged, and so does not support the new partial execution feature. For the feature to be most useful, it would have to be integrated into the editor.

3 Requirements

Before designing and implementing a system, the requirements for the system need to be considered. These requirements should be based on expected real-world usage of the tool and keep the goals of the tool in mind.

3.1 Potential Users

In order to decide what the requirements for a debugging tool are, it is useful to consider the types of user who would potentially use such a tool. There are two main potential audiences for a GP2 debugging tool:

- Programmers who have written a GP2 program which they would like to debug. Either the program produces unexpected output, or it never terminates, so the programmer wishes to use the debugging tools to understand why their program is behaving incorrectly, and then fix the bug.

- New users of GP2 who are still learning the language. GP2 is an unconventional language and its concepts can be unfamiliar to inexperienced users. Allowing these users to step through a GP2 program would let them see how GP2 works and help them to understand the language faster.

3.2 Integration and Maintainability

Consideration should also be given to GP2 itself as a whole, both in terms of the compiler and IDE, and in terms of developers who will work on GP2 in future.

- *Something insightful...*

4 Design

Explain the design phase, what was considered, and what ultimately became the choice for what to do.

4.1 Design Considerations

4.1.1 Implementations of GP2

There are two implementations of GP2, an interpreter written in Haskell [5, ch. 5.3], and a compiler written in C [5, ch. 5.5]. The interpreter is intended to provide a reference for other implementations of GP2, and for the GP2 developers. The GP2 IDE uses the compiler, not the interpreter, to run the user's program.

The interpreter may be of some interest, since an interpreter runs "live", moving through the program executing each statement as it is reached. This behaviour could be exploited to implement a form of debugging, by pausing execution of the interpreter at various points and outputting the current state of the program.

To take advantage of the interpreter, the GP2 editor would have to be modified so that it runs the user's program using the interpreter rather than the compiler.

The other difference between the interpreter and the compiler is that the compiled program only produces one output for a given input to a program. The interpreter returns all unique output graphs, up to isomorphism. For debugging purposes, this may be of interest to the user, since it allows them to see all the possibilities of their program. To the developer of the debugger, this is a disadvantage, since the GP2 IDE does not currently support displaying all possible outputs.

Additionally, because the interpreter is only a reference implementation, the compiler is the implementation intended for most users. If the IDE were to be changed to run the interpreter for debugging programs, checks would have to be made to ensure that the interpreter produces identical outputs to a compiled version of the same program. This may involve adding a "single-result mode" to the interpreter, where only one

output graph is produced, instead of all possibilities. This would require substantial changes to the interpreter.

4.1.2 Backtracking in the GP2 Compiler

To support some operations, such as IF-THEN-ELSE, the GP2 compiler uses *backtracking*, where a changes to the graph are reversed [5, ch. 5.8]. If the condition in an IF-THEN-ELSE structure fails, any changes need to be reversed before applying the ELSE subprogram.

This feature of the compiler could be used as part of the debugging features, by using it to allow the user to step backwards through the program as it runs, similar to the reverse debugging mentioned in section 2.2.1. It would allow the user to see the state of the graph before a certain rule was applied, for instance.

However, this backtracking is not available at all points in a program's execution; backtracking code is only added by the compiler if static analysis shows that it is necessary. For example, since the AS-LONG-AS-POSSIBLE construct cannot fail, the compiler does not add backtracking code for it. The compiler would have to be modified to add backtracking code to the entire program.

4.1.3 Non-determinism

GP2's definition supports non-determinism but the compiler doesn't. How does this affect the design decisions for the debugger?

5 Implementation

What has changed in the GP2 compiler and in the editor, and how does this implement debugging or tracing for the end user?

6 Evaluation

6.1 Requirements Tracing

Go back and compare the implemented debugging tools to the requirements from ??.

6.2 Performance

Test the performance of some GP2 alogrithms with tracing turned on and off.

6.3 User Feedback

(If there's time) Get some users to use the new features and get feedback from them.

7 Conclusions

Summary of what has been achieved in the project.

7.1 Future Work

What's missing (e.g. what requirements weren't met) and what other improvements could be made by someone else?

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