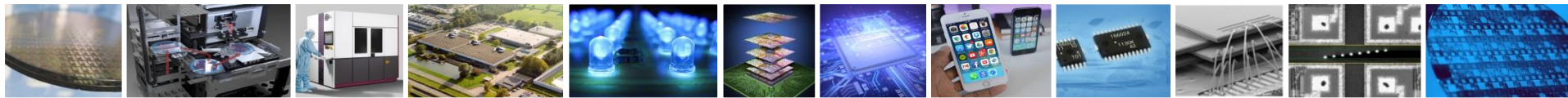


Modeling for Control

Training Session 4: Feedback & feedforward control

COC
January 11th, 2023



Content

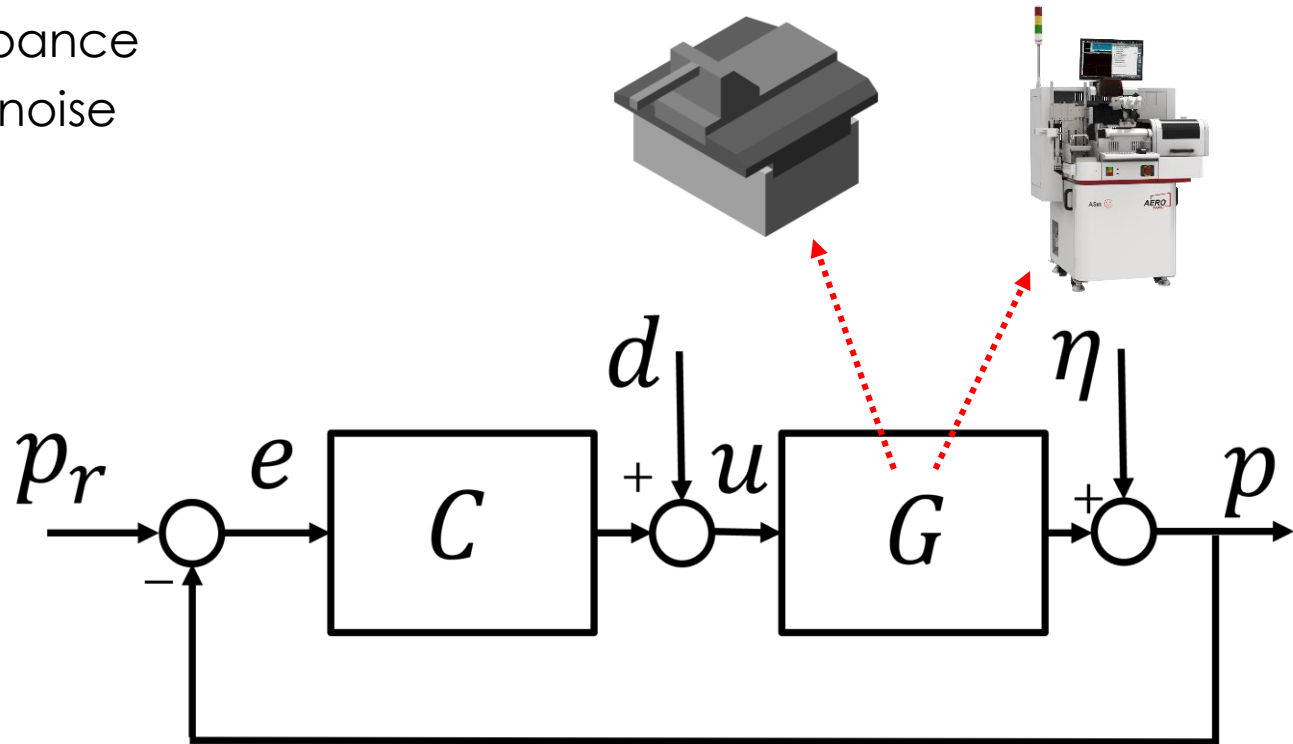
- ▣ Feedback control
- ▣ Feedforward control
- ▣ Self-study assignment

FEEDBACK CONTROL

Motion control system (without feedforward control)

- p_r : reference position
- p : encoder position
- e : error
- d : external disturbance
- η : measurement noise
- u : motor input

- G : plant
- C : feedback controller



How to design for closed-loop performance?

□ Open loop: $L = G \cdot C$

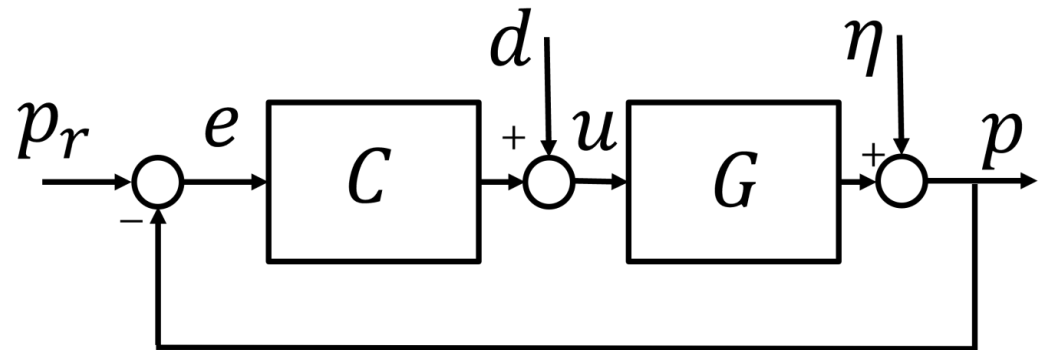
□ Closed-loop transfer-functions:

1. Sensitivity: $S := \frac{e}{p_r} = \frac{u}{d} = \frac{1}{1+L}$

2. Complementary sensitivity: $T := \frac{p}{p_r} = \frac{p}{\eta} = \frac{L}{1+L}$

3. Process sensitivity: $GS := \frac{p}{d} = \frac{G}{1+L}$

4. Control sensitivity: $CS := \frac{u}{p_r} = \frac{C}{1+L}$



Feedback controller design: general rules of thumb

□ Typical controller structure: $C = P \cdot \underbrace{\left(1 + \frac{2\pi f_i}{s}\right)}_I \cdot \underbrace{\frac{1 + \frac{s}{2\pi f_{lead}}}{1 + \frac{s}{2\pi f_{lag}}}}_D$

□ General tuning procedure:

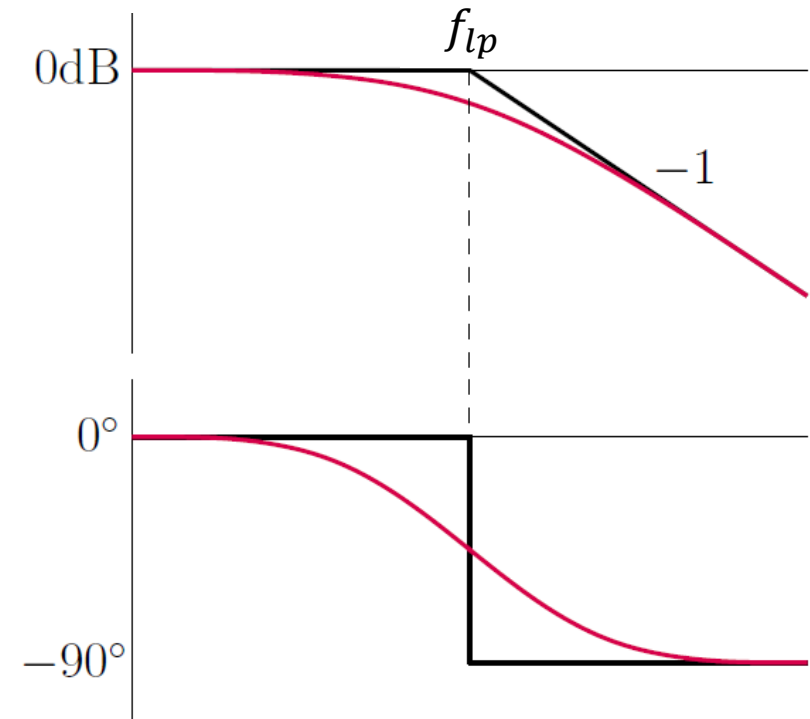
1. Select desired control bandwidth f_{bw} (0dB magnitude-point in open-loop),
2. Set proportional gain $P = \frac{1}{3} \frac{1}{|G|_{@f_{bw}}}$,
3. The derivative-action should start at frequency $f_{lead} = \frac{f_{bw}}{3}$ and end at frequency $f_{lag} = 3f_{bw}$,
4. The integrator action should stop before the start of the lead-action, typically at frequency $f_i = \frac{f_{bw}}{10}$ or $f_i = \frac{f_{bw}}{5}$.

Feedback controller design: other useful control elements (1/2)

- If necessary, a first-order low-pass filter can be used to further suppress the high-frequency noise and resonance-modes:

- $C_{lp} = \frac{1}{1 + \frac{s}{2\pi f_{lp}}}$

- with, typically, $f_{lp} = 9f_{bw}$ or $f_{lp} = 6f_{bw}$

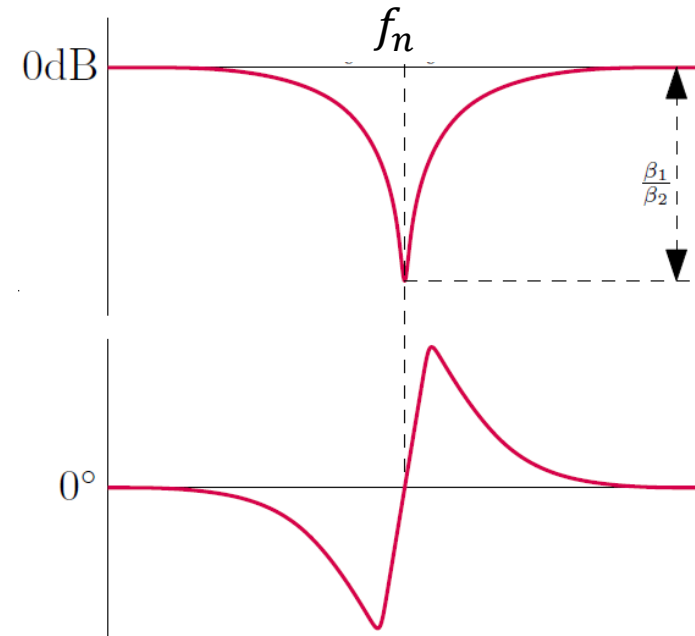


Feedback controller design: other useful control elements (2/2)

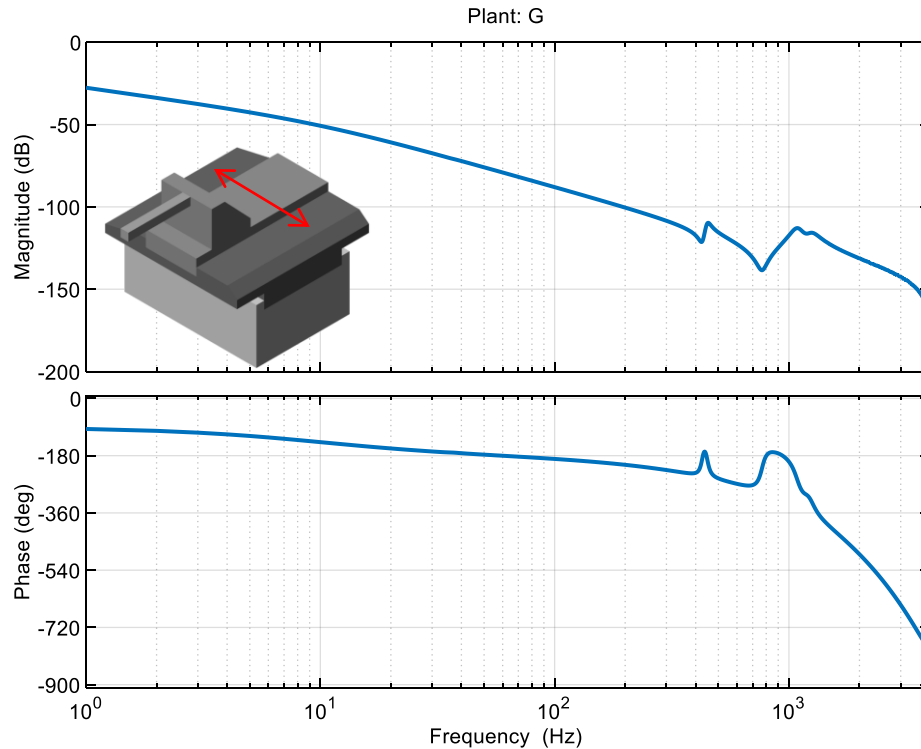
- If necessary, notch-filters can be used to selectively target specific resonance frequencies:

- $C_n = \frac{\left(\frac{1}{(2\pi f_n)^2} s^2 + \frac{2\beta_1}{2\pi f_n} s + 1\right)}{\left(\frac{1}{(2\pi f_n)^2} s^2 + \frac{2\beta_2}{2\pi f_n} s + 1\right)},$

- with f_n the resonance frequency that we want to suppress.

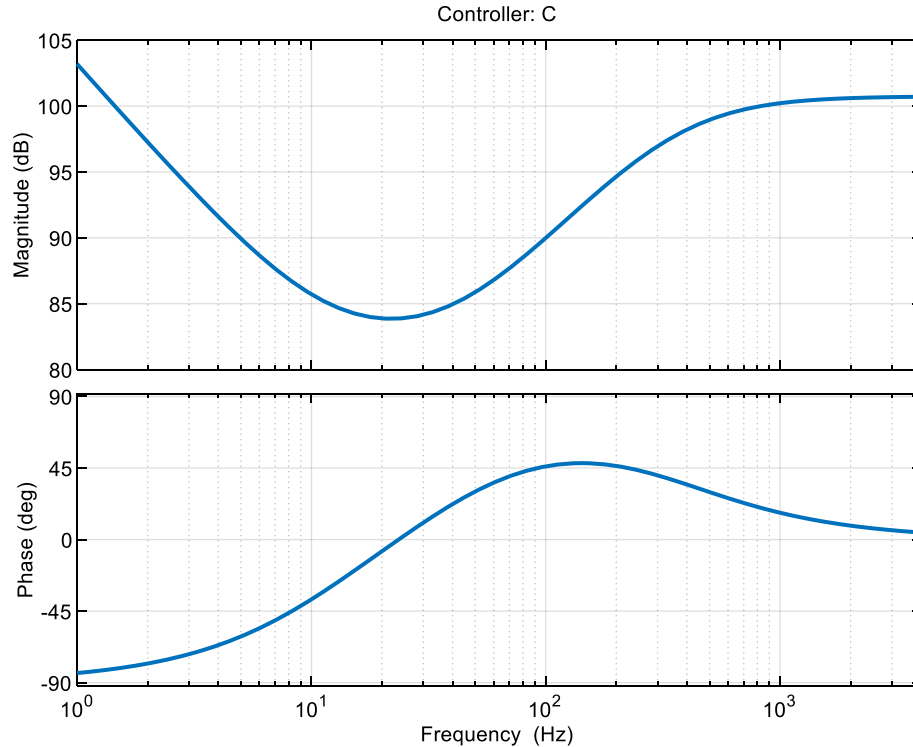


Case study: X-stage of the AB383 Simscape model



- ❑ The first clearly visible resonance frequency lays at 452 Hz.
- ❑ The time-delay results in a phase loss linearly related to the frequency.
- ❑ The combination of flexible dynamics and phase loss caused by time-delay results in a limited obtainable bandwidth.
- ❑ Let us try to tune an open loop bandwidth $f_{bw} = 120$ Hz.

Case study: feedback controller C



$$C = P \cdot \left(1 + \frac{2\pi f_i}{s}\right) \cdot \frac{1 + \frac{s}{2\pi f_{lead}}}{1 + \frac{s}{2\pi f_{lag}}}$$

Gain:

$$|G|_{@120 \text{ Hz}} = \text{db2mag}(-91.2)$$

$$P = \frac{1}{3} \frac{1}{|G|_{@f_{bw}}} = 11982$$

Lead/lag:

$$f_{lead} = \frac{f_{bw}}{3} = 40 \text{ Hz}$$

$$f_{lag} = 3f_{bw} = 360 \text{ Hz}$$

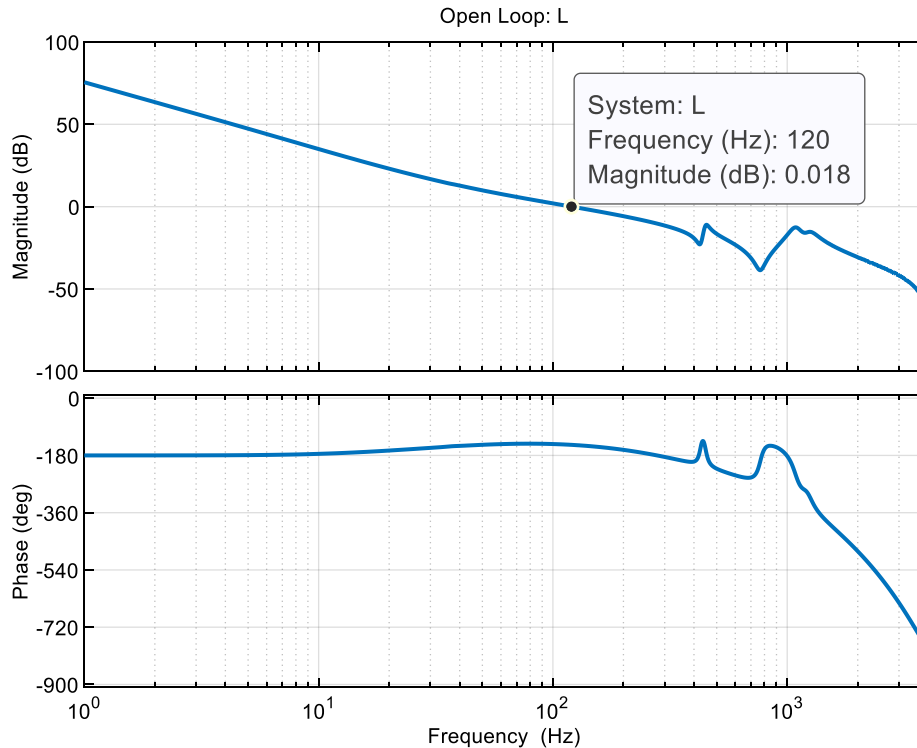
Integrator:

$$f_i = \frac{f_{bw}}{10} = 12 \text{ Hz}$$

Total controller:

$$C = 11982 \cdot \left(1 + \frac{75.4}{s}\right) \cdot \frac{1 + 0.004019s}{1 + 0.0004421s}$$

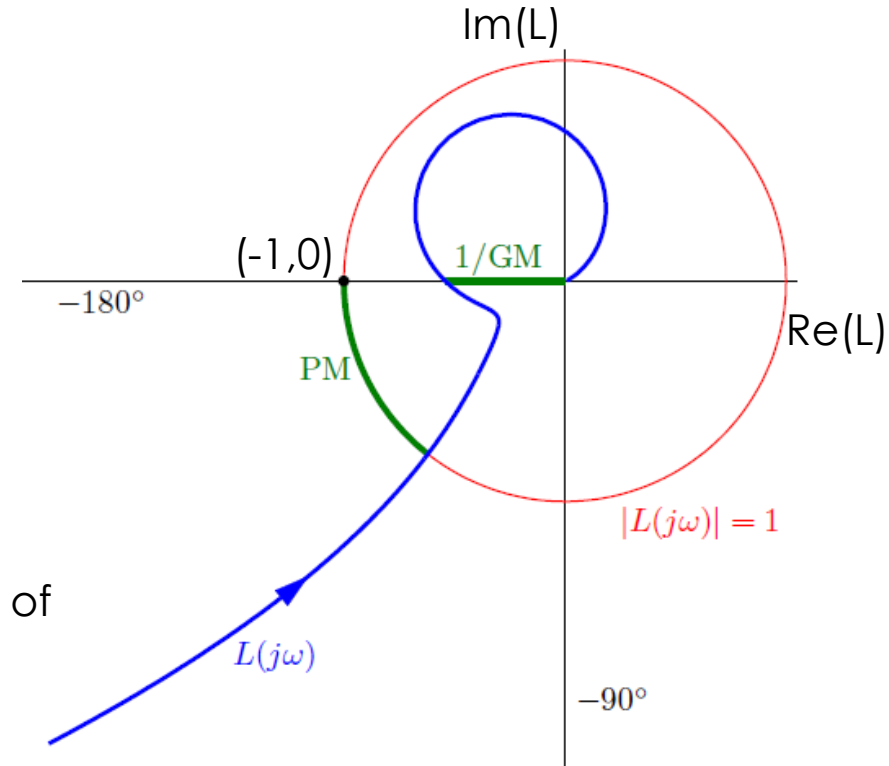
Case study: open loop L



- ❑ Open loop: $L = G \cdot C$.
- ❑ Open loop bandwidth is 120 Hz, as desired.
- ❑ The next step is to check if the controller is indeed stable.

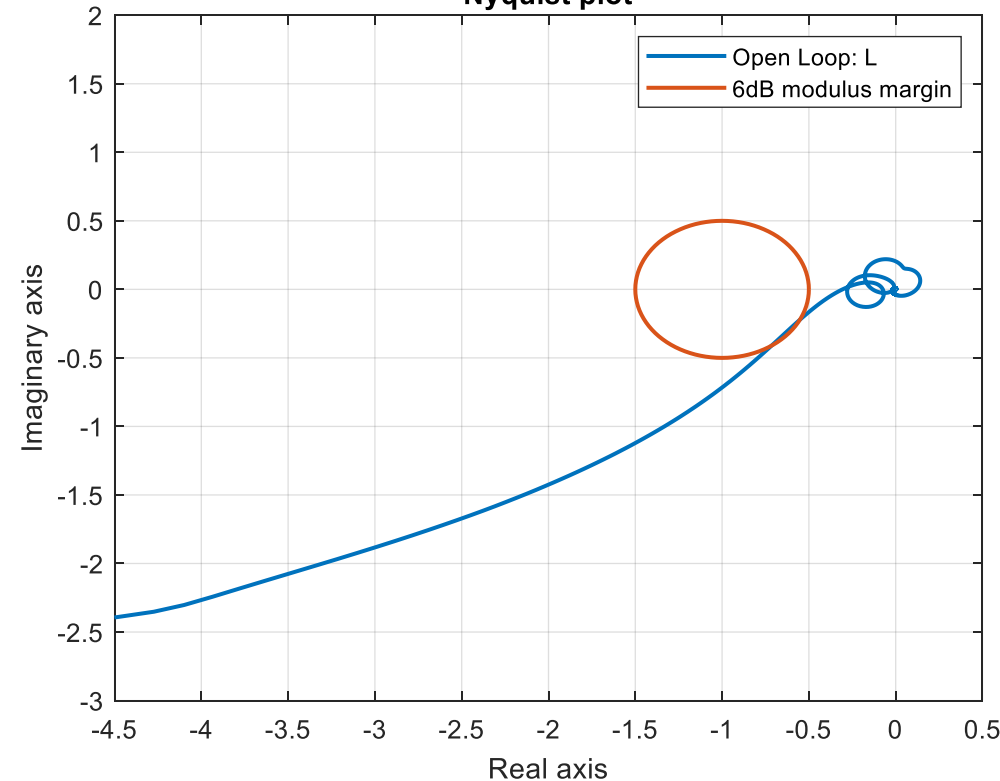
Intermezzo: Nyquist Stability Criterion

- ❑ The Nyquist Stability Criterion can be used to assess closed-loop stability:
 - graphical check
 - Based on frequency-response function (FRF) of the plant, i.e. mechanical spectrum
- ❑ Nyquist plot:
 - $\text{Re}(L)$ on horizontal axis
 - $\text{Im}(L)$ on vertical axis
- ❑ Necessary requirement for stability:
 - $(-1,0)$ is on the left side of the Nyquist plot of the open loop L
- ❑ Robustness margins:
 - PM: phase margin
 - GM: gain margin



Case study: Nyquist Stability Criterion

Nyquist plot



- The Nyquist plot of L :
 - is on the right hand side of the point $(-1,0)$;
 - shows that the closed loop is stable;
 - only slightly enters the 6dB modulus margin region.
- Note:
 - The modulus margin is a measure for robustness
 - The modulus margin corresponds to the peak in the sensitivity
 - Therefore, the sensitivity is expected to have a peak slightly higher than 6dB

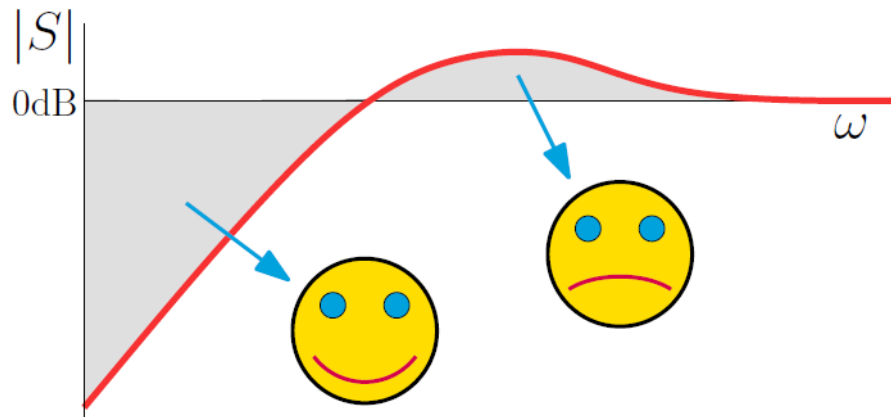
Performance assessment using sensitivity function

□ The sensitivity function:

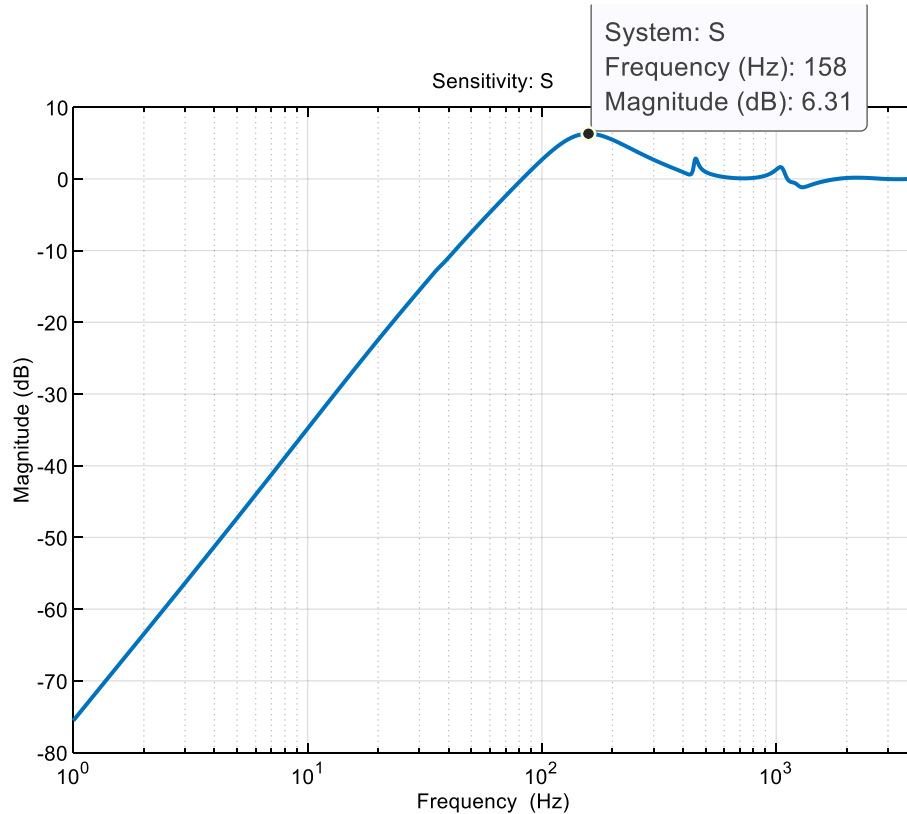
- is a common measure for performance;
- peak corresponds to modulus margin, typically tuned to be below 6dB for robustness;
- magnitude corresponds to the amount of disturbance suppression/amplification at a given frequency:
 - $|S| < 0$ dB \rightarrow Feedback control improves performance;
 - $|S| > 0$ dB \rightarrow Feedback control deteriorates performance.

□ The waterbed effect:

- suppression of $|S|$ at given frequency results in amplification elsewhere;
- is a fundamental limitation of linear control.



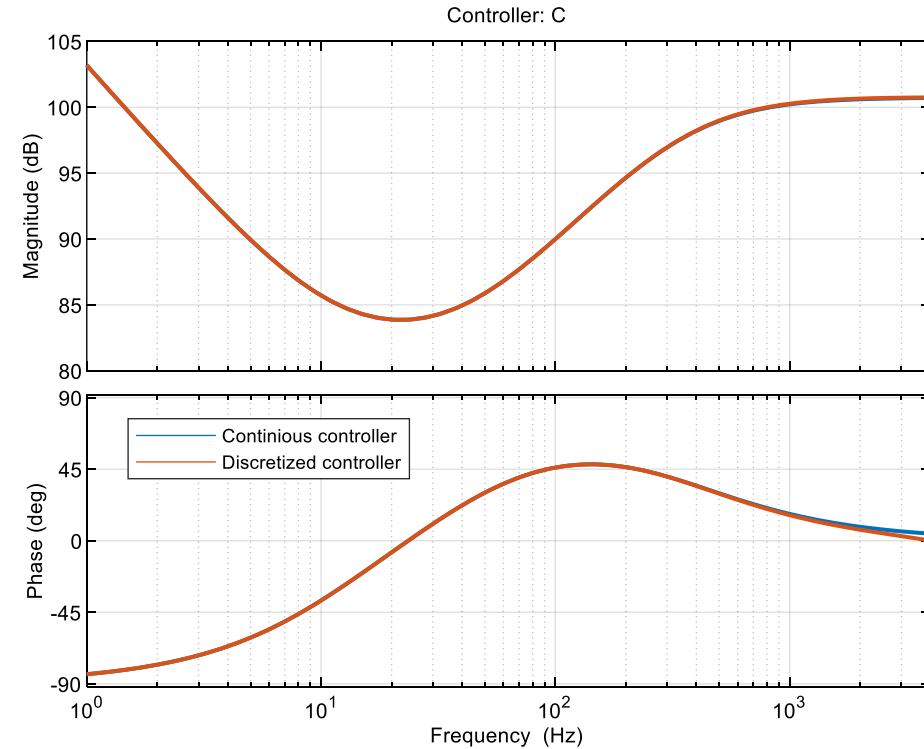
Case study: sensitivity function



- ❑ As expected from the Nyquist plot, the modulus margin is slightly higher than 6 dB
- ❑ Up to 82 Hz, the feedback controller improves the performance of the system
- ❑ Note:
 - Reference profiles used by ASMPT typically have their dominant energy content in the low-frequency range

Case study: discretization of feedback controller

- ❑ Our machines run on a fixed sampling rate
- ❑ Therefore, the feedback controller needs to be discretized before implementation on the machine
- ❑ Tustin-discretization is a common method to convert a system from the continuous to the discrete time domain
- ❑ Discretized and continuous feedback controllers have similar Bode characteristics → discretization successful





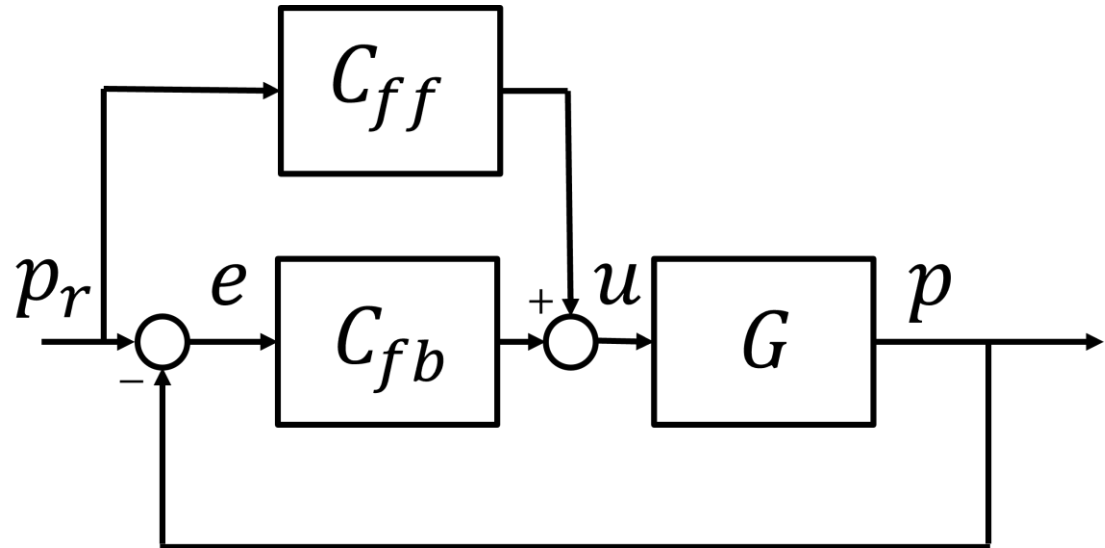
COFFEE BREAK

FEEDFORWARD CONTROL

Motion control system (with feedforward control)

- p_r : reference position
- p : encoder position
- e : error
- u : motor input
- for simplicity, the disturbances are ignored here.

- G : plant
- C_{fb} : feedback controller
- C_{ff} : feedforward controller



Why feedforward control?

- ❑ Feedback reacts to an already existing error and is therefore always lacking behind
- ❑ Feedforward uses knowledge about the motion profile and the plant dynamics to deliver the desired motor input before the error can occur
- ❑ In principle, if the machine dynamics are exactly known, no feedback is needed. However, in practice:
 - disturbances are present;
 - the machine dynamics are not exactly known.
 - Therefore, combining feedback and feedforward is the way to go.



Feedforward: simple example

□ We want to control the following system:

$$\blacksquare G(s) = \frac{p(s)}{I(s)} = \frac{K_f \cdot p(s)}{F(s)} = \frac{K_f}{ms^2 + bs}$$

■ with, position p , force F , current I , mass m , viscous friction b , force constant K_f , and Laplace variable s

□ The optimal feedforward controller is given by:

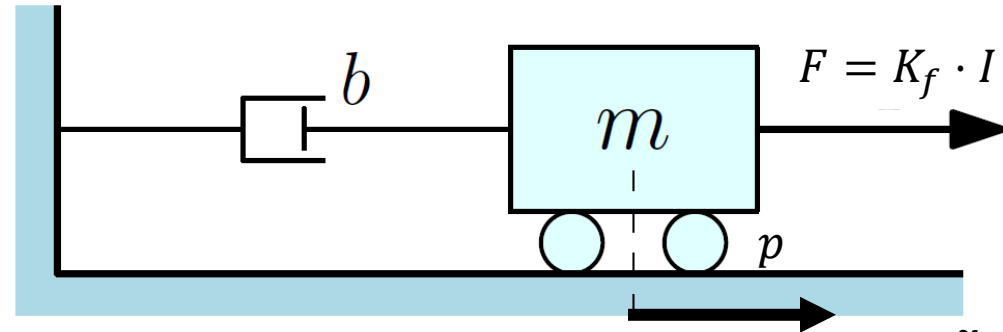
$$\blacksquare C_{ff}(s) = (G(s))^{-1} = \frac{I(s)}{p(s)} = \frac{m}{K_f} s^2 + \frac{b}{K_f} s = K_a s^2 + K_v s$$

$$\blacksquare I(s) = (K_a s^2 + K_v s) p(s)$$

$$\blacksquare \text{Conversion to time domain: } I(t) = K_a \ddot{p}(t) + K_v \dot{p}(t)$$

■ Therefore, an acceleration and velocity feedforward need to be used for this system, with feedforward parameters K_a and K_v .

■ For many motion systems within ASMPT, a feedforward consisting of an acceleration and velocity element are capable to capture the desired current to follow a given motion profile with >90% accuracy.

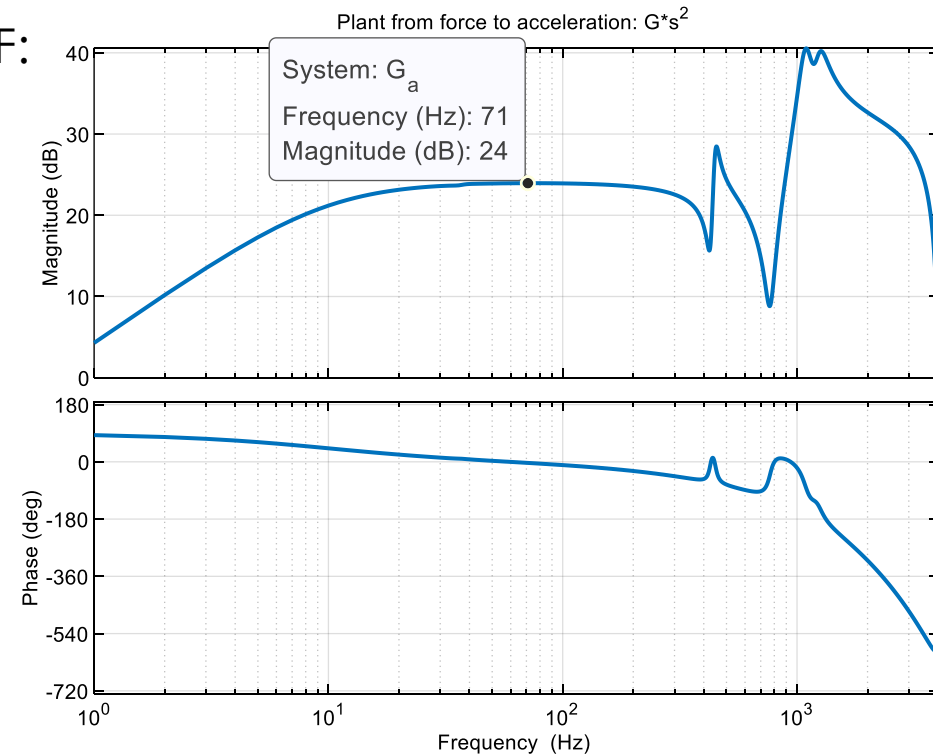


How to obtain the feedforward parameters? (K_a)

■ An initial guess of the acceleration feedforward parameter K_a can be directly estimated from the plant FRF:

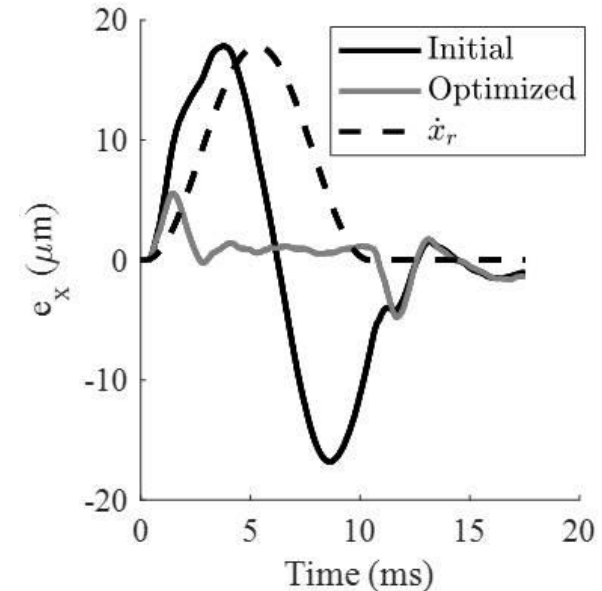
1. Measure the FRF from current I to position p . i.e., $G(s) = \frac{p(s)}{I(s)}$
2. Take the 2nd derivative of this FRF:

$$G(s) \cdot s^2 = \frac{p(s)}{I(s)} \cdot s^2 = \frac{\ddot{p}(s)}{I(s)}$$
3. Obtain the magnitude of the horizontal part of the FRF for the estimation of the acceleration feedforward parameter: $K_a = \frac{1}{db2mag(24)} = 0.0631 \text{ [As}^2/\text{m]}$



How to obtain the feedforward parameters? (K_v)

- ❑ Obtaining an initial guess of the velocity feedforward parameter K_v is much more difficult in practice
- ❑ Starting from the initial estimate of K_a , the feedforward parameters K_a and K_v can be further finetuned with the machine in the loop until the servo errors are minimized:
 - This can be done manually by trial & error, but more advanced automated methods do exist



CONCLUSIONS

Conclusions

- ❑ Feedback and feedforward control should work together in harmony.
 - Feedforward control: to deal with the machine dynamics that are known prior to the movement
 - Feedback control: to deal with the remaining unknown machine dynamics & external disturbances that always exist in practice
- ❑ Loop shaping is one of the easiest methods to tune a feedback controller. General rules of thumb result in a satisfactory controller in many situations
- ❑ Feedforward controller parameters can be partially derived based on machine data, but some manual trial & error will be required for fine-tuning in the explained method

Next steps

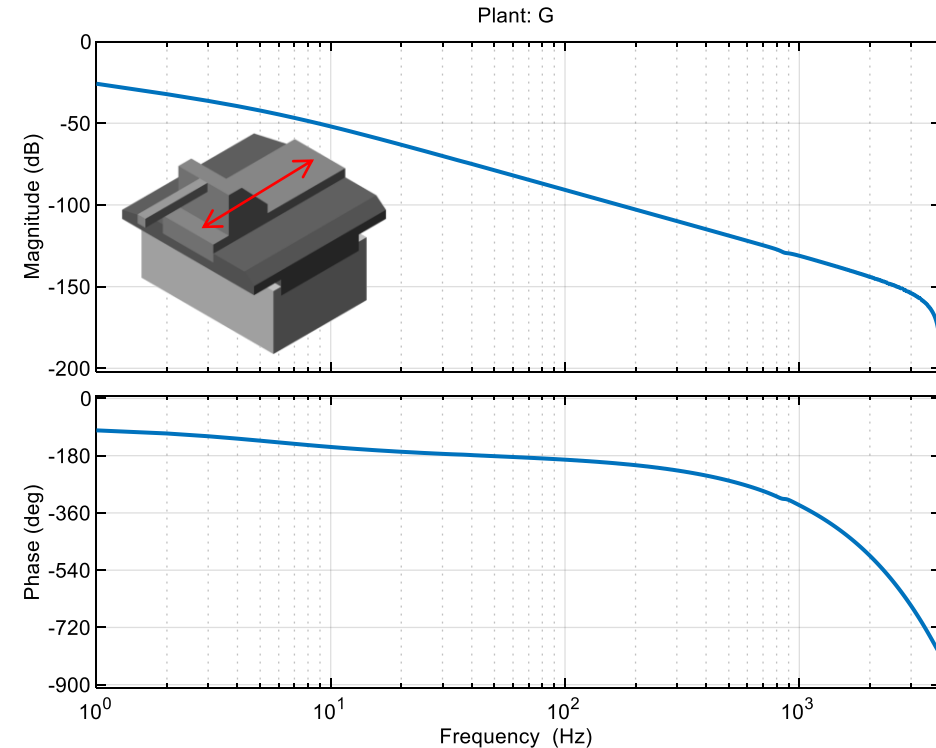
- ❑ Not satisfied with the obtained performance yet?
- ❑ The Center of Competency can help to further improve:
 - Feedback control → by means of the FeedBack Autotuner (FBA)
 - Feedforward control → by means of
 - ❑ Surrogate modelling optimization
 - ❑ Iterative learning control (ILC) with basis functions
- ❑ Feel free to contact us!

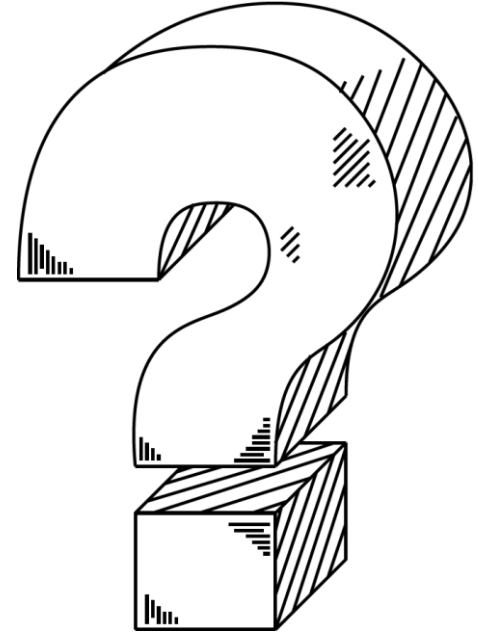


SELF-STUDY ASSIGNMENT

Self-study assignment: Y-stage of AB383 Simscape model

- ❑ In this training, the X-stage of the AB383 Simscape model has been used as an example to design a feedback and feedforward controller.
- ❑ Now, try for the Y-stage:
 1. Design a feedback controller:
 - ❑ using loop-shaping,
 - ❑ with a bandwidth as high as possible,
 - ❑ with a modulus margin of less than 6 dB.
 2. Design a feedforward controller:
 - ❑ by obtaining the acceleration parameter using a frequency domain analysis.





QUESTIONS

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