

Part a)

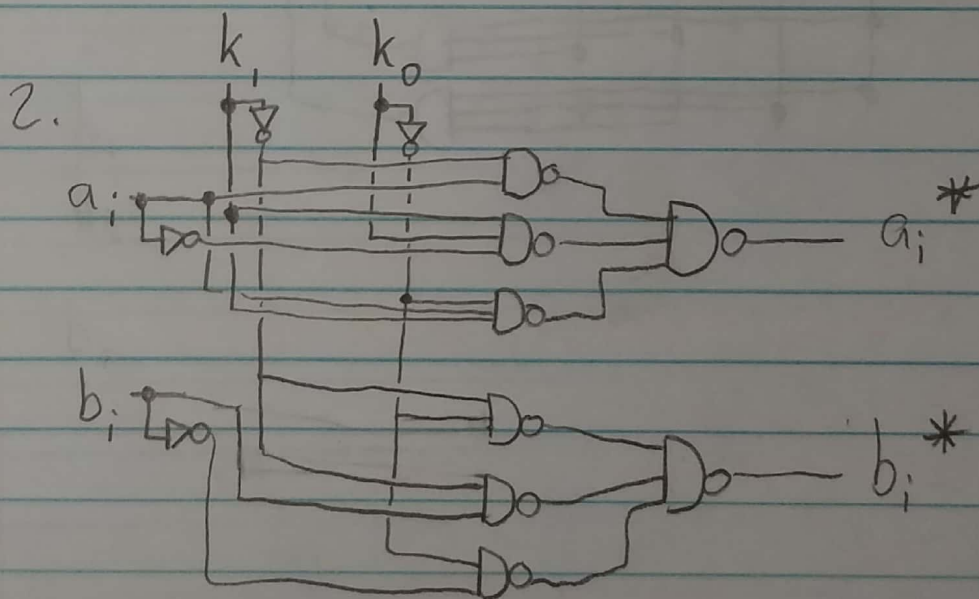
		a_i	
		0	1
k_1, k_0	00	0	1
	01	0	1
	11	1	0
	10	0	1

		b_i	
		0	1
k_1, k_0	00	1	1
	01	0	1
	11	0	0
	10	1	0

		c_0	
		0	1
k_1	0	0	0
	1	1	1

$$1. \quad a_i^* = k_1' a_i + k_1 k_0' a_i' + k_1 k_0' a_i$$

$$b_i^* = k_1' k_0' + k_1' b_i + k_0' b_i'$$



$$3. \quad c_0 = k_1$$

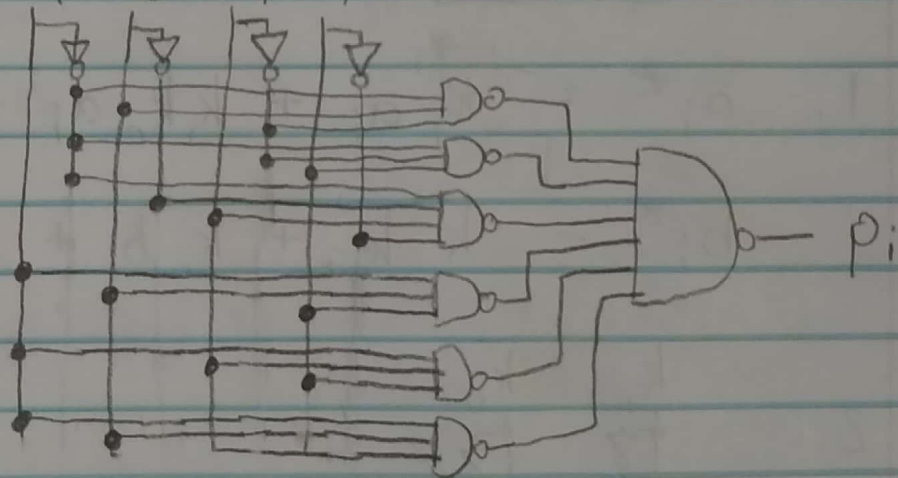
Part 1 b)

p_i a_i, b_i

		00	01	11	10
k_1, k_0	00	0	1	0	1
	01	1	1	0	0
	11	0	1	1	1
	10	0	0	1	0

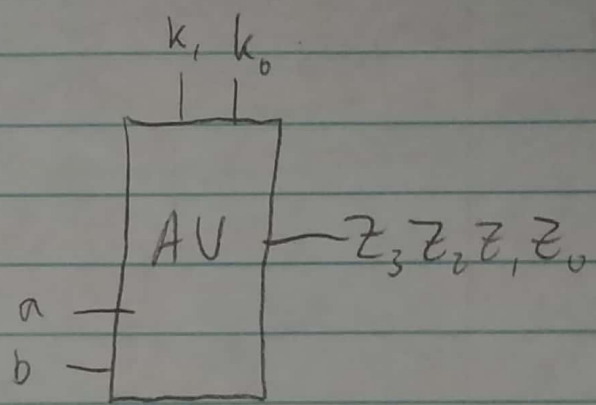
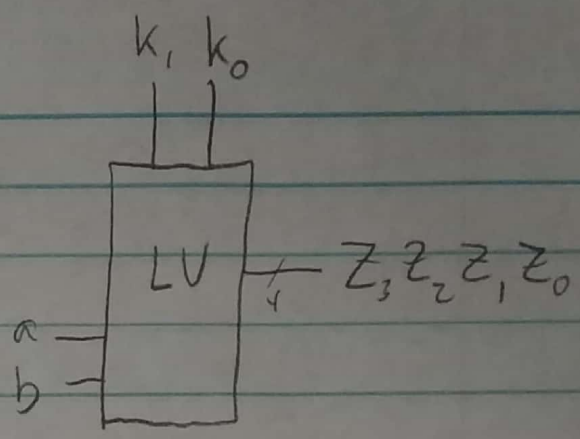
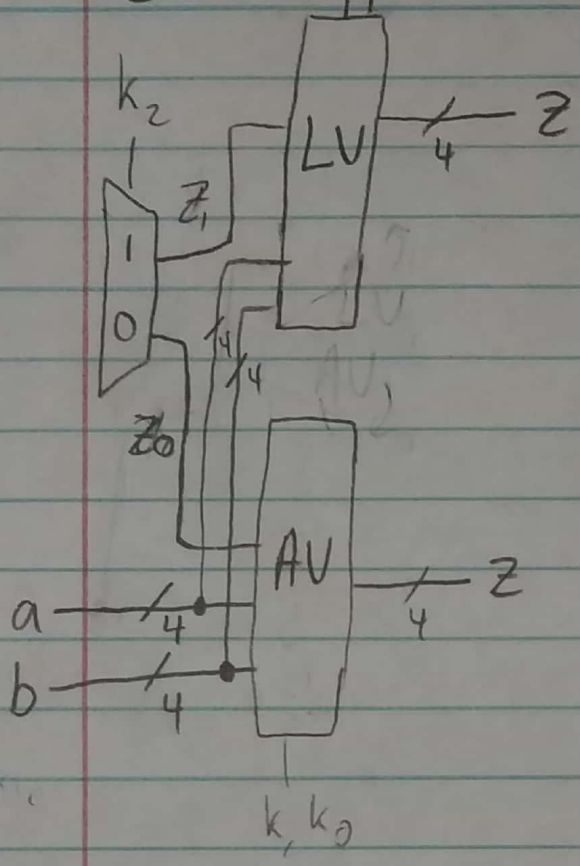
$$1. \quad p_i = k_1' k_0' a_i' + a_i' b_i k_1' + k_1' k_0' a_i b_i' + k_1' k_0' b_i + a_i b_i k_1 + k_1 k_0 a_i$$

2. k_1, k_0, a_i, b_i



Part 1 c) k, k_0

2.



Part 2

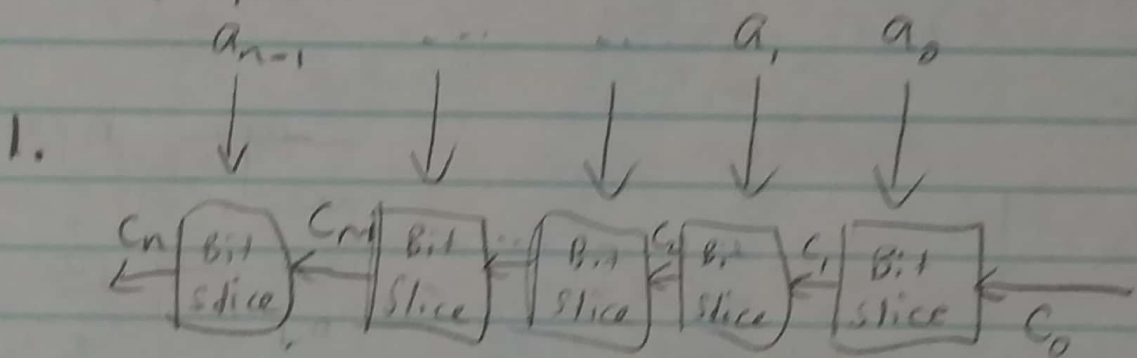
C_i, a_i, C_{i+1}

0	0	0	Post even, now even
0	1	1	Post even, now odd
1	0	1	Post odd, now odd
1	1	0	Post odd, now even

a_i

	0	1
C_i 0	0	1
1	1	0

$$C_i a_i' + C_i' a_i = \text{XOR}(a_i, C_i)$$



2. Inputs: a_i is current digit in binary #
 C_i indicates if previous digits have an odd (1) or even (0) number of 1's

C_{i+1} indicates if previous digits including a_i are negative or positive

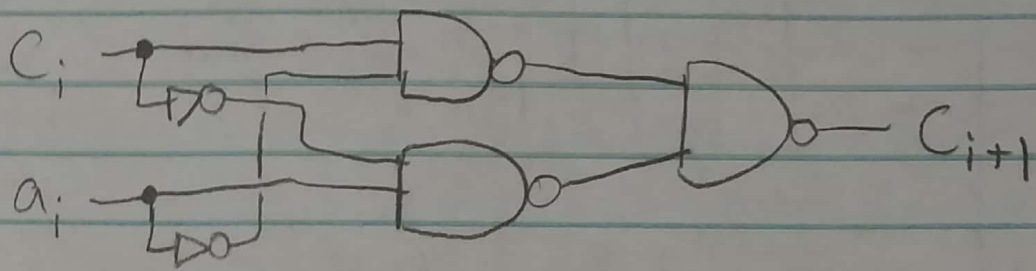
3.

4. $C_{i+1} = C_i a_i' + C_i' a_i$

Part 2 (cont.)

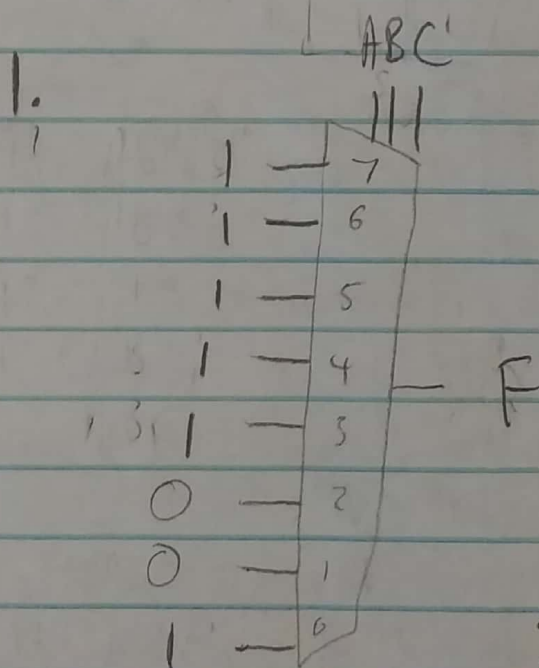
5. $c_i a_i' + c_i' a_i$

$$c_{i+1} = ((c_i a_i')' (c_i' a_i)')'$$

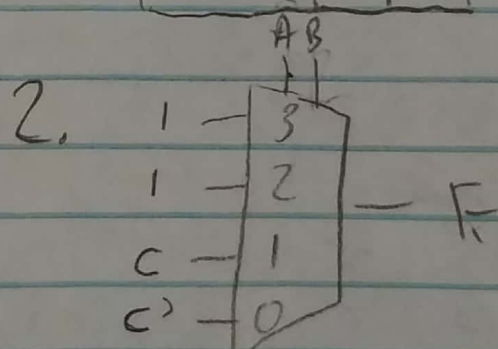


Part 3

$F(A, B, C)$



ABC	F
000	1
001	0
010	0
011	1
100	1
101	1
110	1
111	1

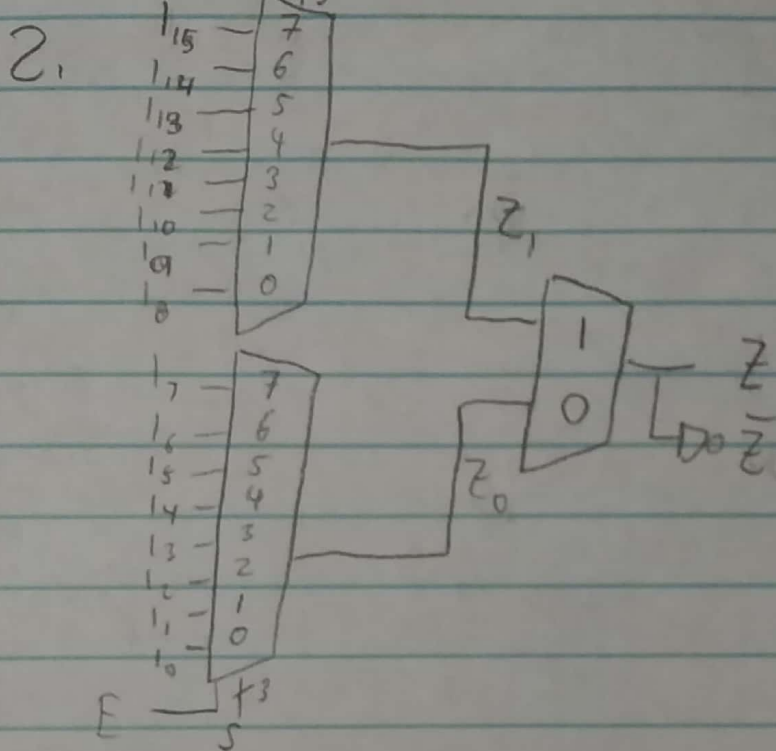


3. Requires 3 bits

3. Requires 2 bits

Part 4

$$1. Z = I_0 S_2' S_1' S_0' E + I_1 S_2' S_1' S_0 E + I_2 S_2' S_1 S_0' E + I_3 S_2' S_1 S_0 E \\ + I_4 S_2 S_1' S_0' E + I_5 S_2 S_1' S_0 E + I_6 S_2 S_1 S_0' E + I_7 S_2 S_1 S_0 E$$



```
main.c | CMake
1 #include <stdio.h>
2 int main()
3 {
4     unsigned int w, x, y, z, e, f;
5     unsigned int g;
6
7     /* Print header for K-map. */
8     printf("      yz\n");
9     printf("    00 01 11 10\n");
10    printf("    _____\n");
11
12    /* row-printing loop */
13    for (w = 0; 2 > w; w = w + 1) {
14
15        for (f = 0; 2 > f; f = f + 1) { /* used to get the special pattern 00,01,11,10 instead of 00,01,10,11 */
16
17            if (w == 0) {
18                x = f;
19            } else {
20                x = 1 - f;
21            }
22            printf("wx=%02u | ", w, x);
23
24            /* Loop over input variable y in binary order. */
25            for (y = 0; 2 > y; y = y + 1) {
26                /* Loop over z in binary order. */
27                for (g = 0; 2 > g; g = g + 1) { /* used to get the special pattern 00,01,11,10 instead of 00,01,10,11 */
28                    if (y == 0) {
29                        z = g;
30                    } else {
31                        z = 1 - g;
32                    }
33                    if ((x & z) | (w & y)) {
34                        printf("1 ");
35                    } else {
36                        printf("0 ");
37                    }
38                }
39            }
40
41            /* End of row reached: print a newline character. */
42            printf("\n");
43        }
44    }
45
46    return 0;
47 }
```

Input

	yz
	00 01 11 10
wx=00	0 0 1 1
wx=01	1 0 1 1
wx=11	1 0 0 1
wx=10	0 0 0 0

```
main.c
1 #include <stdio.h>
2 int main()
3 {
4     unsigned int w, x, y, z, e, f;
5     unsigned int g;
6
7     /* Print header for K-map. */
8     printf("      yz      \n");
9     printf("      00 01 11 10 \n");
10    printf("      _____ \n");
11
12    /* row-printing loop */
13    for (w = 0; 2 > w; w = w + 1) {
14        for (f = 0; 2 > f; f = f + 1) { /* used to get the special pattern 00,01,11,10 instead of 00,01,10,11 */
15            if (w == 0) {
16                x = f;
17            } else {
18                x = 1 - f;
19            }
20            printf("wx=%02u | ", w, x);
21
22            /* Loop over input variable y in binary order. */
23            for (y = 0; 2 > y; y = y + 1) {
24                /* Loop over z in binary order. */
25                for (g = 0; 2 > g; g = g + 1) { /* used to get the special pattern 00,01,11,10 instead of 00,01,10,11 */
26                    if (y == 0) {
27                        z = g;
28                    } else {
29                        z = 1 - g;
30                    }
31                    if ((w & !x & y & !z) | !w | (!x & !y)) {
32                        printf("1 ");
33                    } else {
34                        printf("0 ");
35                    }
36                }
37            }
38
39            /* End of row reached: print a newline character. */
40            printf("\n");
41        }
42    }
43    return 0;
44 }
```

Input

	yz
	00 01 11 10
wx=00	1 1 1 1
wx=01	1 1 1 1
wx=11	0 0 0 0
wx=10	1 1 0 1