

Let c is a constant:

$$* E[c] = c$$

$$* E[cx] = c\mu_x$$

$$* V[c] = 0$$

$$* V[x] = E[(x - \mu_x)^2] =$$

$$E[x^2 - 2x\mu_x + \mu_x^2] =$$

$$E[x^2] - 2\mu_x E[x] + E[\mu_x^2]$$

$$V[x] = E[x^2] - \mu_x^2$$

$$* V[cx] = E[(y - \mu_y)^2] =$$

$$E[y^2] - \mu_y^2$$

$$E[(cx)^2] - (E[cx])^2$$

$$c^2 E[x^2] - c^2 (E[x])^2$$

$$c^2 (E[x^2] - \mu_x^2)$$

$$V[cx] = c^2 V[x]$$

if we have two random variables $x \begin{cases} E[x] = \mu_x \\ V[x] = \sigma_x^2 \end{cases} y = \begin{cases} E[y] = \mu_y \\ V[y] = \sigma_y^2 \end{cases}$

$$* E[x + y] = E[x] + E[y] = \mu_x + \mu_y$$

$$* V[x + y] = E[z^2] - z^2 = E[(x + y)^2] - (E[(x + y)])^2$$

$$= E[(x^2 + 2xy + y^2)] - (\mu_x^2 + 2\mu_x\mu_y + \mu_y^2)$$

$$= E[x^2] + 2E[xy] + E[y^2] - \mu_x^2 - 2\mu_x\mu_y - \mu_y^2$$

$$= V[x] + V[y] + 2\text{Cov}(x, y)$$

$$* \text{Cov}(x, y) = E[(x - \mu_x)(y - \mu_y)]$$

* If x and y are independent, $\text{Cov}(x, y) = 0$