

$$v(s) = E[G_\tau | S_\tau = s]$$

$$E[R_{\tau+1} + \gamma R_{\tau+2} + \gamma^2 R_{\tau+3} + \dots | S_\tau = s]$$

$$E[R_{\tau+1} + \gamma (R_{\tau+2} + \gamma R_{\tau+3} + \dots) | S_\tau = s]$$

$G_{\tau+1}$

$$E[\underbrace{R_{\tau+1}}_{\text{Immediate Reward}} + \gamma \underbrace{v(s')}_{\text{Discounted value of successor state } (s')}} | S_\tau = s]$$

Immediate
Reward

Discounted
value of successor
state (s')