

# Inhomogeneous Lattice Systems

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# Chapter 1

## Hierarchical Index

### 1.1 Class Hierarchy

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inhLatticeSystem . . . . .	9
linAssignInfoType . . . . .	15
ostream	
fileStdoutStream . . . . .	8
physical_parameters . . . . .	15





## Chapter 2

# Class Index

### 2.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

<a href="#">arguments</a>	7
<a href="#">blochFindMultipleRoots</a>	7
<a href="#">fileStdoutStream</a>	8
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<a href="#">inhLatticeSystem</a>	9
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## Chapter 3

# File Index

### 3.1 File List

Here is a list of all documented files with brief descriptions:

<a href="#">inhLatticeSystem.cpp</a> . . . . .	17
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## Chapter 4

# Class Documentation

### 4.1 arguments Struct Reference

#### Public Attributes

- unsigned **sites**
- double **latticeDepth**
- double **inhStrength**
- char \* **outPath**

#### 4.1.1 Detailed Description

responsible for program parameters

#### See Also

'argp' from gnu

The documentation for this struct was generated from the following file:

- [inhLatticeSystem.cpp](#)

### 4.2 blochFindMultipleRoots Struct Reference

#### Public Member Functions

- void **searchDownUp** ()
- void **findMin** (mt start, mt end, mt precision)

#### Public Attributes

- mt **intervalStart**
- mt **intervalEnd**
- mt **rootValueAccuracy**
- mt **takenZero**
- mt(\* **rf** )(mt)
- mt(\* **mf** )(mt, void \*)
- set< mt > **allRoots**
- set< mt > **allMins**
- mt **intervalForMinSearch**

### 4.2.1 Detailed Description

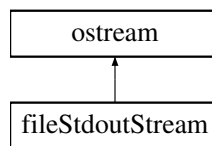
Searches for roots in an input function

The documentation for this struct was generated from the following file:

- [inhLatticeSystem.cpp](#)

## 4.3 fileStdoutStream Class Reference

Inheritance diagram for fileStdoutStream:



### Public Types

- typedef std::ostream &(\* **stream\_function** )(std::ostream &)

### Public Member Functions

- void **open** (const char \*filename)
- template<typename T >  
fileStdoutStream & **operator**<< (const T &arg)
- fileStdoutStream & **operator**<< (stream\_function func)
- fileStdoutStream & **flush** ()

### Public Attributes

- ofstream **file**

### 4.3.1 Detailed Description

This class introduces the functionality for the object 'fout' which is similar to the standard c++ object 'cout' but different in that it streams all the output to a file in addition to 'cout'.

The documentation for this class was generated from the following file:

- [inhLatticeSystem.cpp](#)

## 4.4 FsOverTS Struct Reference

### Public Member Functions

- **FsOverTS** (unsigned n)

## Public Attributes

- Col< mt > **Heigenvalues**
- Col< mt > **HeigenvaluesDeriv**
- Col< mt > **PositionOverTrapStrength**
- Col< mt > **BpPositionOverTrapStrength**

### 4.4.1 Detailed Description

needed to return information from the calcFsOverTS procedure

See Also

[calcFsOverTS](#)

The documentation for this struct was generated from the following file:

- [inhLatticeSystem.cpp](#)

## 4.5 inhLatticeSystem Class Reference

### Public Member Functions

- void [outputPropagatedWavefunctionEndValueOverE](#) ()
- void [outputPotential0](#) ()
- void [outputPotential](#) ()
- void [calculateH0eigenvalues](#) ()
- void [calculateH0eigenfunctions](#) ()
- void [calculateOverlapWithH0eigenfunctionsFromFile](#) ()
- void [calculateSchroedinger0Error](#) ()
- void [H0H0Overlap](#) ()
- void [hopping0OverDI](#) ()
- void [calculateCenteredWannier0Functions](#) ()
- void [calculateWannier0Functions](#) ()
- void [calculateWannier0Overlap](#) ()
- void [calculateGaussianInWannier0Basis](#) ()
- void [calculateOverlapWithWannierStatesFromFile](#) ()
- void [hopping0viaInt](#) ()
- bool [calculateHinW0](#) (unsigned n, unsigned m, unsigned &count)
- void [calculateHinW0](#) ()
- void [calculateHeigenvaluesESorted](#) ()
- void [calculateBand0ProjectorsExpectationInHeigenstates](#) ()
- void [calculateHeigenvaluesOverTrapStrength](#) ()
- void [calculateXinW0](#) ()
- void [calculateHlocalization](#) ()
- void [assignBandOrderEqualHeigenvalueOrder](#) ()
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- void [calculateWannier0Eigenvalues](#) ()
- void [calculateFOverTrapStrength](#) ()
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- void [calculateLeftRightSideOfHinW0EigenvalueEquation](#) ()
- void [calculateProductOfHWannier0overlapMatrixWithItselfsAdjoint](#) ()
- void [calculateBandOrderedVariables](#) ()

- void [calculateHeigenstates](#) ()
- void [outputSelectedFunctions](#) ()
- void [compareWithHeigenstatesFromFile](#) ()
- void [calculateSchroedingerError](#) ()
- void [calculateOverlapWithHarmonicOscillator](#) ()
- void [calculateWinE](#) ()
- void [calculateWannierEigenvalues](#) ()
- void [calculateLeftRightSideOfWannierInHEigenvalueEquation](#) ()
- void [calculateProductOfWannierHoverlapMatrixWithItselfsAdjoint](#) ()
- void [calculateWannierFunctions](#) ()
- void [calculateWannierFunctionsRephased](#) ()
- void [calculateHopping](#) ()
- void [calculateU](#) ()
- void [calculateHeigenstatesFromWannier](#) ()
- void [calculateWannierFunctionValueUsingHeigenfunctions](#) ()
- void [calculateWannierOverlap](#) ()
- void [calculateBorderEffects](#) ()
- void [calc](#) ()

## Public Attributes

- ofstream **file**
- ifstream **ifile**
- mt **sampleWidth**
- mt **odeSampleWidth**
- mt **wannier0FunctionCutoff**
- mt **HinW0cutoff**
- unsigned **kSteps**
- unsigned **nrSites**
- [blochFindMultipleRoots](#) **fR**
- unsigned **minBands**
- clock\_t **tMark**
- Col< mt > **H0eigenvalues**
- Col< mt > **H0kvalues**
- vector< fct< complex< mt > > > **H0eigenfunctions**
- vector< fct< complex< mt > > > **centeredWannier0Functions**
- vector< fct< complex< mt > > > **wannier0Functions**
- vector< fct< complex< mt > > > **wannier0FunctionsPeriod**
- Col< mt > **wannier0Eigenvalues**
- Mat< cx\_double > **HinW0partV**
- Mat< cx\_double > **HinW0partH0**
- Mat< cx\_double > **HinW0**
- Col< mt > **HeigenvaluesESorted**
- Mat< cx\_double > **W0HOverlapESorted**
- Mat< complex< mt > > **XinW0**
- Col< mt > **Hlocalization**
- Col< mt > **bandToEindex**
- Col< mt > **Heigenvalues**
- Mat< cx\_double > **W0HOverlap**
- vector< fct< complex< mt > > > **Heigenfunctions**
- Mat< cx\_double > **wannierInH**
- Col< mt > **wannierEigenvalues**
- Mat< cx\_double > **HWannierOverlap**
- Mat< cx\_double > **HWannierOverlapRephased**
- vector< fct< complex< mt > > > **wannierFunctions**



### 4.5.1 Detailed Description

This is the most essential class of the program. It includes most of the functionality for solving inhomogeneous lattice systems.

Thus, it contains methods for

- finding the homogeneous system eigenvalues, eigenfunctions and Wannierfunctions
- diagonalizing the complete (inhomogeneous) Hamiltonian in the homogeneous system Wannier basis, giving the inhomogeneous system eigenvalues and eigenfunctions
- systematically assigning states to bands
- applying Kivelson's generalized definition of the Wannierfunctions to obtain inhomogeneous Wannier functions
- calculating inhomogeneous system Hubbard parameters

### 4.5.2 Member Function Documentation

**4.5.2.1** `void inhLatticeSystem::assignBandOrderEqualHeigenvalueOrder ( ) [inline]`

assume energy gap still present i.e. define band projectors in terms energy ordered eigenstates

**4.5.2.2** `void inhLatticeSystem::assignBandOrderUsingLocalization ( ) [inline]`

define band projectors using the localization of the energy eigenstates

**4.5.2.3** `void inhLatticeSystem::calc ( ) [inline]`

MAIN EXECUTION PROCEDURE: uncomment everything you want calculated

**4.5.2.4** `void inhLatticeSystem::calculateBand0ProjectorsExpectationInHeigenstates ( ) [inline]`

calculate the expectation value of multiple primary lattice band projection operators for every eigenstate

**4.5.2.5** `void inhLatticeSystem::calculateBandOrderedVariables ( ) [inline]`

resort quantities taking band assigning into account

**4.5.2.6** `void inhLatticeSystem::calculateBorderEffects ( ) [inline]`

calculate system edge influences shape of Wannier state

**4.5.2.7** `void inhLatticeSystem::calculateCenteredWannier0Functions ( ) [inline]`

calculate one primary lattice Wannier function per band

**4.5.2.8** `void inhLatticeSystem::calculateChangeInLocalizations ( ) [inline]`

calculate how the localization changes as function of the inhomogeneity strength

**4.5.2.9** `void inhLatticeSystem::calculateFOverTrapStrength ( ) [inline]`

calculate eigenvalues, derivative of eigenvalues, expectation of position and expectation of band projected position operator for a range of inhomogeneity strength

**4.5.2.10** `void inhLatticeSystem::calculateGaussianInWannier0Basis ( ) [inline]`

calculate overlap between Gaussian and Wannier basis

**4.5.2.11** `void inhLatticeSystem::calculateH0eigenfunctions ( ) [inline]`

calculate the eigenfunctions of the homogeneous lattice system

**4.5.2.12** `void inhLatticeSystem::calculateH0eigenvalues ( ) [inline]`

calculate the eigenvalues of the homogeneous lattice system

**4.5.2.13** `void inhLatticeSystem::calculateHeigenstates ( ) [inline]`

calculate the real space eigenfunctions for the whole system

**4.5.2.14** `void inhLatticeSystem::calculateHeigenstatesFromWannier ( ) [inline]`

recalculate the eigenstates from the Wannier states

**4.5.2.15** `void inhLatticeSystem::calculateHeigenvaluesESorted ( ) [inline]`

calculate system energy eigenvalues and overlap elements with primary lattice Wannier basis

**4.5.2.16** `void inhLatticeSystem::calculateHeigenvaluesOverTrapStrength ( ) [inline]`

calculate energy eigenvalues for a whole range of inhomogeneity strength

**4.5.2.17** `bool inhLatticeSystem::calculateHinW0 ( unsigned n, unsigned m, unsigned & count ) [inline]`

calculate single element with index (n,m) of Hamiltonian in primary lattice Wannier basis using primary lattice hopping elements and real space integration with inhomogeneity potential

**4.5.2.18** `void inhLatticeSystem::calculateHinW0 ( ) [inline]`

calculate Hamiltonian in primary lattice Wannier basis using primary lattice hopping elements and real space integration with inhomogeneity potential

**4.5.2.19** `void inhLatticeSystem::calculateHlocalization ( ) [inline]`

calculate expectation of position operator for every energy eigenstate

**4.5.2.20** `void inhLatticeSystem::calculateHopping ( ) [inline]`

calculate the hopping using the generalized Wannier basis

4.5.2.21 `void inhLatticeSystem::calculateLeftRightSideOfHinW0EigenvalueEquation ( ) [inline]`

calculate both sides of eigenvalue equation

4.5.2.22 `void inhLatticeSystem::calculateLeftRightSideOfWannierInHEigenvalueEquation ( ) [inline]`

calculate both sides of eigenvalue equation

4.5.2.23 `void inhLatticeSystem::calculateOverlapWithH0eigenfunctionsFromFile ( ) [inline]`

calculate the overlap of the homogeneous eigenfunctions with other functions supplied through a file

4.5.2.24 `void inhLatticeSystem::calculateOverlapWithHarmonicOscillator ( ) [inline]`

calculate overlap between eigenstates and harmonic Oscillator states (verification procedure/relevant if primary lattice depth is zero)

4.5.2.25 `void inhLatticeSystem::calculateOverlapWithWannierStatesFromFile ( ) [inline]`

calculate overlap between primary lattice Wannier states and states in file

4.5.2.26 `void inhLatticeSystem::calculateProductOfHWannier0overlapMatrixWithItselfsAdjoint ( ) [inline]`

see if overlaps between eigenstates and primary lattice Wannier states are unitary

4.5.2.27 `void inhLatticeSystem::calculateProductOfWannierHoverlapMatrixWithItselfsAdjoint ( ) [inline]`

verify unity of overlap matrix

4.5.2.28 `void inhLatticeSystem::calculateSchroedinger0Error ( ) [inline]`

calculate the error in the eigenfunctions for every band, function and position

4.5.2.29 `void inhLatticeSystem::calculateSchroedingerError ( ) [inline]`

calculate the band, state and position error of eigenfunctions using the Schroedinger equation

4.5.2.30 `void inhLatticeSystem::calculateU ( ) [inline]`

calculate the onsite interaction using the generalized Wannier basis

4.5.2.31 `void inhLatticeSystem::calculateWannier0Eigenvalues ( ) [inline]`

calculate eigenvalues of primary lattice band projected position operator assuming non-periodic states

4.5.2.32 `void inhLatticeSystem::calculateWannier0Functions ( ) [inline]`

calculate all primary lattice Wannier functions using translation symmetry

**4.5.2.33** `void inhLatticeSystem::calculateWannier0Overlap ( ) [inline]`

calculate overlap between all primary lattice Wannier functions

**4.5.2.34** `void inhLatticeSystem::calculateWannierEigenvalues ( ) [inline]`

calculate eigenvalues and overlaps for generalized Wannier states with energy eigenstates

**4.5.2.35** `void inhLatticeSystem::calculateWannierFunctions ( ) [inline]`

calculate generalized Wannier states in real space

**4.5.2.36** `void inhLatticeSystem::calculateWannierFunctionsRephased ( ) [inline]`

rephase the generalized Wannier states

**4.5.2.37** `void inhLatticeSystem::calculateWannierFunctionValueUsingHeigenfunctions ( ) [inline]`

calculate value of Wannier function using energy eigenfunctions

**4.5.2.38** `void inhLatticeSystem::calculateWannierOverlap ( ) [inline]`

calculate overlaps between Wannier states

**4.5.2.39** `void inhLatticeSystem::calculateWinE ( ) [inline]`

calculate band projected position operator in the basis of energy eigenstates

**4.5.2.40** `void inhLatticeSystem::calculateXinW0 ( ) [inline]`

calculate band projected position operator in the primary lattice Wannier basis

**4.5.2.41** `void inhLatticeSystem::compareWithHeigenstatesFromFile ( ) [inline]`

compare real space eigenfunctions with functions from a file

**4.5.2.42** `void inhLatticeSystem::H0H0Overlap ( ) [inline]`

calculate overlaps among homogeneous eigenfunctions

**4.5.2.43** `void inhLatticeSystem::hopping0OverDI ( ) [inline]`

calculate primary lattice hopping using Fourier transform of dispersion relation

**4.5.2.44** `void inhLatticeSystem::hopping0viaInt ( ) [inline]`

calculate primary lattice hopping via integration over Wannierfunctions

4.5.2.45 `void inhLatticeSystem::outputPotential ( ) [inline]`

Output the inhomogeneous lattice potential

4.5.2.46 `void inhLatticeSystem::outputPotential0 ( ) [inline]`

Output the homogeneous lattice potential

4.5.2.47 `void inhLatticeSystem::outputPropagatedWavefunctionEndValueOverE ( ) [inline]`

Output the end value of the propagated u function for a range of E values

4.5.2.48 `void inhLatticeSystem::outputSelectedFunctions ( ) [inline]`

output a desired set of quantities

The documentation for this class was generated from the following file:

- [inhLatticeSystem.cpp](#)

## 4.6 linAssignInfoType Struct Reference

### Public Attributes

- unsigned **n**
- `Mat< cx_double >` **HinW0partH0**
- `Mat< cx_double >` **HinW0partV**
- `mt` **errThreshold**
- `vector< fct< complex< mt > > > *` **HeigenvaluesOverTrapStrength**
- `vector< fct< complex< mt > > > *` **HeigenvaluesOverTrapStrengthDeriv**
- `Col< mt >` **wannier0Eigenvalues**
- `Mat< cx_double >` **XinW0**
- `vector< fct< complex< mt > > > *` **PositionOverTrapStrength**
- `vector< fct< complex< mt > > > *` **BpPositionOverTrapStrength**

### 4.6.1 Detailed Description

needed to pass information to the calcFsOverTS procedure

See Also

[calcFsOverTS](#)

The documentation for this struct was generated from the following file:

- [inhLatticeSystem.cpp](#)

## 4.7 physical\_parameters Class Reference

### Public Attributes

- `mt` **hbar**

- `mt m`
- `mt a`
- `mt lambda`
- `mt k_L`
- `mt E_r`
- `mt s_bound`
- `mt A`
- `mt ld`
- `mt E`
- `mt k`
- `mt inhShift`
- `mt a_0`
- `mt a_s`
- `mt g`
- `mt inhS`
- `mt borderTrapHeight`
- `mt inhLatRatio`
- `mt alpha`
- `mt delta`

#### 4.7.1 Detailed Description

All the system information is contained in the variables in this class. One global object called 'pp' is created from this class and used throughout the calculations.

The documentation for this class was generated from the following file:

- [inhLatticeSystem.cpp](#)

## Chapter 5

# File Documentation

### 5.1 inhLatticeSystem.cpp File Reference

```
#include <cmath>
#include <cstdio>
#include <cstdlib>
#include <cmath>
#include <fstream>
#include <iostream>
#include <iomanip>
#include <set>
#include <map>
#include <sys/stat.h>
#include <argp.h>
#include <armadillo>
#include <gsl/gsl_errno.h>
#include <gsl/gsl_math.h>
#include <gsl/gsl_min.h>
#include <nr/nr.h>
#include <nr/nrtypes.h>
#include <nr/nrutil.h>
#include <boost/math/special_functions/hermite.hpp>
#include <utils.cpp>
#include <ODE_integration.cpp>
#include <diag_Householder_QL/diag_hermitian_Householder_QL.cpp>
#include <fct_classes/fct_class.cpp>
#include <fct_classes/fct_class_functions.cpp>
#include <jHelper.cpp>
#include <findMultipleBunchedRoots.cpp>
#include <iterators.cpp>
#include <RK4solver.hpp>
#include <DynStep.hpp>
#include <DGLsolver.hpp>
#include "streamer.cpp"
```

#### Classes

- class [fileStdoutStream](#)
- class [physical\\_parameters](#)
- struct [blochFindMultipleRoots](#)

- struct [linAssignInfoType](#)
- struct [FsOverTS](#)
- class [inhLatticeSystem](#)
- struct [arguments](#)

## Macros

- `#define outputWithHeader(x, header)`
- `#define outputWO(x) outputWithHeader(x,"");`

## Functions

- `mt Vlat (mt x, physical\_parameters &pp)`
- `complex< mt > Vinh (mt x)`
- `mt Vlat (mt x)`
- `complex< mt > V (mt x, physical\_parameters &pp)`
- `complex< mt > testF (mt x)`
- `void ODE\_derivs (const double x, double *y, double *dydx, physical\_parameters &pp)`
- `void dglSolve (ODE< physical\_parameters > *&D, unsigned eqncount, mt const xinit, mt *const &yinit)`
- `mt propagateFunction (mt par)`
- `mt invPropagateFunction (mt par)`
- `mt propagateFunction (mt par, void *)`
- `mt invPropagateFunction (mt par, void *)`
- `void outputPropagatedWavefunctionEndValueOverE (mt const Estart, mt const Eend, mt const step)`
- `unsigned bandToIndex0 (unsigned band, unsigned stateIndexInBand)`
- `unsigned bandToIndex (unsigned band, unsigned stateIndexInBand)`
- `void normalizeFct (fct< complex< mt > > &par)`
- `Mat< cx_double > calculateOverlapMatrix (vector< fct< complex< double > > > const &Es)`
- `Mat< cx_double > calculateEigenstatesBlockwise (Mat< cx_double > const symmetricMatrix, Col< mt > &eigenvals, unsigned statesPerBand)`
- `Mat< mt > createDiagonalMatrixFromVector (Col< mt > const eigenvalues)`
- `void addPhaseToLocalizeOnRealAxis (fct< complex< mt > > &f)`
- `template<typename fctRangeType , typename Fret >  
fctRangeType trapez\_int\_refined\_f (fct< fctRangeType > func1, Fret(*f)(mt), fctDomainType x_lo, fctDomainType x_hi, int n, fctRangeType &s)  
  
the same integration procedure for a product of two functions`
- `template<typename fctRangeType , typename Fret >  
fctRangeType trapez\_int\_refined\_f (fct< fctRangeType > func1, fct< fctRangeType > func2, Fret(*f)(mt), fctDomainType x_lo, fctDomainType x_hi, int n, fctRangeType &s)  
  
the same integration procedure for a product of two functions`
- `template<typename fctRangeType , typename Fret >  
fctRangeType romberg\_integral\_f (fct< fctRangeType > func1, Fret(*f)(mt), double romberg_precision=romberg_integration_precision)  
  
Romberg integration routine taken from numerical recipes in C++, the file qromb.c.`
- `template<typename fctRangeType , typename Fret >  
fctRangeType romberg\_integral\_f (fct< fctRangeType > func1, fct< fctRangeType > func2, Fret(*f)(mt), double romberg_precision=romberg_integration_precision)  
  
Romberg integration routine taken from numerical recipes in C++, the file qromb.c.`
- `mt constantOp (mt par)`
- `mt unityOp (mt par)`
- `mt absUnityOp (mt par)`
- `mt squareOp (mt par)`
- `FsOverTS calcFsOverTS (mt const inhStrength)`



- void [saveFsOverTS](#) (mt const inhStrength, [FsOverTS](#) const &F)
- unsigned [findClosest](#) (mt const &value, Col< mt > const &vec, mt &error)
- void [linAssign](#) (mt const start, mt const end, [FsOverTS](#) const &startF, [FsOverTS](#) &endF)
- template<typename fctRangeType >  
string [getFileExt](#) (vector< fct< fctRangeType > > var)  
*determine file extension from variable type*
- template<typename fctRangeType >  
string [getFileExt](#) (fct< fctRangeType > var)  
*determine file extension from variable type*
- template<typename matType >  
string [getFileExt](#) (Mat< matType > var)  
*determine file extension from variable type*
- template<typename type >  
string [getFileExt](#) (type var)  
*determine file extension from variable type*
- template<typename fctRangeType >  
vector< fct< fctRangeType > > [outputModifier](#) (vector< fct< fctRangeType > > var)  
*allows to modify file output independence on variable type*
- template<typename fctRangeType >  
fct< fctRangeType > [outputModifier](#) (fct< fctRangeType > var)  
*allows to modify file output independence on variable type*
- template<typename matType >  
Mat< matType > [outputModifier](#) (Mat< matType > var)  
*allows to modify file output independence on variable type*
- Mat< mt > [outputModifier](#) (Mat< complex< mt > > var)
- template<typename type >  
type [outputModifier](#) (type var)  
*allows to modify file output independence on variable type*
- int [main](#) (int argc, char \*\*argv)

## Variables

- string **dirName**
- [fileStdoutStream](#) fout
- class [physical\\_parameters](#) pp
- unsigned **kmax**
- ODE< [physical\\_parameters](#) > \* **D1** =NULL
- ODE< [physical\\_parameters](#) > \* **D2** =NULL
- mt **odeStepWidth**
- mt **propStart**
- mt **propEnd**
- fct< complex< mt > > **phiEndPoints**
- map< mt, mt > **calculatedValues**
- mt **lastk** =DBL\_MAX
- unsigned [statesPerBand0](#)
- unsigned [statesPerBand](#)
- struct [linAssignInfoType](#) **linAssignInfo**
- const char \* **argp\_program\_version**
- const char \* **argp\_program\_bug\_address**

### 5.1.1 Detailed Description

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#### Version

1.0

### 5.1.2 DESCRIPTION

Calculate Hubbard parameters in inhomogeneous lattices using generalized Wannier functions.

armadillo (linear algebra library) and gsl (gnu scientific library) need to be installed

comp.sh can be executed to compile the program, type `./comp.sh`

the program can be found in a.out, to execute type `./a.out`

the program will try to create a folder named output. If such a folder is already present the program will fail.

after the program finished execution the scripts 'plot.sh' and 'plotm.sh' can be used to plot the data in the output directory:

```
./plot.sh output/Heigenfunctions.gpf
./plotm.sh output/HinW0.gpm
```

(gnuplot needs to be installed for plotting)

### 5.1.3 Macro Definition Documentation

#### 5.1.3.1 #define outputWithHeader( x, header )

##### Value:

```
file.open( (dirName+string("/") + string(#x) + getFileExt(x)).c_str()); \
    file << header << endl << outputModifier(x) << endl; \
    file.close();
```

### 5.1.4 Function Documentation

#### 5.1.4.1 mt absUnityOp ( mt par )

needed as input for romberg integration procedure

#### 5.1.4.2 FsOverTS calcFsOverTS ( mt const inhStrength )

calculates measures used for the band assigning

#### 5.1.4.3 Mat<cx\_double> calculateEigenstatesBlockwise ( Mat< cx\_double > const symmetricMatrix, Col< mt > & eigenvals, unsigned statesPerBand )

Given a block-diagonal matrix this calculates the eigenvalues and eigenstates for each block individually

#### 5.1.4.4 Mat<cx\_double> calculateOverlapMatrix ( vector< fct< complex< double > > > const & Es )

calculates the overlap matrix of the argument functions using a real space integration

5.1.4.5 `mt constantOp ( mt par )`

needed as input for romberg integration procedure

5.1.4.6 `Mat<mt> createDiagonalMatrixFromVector ( Col< mt > const eigenvalues )`

Puts the elements of an input vector on the diagonal of an output matrix

5.1.4.7 `void dglSolve ( ODE< physical_parameters > *& D, unsigned eqncount, mt const xinit, mt *const & yinit )`

Interfacing with the differential equation solver.

5.1.4.8 `unsigned findClosest ( mt const & value, Col< mt > const & vec, mt & error )`

return the index of the element in *vec*, which is closest to *value*

5.1.4.9 `mt invPropagateFunction ( mt par )`

See Also

[propagateFunction](#) This is needed because 'gsl' only supplies a minimum finder. The minimum of this function is a maximum for [propagateFunction](#).

5.1.4.10 `mt invPropagateFunction ( mt par, void * )`

See Also

[invPropagateFunction](#)

5.1.4.11 `void linAssign ( mt const start, mt const end, FsOverTS const & startF, FsOverTS & endF )`

assign states to bands assuming a linear behaviour with respect to the inhomogeneity strength

5.1.4.12 `int main ( int argc, char ** argv )`

## THE USER INTERFACE

Here all the important parameters are set to determine the physical system. And to control the numerics.

5.1.4.13 `void ODE_derivs ( const double x, double * y, double * dydx, physical_parameters & pp )`

Setting derivatives for the differential equation solver. Given by the effective stationary Schroedinger equation

5.1.4.14 `void outputPropagatedWavefunctionEndValueOverE ( mt const Estart, mt const Eend, mt const step )`

This function outputs the results of the propagation procedure for different energies to a file

5.1.4.15 `mt propagateFunction ( mt par )`

Calls the differential equation solver with a certain energy '*par*' set and returns the value that needs to be zero for a valid eigenenergy state. This function is used by the root finding procedure.

#### 5.1.4.16 `mt propagateFunction ( mt par, void * )`

See Also

[propagateFunction](#)

#### 5.1.4.17 `template<typename fctRangeType , typename Fret > fctRangeType romberg_integral_f ( fct< fctRangeType > func1, Fret(*)(mt) f, double romberg_precision = romberg_integration_precision )`

Romberg integration routine taken from numerical recipes in C++, the file qromb.c.

initially declared as a static variable in trapez\_int\_refined - pass this ba reference

determines quality: if too low the method seems to sometime have thought that it has converged, where it hasn't

#### 5.1.4.18 `template<typename fctRangeType , typename Fret > fctRangeType romberg_integral_f ( fct< fctRangeType > func1, fct< fctRangeType > func2, Fret(*)(mt) f, double romberg_precision = romberg_integration_precision )`

Romberg integration routine taken from numerical recipes in C++, the file qromb.c.

initially declared as a static variable in trapez\_int\_refined - pass this ba reference

determines quality: if too low the method seems to sometime have thought that it has converged, where it hasn't

#### 5.1.4.19 `void saveFsOverTS ( mt const inhStrength, FsOverTS const & F )`

saves information into the linAssignInfo struct

#### 5.1.4.20 `mt squareOp ( mt par )`

needed as input for romberg integration procedure

#### 5.1.4.21 `template<typename fctRangeType , typename Fret > fctRangeType trapez_int_refined_f ( fct< fctRangeType > func1, Fret(*)(mt) f, fctDomainType x_lo, fctDomainType x_hi, int n, fctRangeType & s )`

the same integration procedure for a product of two functions

trapez integration from numerical recipes

#### 5.1.4.22 `template<typename fctRangeType , typename Fret > fctRangeType trapez_int_refined_f ( fct< fctRangeType > func1, fct< fctRangeType > func2, Fret(*)(mt) f, fctDomainType x_lo, fctDomainType x_hi, int n, fctRangeType & s )`

the same integration procedure for a product of two functions

trapez integration from numerical recipes

#### 5.1.4.23 `mt unityOp ( mt par )`

needed as input for romberg integration procedure

#### 5.1.4.24 `complex< mt > V ( mt x, physical_parameters & pp )`

The potential of inhomogeneous system, i.e. lattice + inhomogeneity

#### 5.1.4.25 `complex< mt > Vinh ( mt x )`

The potential of inhomogeneity only quasi disorder

#### 5.1.4.26 `mt Vlat ( mt x, physical_parameters & pp )`

The homogeneous system potential

### 5.1.5 Variable Documentation

#### 5.1.5.1 `const char* argp_program_bug_address`

**Initial value:**

```
=  
"<jonathanenders@gmx.de>"
```

#### 5.1.5.2 `const char* argp_program_version`

**Initial value:**

```
=  
"inWan 1.0"
```

#### 5.1.5.3 `fileStdoutStream fout`

**See Also**

[fileStdoutStream](#)

#### 5.1.5.4 `unsigned statesPerBand`

The amount of states in a inhomogeneous system band. Equals the amount of inhomogeneous system lattice sites.

#### 5.1.5.5 `unsigned statesPerBand0`

The amount of states in a homogeneous system band. Equals the amount of homogeneous system lattice sites.

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