

Cormen Exercises I.2.1

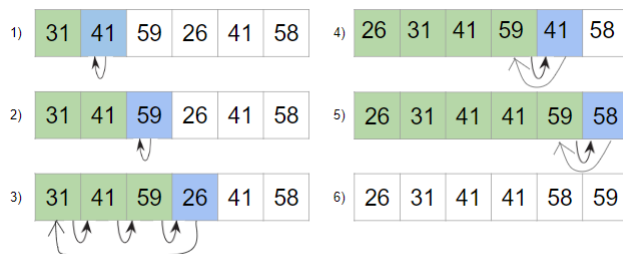
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Exercises

2.1-1

Using Figure 2.2 as a model, illustrate the operation of INSERTION-SORT on the array $A = \{31, 41, 59, 26, 41, 58\}$.



2.1-2

Rewrite the INSERTION-SORT procedure to sort into nonincreasing instead of nondecreasing order.

```
INSERTION-SORT(A)
1 for j = 2 to A.length
2   key = A[j]
3   i = j - 1
4   while i > 0 and A[i] > key
5     A[i + 1] = A[i]
6     i = i - 1
7   A[i + 1] = key
```

2.1-3

Consider the *searching problem*:

Input: A sequence of n numbers $A = \{a_1, a_2, \dots, a_n\}$ and a value v .

Output: An index i such that $v = A[i]$ or the special value NIL if v does not appear in A .

Write pseudocode for linear search, which scans through the sequence, looking for v . Using a loop invariant, prove that your algorithm is correct. Make sure that your loop invariant fulfills the three necessary properties.

Pseudocódigo
LinearSearch(A, v)
1 $i = \text{NIL}$
2 **for** $j = 1$ **to** $A.\text{length}$
3 **if** $A[j] = v$ **then**
4 $i = j$
5 **break**
6 **return** i

Tenemos como invariante que no existe un índice k menor a j tal que $A[k]=v$ por cada iteración en el loop. Si en un caso se llega a cumplir que $A[j] = v$ el ciclo retorna i y se cumple la invariante dado que j es mayor a k y no existe un índice k menor a j tal que $A[k]=v$. En caso contrario se realizan todas las comparaciones entre $A[j]$ con v se termina el loop y se retorna i que ha sido inicializado con NIL. La invariante se conserva, dado que en ningún punto existió un k menor a j tal que $A[k] = v$

2.1-4

Consider the problem of adding two n -bit binary integers, stored in two n -element arrays A and B . The sum of the two integers should be stored in binary form in an $(n+1)$ element array C . State the problem formally and write pseudocode for adding the two integers.

Pseudocódigo
Input: A, B arreglos de tamaño n
Output: C , un arreglo de tamaño $(n + 1)$ con la suma de A y B
addingBinary(A, B)
1 $C = [], \text{carry} = 0$
2 **for** $i = n$ **to** 1
3 $C[i+1] = (A[i] + B[i] + \text{carry}) \bmod 2$
4 **if** $(C[i+1] = (A[i] + B[i] + \text{carry}) \geq 2)$ **then**
5 $\text{carry} = 1$
6 **else**
7 $\text{carry} = 0$
8 $C[1] = \text{carry}$
9 **return** C