

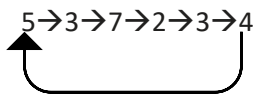
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- **WRITE your name and NetID on EVERY page.**
- **DO NOT REMOVE THE STAPLE IN YOUR EXAM.**
- **DO NOT BEGIN UNTIL INSTRUCTED TO DO SO.**
- WRITE NEATLY AND CLEARLY. If we cannot read your handwriting, you will not receive credit. Please plan your space usage. No additional paper will be given.
- This exam is worth 150 points.

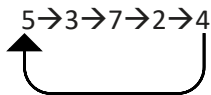
Problem 1 – Special Linked Structures (20 points)

Implement the following method to delete the last occurrence (starting from the front) of an item from a circular linked list, given a pointer rear to its last node. For example:

Input (rear points to 4):



Resulting list after deleting the last occurrence of 3 (rear points to 4):



```

public class CLLNode {
    public int    data;
    public CLLNode next;
}

public class CLL {
    public CLLNode rear; // point to last node in a CLL
    ...

    // Deletes LAST occurrence (from front) of given item from a CLL
    // Returns pointer to rear node of the updated CLL
    // Throws NoSuchElementException if item is not in the CLL

    public void deleteLastOccurrence ( int item )
    throws NoSuchElementException {
        // COMPLETE THIS METHOD
    }
}

```

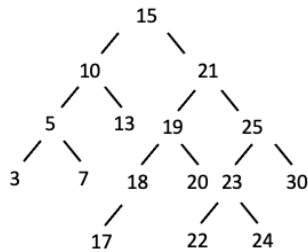
CS112 Data Structures - Midterm 2 - Spring 2022

Name: _____ NetID: _____

Name: _____ NetID: _____

Problem 2 – Binary Search Tree (30 points)

Implement the following method to return the inorder successor of a node.



On the BST tree to the left:

- the inorder successor of node 21 is node 22.
- the inorder successor of node 10 is 13.

```

// Node class
private class Node <K extends Comparable<K>, V> {
    K key;
    V value;
    Node left;
    Node right;
}

// Returns the inorder successor of node h
public Node successor (Node h) {
    // COMPLETE THIS METHOD
}
  
```

Name: _____ NetID: _____

Problem 3 – 2-3 trees and left-leaning red-black trees (40 points)

Construct a 2-3 tree and the corresponding left-leaning red-black tree whose keys are inserted in the following sequence. Label the links as R (red) or B (black), or use color in your answer.

3 5 21 8 15 11 26 9 2

(a) **(10 points)** Draw the 2-3 tree after the insertions of 3 5 21, and the corresponding left-leaning red-black tree.

(b) **(12 points)** Draw the 2-3 tree after the insertions of 3 5 21 8 15 11, and the corresponding left-leaning red-black tree.

Name: _____ NetID: _____

(c) **(14 points)** Draw the 2-3 tree after the insertion sequence completed, and the corresponding left-leaning red-black tree.

(d) **(4 points)** What is the minimum height of a 2–3 tree with n keys?

- A. $\sim \log_3 n$
- B. $\sim \log_2 n$
- C. $\sim 2 \log_2 n$
- D. $\sim n$

Name: _____ NetID: _____

Problem 4 - Priority Queue (30 points)

- (a) **(5 points)** Assume the array below will be used to hold the keys of a MAX priority queue. Based on the array contents shown below. Is this a valid binary heap? Justify your answer according to the properties of a valid binary heap.

	index											
	0	1	2	3	4	5	6	7	8	9	10	11
Key[]		100	19	36	2	3	25	1	17	7		

- (b) Below is an array representing a valid binary heap for a MAX priority queue.

	index															
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
key[]		60	53	3	49	46	1	2	48	16	25	40				

- (b.1) **(10 points)** Show the array contents after 2 insertions: first insert key 55 and then insert key 44.

	index															
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
key[]																

- (b.2) **(10 points)** After the above insert operations, assume 2 (two) delMax() operations were performed, show the contents of the array.

	index															
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
key[]																

Name: _____ NetID: _____

- (c) **(5 points)** Assume there are n keys in a binary heap for a MAX priority queue. If a `delMax()` operation is performed, how many compares in the worst case, in terms of n , to restore the heap-order property? Justify your answer.

Name: _____ NetID: _____

Problem 5 – Hash Table (30 points)

Assume the following keys 4371, 1323, 6173, 4199, 4344, 9679, 1989 are inserted in sequence to a hash table of size 10 where the hash function is $\text{hash}(\text{key}) = \text{key} \% 10$. For simplicity, we omit the “values” associated with the keys and assume that no rehashing happens.

(a) **(10 points)** Show the hash table if separate chaining is used (insert at front of a chain).

(b) **(10 points)** Show the hash table if linear probing is used.

Name: _____ NetID: _____

- (c) **(10 points)** Assuming the following code segment implements the delete() method as part of the Linear Probing API for (b) , show the hash table after deleting the key 4199 from the hash table in (b). The method contains (key) returns true if key is present in the hash table.

```

public void delete(Key key) {
    if (key == null) return;
    if (!contains(key)) return;
    int i = hash(key);
    while (!key.equals(keys[i])) {
        i = (i + 1) % m;
    }

    keys[i] = null;
    vals[i] = null;

    i = (i + 1) % m;
    while (keys[i] != null) {
        Key keyToRehash = keys[i];
        Value valToRehash = vals[i];
        keys[i] = null;
        vals[i] = null;
        n--;
        put(keyToRehash, valToRehash);
        i = (i + 1) % m;
    }
    n--;
}

```