

7-05-20

DAA - Revision

JOVIAL JOE
IESITCS016

Q.1) @ Discuss about the fractional and 0/1 knapsack problem.

A1) Knapsack Problem

~ It is an optimization problem when considered from an computer science perspective.

~ The problem goes like this:

"A hiker tries to pack the most valuable items without overloading the knapsack. Each item has a certain value/profit/benefit and weight.

An overall weight limitation gives the single constraint."

Fractional Knapsack

~ In this case, the item can be filled into the knapsack even if it had only a fraction of it would go into the knapsack.

~ Mainly, three approaches are used to solve this problem, one moving from highest profit to lowest.

- ~ Second, moving from least weight to maximum weight.
- ~ Finally from maximum profit/weight ratio to the lowest of the same.

0-1 Knapsack Problem

- ~ In this type of problem, ^{tricker is} ~~people are~~ ~~only~~ allowed to take items as a whole.
- ~ If an item ^{cannot} ~~can~~ be taken as a whole, it must be left behind.
- ~ Parts of items cannot be taken.

Q 1 (b) Calculate the knapsack solution, where $j = 3$, $m = 30$
weights are (10, 12, 15) and profits are (20, 28, 22)

Sol

Using 0-1 Knapsack Method

Given: $j = 3$

$m = 30$

weights = 10, 12, 15

profit = 20 28 22

$$\sum_{j=1}^3 P_i x_i = \text{net profit.}$$

($x_i = 0$ or 1)

(i) Selection of object with largest profit:

A (28, 12) B (20, 10)

selected	profit	remain-weight
A	28	18
B	22	3

$$\Rightarrow \text{Profit} = 28 \times 1 + 22 \times 1 = 50$$

(ii) Selection of object with smallest weight.

B (20, 10), A (28, 12), C (22, 15)

<u>Selected</u>	<u>Profit</u>	<u>Remaining weight</u>
A	20	20
A	28	8

$$\rightarrow \text{Profit} = 20 \times 1 + 28 \times 1 + 22 \times 0 = \underline{\underline{40}}$$

\therefore Use maximum profit method.

Q 1 C)

Greedy Method

- ~ Greedy algorithm makes whatever choice that seems best at the moment.
- ~ No guarantee of getting an optimal solution.
- ~ It is storage efficient
- ~ Generally faster - in the order of $\log n$.

eg- fractional knapsack (without ordering)

Dynamic Programming

- ~ Decision are made considering current and previous problem & solution to previously solved subproblem
- ~ Will produce an optimal solution for sure
- ~ Increases in space complexity.
- ~ Generally slower - in the order of n^2 .

eg:- 0/1 knapsack problem.

Using Fractional - knapsack

1.) Maximum Profit First

<u>Selected</u>	<u>Profit</u>	<u>Remaining</u>
A	28	18
B C	22	3
$\frac{3}{10} B$	$\frac{3}{10} \times 20$	0

$$\Rightarrow \text{Net profit} = 28 + 22 + 6 = 56.00$$

2.) Minimum Weight First

<u>Selected</u>	<u>Profit</u>	<u>Remaining</u>
B	20	20
A	28	18
$\frac{8}{15} C$	$\frac{8}{15} \times 22$	0

$$\text{Net profit} = 20 + 28 + \frac{8}{15} \times 22 = 59.73$$

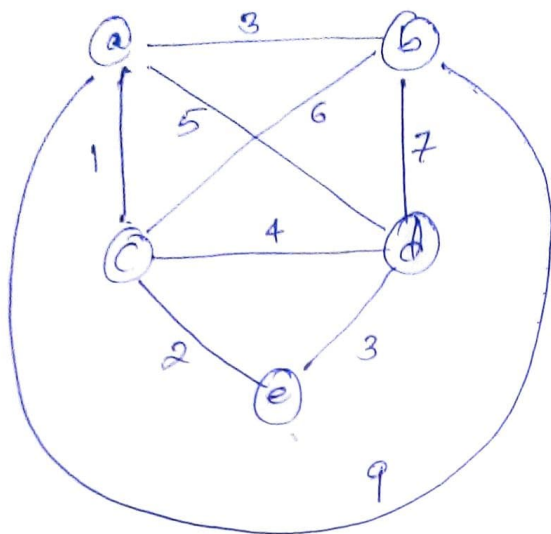
3.) Maximum profit/weight ratio first

$$A (P/w) = 2.33 \quad B (P/w) = 2.00 \quad C (P/w) = 1.466$$

<u>Selected</u>	<u>Profit</u>	<u>Remaining</u>
A	28	18
B	20	8
$\frac{8}{15} C$	$\frac{8}{15} \times 22$	0

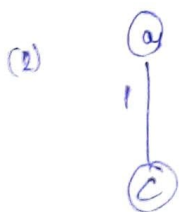
$$\text{Net profit} = 28 + 20 + \frac{8}{15} \times 22 = \underline{\underline{59.73}}$$

Q 2(a) Construct a minimum spanning tree for the below graph using Prim's algorithm.
(source node = a)

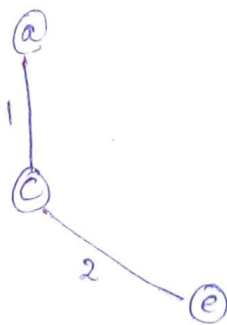


Using Prim's Algorithm

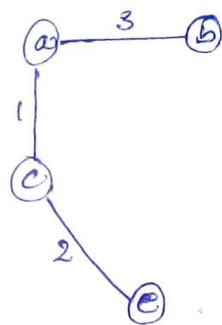
(1) a



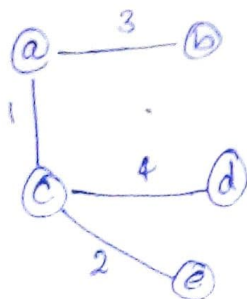
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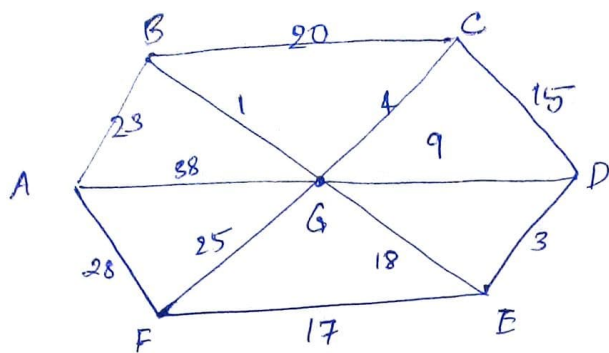
(4)



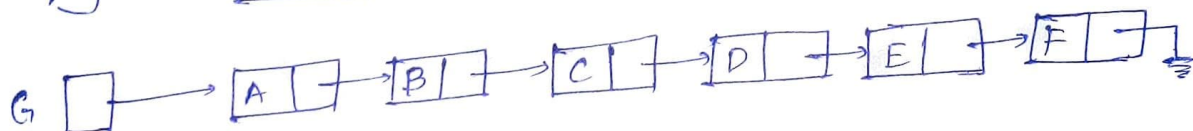
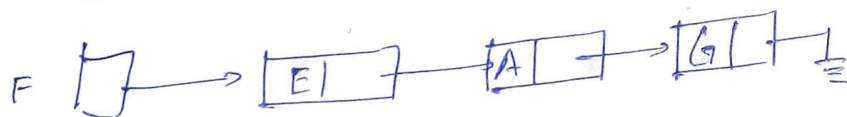
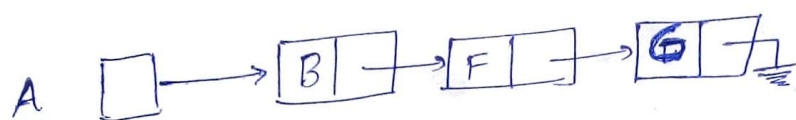
(5)



8 (b.)

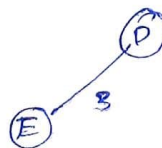
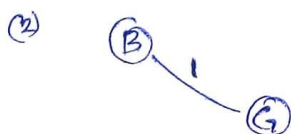


(i) A adjacency list representation of the graph.

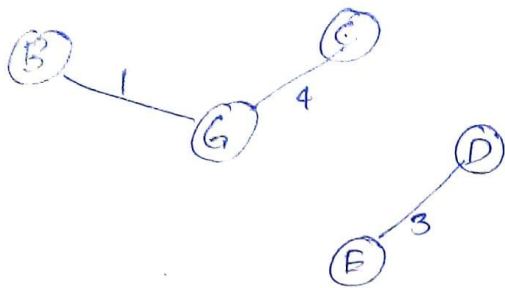


This is the adjacency ^{list} representation of the graph.

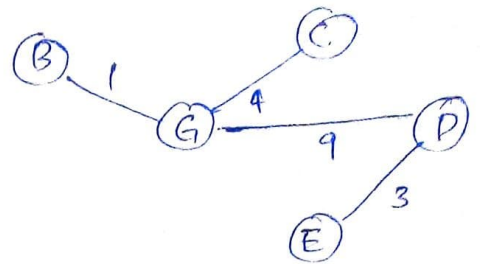
(ii) MST using Kruskal's algorithm



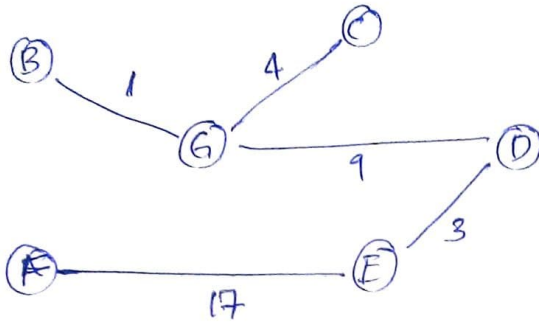
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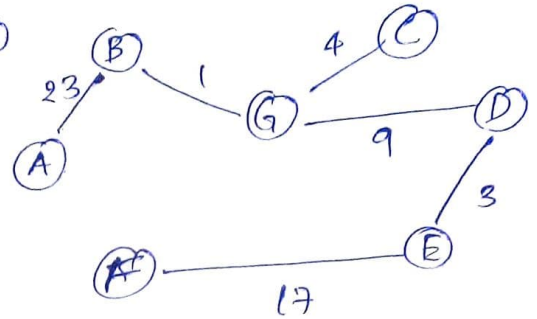
4



5



6



This is the required
MST.