

7.05.20

## DAA Revision - 2

Q.1.) Write Prim's Algorithm

Q.2.) Write Kruskal's Algorithm

Q.3.) Write the algorithm for fractional Knapsack's Problem.

A.1.) Prim's Algorithm for MST

Step 1: Obtain a graph  $G$  with  $V$  vertices and  $E$  edges with  $w_i$  weights for each edge  $e \in E$ .

Step 2: Select a random vertex  $u$ , next select an adjacent vertex  $v$  such that the weight for the edge  $e_{uv}$  between the vertices  $u$  &  $v$  is minimum.

Step 3: Consider another vertex  $x$ , such that  $x$  is adjacent either to  $u$  or to  $v$  but not to both, and the weight to  $x$  must be

~~Step 4~~ smallest among the available choices.

Step 4: Repeat step 2 & 3 keeping note that no loops are formed.

Step 5: Stop the iteration if all the vertices are ~~exet~~ exhausted.

## A2.) Kruskal's Algorithm

Step 1: Obtain the graph  $G$  with vertex set  $V$  and edge set  $E$ .

Step 2: Sort the edges according to their weights in the ascending order.

Step 3: Select the edge with minimum weight and create a new sub tree.

Step 4: Again select a new edge, this time 4 cases may occur.

(i) Both ~~vertices~~ of the selected edge may lie in an existing sub tree - discard the edge.

(ii) One of the vertex of the selected edge may lie in an existing sub tree - add edge ~~to~~ that sub tree

(iii) One edge may lie in one sub tree say  $T_1$  and other may lie in edge  $T_2$  - merge  $T_1$  &  $T_2$

(iv) No ~~vert~~ end vertices lie in any sub tree - create a new sub tree.

### A3.) KnapSack Algorithm (Greedy & Fractional)

Step 1: current knapsack load is set to zero  
 $\text{load} \leftarrow 0$ , and counter is initialized to 1.

Step 2: Repeat the following steps while the  
current load  $<$  Maximum load.

Step 3: if  $w_i + \text{load} \leq \text{Maxload}(W)$   
and  $i \leq \text{no. of items}$  goto step 4  
also goto step 5.

Step 4: take the whole of  $i^{\text{th}}$  item.

Step 5: Take only the possible fraction of  $i^{\text{th}}$  item.  
ie  $\text{load} += \frac{(W - \text{load})}{w_i}$   
 $\text{profit} += \frac{W - \text{load}}{w_i} \times \text{profit of } i^{\text{th}} \text{ item}$

Step 6: Increment counter  $i \leftarrow i + 1$

Step 7: Stop.