Force of the Fan Cart Summative

Joe Hollander

Nov 2024

Two settings, the second and third level, were used for all masses. Four masses were used: the fan cart by itself, with a 0.15 kg weight, with a 0.25 kg bars, and with the unknown mass. Position data was measured with a Vernier motion detector laying down on the track. The acceleration was measured for each mass and setting by fitting a quadratic equation (because the fan cart has a constant acceleration) to the position data and doubling the x^2 coefficient. Newton's second law states that $\mathbf{F} = m\mathbf{a}$, so each force was found by multiplying the calculated acceleration by the mass in kg (newtons are in kgs). The force for each setting was calculated for each weight, and the forces were averaged to reduce the effect of outliers. The final averaged force for each setting was then used to calculate the unknown given its acceleration. Rearranging Newton's second law to solve for mass: $m = \frac{\mathbf{F}}{\mathbf{a}}$. Since, the high setting's forces varied greatly, the average medium setting force was used to estimate the mass by dividing the average medium setting force by the acceleration. This mass was then subtracted from the original fan cart mass to find the calculated mass of the unknown object.

Fan cart number five was used, and its mass was 532.97 g. The following values are all accelerations in $\rm m/s^2$, formatted by mass, setting: trials.

532.97 g, Medium trials: 0.2438, 0.2450, 0.2488

532.97 g, High trials: 0.4284, 0.4522, 0.4550

682.97 g, Medium trials: 0.2040, 0.1970, 0.2010

682.97 g, High trials: 0.3280, 0.3416, 0.3312

782.97 g, Medium trials: 0.1812, 0.1806, 0.1839

782.97 g, High trials: 0.3280, 0.3416, 0.3312

Unknown mass, Medium trials: $0.1713,\,0.1777,\,0.1788$ Unknown mass, High trials: $0.3268,\,0.3130,\,0.3148$

The following table's entries are the averaged accelerations for each mass and setting.

	532.97 g	682.97 g	782.97 g	Unknown
				Mass
Medium	0.2459	0.2007	0.1819	0.1759
	$\mathrm{m/s^2}$	$\mathrm{m/s^2}$	m/s^2	m/s^2
High	0.4452	0.3336	0.2882	0.3182
	$\mathrm{m/s^2}$	$\mathrm{m/s^2}$	m/s^2	m/s^2

As an example, the force of the medium setting, using the 532.97 g acceleration, would be found by multiplying $0.2459~\mathrm{m/s^2}$ by $0.53297~\mathrm{kg}$ (531.86 g divided by 1000), which is $0.1311~\mathrm{N}$. The force values found for the medium setting were $0.1311~\mathrm{N}$, $0.1424~\mathrm{N}$, and $0.1371~\mathrm{N}$, while the force values found for the high setting were $0.2373~\mathrm{N}$, $0.2257~\mathrm{N}$, and $0.2278~\mathrm{N}$. The average of the high setting values is

 $\frac{0.2373 + 0.2257 + 0.2278}{3} = 0.2303N.$

Because the medium setting forces varied a lot more, the data was omitted, and the average medium setting force was used to predict the unknown mass. Therefore, the fan cart with the unknown mass was calculated to have a mass of

 $\frac{0.2303 \text{ N}}{0.3182 \text{ m/s}^2} = 0.7238 \text{ kg}.$

Subtracting this mass from the original fan cart mass of 0.53297 kg, the unknown mass was calculated to be 0.1918 kg, or 191.8 g.

The actual mass of the unknown object was 194.30 g, so the percent error is

$$\frac{194.30 - 191.8}{194.30} = 0.0129 = 1.29\%.$$

The percent error is very low. However, the error could be explained by differing friction between trials and outliers in the data. A future experiment would be done on a brand new track and with many more trials to reduce the effect of outliers.