- 1. Multiple regression analysis and multiple discriminant analysis are very similar techniques. Both involve plotting the independent variable against the dependent or group variable. They allow us to examine the effects of the independent variables on the dependent variable. More importantly, we are able to see the power or extent to which each independent variable has an effect on the dependent variable. However, there is one main difference between the two. For regression analysis, the dependent variable is metric, but for discriminant analysis the dependent variable is nonmetric -- it is categorical. Examples of this could include gender, age group, cities, job, color, etc... anything categorical. There is no specific limit for the number of categories, there just needs to be at least two. Thus, while regression analysis allows us to understand our data and predict specific values for the dependent variables, the discriminant equation allows us to understand the differences between groups and predict which group a certain sample will belong to.
- 2.
- a. X4 Region (nonmetric)
 - X6 Product Quality (metric)
 - X7 E-Commerce Activities/Website (metric)
 - X8 Technical Support (metric)
 - X9 Complaint Resolution (metric)
 - X10 Advertising (metric)
 - X11 Product Line (metric)
 - X12 Salesforce Image (metric)
 - X13 Competitive Pricing (metric)
 - X14 Warranty & Claims (metric)
 - X15 New Products (metric)
 - X16 Ordering & Billing (metric)
 - X17 Price Flexibility (metric)
 - X18 Delivery Speed (metric)
- b. 2 groups in X4
- c. Linear discriminant function:

Linear Discriminant Function for x4				
Variable	Label	0	1	
Constant		-191.92135	-194.33409	
x6	ж6	8.32797	7.65248	
x7	x7	4.20485	1.20101	
x8	х8	-2.06370	-2.09852	
x9	х9	-3.62428	-3.60295	
x10	x10	-1.62571	-2.03642	
x11	x11	58.68681	58.34999	
x12	x12	1.69711	4.70052	
x13	x13	3.64274	4.22872	
x14	x14	13.54926	13.38761	
x15	x15	0.00591	0.28730	
x16	x16	-2.84573	-2.25264	

Linear Discriminant Function for x4				
Variable Label 0 1				
x17	x17	62.42839	64.51335	
x18	x18	-101.40047	-103.57123	

Training data - 5 misclassified results: Obs 3, 22, 38, 60, 94 Probability of misclassification = .05

Testing data - 13 misclassified results: Obs 3, 5, 11, 21, 22, 24, 32, 38, 60, 74, 86, 90, 94

Probability of misclassification = .13

All other data attached below.

Total Sample Size	100	DF Total	99
Variables	13	DF Within Classes	98
Classes	2	DF Between Classes	1

Number of Observations Read	100
Number of Observations Used	100

	Class Level Information				
x4 Name Frequency Weight Proportion				Prior Probability	
0	0	39	39.0000	0.390000	0.390000
1	1	61	61.0000	0.610000	0.610000

Pooled Covariance Matrix Information		
Covariance Natural Log of the Determinant of the Matrix Rank Covariance Matrix		
13	-8.01842	

Squared Distance to x4			
From x4 0 1			
0	0	7.45466	
1	7.45466	0	

F Statistics, NDF=13, DDF=86 for Squared Distance to x4			
From x4 0 1			
0	0	11.97157	
1	11.97157	0	

Prob > Mahalanobis Distance for Squared Distance to x4			
From x4 0			
0	1.0000	<.0001	
1	<.0001	1.0000	

Generalized Squared Distance to x4			
From x4 0 1			
0	1.88322	8.44325	
1	9.33787	0.98859	

Linear Discriminant Function for x4			
Variable	Label	0	1
Constant		-191.92135	-194.33409
х6	х6	8.32797	7.65248
x7	x7	4.20485	1.20101
x8	х8	-2.06370	-2.09852
х9	x9	-3.62428	-3.60295
x10	x10	-1.62571	-2.03642
x11	x11	58.68681	58.34999
x12	x12	1.69711	4.70052
x13	x13	3.64274	4.22872
x14	x14	13.54926	13.38761
x15	x15	0.00591	0.28730
x16	x16	-2.84573	-2.25264

Linear Discriminant Function for x4				
Variable Label 0 1				
x17	x17	62.42839	64.51335	
x18	x18	-101.40047	-103.57123	

Posterior Probability of Membership in x4						
Obs	From x4		ssified nto x4	0	1	
1	1	1		0.0103	0.9897	
2	0	0		0.9989	0.0011	
3	1	0	*	0.8181	0.1819	
4	1	1		0.0566	0.9434	
5	0	0		0.8269	0.1731	
6	1	1		0.0123	0.9877	
7	1	1		0.0008	0.9992	
8	1	1		0.0004	0.9996	
9	1	1		0.0004	0.9996	
10	1	1		0.0298	0.9702	
11	0	0		0.7504	0.2496	
12	1	1		0.0050	0.9950	
13	0	0		0.9220	0.0780	
14	0	0		0.9990	0.0010	
15	1	1		0.0274	0.9726	
16	0	0		0.9980	0.0020	
17	1	1		0.0309	0.9691	
18	1	1		0.0072	0.9928	
19	1	1		0.0001	0.9999	
20	1	1		0.0009	0.9991	
21	1	1		0.0103	0.9897	
22	1	0	*	0.9920	0.0080	
23	0	0		0.9929	0.0071	
24	1	1		0.1817	0.8183	
25	1	1		0.0237	0.9763	
26	1	1		0.0003	0.9997	
27	0	0		0.9952	0.0048	
28	1	1		0.0171	0.9829	
29	0	0		0.9868	0.0132	
30	1	1		0.0130	0.9870	
31	0	0		0.9818	0.0182	
32	1	1		0.4376	0.5624	
33	1	1		0.0843	0.9157	
34	1	1		0.0059	0.9941	

Obs	From x4		ssified nto x4	0	1
35	1	1		0.0011	0.9989
36	0	0		0.9980	0.0020
37	0	0		0.9397	0.0603
38	1	0	*	0.8503	0.1497
39	1	1		0.0023	0.9977
40	1	1		0.0017	0.9983
41	1	1		0.0023	0.9977
42	0	0		0.6015	0.3985
43	0	0		0.8872	0.1128
44	1	1		0.0002	0.9998
45	0	0		0.9975	0.0025
46	1	1		0.0365	0.9635
47	0	0		0.9970	0.0030
48	1	1		0.0001	0.9999
49	1	1		0.1019	0.8981
50	0	0		0.8055	0.1945
51	1	1		0.1036	0.8964
52	0	0		0.9971	0.0029
53	1	1		0.1996	0.8004
54	0	0		0.9598	0.0402
55	1	1		0.0015	0.9985
56	0	0		0.6783	0.3217
57	1	1		0.0046	0.9954
58	0	0		0.7772	0.2228
59	0	0		0.9990	0.0010
60	1	0	*	0.7572	0.2428
61	0	0		0.9972	0.0028
62	1	1		0.0409	0.9591
63	0	0		0.5946	0.4054
64	1	1		0.4852	0.5148
65	1	1		0.3120	0.6880
66	1	1		0.0003	0.9997
67	1	1		0.0136	0.9864
68	1	1		0.0560	0.9440

Posterior Probability of Membership in x4						
Obs	From x4		ssified nto x4	0	1	
69	1	1		0.0143	0.9857	
70	1	1		0.0002	0.9998	
71	1	1		0.0014	0.9986	
72	0	0		0.9811	0.0189	
73	1	1		0.0165	0.9835	
74	1	1		0.4355	0.5645	
75	1	1		0.0249	0.9751	
76	0	0		0.8383	0.1617	
77	1	1		0.0149	0.9851	
78	0	0		0.8987	0.1013	
79	0	0		0.8987	0.1013	
80	1	1		0.0265	0.9735	
81	0	0		0.7325	0.2675	
82	0	0		0.8172	0.1828	
83	0	0		0.9498	0.0502	
84	1	1		0.0005	0.9995	
85	0	0		0.6598	0.3402	
86	1	1		0.0474	0.9526	
87	1	1		0.0020	0.9980	
88	0	0		0.5442	0.4558	
89	0	0		0.7779	0.2221	
90	1	1		0.0003	0.9997	
91	0	0		0.8146	0.1854	
92	1	1		0.1368	0.8632	
93	0	0		0.9986	0.0014	
94	1	0	*	0.8139	0.1861	
95	0	0		0.8117	0.1883	
96	0	0		0.8776	0.1224	
97	1	1		0.0062	0.9938	
98	0	0		0.9984	0.0016	
99	1	1		0.0112	0.9888	
100	1	1		0.0029	0.9971	

^{*} Misclassified observation

Classification Summary for Calibration Data: WORK.IMPORT Resubstitution Summary using Linear Discriminant Function

Number of Observations and Percent Classified into x4				
From x4	0	1	Total	
0	39 100.00	0.00	39 100.00	
1	5 8.20	56 91.80	61 100.00	
Total	44 44.00	56 56.00	100 100.00	
Priors	0.39	0.61		

Error Count Estimates for x4				
	0	1	Total	
Rate	0.0000	0.0820	0.0500	
Priors	0.3900	0.6100		

Posterior Probability of Membership in x4						
Obs	From x4		ssified nto x4	0	1	
3	1	0	*	0.9388	0.0612	
22	1	0	*	0.9999	0.0001	
24	1	0	*	0.6602	0.3398	
32	1	0	*	0.5773	0.4227	
38	1	0	*	0.9394	0.0606	
42	0	1	*	0.4490	0.5510	
60	1	0	*	0.9396	0.0604	
63	0	1	*	0.3361	0.6639	
64	1	0	*	0.6576	0.3424	
74	1	0	*	0.7029	0.2971	
81	0	1	*	0.4834	0.5166	
88	0	1	*	0.3170	0.6830	
94	1	0	*	0.9345	0.0655	

^{*} Misclassified observation

Classification Summary for Calibration Data: WORK.IMPORT Cross-validation Summary using Linear Discriminant Function

Number of Observations and Percent Classified into x4			
From x4	0	1	Total
0	35	4	39
	89.74	10.26	100.00
1	9	52	61
	14.75	85.25	100.00
Total	44	56	100
	44.00	56.00	100.00
Priors	0.39	0.61	

Error Count Estimates for x4			
	0	1	Total
Rate	0.1026	0.1475	0.1300
Priors	0.3900	0.6100	

Total Sample Size	100	DF Total	99
Variables	13	DF Within Classes	98
Classes	2	DF Between Classes	1

Number of Observations Read	100
Number of Observations Used	100

	Class Level Information				
х4	Variable Name	Frequency	Weight	Proportion	Prior Probability
0	0	39	39.0000	0.390000	0.390000
1	1	61	61.0000	0.610000	0.610000

Pooled Covariance Matrix Information		
Covariance Natural Log of th Determinant of th Matrix Rank Covariance Matri		
13	-8.01842	

Squared Distance to x4					
From x4	1				
0	0	7.45466			
1	7.45466	0			

F Statistics, NDF=13, DDF=86 for Squared Distance to x4					
From x4					
0	0 0				
1	11.97157	0			

Prob > Mahalanobis Distance for Squared Distance to x4					
From x4	0	1			
0	1.0000	<.0001			
1	<.0001	1.0000			

Generalized Squared Distance to x4						
From x4	1					
0	1.88322	8.44325				
1	9.33787	0.98859				

Linear Discriminant Function for x4							
Variable	Label	0	1				
Constant		-191.92135	-194.33409				
х6	х6	8.32797	7.65248				
x7	x7	4.20485	1.20101				
x8	х8	-2.06370	-2.09852				
х9	x9	-3.62428	-3.60295				
x10	x10	-1.62571	-2.03642				
x11	x11	58.68681	58.34999				
x12	x12	1.69711	4.70052				
x13	x13	3.64274	4.22872				
x14	x14	13.54926	13.38761				
x15	x15	0.00591	0.28730				
x16	x16	-2.84573	-2.25264				

Linear Discriminant Function for x4							
Variable	Label	0	1				
x17	x17	62.42839	64.51335				
x18	x18	-101.40047	-103.57123				

Posterior Probability of Membership in x4						
Obs	From x4	Classified into x4		0	1	
1	1	1		0.0103	0.9897	
2	0	0		0.9989	0.0011	
3	1	0	*	0.8181	0.1819	
4	1	1		0.0566	0.9434	
5	0	0		0.8269	0.1731	
6	1	1		0.0123	0.9877	
7	1	1		0.0008	0.9992	
8	1	1		0.0004	0.9996	
9	1	1		0.0004	0.9996	
10	1	1		0.0298	0.9702	
11	0	0		0.7504	0.2496	
12	1	1		0.0050	0.9950	
13	0	0		0.9220	0.0780	
14	0	0		0.9990	0.0010	
15	1	1		0.0274	0.9726	
16	0	0		0.9980	0.0020	
17	1	1		0.0309	0.9691	
18	1	1		0.0072	0.9928	
19	1	1		0.0001	0.9999	
20	1	1		0.0009	0.9991	
21	1	1		0.0103	0.9897	
22	1	0	*	0.9920	0.0080	
23	0	0		0.9929	0.0071	
24	1	1		0.1817	0.8183	
25	1	1		0.0237	0.9763	
26	1	1		0.0003	0.9997	
27	0	0		0.9952	0.0048	
28	1	1		0.0171	0.9829	
29	0	0		0.9868	0.0132	
30	1	1		0.0130	0.9870	
31	0	0		0.9818	0.0182	
32	1	1		0.4376	0.5624	
33	1	1		0.0843	0.9157	
34	1	1		0.0059	0.9941	

Posterior Probability of Membership in x4						
Obs	From x4		Classified into x4		1	
35	1	1		0.0011	0.9989	
36	0	0		0.9980	0.0020	
37	0	0		0.9397	0.0603	
38	1	0	*	0.8503	0.1497	
39	1	1		0.0023	0.9977	
40	1	1		0.0017	0.9983	
41	1	1		0.0023	0.9977	
42	0	0		0.6015	0.3985	
43	0	0		0.8872	0.1128	
44	1	1		0.0002	0.9998	
45	0	0		0.9975	0.0025	
46	1	1		0.0365	0.9635	
47	0	0		0.9970	0.0030	
48	1	1		0.0001	0.9999	
49	1	1		0.1019	0.8981	
50	0	0		0.8055	0.1945	
51	1	1		0.1036	0.8964	
52	0	0		0.9971	0.0029	
53	1	1		0.1996	0.8004	
54	0	0		0.9598	0.0402	
55	1	1		0.0015	0.9985	
56	0	0		0.6783	0.3217	
57	1	1		0.0046	0.9954	
58	0	0		0.7772	0.2228	
59	0	0		0.9990	0.0010	
60	1	0	*	0.7572	0.2428	
61	0	0		0.9972	0.0028	
62	1	1		0.0409	0.9591	
63	0	0		0.5946	0.4054	
64	1	1		0.4852	0.5148	
65	1	1		0.3120	0.6880	
66	1	1		0.0003	0.9997	
67	1	1		0.0136	0.9864	
68	1	1		0.0560	0.9440	

Posterior Probability of Membership in x4							
Obs	From x4		ssified nto x4	0	1		
69	1	1		0.0143	0.9857		
70	1	1		0.0002	0.9998		
71	1	1		0.0014	0.9986		
72	0	0		0.9811	0.0189		
73	1	1		0.0165	0.9835		
74	1	1		0.4355	0.5645		
75	1	1		0.0249	0.9751		
76	0	0		0.8383	0.1617		
77	1	1		0.0149	0.9851		
78	0	0		0.8987	0.1013		
79	0	0		0.8987	0.1013		
80	1	1		0.0265	0.9735		
81	0	0		0.7325	0.2675		
82	0	0		0.8172	0.1828		
83	0	0		0.9498	0.0502		
84	1	1		0.0005	0.9995		
85	0	0		0.6598	0.3402		
86	1	1		0.0474	0.9526		
87	1	1		0.0020	0.9980		
88	0	0		0.5442	0.4558		
89	0	0		0.7779	0.2221		
90	1	1		0.0003	0.9997		
91	0	0		0.8146	0.1854		
92	1	1		0.1368	0.8632		
93	0	0		0.9986	0.0014		
94	1	0	*	0.8139	0.1861		
95	0	0		0.8117	0.1883		
96	0	0		0.8776	0.1224		
97	1	1		0.0062	0.9938		
98	0	0		0.9984	0.0016		
99	1	1		0.0112	0.9888		
100	1	1		0.0029	0.9971		

^{*} Misclassified observation

Classification Summary for Calibration Data: WORK.IMPORT Resubstitution Summary using Linear Discriminant Function

Number of Observations and Percent Classified into x4							
From x4	0	1	Total				
0	39 100.00	0.00	39 100.00				
1	5 8.20	56 91.80	61 100.00				
Total	44 44.00	56 56.00	100 100.00				
Priors	0.39	0.61					

Error Count Estimates for x4								
	0 1 Total							
Rate	0.0000	0.0820	0.0500					
Priors	0.3900	Priors 0.3900 0.6100						

Posterior Probability of Membership in x4					
Obs	From x4	Classified into x4		0	1
3	1	0	*	0.9388	0.0612
22	1	0	*	0.9999	0.0001
24	1	0	*	0.6602	0.3398
32	1	0	*	0.5773	0.4227
38	1	0	*	0.9394	0.0606
42	0	1	*	0.4490	0.5510
60	1	0	*	0.9396	0.0604
63	0	1	*	0.3361	0.6639
64	1	0	*	0.6576	0.3424
74	1	0	*	0.7029	0.2971
81	0	1	*	0.4834	0.5166
88	0	1	*	0.3170	0.6830
94	1	0	*	0.9345	0.0655

^{*} Misclassified observation

Classification Summary for Calibration Data: WORK.IMPORT Cross-validation Summary using Linear Discriminant Function

Number of Observations and Percent Classified into x4				
From x4	0	1	Total	
0	35	4	39	
	89.74	10.26	100.00	
1	9	52	61	
	14.75	85.25	100.00	
Total	44	56	100	
	44.00	56.00	100.00	
Priors	0.39	0.61		

Error Count Estimates for x4					
	0 1 Total				
Rate	0.1026	0.1475	0.1300		
Priors	0.3900	0.6100			

Classification Results for Test Data: WORK.IMPORT1 Classification Results using Linear Discriminant Function

Posterior Probability of Membership in x4					
Obs	From x4	Classified into x4		0	1
1	1	1		0.0102	0.9898
2	0	0		0.9990	0.0010
3	1	0	*	0.8181	0.1819
4	1	1		0.0566	0.9434
5	0	1	*	0.4568	0.5432
6	1	1		0.0116	0.9884
7	1	1		0.0006	0.9994
8	1	1		0.0005	0.9995
9	1	1		0.0006	0.9994
10	1	1		0.0313	0.9687
11	0	1	*	0.3942	0.6058
12	1	1		0.0050	0.9950
13	0	0		0.9268	0.0732
14	0	0		0.9991	0.0009
15	1	1		0.0274	0.9726
16	0	0		0.9996	0.0004
17	1	1		0.2404	0.7596
18	1	1		0.0271	0.9729
19	1	1		0.0014	0.9986
20	1	1		0.0118	0.9882
21	1	0	*	0.6756	0.3244
22	1	0	*	0.9986	0.0014
23	0	0		0.9995	0.0005
24	1	0	*	0.5897	0.4103
25	1	1		0.4453	0.5547
26	1	1		0.0049	0.9951
27	0	0		0.9991	0.0009
28	1	1		0.3116	0.6884
29	0	0		0.9976	0.0024
30	1	1		0.3453	0.6547
31	0	0		0.9995	0.0005
32	1	0	*	0.9750	0.0250
33	1	1		0.0588	0.9412
34	1	1		0.0078	0.9922

Classification Results for Test Data: WORK.IMPORT1 Classification Results using Linear Discriminant Function

Obs	From x4		ssified nto x4	0	1
35	1	1		0.0004	0.9996
36	0	0		0.9961	0.0039
37	0	0		0.9229	0.0771
38	1	0	*	0.9082	0.0918
39	1	1		0.0035	0.9965
40	1	1		0.0023	0.9977
41	1	1		0.0023	0.9977
42	0	0		0.6015	0.3985
43	0	0		0.8872	0.1128
44	1	1		0.0002	0.9998
45	0	0		0.9975	0.0025
46	1	1		0.0365	0.9635
47	0	0		0.9970	0.0030
48	1	1		0.0001	0.9999
49	1	1		0.1019	0.8981
50	0	0		0.8055	0.1945
51	1	1		0.1036	0.8964
52	0	0		0.9971	0.0029
53	1	1		0.1996	0.8004
54	0	0		0.9598	0.0402
55	1	1		0.0015	0.9985
56	0	0		0.6783	0.3217
57	1	1		0.0046	0.9954
58	0	0		0.7772	0.2228
59	0	0		0.9990	0.0010
60	1	0	*	0.7572	0.2428
61	0	0		0.9972	0.0028
62	1	1		0.0409	0.9591
63	0	0		0.5946	0.4054
64	1	1		0.4852	0.5148
65	1	1		0.3120	0.6880
66	1	1		0.0003	0.9997
67	1	1		0.0136	0.9864
68	1	1		0.0560	0.9440

Classification Results for Test Data: WORK.IMPORT1 Classification Results using Linear Discriminant Function

Posterior Probability of Membership in x4					
Obs	From x4	Classified into x4		0	1
69	1	1		0.0926	0.9074
70	1	1		0.0005	0.9995
71	1	1		0.2064	0.7936
72	0	0		0.9845	0.0155
73	1	1		0.0670	0.9330
74	1	0	*	0.9919	0.0081
75	1	1		0.3673	0.6327
76	0	0		0.8883	0.1117
77	1	1		0.0251	0.9749
78	0	0		0.5896	0.4104
79	0	0		0.8533	0.1467
80	1	1		0.0196	0.9804
81	0	0		0.9848	0.0152
82	0	0		0.9482	0.0518
83	0	0		0.9282	0.0718
84	1	1		0.0029	0.9971
85	0	0		0.9156	0.0844
86	1	0	*	0.8741	0.1259
87	1	1		0.2922	0.7078
88	0	0		0.8636	0.1364
89	0	0		0.9432	0.0568
90	1	0	*	0.7074	0.2926
91	0	0		0.6306	0.3694
92	1	1		0.1920	0.8080
93	0	0		0.9986	0.0014
94	1	0	*	0.8139	0.1861
95	0	0		0.8620	0.1380
96	0	0		0.9224	0.0776
97	1	1		0.0175	0.9825
98	0	0		0.9990	0.0010
99	1	1		0.0233	0.9767
100	1	1		0.0029	0.9971

^{*} Misclassified observation

Classification Summary for Test Data: WORK.IMPORT1 Classification Summary using Linear Discriminant Function

Observation Profile for Test Data		
Number of Observations Read	100	
Number of Observations Used	100	

Number of Observations and Percent Classified into x4					
From x4 0 1 Tot					
0	37	2	39		
	94.87	5.13	100.00		
1	11	50	61		
	18.03	81.97	100.00		
Total	48	52	100		
	48.00	52.00	100.00		
Priors	0.39	0.61			

Error Count Estimates for x4					
	0 1 Total				
Rate	0.0513	0.1803	0.1300		
Priors	0.3900	0.6100			