# Precedence Climbing Parsing based on Binding Powers and Token Insertion

#### 1. Introduction

The repository contains several demo implementations of expression parsers based on binding powers, precedence climbing and insertion of fake operands.

Very few lines of Python code are enough for the core of a parser that creates parse trees from operands and operators (prefix, infix, postfix) with virtually arbitrary binding powers. The parsing algorithms are iterative, recursive, or mixed (based on loops and recursion).

The expressions to be parsed can consist of atomic operands, binary infix operators, unary prefix and unary postfix operators. In the following example, & is a prefix operator, ! is a postfix operator, and >, \*, \* are infix operators:

(1) & a > 7 \* b ! + 2

#### 1.1 Basics of expression parsing

### 1.1.1 Binding powers

An infix operator has a *left* and a *right binding power* (*lbp* and *rbp*). Initially, prefix operators have only an *rbp*, and postfix operators have only an *lbp*. Binding are numbers (often integers); they indicate the strength of binding in the corresponding direction. Frequently, *lbp* and *rbp* of a specific operator are equal or differ only by one. They can, however, differ by any number, as long as they are in an allowed range (here: 6 to 99). Binding powers of unary operators can be smaller than the binding powers of infix operators in the same expression.

Parsing based on binding powers can be more powerful than the usual approach based on *precedence* and *associativity*. Precedence and associativity can be expressed by equivalent definitions of binding powers, but not always vice versa.

An infix operator will be right associative if its rbp is less than its lbp.

## 1.1.2 Unary operators, token insertion

The left operand \$PRE is inserted before a prefix operator, and the right operand \$POST is inserted after a postfix operator. Furthermore, prefix operators are assigned a fake left binding power of 100, and postfix operators are assigned a fake right binding power of 100. This procedure virtually converts the unary operators to infix operators. The result is an alternating sequence of operands and infix operators, starting and ending with an operand.

In addition, a special \$BEGIN token is placed at the beginning, and an \$END token is placed at the end of the token sequence. \$BEGIN and \$END can act as a kind of *operators* in the process of parsing. A negative rbp is assigned to \$BEGIN and a negative lbp to \$END.

Insertion of tokens is done during the tokenization, i.e., by the *tokenizer*. The complete token sequence generated by the tokenizer for the example (1) is

(2) \$BEGIN \$PRE & a > 7 \* b ! \$POST + 2 \$END

#### 1.1.3 Results of parsing. Parse trees

The parsers return nested lists that represent parse trees. These lists can be formatted as Lisp-like S-expressions. E.g., parsing 5 + 3 ! \* 4 will create the list [+, 5, [\*, [!, 3, \$POST], 4]], or (+ 5 (\* (! 3 \$POST) 4)) as S-expression. Without the fake operand POST this is (+ 5 (\* (! 3) 4)).

#### 1.2 The main goals of the project. Limitations

- 1. Find and compare demo implementations of precedence climbing algorithms based on binding powers. Encourage experimentation.
- 2. Use insertion of fake operands to facilitate parsing of unary operators.
- 3. Separate definition of parsing rules from the implementation of the parsers.
- 4. Better understand the meaning of precedence correct parsing.

Exploring the full potential of precedence climbing parsing based on binding powers and token insertion is not the goal of this project.

The software does not contain evaluators of the parsed expressions.

### 2. Prerequisites

The Python interpreter (Python 3.8 or higher) is enough for the actual parsers. The bash shell is required for a test script.

## 3. Overview on the parsers

There are ten parsers, in separate modules. Nine of them, which shall be called *basic parsers* here, share the same high-level interface:

pcp\_ir\_0 and pcp\_ir\_0\_no\_ins are *iterative* and *recursive*. Contrary to the general setting, the latter it is not based on token insertion. Instead, special code takes care of prefix and postfix operators.

pcp\_it\_0\_1w, pcp\_it\_0\_1wg and pcp\_it\_0\_2w implement iterative algorithms.

pcp\_rec\_0\_0, pcp\_rec\_0\_1, pcp\_rec\_0\_2 and pcp\_rec\_03 are recursive (without loops) and more or less *functional* (in the sense of functional programming).

All these parsers accept the same operator definitions.

Analysis of the code and test results support this claim:

All basic parsers accept the same set of expressions and create identical results with identical input, provided they use identical operator and binding power definitions. In the parse process, they create subexpressions in the same order.

This should also justify the use of the generic term precedence climbing.

The remaining parser, direct\_pcp\_ir\_0, uses the algorithm of pcp\_ir\_0 to parse some 'hard coded' examples. It is 'self-contained' (no imports).

The software is contained in ten parser modules, the modules helpers.py and bintree.py, the JSON file binding\_powers.json (syntax), the shell script run\_tests.sh and the file basic\_tests.txt (test data for the shell script).

## 4. Usage of the parsers

Put all project files in one directory, or clone the repo. Note that there is only minimal error handling. Run the parsers from the command line.

The parser direct\_pcp\_ir\_0.py is simply run by

```
python direct_pcp_ir_0.py
```

The rest of this section refers to the nine basic parsers.

The syntax definition is loaded from the file binding\_powers.json unless one of the options -r, -d is specified. See below. Edit the definition if desired.

A basic parser can be run by

```
python PARSER_MODULE 'CODE'
```

where PARSER\_MODULE is one of the basic parser modules. Example:

```
python pcp_rec_0_0.py '3 + 5 ! * 6 ^ 2'
```

Use python3 instead of python if required. Enclose the code in single quotes or (on Windows?) double quotes. Tokens are separated by whitespace, or by transition from an alphanumeric to a special character or vice versa. In this regard, \_, (, ), ; are considered alphanumeric. A minus sign that is followed by a digit is also considered alphanumeric.

This command will parse the code by the specified parser and generate detailed output – among others, a two-dimensional representation of the parse tree and indications of *correctness* of the parsing. This is to facilitate experimentation.

The call syntax ./PARSER\_MODULE 'CODE' may work, depending on the operating system and the shell. Set the *executable* flag of the parser module. An example:

```
./pcp_it_0_1w.py'3 + 5! * 6^2'
```

The output can be made more verbose or more concise. Use the option -h (with any basic parser module) to find out all ways to run the parsers:

```
python pcp_ir_0.py -h
```

The bash shell script run\_tests.sh reads and parses test codes from the file basic\_tests.txt by the nine basic parsers. It should work on systems that support bash scripts. Run the script without arguments: ./run tests.sh

## 4.1 Randomly generated expressions (option -r)

The command

```
python PARSER_MODULE -r [nop [nbp [lexpr]]]
```

will parse a generated expression containing *lexpr* infix operators which are taken randomly from a collection of up to *nop* operators. The *lbp* and *rbp* values of the operators are taken randomly and independently, from the range 6 ... 6+nbp-1. Non-specified values default to 6. An example:

Results of calls with option -r are not reproducible.

## 4.2 Expressions with explicitly specified binding powers (option -d)

The command

```
python PARSER_MODULE -d lbp1 rbp1, lbp2 rbp2, ..., lbpn rbpn
```

will parse an expression with operators (lbp1;rbp1) to (lbpn;rbpn) and operands AO, ..., An, where lbpk, rbpk are the binding powers of the k-th operator. All binding powers should be in range 6 ... 99. An example:

will create and parse the expression

Unary operators can also be included. Use the help option (-h) for details.

#### 5. License

The project is licensed under the terms of the MIT License. See LICENSE.

## 6. Acknowledgements

This project was inspired by works of *Theodore Norvell*, *Aleksey Kladov* (matklad), *Andy Chu*, *Eli Bendersky*, *Jean-Marc Bourguet*, *Fredrik Lundh* (effbot), *Bob Nystrom* and others.

The correctness test and the definitions of operator ranges (see the functions \_is\_prec\_correct, \_lrange, \_rrange in the module helpers.py) are adapted from definitions by Annika Aasa in Precedences in Specifications and Implementations of Programming Languages (1995).

#### 7. More information

See the Detailed Guide in this repo.