

Attempt History

	Attempt	Time	Score
LATEST	Attempt 1	117 minutes	82 out of 100

Score for this quiz: **82** out of 100

Submitted Feb 18 at 7:01am

This attempt took 117 minutes.

Question 1

3 / 3 pts

There are 6 random people in a room. What is the probability that none of them share the same birthday? (Assume 365 days are equally likely.)

☐ 0.901

☐ 0.943

☒ 0.960

☐ 0.973

☐ 0.989

Correct!

Question 2

3 / 3 pts

Consider a family that has 4 children. Assume that $\Pr(\text{kid is a boy}) = \Pr(\text{kid is a girl}) = 1/2$, and that the genders of the 4 kids are independent. What is the probability that all 4 kids are boys given that we know at least 3 of them are boys?

☐ 1/16☐ 1/8

Correct!

☒ 1/5☐ 1/4☐ 1/2

Question 3

3 / 3 pts

TRUE or FALSE? Randomly select one card from a standard deck of 52 cards. Suppose we define the event A to be that the selected card is a Diamond, and the event B is that the selected card is a Spade. Then A and B are independent.

Note: A standard deck of playing cards contains a total of 52 cards of 4 types: 13 each of Spades, Clubs, Hearts, and Diamonds.

☐ True

Correct!

☒ False

Question 4

3 / 3 pts

TRUE or FALSE? The function $F(x) = 1 - (1/5)e^{-x/5}$ for $x \geq 0$ is a valid c.d.f.

☐ True

Correct!

☒ False

Question 5

3 / 3 pts

If the random variable X has p.d.f. $f(x) = 2(1 - x)$, for $0 \leq x \leq 1$, what is the distribution of the slightly nasty random variable $2X - X^2$?

☐ Triangular☐ Gamma☐ Exponential☐ Normal

Correct!

☒ Uniform

Question 6

3 / 3 pts

Consider the discrete random variable X such that

$$P(X = x) = \begin{cases} 0.5, & \text{if } x = -2 \\ 0.2, & \text{if } x = 0.2 \\ 0.3, & \text{if } x = 7 \\ 0, & \text{otherwise} \end{cases}$$

Use the discrete version of the Inverse Transform method from class and the $\text{Unif}(0, 1)$ pseudo-random number $U = 0.99$ to generate one observation X coming from this p.m.f.

☐ $X = -2$

☐ $X = 0.2$

☐ $X = 3$

☒ $X = 7$

Correct!

Question 7

3 / 3 pts

Suppose that U and V are i.i.d. $\text{Unif}(0, 1)$ random variables. How would you simulate the sum of two 6-sided dice tosses?

- ☐ (a) $12U$
- ☐ (b) $\lceil 12U \rceil$
- ☐ (c) $\lceil 12V \rceil$
- ☒ (d) $\lceil 6U \rceil + \lceil 6V \rceil$
- ☐ (e) Both (b) and (c)
- ☐ (f) None of the above

Correct!

Question 8

3 / 3 pts

Suppose that $X \sim \text{Bern}(0.2)$. What is $\text{Var}[X^{3.5}]$?

- ☐ 0.2
- ☐ $(0.2)^{3.5}$
- ☐ 5
- ☐ $5^{3.5}$
- ☒ $(0.2)(0.8)$

Correct!

Question 9

3 / 3 pts

TRUE or FALSE? Let X denote the number of tails from two fair coin tosses. Then the probability mass function for $Y = X^2 - 1$ is

$$P(Y = y) = \begin{cases} 1/4, & \text{if } y = -1 \\ 1/2, & \text{if } y = 0 \\ 1/4, & \text{if } y = 3 \end{cases}$$

Correct!

☒ True☐ False

Question 10

3 / 3 pts

YES or NO? Suppose X and Y are random variables that have joint p.d.f.

$$f(x, y) = cx^2 \ln(1 + y) \quad \text{for } 0 \leq x \leq 1 \text{ and } 0 \leq y \leq 1,$$

where c is the constant that makes this integrate to 1. Are X and Y independent?

Correct!

☒ YES☐ NO

Question 11

0 / 3 pts

Suppose X and Y are two random variables for which the joint probability density function is given by

$$f(x, y) = 6e^{-x-2y} \quad \text{for } 0 < x < y < \infty$$

What is the probability that $2Y > X$?

☐ 0☐ 0.324

You Answered

☒ 0.623☐ 0.915

Correct Answer

☐ 1

Question 12

3 / 3 pts

Suppose that X is a random variable with a mean of 6 and variance of 8; Y is a random variable with a mean of -10 and variance of 18; and $\text{Cov}(X, Y) = -8$. Find $\text{Corr}(X, Y)$.

Correct!

☐ $-1/3$

☐ $-1/2$

☒ $-2/3$

☐ $-3/4$

☐ $-4/5$

Question 13

3 / 3 pts

Given an exponential random variable $X \sim \text{Exp}(\lambda = 1/180)$, what is the conditional probability $P(X > 100 | X > 40)$?

Correct!

☒ $e^{-1/3}$

☐ $e^{-2/9}$

☐ $e^{-1/9}$

☐ $e^{-1/18}$

☐ $1 - e^{-2/9}$

Question 14

3 / 3 pts

On a particular river, floods occur once every year on average. If the number of floods follows a Poisson distribution, calculate the probability of exactly 3 floods during a particular two-year period.

☐ 0.003☐ 0.015☐ 0.061

Correct!

☒ 0.180☐ 0.368

Question 15

3 / 3 pts

If X_1, X_2, \dots, X_{100} are i.i.d. $\text{Nor}(300, 500)$, then what is the distribution of the sample mean \bar{X} ?

☐ $\text{Nor}(3, 0.05)$ ☐ $\text{Nor}(3, 5)$ ☐ $\text{Nor}(3, 500)$ ☐ $\text{Nor}(300, 0.05)$

Correct!

☒ $\text{Nor}(300, 5)$

Question 16

3 / 3 pts

Suppose X_1, \dots, X_{100} are i.i.d. from an $\text{Exp}(1)$ distribution. If we use the Central Limit Theorem approximation, what is

$$P\left(\sum_{i=1}^{100} X_i < 97\right)?$$

☐ 0.242☒ 0.382☐ 0.421☐ 0.460☐ 0.618

Correct!

Question 17**3 / 3 pts**

Suppose you approximating the solution of a simple differential equation involving the function $f(x)$, and you appeal to the relation

$f(x + h) \doteq f(x) + hf'(x)$, where h is some "small" number.

What is this method called?

☐ Inverse Transform

☐ LOTUS

☐ Newton's Method

☐ Bisection Method

Correct!

☒ Euler's Method

Question 18**3 / 3 pts**

Consider a circle inscribed in a unit square (so that the circle has area $\pi/4$). We toss 1000 darts randomly into the square, and it turns out that 784 of those darts land in the circle. Using the method described in class, estimate π .

Correct!☒ 3.136☐ 3.156☐ 3.208☐ 3.422☐ 3.568

Question 19

3 / 3 pts

Suppose we use Monte Carlo integration to approximate $I = \int_2^5 \ln(2x - 4) dx$. If U_1, U_2, \dots, U_n are i.i.d. $\text{Unif}(0, 1)$ random numbers, which of the following is a good approximation \bar{I}_n for I ?

Correct!

☐ $\frac{1}{n} \sum_{i=1}^n \ln(6U_i)$

☒ $\frac{3}{n} \sum_{i=1}^n \ln(6U_i)$

☐ $\frac{1}{n} \sum_{i=1}^n \ln(6U_i - 4)$

☐ $\frac{3}{n} \sum_{i=1}^n \ln(6U_i - 4)$

☐ $\frac{6}{n} \sum_{i=1}^n \ln(6U_i - 2)$

Question 20

3 / 3 pts

Consider the following event list for a FIFO single-server queue, where i is the customer's sequence number, A_i is the i th customer's arrival time, T_i is the customer's service start time, and S_i is the customer's service time.

i	A_i	T_i	S_i
1	2	2	6
2	7	8	4
3	10	12	7
4	15	19	3
5	21	22	2

Event list for FIFO

What is the average time in system (service + waiting time) for all 5 customers?

☐ 1.6☐ 2.4☐ 3.4☐ 4.6☒ 6.0

Correct!

Question 21

0 / 3 pts

Consider the same FIFO single-server queue event list as in the previous question (table repeated below). What is the maximum number of customers in the system (queue + in-service) at any point in time?

i	A_i	T_i	S_i
1	2	2	6
2	7	8	4
3	10	12	7
4	15	19	3
5	21	22	2

Event list for FIFO

You Answered

☒ 1

Correct Answer

☐ 2

☐ 3

☐ 4

☐ 5

Question 22

3 / 3 pts

Consider once again the FIFO single-server queue event list (table below). If the queue had instead been a LIFO queue, then which of the following statements would be TRUE?

i	A_i	T_i	S_i
1	2	2	6
2	7	8	4
3	10	12	7
4	15	19	3
5	21	22	2

Event list for FIFO

- ☐ The arrival times A_1, A_2, \dots, A_5 would be different.
- ☐ Customer 4 would have been the last to be serviced.
- ☐ The average of the service times S_1, S_2, \dots, S_5 would be changed.
- ☐ Customer 5 would have been the first to leave the system.
- ☒ None of the above.

Correct!

Question 23

0 / 3 pts

TRUE or FALSE? As crazy as it sounds, the $\text{Unif}(0, 1)$ random numbers generated on a computer are actually deterministic!

Correct Answer

☐ True

You Answered

☒ False

Question 24

3 / 3 pts

If x and y are two consecutive event times in a discrete-event simulation model, what can happen during the time interval $x < t < y$?

- ☐ An arrival can occur.
- ☐ A departure can occur.
- ☐ A machine breakdown can occur.
- ☐ The simulation can end.
- ☐ We can insert an event into the Future Events List (FEL).
- ☒ Nothing can happen.

Correct!

Question 25**3 / 3 pts**

In the course of a simulation study, we should stop to ask, "Does our simulation model correctly mimic the real-world system under study?" What step of the simulation study process is this?

- ☐ Problem Formulation
- ☐ Data Collection
- ☐ Verification
- ☒ Validation
- ☐ Output Analysis

Correct!**Question 26****0 / 3 pts**

TRUE or FALSE? A fixed-increment simulation clock is well-suited for simulations that model continuous-time systems such as the movement of an approaching weather system.

Correct Answer

- ☐ True

You Answered

- ☒ False

Question 27

0 / 3 pts

Which of the following statements about the future events list (FEL) is TRUE?

- ☐ The order of events in the FEL can never change.
- ☐ Events can be deleted from the FEL, but not inserted.
- ☐ Most of the programming effort when using a commercial simulation package is spent directly managing the FEL.
- ☐ Arena -- and in fact every commercial discrete-event simulation package -- maintains a FEL.

Correct Answer

You Answered

- ☒ All of the above.

Question 28

3 / 3 pts

Which high-level simulation modeling approach does ARENA employ?

Correct!

- ☐ Event-Scheduling
- ☒ Process-Interaction
- ☐ Customer-Process
- ☐ Entity-Solving
- ☐ Attribute-Recording

Question 29

3 / 3 pts

TRUE or FALSE? In the process-interaction worldview, at any time the system may have many entities interacting with each other as they compete for resources.

Correct!

- ☒ True
- ☐ False

Question 30

3 / 3 pts

TRUE OR FALSE? In ARENA, we can use a SEIZE command to grab one or more resources (servers).

Correct!

☒ True

☐ False

Question 31

0 / 3 pts

Which of the following statements about ARENA is **incorrect**?

☐ The system state is a set of variables containing enough information to describe the system.

☐ Entities can be dynamic elements that pass through the system.

You Answered

☒ You don't have to explicitly handle event scheduling and bookkeeping while using ARENA.

Correct Answer

☐ Attributes are global.

Question 32**3 / 3 pts**

What ARENA module is used to generate new customers?

☐ Generate

☐ Enter

Correct!

☒ Create

☐ Start

☐ Seize

Question 33**3 / 3 pts**

What command sequences are possible in an ARENA PROCESS module?

☐ DELAY

☐ SEIZE-DELAY

☐ DELAY-RELEASE

☐ SEIZE-DELAY-RELEASE

Correct!

☒ All of the above

Question 34

1 / 1 pts

Who is the best teacher ever?

Correct!

☒ Dave Goldsman

☐ Justin Bieber