

Trajectory Mining

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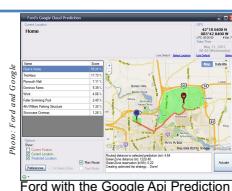
Background and Motivation

- Nowadays, many electronic devices are used for real world applications
GPS, sensor networks, mobile phone, ..
- « interesting » patterns for:
movement pattern analysis, animal behavior, route planning and vehicle control, location prediction, ...



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Some Examples



Ford with the Google Api Prediction



The world's largest traffic jam in history (China)

Free, online database of animal tracking data
Animal migration analysis

Hurricane Trajectory Prediction

Some Examples

- Location Prediction

According to the frequent behavior of the Second Big Data School attendees, the next place, after São Carlos to visit is:

Montpellier and its Region !!!



Antigone



Place de la Comédie



Nîmes



Beaches



Pont du Diable



Sète

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Spatio-Temporal Data

- Represented as a set of points, located in space and time.
 - $T=(x_1, y_1, t_1), \dots, (x_n, y_n, t_n) \rightarrow$ position in space at time t_i was (x_i, y_i) .



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Using Ad-hoc Queries

- Spatial query extensions in GIS applications
 - « find all the moving objects inside area A between 10:00 am and 2:00 pm »
 - « how many cars were driven between Main Square and the Airport on Friday? »
- Find the best solution by exploring each spatial object at a specific time according to some metric distance measurement

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Capture Collective Behavior

- Extracting patterns which capture 'group' or 'common' behaviour among moving entities:
Trajectories
- Development of approaches to identify groups of moving objects
strong relationship and interaction exist within a defined spatial region during a given time duration



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Outline

- A quick reminder on pattern discovery
- The different kinds of patterns from trajectory
- Towards a unified approach for extracting trajectories
- Deal with and without a spatial component?
- A concrete illustration
- Conclusion



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Outline

- **A quick reminder on pattern discovery**
 - Association Rules
 - Sequential Patterns
- The different kinds of patterns from trajectory
- Towards a unified approach for extracting trajectories
- Deal with and without a spatial component?
- A concrete illustration
- Conclusion



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Association Rule Mining

- Items : A, B, C, D, E, F
- 4 transactions (subset of items)
 - T1 : {A,D}
- Support for an itemset
 - Supp ({A,D})=1/4
 - Supp ({A,C})=2/4
- Frequent Itemsets (minSupp=50%)
 - {A,C} is a frequent itemset
- Rules : (minSupp and minConf = 50%)
 - A → C [50%, 50%]
 - C → A [50%, 100%]

Trans ID	Items
1	A, D
2	A, C
3	A, B, C
4	A, B, E, F

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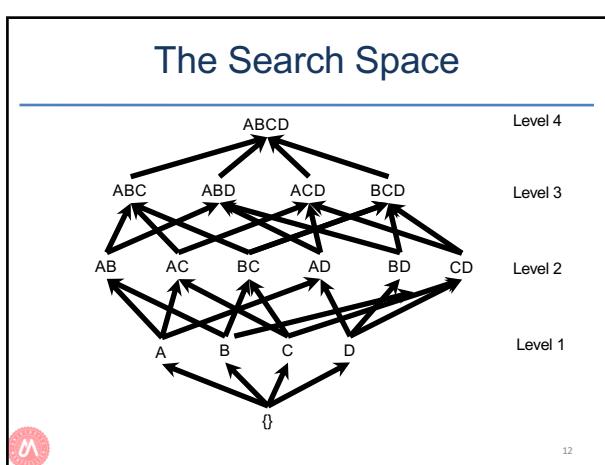
Association Rule Mining

- The corresponding matrix with the frequent itemset {A,C}

	A	B	C	D	E	F
1	1	0	0	1	0	0
2	1	0	1	0	0	0
3	1	1	1	0	0	0
4	1	1	0	0	1	1

Trans ID	Items
1	A, D
2	A, C
3	A, B, C
4	A, B, E, F

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Sequential Pattern Mining

- Items : A, B, C, D, E, F

- Support of a sequence**

- Supp((A)(C))=2/4
- Supp((A)(B)=2/4

- Frequent sequences**

(minSupp=50%) :

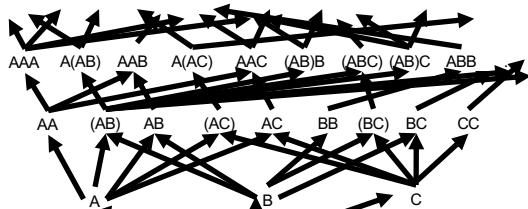
- (A) (C) and (A) (B) are frequent sequences

Trans ID	Sequences
1	(A, D)
2	(A) (C) (A) (C)
3	(A) (B, C)
4	(A) (E, F) (B)

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The Search Space for SP



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What kinds of patterns can be mined?

- 1, {A,B,C,D}
 - Association rules
- 1, <(A,t1) (B,C, t2) (D, t3)>
 - Sequences
- What can we do with the spatial dimension?
 - 1, <(x1,y1,t1) (x2,y2,t2) (x3,y3,t3)>

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Outline

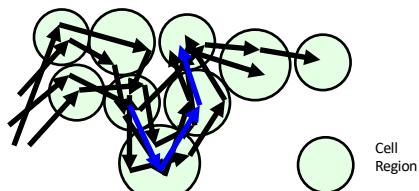
- A quick reminder on pattern discovery
- **The different kinds of patterns from trajectory**
 - Frequent Patterns
 - Moving Object
- Towards a unified approach for extracting trajectories
- Deal with and without a spatial component?
- A concrete illustration
- Conclusion



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Mining Spatio-Temporal Patterns from Trajectory Data

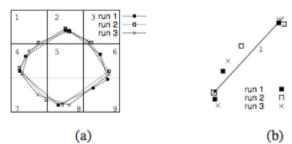
- Frequent Patterns:
 - Frequent followed paths



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Frequent Spatio-Temporal Sequence

- One spatio-temporal sequence:
 $S = \langle (x_1, y_1, t_1) (x_2, y_2, t_2) \dots (x_n, y_n, t_n) \rangle$
- Movement patterns that occurs frequently in the sequence: Frequent spatio-temporal sequence

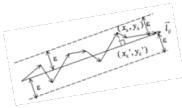


H. Cao et al., ICDM 05 18



Frequent Spatio-Temporal Sequence

- A three step process
 - Transform each trajectory in a line with several segments
 - A distance tolerance measure ϵ is defined
 - All trajectory points inside this distance can be projected in a representative line segment

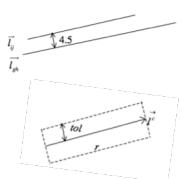


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Frequent Spatio-Temporal Sequence

- Group together similar segments and define a region
 - The similarity is based on the angle and the spatial length of the segment
 - A line segment with same angle and length is close to another one if their distance is lower than a distance threshold d
 - A medium segment is created, i.e. a region
 - Compute frequent sequences of

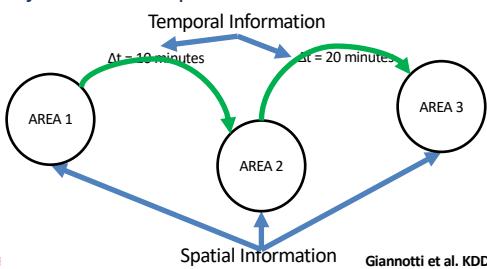
$r1-r2-r3-r1-r2 \Rightarrow r1, r2, r1-r2$
 $(minSup=2)$



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Trajectory Pattern Mining

- A trajectory pattern describes the movements of objects both in space and in time



Giannotti et al. KDD'07

Trajectory (T-) Patterns

- A Trajectory Pattern (*T*-pattern) is a couple (s, α) :
 - $s = <(x_0, y_0), \dots, (x_k, y_k)>$ is a sequence of $k+1$ locations
 - $\alpha = <\alpha_1, \dots, \alpha_k>$ are the transition times

$$(x_0, y_0) \xrightarrow{\alpha_1} (x_1, y_1) \xrightarrow{\alpha_2} \dots \xrightarrow{\alpha_k} (x_k, y_k)$$

- A T-pattern T_p occurs in a trajectory if the trajectory contains a subsequence S such that:
 - Each (x_i, y_i) in T_p matches a point (x'_i, y'_i) in S , and the transition times in T_p are similar to those in S



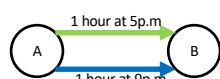
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Characteristics of Trajectory-Patterns

- Routes between two consecutive regions are not relevant



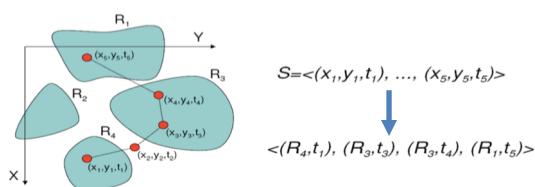
- Absolute times are not relevant



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Trajectory-Pattern Mining

- A preprocessing step is performed :
 - Convert each trajectory to a sequence, i.e., by converting a location (x, y) into a region



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A Neighborhood Function

- A preprocessing step
 - Neighborhood Function
 - Calculates spatial containment of regions
 - Input point to find enclosing Region of Interest
 - Defines the necessary proximity to fall into a region
 - Parameters: e – radius or necessary proximity of points
 - Translate each set of points into regions
 - Timestamp is selected from when the trajectory first entered the region



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Using prior Knowledge

- Static Region of Interest
 - Initially receives set of **R** disjoint spatial regions
 - **R** regions are predefined based on prior knowledge
 - Each represents relevant place for processing



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Popular Regions

- Data sets often do not possess predetermined regions
 - Regions based on criteria of density of the trajectories
 - A grid G of $n \times m$ cells
 - A density Threshold d
 - Each cell with density $G(l,j)$
 - Each region forms rectangular region
 - Dense cells always contained in some region
 - All regions have average density above d
 - All regions cannot expand without their average density decreasing below d



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Grid Density Preparation

- Split space into $n \times m$ grid with small cells
- Increment cells where trajectory passes
- Neighborhood Function $NR()$ determines which surrounding cells
- Regression - increment continuously along trajectory

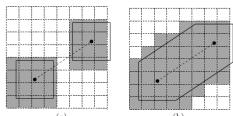


Figure 2: Density with and without regression

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Popular Regions Algorithm

- Iteratively consider each dense cell
- For each:
 - Expands in all four directions
 - Select expansion that maximizes density
 - Repeat until expansion would decrease below density threshold



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Trajectory-Pattern Mining

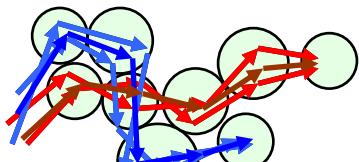
- After the preprocessing
- Execute a TAS (temporally annotated sequence) algorithm
 - A TAS is a sequential pattern annotated with typical transition times between its elements
 - The algorithm of TAS mining is an extension of PrefixSpan



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Mining Spatio-Temporal Patterns from Trajectory Data

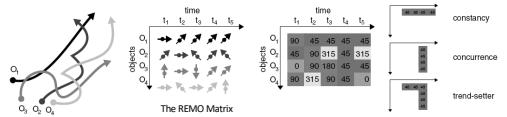
- Clustering:
 - Group together similar trajectories
 - For each group produce a summary



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Relative Motion Patterns

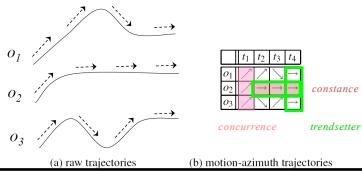
- Identify similar movements in a collection of moving-object trajectories
- Transform raw trajectories into motion attributes (speed, motion azimuth)



Laube, P. et al. GIScience, 2002
Laube, P. et al., IJGIS, 2005¹²

Basic Motion Patterns

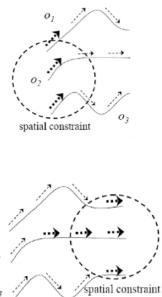
- Describing motion events, disregarding absolute positions
 - **Constance:** a sequence of equal motion attributes for consecutive times
 - **Concurrence:** the incidence of multiple objects with the same motion attributes
 - **Trendsetter:** a certain motion pattern that is shared by a set of other objects in the future. E.g., “constance” + “concurrence.”



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Relative Motion Patterns

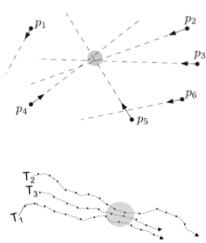
- *Flock* ($m > 1, r > 0$): At least m entities are within a circular region of radius r and they move in the same direction ("constance" + a spatial constraint)
- *Leadership* ($m > 1, r > 0, s > 0$) At least m entities are within a circular region of radius r , they move in the same direction, and at least one of the entities was already heading in this direction for at least s time steps



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Relative Motion Patterns

- *Convergence* ($m > 1, r > 0$) At least m entities will pass through the same circular region of radius r (assuming they keep their direction)
- *Encounter* ($m > 1, r > 0$) At least m entities will be simultaneously inside the same circular region of radius r (assuming they keep their speed and direction)



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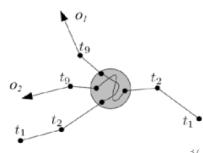
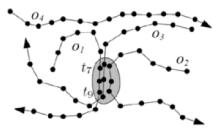
Disc-Based Trajectory Patterns

- Circular spatial constraint is considered (Disc-Based)
- Basic relative motion patterns are no longer considered
- Integration of time constraints in pattern

Gudmundsson et al. GIS'06,
Berkert et al. SAC'07
Vieira, M. Et al. SIGSPATIAL'09

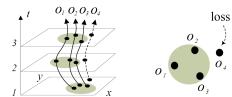
Disc-Based Trajectory Patterns

- **Flock** (m, k, r): a group of at least m objects that move together for at least k consecutive time points, while staying within a disc with radius r
- **Meet** (m, k, r): a group of at least m objects that stay together in a stationary disc with radius r for at least k consecutive time points



Density-Based Trajectory Patterns

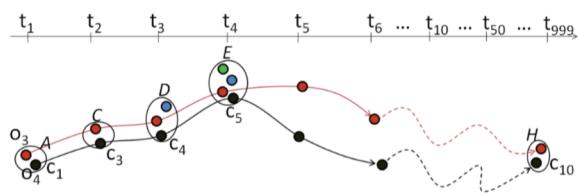
- The selection of a proper disc size r is difficult
 - A large r may capture objects that are intuitively not in the same group
 - A small r may miss some objects that are intuitively in the same group
- *lossy-flock* problem
- Employ density concepts



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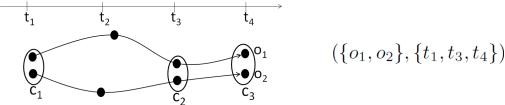
Swarm

- Swarm : At least ε objects move together (density-connected objects) during min_t timestamps



Li et al. VLDB'10 39

Swarm – Closed Swarm



DEFINITION 1. Swarm [6]. A pair (O, T) is a swarm if:

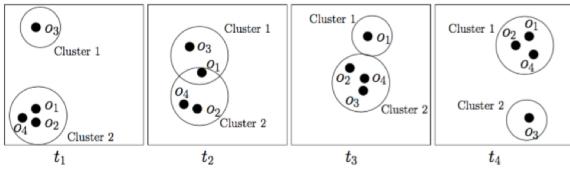
- (1) : $\forall t_{a_i} \in T, \exists c \text{ s.t. } O \subseteq c, c \text{ is a cluster.}$
There is at least one cluster containing all the objects in O at each timestamp in T .
- (2) : $|O| \geq \varepsilon.$
There must be at least ε objects.
- (3) : $|T| \geq min_t.$
There must be at least min_t timestamps.



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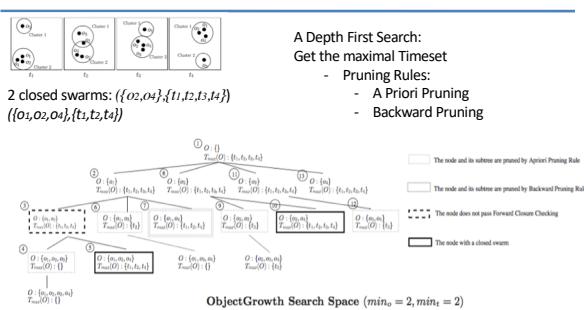
An illustrative Example

- How many Swarms?



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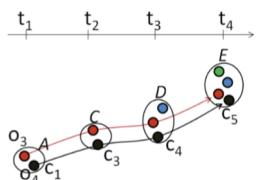
The Algorithm



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Convoy

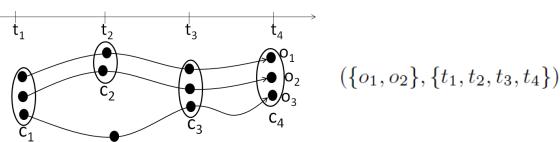
- Convoy: At least ε objects move together (density-connected objects) during \min_t consecutive timestamps



Jeung et al. ICDE'08 & VLDB'08

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Convoy

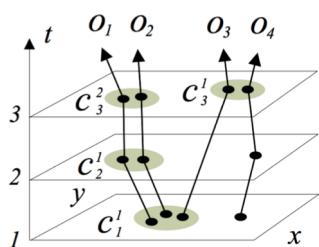
DEFINITION 3. Convoy [3]. A pair (O, T) , is a convoy if:

- $$\left\{ \begin{array}{l} (1) : (O, T) \text{ is a swarm.} \\ (2) : \forall i, 1 \leq i < |T|, t_{a_i}, t_{a_{i+1}} \text{ are consecutive.} \end{array} \right.$$

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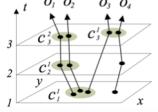
An illustrative Example

- How many Convoys?



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The Algorithm



Applying DBSCAN at each timestamp

1 convoy: $\{\{O_2, O_3\}, \{t_1, t_3\}\}$

Timestamp	Clusters	Candidate set V
t_1	c_1^1	$v_1 = c_1^1$
t_2	c_2^1	$v_1 = c_1^1 \cap c_2^1$
t_3	c_3^1, c_3^2	$v_1 = c_1^1 \cap c_2^1 \cap c_3^2, v_2 = c_3^2$

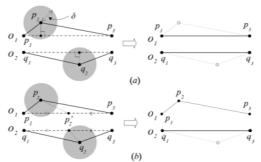
$$\begin{aligned} V_1 &= \{O_1, O_2, O_3\} \\ V_2 &= \{O_1, O_2\} \\ V_3 &= \{O_1, O_2\} \end{aligned}$$

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Algorithm Improvements

- Reducing the search space:
 - Simplifying the original trajectories



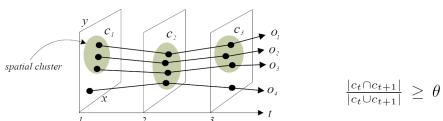
- Apply DBSCAN at each timestamp: CUTS, CUTS+



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Moving Clusters

- Moving Cluster : At least ϵ common objects move together (density-connected objects) during min_t consecutive timestamps



$$\frac{|c_t \cap c_{t+1}|}{|c_t \cup c_{t+1}|} \geq \theta$$

- Convoys + additional condition that they need to share some objects between two consecutive timestamps

Kalnis, SSTD 2005



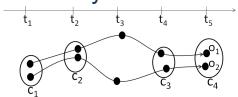
Group Pattern

- Combination of both convoy and closed swarm

– A closed swarm of disjointed convoys

$$T_S = \{(\{o_1, o_2\}, \{t_1, t_2\}), (\{o_1, o_2\}, \{t_4, t_5\})\}$$

$(\{o_1, o_2\}, T_S)$ is a closed swarm of convoys



Definition 4. *Group Pattern*²¹. Given a set of objects O , a minimum weight threshold min_{wei} , a set of disjointed convoys $T_S = \{s_1, s_2, \dots, s_n\}$, a minimum number of convoys $mine$. (O, T_S) is a group pattern if:

$$\begin{cases} (1) : (O, T_S) \text{ is a closed swarm w.r.t } min_e \\ (2) : \frac{\sum |r_{S_i}| |s_i|}{|T_{DB}|} \geq min_{wei} \end{cases}$$

Note that min_e is only applied for T_S (i.e. $|T_S| \geq min_e$).

Wang, DKE 2006

Periodic Patterns

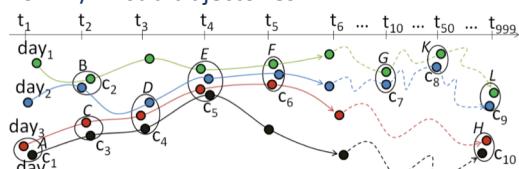
- An object follows the same routes (approximately) over regular time intervals
 - People wake up at the same time and generally follow the same route to their work everyday
- Given an object's trajectory including N time-points, T_p which is the number of timestamps that a pattern may reappear.
- The object's trajectory is decomposed into N / T_p sub-trajectories
- T_p is data dependent
 - T_p = 'a day' in traffic control applications since many vehicles have daily patterns
 - T_p = 'a year' for annual animal migration patterns

N. Mamoulis, KDD04

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Periodic Patterns

- A periodic pattern is a closed swarm discovery from N / T_p sub-trajectories.



4 daily sub-trajectories

We extract potential periodic patterns such as {c1, c3, c4, c5}, {c2, c5, c6}

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Outline

- A quick reminder on pattern discovery
- The different kinds of patterns from trajectory
- **Towards a unified approach for extracting trajectories**
 - Cluster Matrix
 - Properties
 - GetMove
 - How to Manage Blocks
 - Lord of the Rings
 - Gradual Spatio-Temporal Rules
 - The top-k informative Patterns
- Deal with and without a spatial component?
- An illustration
- Conclusion



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Motivations

- Clustering:
 - Flock, convoy, moving cluster, swarm, closed swarm, k-Stars,
- Different approaches to mine them:
 - CuTS*, ObjectGrowth, CMC, Vg-Growth, ...
 - Complexity, computation cost, time consuming!!!
- *How about unifying algorithm?*
- What happen when new data arriving?
 - *How about incremental algorithm?*



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The main intuition

- Very efficient approaches have been defined for extracting a set of association rules
 - Apriori, Closed, Derivable, ...

	A	B	C	D	E	F
1	1	0	0	1	0	0
2	1	0	1	0	0	0
3	1	1	1	0	0	0
4	1	1	0	0	1	1



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Cluster Matrix

- Patterns:
 - Evolution of clusters
- Objects: transactions
- Clusters: items

Cluster Matrix

T_{DB}		t_1			t_2			t_3		
		C_{DB}	beer	c_{21}	c_{31}	c_{12}	c_{22}	c_{32}	diaper	c_{23}
O_{DB}	o_1	1				1			1	
	o_2	1				1			1	
	o_3	1				1			1	
	o_4				1	1			1	
	o_5			1				1	1	

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Frequent Closed Itemset from Cluster Matrix

Frequent Closed Itemset $\Upsilon = \{c_{t_{a_1}}, c_{t_{a_2}}, \dots, c_{t_{a_p}}\}$
 Life Time $T_\Upsilon = \{t_{a_1}, t_{a_2}, \dots, t_{a_p}\}$
 Set of Objects $O(\Upsilon) = \bigcap_{i=1}^p c_{t_{a_i}}$ Support $\sigma(\Upsilon)$
 $\Upsilon = \{c_{11}, c_{13}\}$ ($O(\Upsilon) = \{o_1, o_2, o_3\}$, $T_\Upsilon = \{t_1, t_3\}$)
 $\sigma(\Upsilon) = 3$

$|\Upsilon| = 2$

Cluster Matrix

T_{DB}		t_1			t_2			t_3		
		C_{DB}	c_{11}	c_{21}	c_{31}	c_{12}	c_{22}	c_{32}	c_{13}	c_{23}
O_{DB}	o_1	1				1			1	
	o_2	1				1			1	
	o_3	1				1			1	
	o_4				1	1			1	
	o_5			1				1	1	

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Periodic Cluster Matrix

Cluster Matrix

T_{db}		t_1			t_2			t_3			t_4			t_5			t_{10}			t_{50}			t_{999}		
		C_{db}	c_1	c_2	c_3	c_4	c_5	c_6	c_7	c_8	c_9	c_{10}	c_1	c_2	c_3	c_4	c_5	c_6	c_7	c_8	c_9	c_{10}			
ST_{db}	st_1				1			1	1	1		1													
	st_2		1			1	1	1	1	1	1														
	st_3	1		1	1	1	1																		
	st_4	1		1	1	1																			

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The main intuition (following...)

- We are now able to extract itemsets corresponding to a set of clusters occurring over time
- Not trajectories yet!
- *What about properties on Itemsets?*



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Property for Swarm

DEFINITION 1. *Swarm* [6]. A pair (O, T) is a swarm if:

$$\left\{ \begin{array}{l} (1) : \forall t_{a_i} \in T, \exists c \text{ s.t. } O \subseteq c, c \text{ is a cluster.} \\ \text{There is at least one cluster containing} \\ \text{all the objects in } O \text{ at each timestamp in } T. \\ (2) : |O| \geq \varepsilon. \\ \text{There must be at least } \varepsilon \text{ objects.} \\ (3) : |T| \geq min_t. \\ \text{There must be at least } min_t \text{ timestamps.} \end{array} \right.$$

PROPERTY 1. *Swarm*. Given a frequent itemset $\Upsilon = \{c_{t_{a_1}}, c_{t_{a_2}}, \dots, c_{t_{a_p}}\}$. $(O(\Upsilon), T_\Upsilon)$ is a swarm if, and only if:

$$\left\{ \begin{array}{l} (1) : \sigma(\Upsilon) \geq \varepsilon \\ (2) : |\Upsilon| \geq min_t \end{array} \right.$$

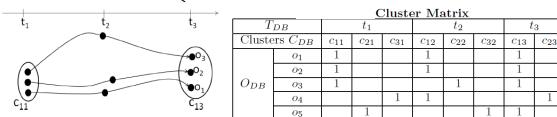


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Swarm

PROPERTY 1. *Swarm*. Given a frequent itemset $\Upsilon = \{c_{t_{a_1}}, c_{t_{a_2}}, \dots, c_{t_{a_p}}\}$. $(O(\Upsilon), T_\Upsilon)$ is a swarm if, and only if:

$$\left\{ \begin{array}{l} (1) : \sigma(\Upsilon) \geq \varepsilon \\ (2) : |\Upsilon| \geq min_t \end{array} \right.$$



$\Upsilon = \{c_{11}, c_{13}\}$ ($O(\Upsilon) = \{o_1, o_2, o_3\}$, $T_\Upsilon = \{t_1, t_3\}$)
 $\sigma(\Upsilon) = 3 > \varepsilon$ and $|\Upsilon| = 2 \geq min_t$



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Convoy

PROPERTY 3. Convoy. Given a frequent itemset $\Upsilon = \{c_{t_{a_1}}, c_{t_{a_2}}, \dots, c_{t_{a_p}}\}$. $(O(\Upsilon), T_\Upsilon)$ is a convoy if and only if:

$$\begin{cases} (1) : (O(\Upsilon), T_\Upsilon) \text{ is a swarm.} \\ (2) : \forall j, 1 \leq j < p : t_{a_j}, t_{a_{j+1}} \text{ are consecutive.} \end{cases}$$

		t_1	t_2	t_3
		c_{11}	c_{21}	c_{31}
O_{DB}	t_{DB}	1	1	1
	C_{DB}	0 ₁	0 ₂	0 ₃
O_{DB}	0 ₁	1	1	1
O_{DB}	0 ₂	1	1	1
O_{DB}	0 ₃	1	1	1
O_{DB}	0 ₄	1	1	1
O_{DB}	0 ₅	1	1	1

$\Upsilon = \{c_{11}, c_{12}, c_{13}\}$
 $(O(\Upsilon) = \{o_1, o_2\}, T_\Upsilon = \{t_1, t_2, t_3\})$

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Properties

- In the same way it is possible to define properties for:
Swarm, Closed Swarm, Convoy, Moving Cluster, Periodic Pattern, ...
- We are now able to extract trajectories!

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The Main Process

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GeT_Move – Pruning Rule

- Spatio-temporal patterns:
 - Clusters (items) must belong to different timestamps
 - Items which form FCIs must be in different timestamps
- FCIs include more than 1 item in the same timestamp will be discarded



		Cluster Matrix					
		t_1		t_2		t_3	
Clusters C_{DB}	C_{DB}	c_{11}	c_{21}	c_{31}	c_{12}	c_{22}	c_{32}
		o_1	1		1		1
O_{DB}	o_1						
	o_2	1			1		1
	o_3	1				1	
	o_4			1	1		
	o_5		1			1	1

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GeT_Move

- Frequent closed itemset mining algorithm to extract FCIs:
 - LCM Algorithm (Linear time Closed itemset Miner)
- Extract patterns from FCIs

X
 $|X| \geq min_t : \text{Closed Swarm}$



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GeT_Move

- Frequent closed itemset mining algorithm to extract FCIs:
 - LCM Algorithm (Linear time Closed itemset Miner)
- Extract patterns from FCIs

X

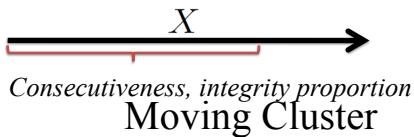
Consecutiveness, object correctness, min_t
Convoy



Set of disjointed convoys is a **Group Pattern**

GeT_Move

- Frequent closed itemset mining algorithm to extract FCIs:
LCM Algorithm (Linear time Closed itemset Miner)
- Extract patterns from FCIs



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Two remaining problems

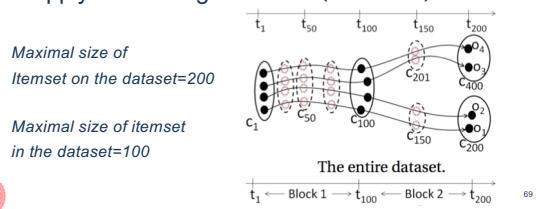
- Association rule mining algorithms have some problems when dealing with a huge number of items, i.e. long transactions!
- What happens with new data?*



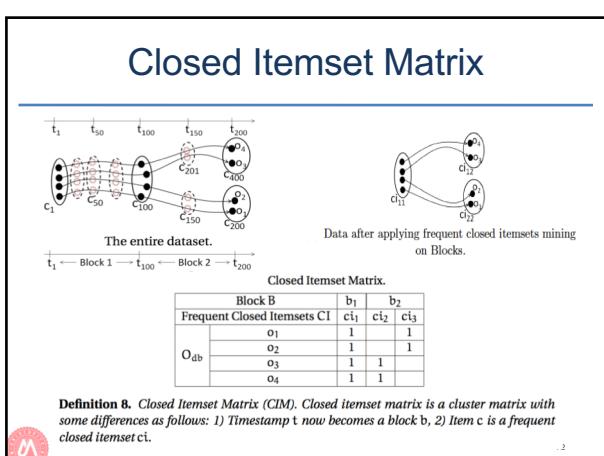
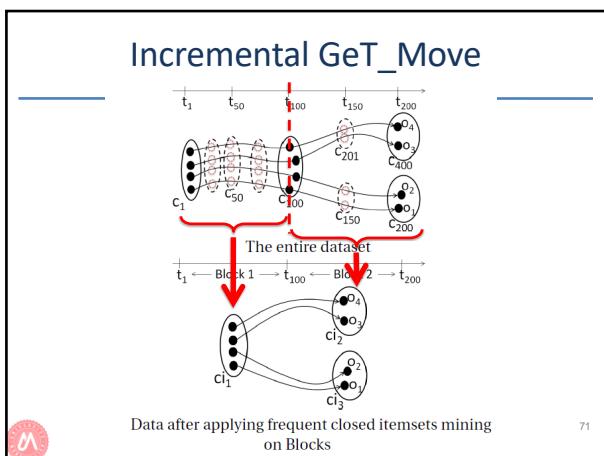
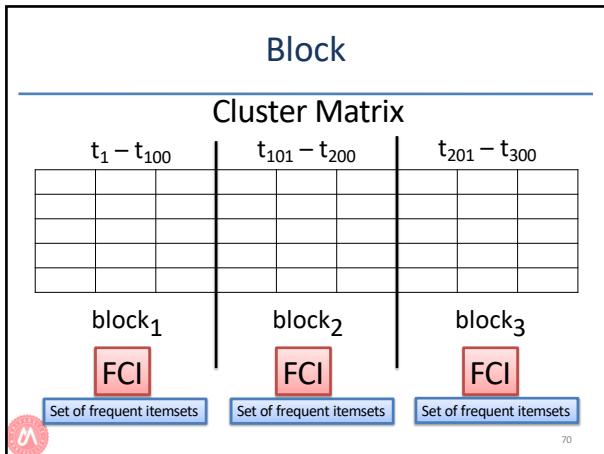
68

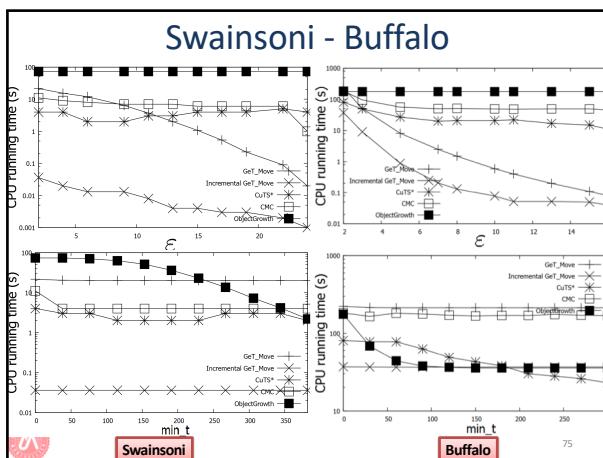
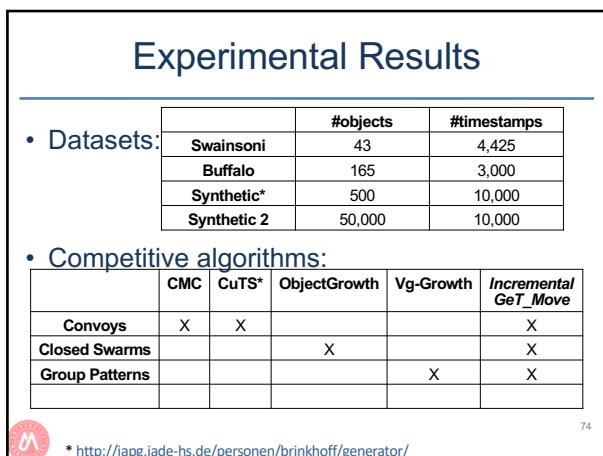
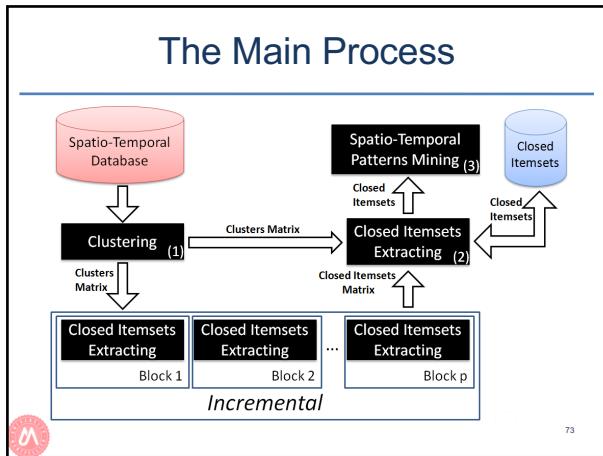
Towards an Incremental Approach

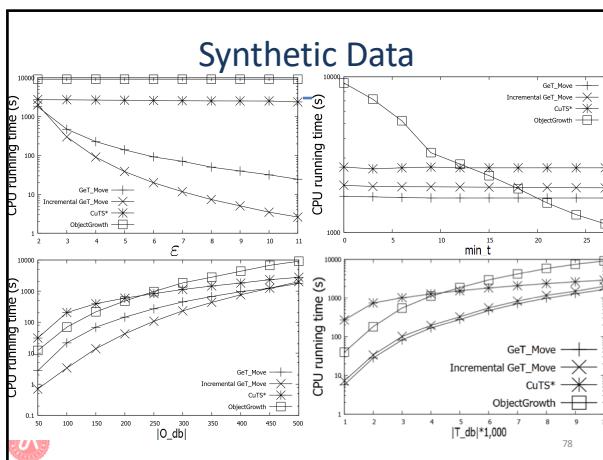
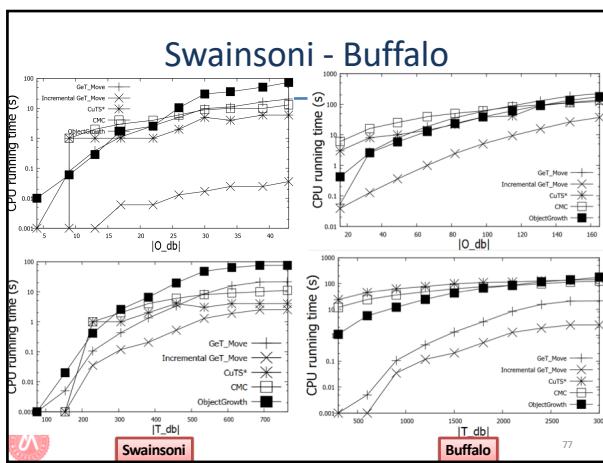
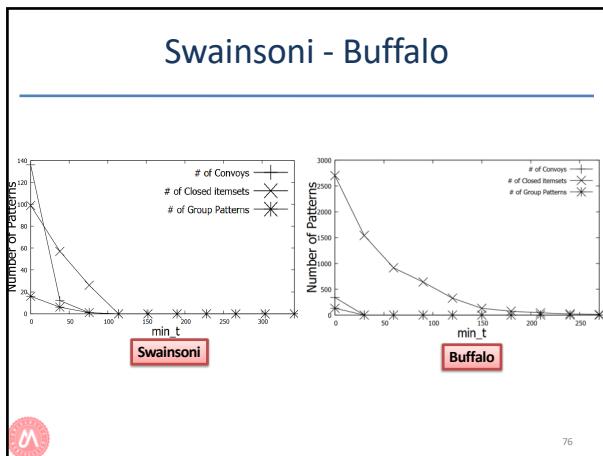
- Main idea: “Compress the dataset”
 - Shorten the transactions by splitting the trajectory matrix into short intervals called Blocks
 - Apply FCI mining on blocks (local FCI)



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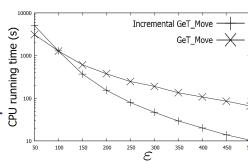






Scalability

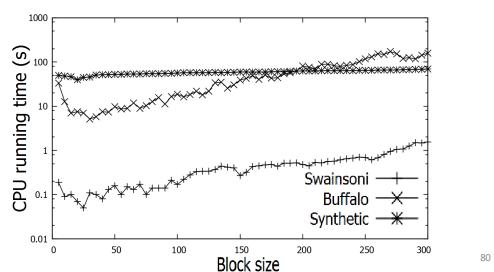
- Synthetic data:
 - 50,000 objects in 10,000 timestamps
 - 500 million locations in total
 - CMC and CuTS* stop due to a lack of memory capacity after processing 300 million locations
 - ObjectGrowth cannot provide the results after 1day running



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Block Size

- Different block sizes:
 - Range 20-30.



Effectiveness



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Effectiveness



One of discovered group pattern

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Towards a Parameter Free

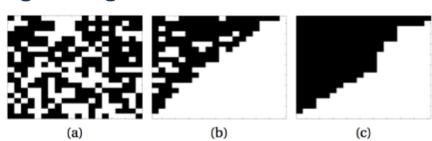
- How to specify the optimal size of blocks?

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Reordering the dataset

- LCM is very efficient for dense data
- Reorganizing the data



Examples of non-nested, almost nested, fully nested datasets [37]. Black = 1, white = 0. (a) Original, (b) Almost nested, (c) Fully nested.

H. Mannila, E. Terzi. *Nestedness and Segmented Nestedness*. In KDD'07

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The Original Distributions



Original Swainsoni cluster matrix.



Original Buffalo cluster matrix.



Original Synthetic cluster matrix.

An Example of Nested



(a) Original Swainsoni cluster matrix.



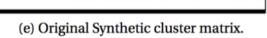
(b) Nested Swainsoni cluster matrix.



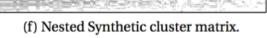
(c) Original Buffalo cluster matrix.



(d) Nested Buffalo cluster matrix.



(e) Original Synthetic cluster matrix.



(f) Nested Synthetic cluster matrix.

Dataset	Matrix fill	#Nested blocks	avg.length
Swainsoni	17.8%	102	4.52
Buffalo	7.2%	602	2.894
Synthetic	0.1%	8	2.00

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Reordering the dataset

- New definition of cluster matrix

Definition 9. Fully nested cluster matrix (resp. block). An $n \times m$ 0-1 block b is fully nested if for any two column r_i and r_{i+1} ($r_i, r_{i+1} \in b$) we have $r_i \cap r_{i+1} = r_{i+1}$.



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The Algorithm

They share the same objects. It is a block.

They do not share the same objects. They are stored in a separate place that will be considered at the end

```

Algorithm 3: Fully Nested Block Partition
Input : a nested cluster matrix  $C_{MN}$ 
Output: a set of blocks  $B$ 
1 begin
2    $B := \emptyset$ ;  $NestedB := \emptyset$ ;  $SpareB := \emptyset$ ;
3   foreach item  $i \in C_{MN}$  do
4     if  $\cap \{i+1\} = \{i+1\}$  then
5        $NestedB := NestedB \cup i$ ;
6     else
7        $NestedB := NestedB \cup i$ ;
8       if  $|NestedB| \leq 1$  then
9          $SpareB.push\_all(NestedB)$ ;
10         $NestedB := \emptyset$ ;
11      else
12         $B := B \cup NestedB$ ;
13         $NestedB := \emptyset$ ;
14   return  $B := B \cup SpareB$ ;
15 where the purpose  $SpareB.push\_all(NestedB)$  function is to put  $NestedB$  to  $SpareB$ .

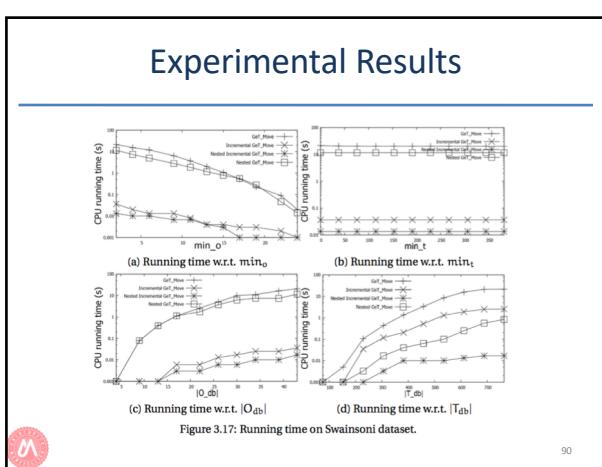
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The Global Approach

- Apply the nested and segment nested Greedy algorithm
- Apply the partition algorithm to get blocks
- Apply incremental mining with FCI

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Experimental Results

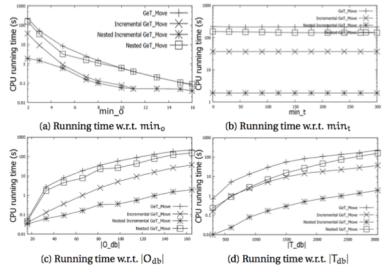
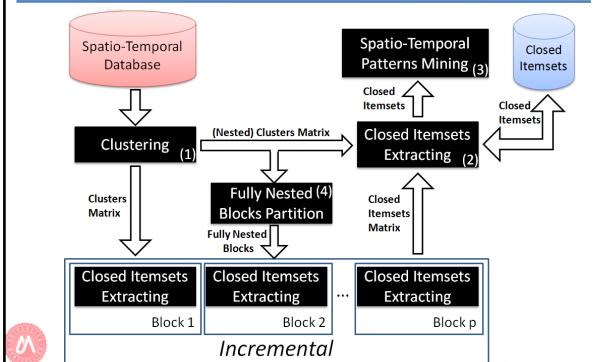


Figure 3.18: Running time on Buffalo dataset.

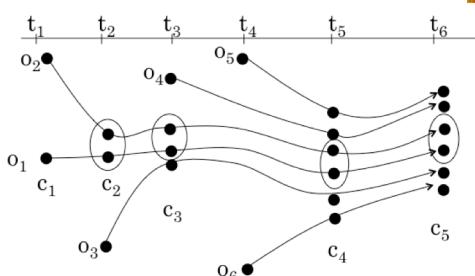
91



The Full Process



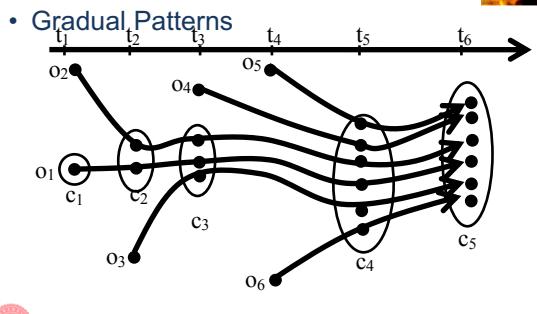
What's about lord of the Rings?



93

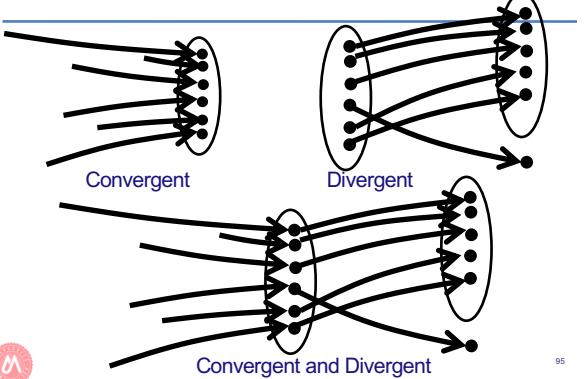


What's about lord of the Rings?



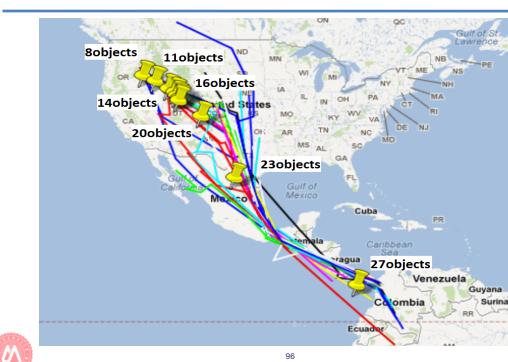
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...Gradual Trajectories



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More seriously



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Pattern Definition

- The objects still remain in the next cluster
- The number of objects is increasing (resp. decreasing)
- At least a number of certain timestamps



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rGpattern

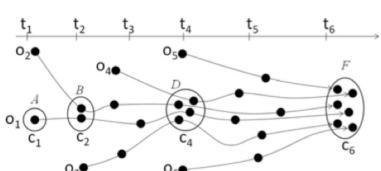
Definition 17. rGpattern. Given a list of clusters $C^* = \{c_1, \dots, c_n\}$ and a minimum threshold \min_t , C^* is a rGpattern if:

$$C^* = C^{\geq} : \begin{cases} (1) : |C^*| \geq \min_t, \\ \forall i \in \{1, \dots, n-1\}, \\ (2) : c_i \subseteq c_{i+1}, \\ (3) : |c_n| > |c_1|. \end{cases}$$

$$C^* = C^{\leq} : \begin{cases} (1) : |C^*| \geq \min_t, \\ \forall i \in \{1, \dots, n-1\}, \\ (2) : c_i \supseteq c_{i+1}, \\ (3) : |c_n| < |c_1|. \end{cases}$$

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Example



$C_1^{\geq} = \{c_1, c_2, c_4\}$ is a rGpattern

$|C_1^{\geq}| \geq \min_t$, $c_1 \subset c_2 \subset c_4$ and $|c_4| = 4 > |c_1| = 1$

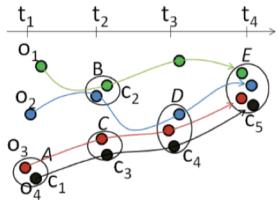
$C_1^{\geq} = \{c_1, c_2, c_4\}$, $C_2^{\geq} = \{c_1, c_2, c_6\}$, $C_3^{\geq} = \{c_2, c_4, c_6\}$ and $C_4^{\geq} = \{c_1, c_2, c_4, c_6\}$

Definition 18. Maximal rGpattern. Given a rGpattern $C^* = \{c_1, \dots, c_n\}$. C^* is maximal if $\nexists C'^*, C^* \subset C'^*$ and C'^* is a rGpattern.

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An Illustrative Example

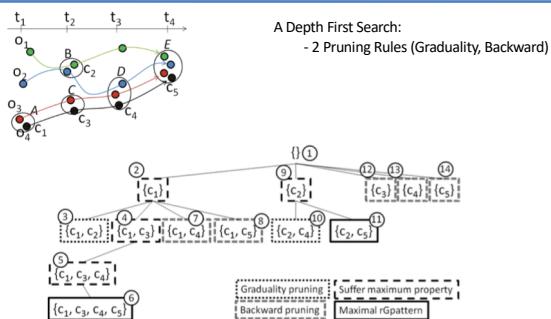
- How many maximal rGpatterns?



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The Algorithm

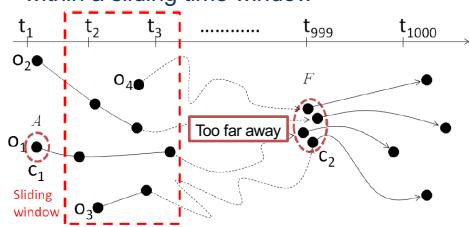


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Time Relaxed Gradual Trajectories

- Timestamps can be:
 - non-consecutive
 - within a sliding time window



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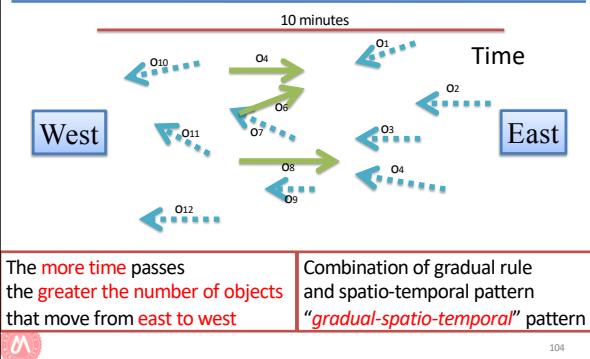
Gradual Rules

- Gradual rules highlight complex order correlations of the form "*The more/less X, then the more/less Y*"
– The nearer to city center, the higher the rent
- Mining gradual patterns plays a crucial role in many applications (numerical data): biological databases, survey databases, data streams...



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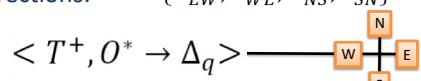
Issues and Motivations



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Rule Definition

- Set of timestamps: $T = \{t_1, t_2, \dots, t_n\}$
- Set of objects: $O = \{o_1, o_2, \dots, o_z\}$
- A variation: $* \in \{+, -\}$
- Set of directions: $\Delta = \{\Delta_{EW}, \Delta_{WE}, \Delta_{NS}, \Delta_{SN}\}$



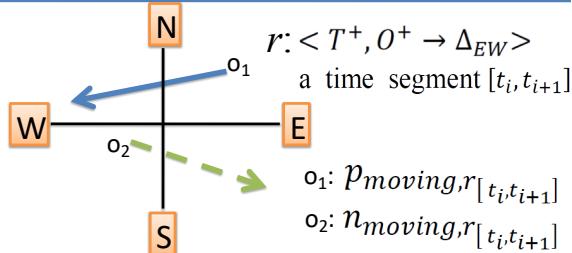
"the more time passes
the greater the number of objects
that move from east to west"

$< T^+, O^+ \rightarrow \Delta_{EW} >$



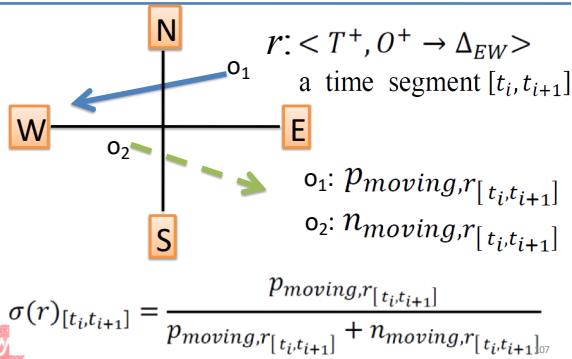
105

Positive Moving Objects



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Support of a Rule on a Timestamp



Supporting Time Segment

- Supporting time segment, non supporting time segment

$r: < T^+, O^* \rightarrow \Delta_q >$

$[t_i, t_{i+1}]$ is a supporting time segment

$$\text{if } O^* = O^+ \text{ then } \begin{cases} p_{moving,r[t_i, t_{i+1}]} \geq p_{moving,r[t_{i-1}, t_i]} : \text{condition(1)} \\ \sigma(r)_{[t_i, t_{i+1}]} \geq \sigma(r)_{[t_{i-1}, t_i]} : \text{condition(2)} \\ \sigma(r)_{[t_i, t_{i+1}]} \geq \sigma_0 : \text{condition(3)} \end{cases}$$

$$\text{if } O^* = O^- \text{ then } \begin{cases} p_{moving,r[t_i, t_{i+1}]} \leq p_{moving,r[t_{i-1}, t_i]} : \text{condition (1)} \\ \sigma(r)_{[t_i, t_{i+1}]} \leq \sigma(r)_{[t_{i-1}, t_i]} : \text{condition(2)} \\ \sigma(r)_{[t_i, t_{i+1}]} \geq \sigma_0 : \text{condition(3)} \end{cases}$$

Supporting Time Pattern

$$p_s = (t_i, t_{i+k}), |p_s| = k \ (k \geq 1)$$

p_s is a *k-supporting time pattern* if and only if

$\forall j \ (0 \leq j < k), [t_{i+j}, t_{i+j+1}]$ is a *supporting time segment*

$p_{ns} = (t_i, t_{i+k})$ is a *k-non-supporting time pattern* if and only if

$\forall j \ (0 \leq j < k), [t_{i+j}, t_{i+j+1}]$ is a *non-supporting time segment*.

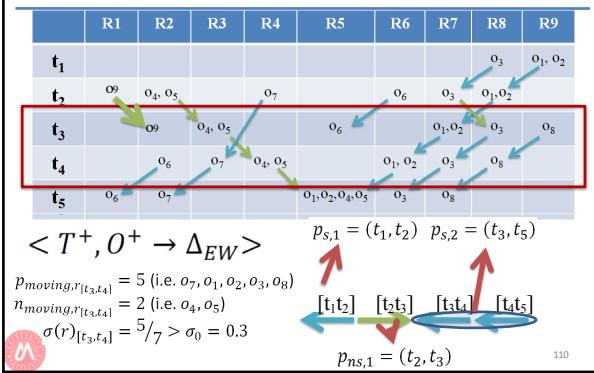
$p_{nt} = (t_i, t_{i+k})$ is a *k-neutral time pattern* if and only if

$\forall j \ (0 \leq j < k), [t_{i+j}, t_{i+j+1}]$ is a *neutral time segment*.

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A Running Example



Support and Confidence of Rules

a set of timestamps $T = \{t_1, t_2, \dots, t_n\}$
 $r: < T^+, O^* \rightarrow \Delta_q >$

- We have already seen the support of a Rule on one Timestamp:

$$\sigma(r)_{[t_i, t_{i+1}]} = \frac{p_{moving,r[t_i, t_{i+1}]}}{p_{moving,r[t_i, t_{i+1}]} + n_{moving,r[t_i, t_{i+1}]}}$$

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111

Support and Confidence of Rules

a set of timestamps $T = \{t_1, t_2, \dots, t_n\}$

$r: < T^+, O^* \rightarrow \Delta_q >$

- p_s : is k -supporting time pattern
- p_{ns} : is k -non supporting time pattern
- p_{nt} : is k -neutral time pattern

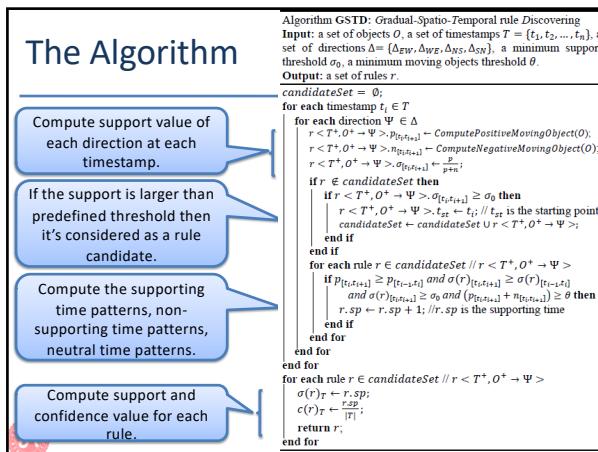
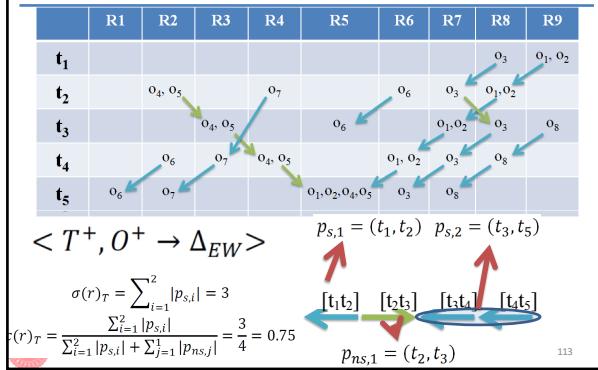
$$\sigma(r)_T = \sum_{i=1}^n |p_{s,i}|$$

$$c(r)_T = \frac{\sum_{i=1}^n |p_{s,i}|}{\sum_{i=1}^n |p_{s,i}| + \sum_{j=1}^m |p_{ns,j}| + \sum_{k=1}^l |p_{nt,k}|}$$

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A Running Example



Experimental Results

- Swainsoni dataset (43 objects evolving over time and 4225 different timestamps). July 1995 to June 1998.

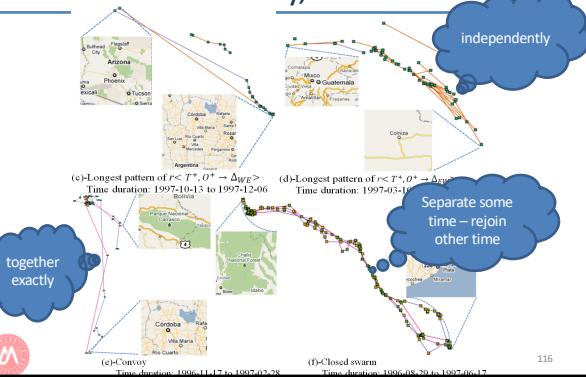
SUPPORT AND CONFIDENCE FOR EACH RULE.

Rule	$\sigma(r)_T$	$c(r)_T$
$< T^+, O^+ \rightarrow \Delta_{NS} >$	2653	0.6416
$< T^+, O^+ \rightarrow \Delta_{SN} >$	1944	0.4617
$< T^+, O^+ \rightarrow \Delta_{WE} >$	2725	0.6472
$< T^+, O^+ \rightarrow \Delta_{EW} >$	2060	0.4903



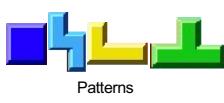
115

Gradual-Spatio-Temporal Rules vs Convoy, Swarm



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The Most Informative Patterns



Group Moving Periodic Pattern Cluster
T-Pattern Convoy Evolving k-Star Tralus Closed Swarm
Flock

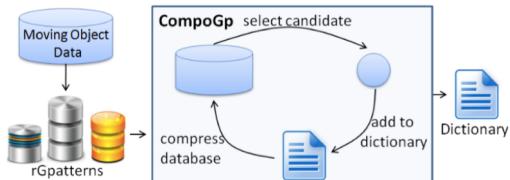


	T_{DB}	t_1	t_2	t_3	t_4	t_5				
C_{DB}	c_1	c_2	c_3	c_4	c_5	c_6	c_7	c_8	c_9	c_{10}
O_{DB}	o_1	1		1	1	1	1			
	o_2			1	1		1			1
	o_3					1				
	o_4	1		1	1	1	1			
	o_5	1	1	1	1	1	1			



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The Main Idea



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Problem Statement

- Given a spatio-temporal DB O_{db} and a set of patterns F (extracted from O_{db})
 - Discover the optimal dictionary P (subset of F)
 - compresses the data best w.r.t. the given encoding schema
- MDL approach: $L_p(O_{db}) = L(P) + L(O_{db}|P)$
- $$\arg \min_{P \subseteq F} \left(\sum_{p \in P} L(p) + L(O_{DB}|P) \right)$$
- $L(p)$: number of bits to encode the pattern p + extra bit to encode the type of pattern
 - $L(O_{db}|P)$: number of bits to encode the dataset O_{db} given P

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Encoding Example

		T_{DB}		t_1		t_2		t_3		t_4		t_5	
		Clusters C_{DB}		c_1	c_2	c_3	c_4	c_5	c_6	c_7	c_8	c_9	c_{10}
O_{DB}	o_1			1			1	1	1	1			
	o_2				1	1	1	1	1	1			1
	o_3							1					
	o_4			1			1	1	1	1			
	o_5			1			1	1	1	1			

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O_{DB}		Patterns F
$o_1 = c_1 c_4 c_6 c_7 c_8$		$p_1 = c_1 c_4 c_6, \bar{1}$
$o_2 = c_3 c_4 c_6 c_7 c_{10}$		$p_2 = c_2 c_5 c_7 c_9, \bar{0}$
$o_3 = c_6$		$p_3 = c_7 c_8, \bar{2}$
$o_4 = c_2 c_5 c_7 c_9$		$p_4 = c_4 c_6 c_7 \bar{0}$
$o_5 = c_2 c_5 c_7 c_9$		



Encoding Example

	T_{DB}	t_1	t_2	t_3	t_4	t_5					
Clusters	C_{DB}	c_1	c_2	c_3	c_4	c_5	c_6	c_7	c_8	c_9	c_{10}
	O_{DB}	o_1	1		1	1	1	1			
		o_2		1	1	1	1				1
		o_3					1				
		o_4		1	1	1	1				1
		o_5	1		1	1	1				

Encoded O_{DB}	Dictionary \mathcal{P}
$o_1 = [p_1, 0][p_3, 0]$	$p_1 = c_1 c_4 c_6, \bar{1}$
$o_2 = c_3[p_1, 1][p_3, 0]c_{10}$	$p_2 = c_2 c_5 c_7 c_9, \bar{0}$
$o_3 = [p_1, 2]$	$p_3 = c_7 c_8, \bar{2}$
$o_4 = p_2$	$p_4 = c_4 c_6 c_7, \bar{0}$
$o_5 = p_2$	

$$\begin{aligned} L(O_{DB}/\mathcal{P}) &= 4 + 6 + 2 + 1 + 1 = 14 \\ L(\mathcal{P}) &= 4 + 5 + 3 + 4 = 16 \\ L(O_{DB}) &= 30 \end{aligned}$$

Encoded O_{DB}	Dictionary \mathcal{P}
$o_1 = [p_1, 0]c_7 c_8$	$p_1 = c_1 c_4 c_6, \bar{1}$
$o_2 = c_3[p_1, 1]c_7 c_{10}$	$p_2 = c_2 c_5 c_7 c_9, \bar{0}$
$o_3 = [p_1, 2]$	
$o_4 = p_2$	
$o_5 = p_2$	

$$\begin{aligned} L(O_{DB}/\mathcal{P}) &= 4 + 5 + 2 + 1 + 1 = 13 \\ L(\mathcal{P}) &= 4 + 5 = 9 \\ L(O_{DB}) &= 22 \end{aligned}$$

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The Algorithm

Compute for each pattern its compression size and select the most efficient

Compute the compression size for each object of the DB. This can be done efficiently by using pointers rather than true value

```

Algorithm 9: NaiveCompo
Input : Database  $O_{db}$ , set of patterns  $\mathcal{F}$ , int K
Output: Compressing patterns  $\mathcal{P}$ 
1 begin
2    $\mathcal{P} \leftarrow \emptyset$ ;
3   while  $|\mathcal{P}| < K$  do
4     foreach  $p \in \mathcal{F}$  do
5        $O_{db}^d \leftarrow O_{db}$ ;
6        $L^*(O_{db}^d, p) \leftarrow \text{CompressionSize}(O_{db}^d, p);$ 
7        $p^* \leftarrow \arg \min_p L^*(O_{db}^d, p);$ 
8        $\mathcal{P} \leftarrow \mathcal{P}; F \leftarrow F \setminus \{p^*\};$ 
9       Replace all instances of  $p^*$  in  $O_{db}$  by its pointers;
10      Replace all instances of  $p^*$  in  $F$  by its pointers;
11    output  $\mathcal{P};$ 
12 CompressionSize( $O_{db}^d, p)$ 
13 begin
14   size  $\leftarrow 0;$ 
15   foreach  $o \in O_{db}^d$  do
16     If  $p.\text{involved}(o) = \text{true}$  then
17       Replace instance of  $p$  in  $o$  by its pointers;
18     foreach  $o \in O_{db}^d$  do
19       size  $\leftarrow$  size + | $o$ |;
20     size  $\leftarrow$  size + | $p$ | + 1;
21   output size;

```

The 3-patterns



From the running Swanson example



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Outline

- A quick reminder on pattern discovery
- The different kinds of patterns from trajectory
- Towards a unified approach for extracting trajectories
- **Deal with and without a spatial component?**
- A concrete illustration
- Conclusion



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Spatial or not spatial?

- Trajectories have been defined for dealing with spatio-temporal data
- What are exactly trajectories?



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Web Usage Mining

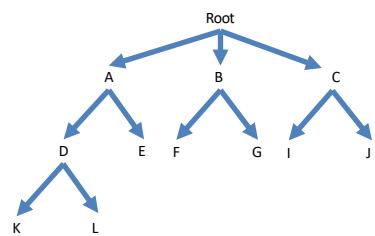
- Web Usage Mining is the application of data mining techniques to discover interesting usage patterns from Web data in order to understand and better serve the needs of Web-based applications. (wikipedia)
- Use log entries

123.456.78.9 -- [24/Apr/2018:19:13:44 -0400] "GET /Images/tagline.gif HTTP/1.0"
200 1449 http://www.teced.com/ "Mozilla/4.51 [en] (Win98;I)"



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An Illustrative Example



127

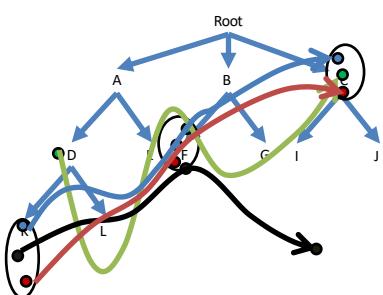


T1										T2										T3																										
A	B	C	D	E	F	G	H	I	J	K	L	A	B	C	D	E	F	G	H	I	J	K	L	A	B	C	D	E	F	G	H	I	J	K	L	A										
C1	1												1																					1												
C2	1													1																								1								
C3		1													1																								1							
C4		1													1																							1								
C5			1													1																						1								
C6				1													1																						1							
C7					1													1																						1						
C8						1													1																						1					



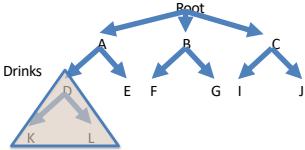
120

An Illustrative Example



129

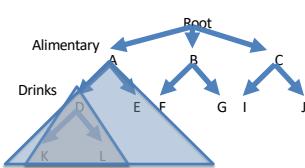
At Different Levels of Granularities



	T1								T2								T3															
	A	B	C	D	E	F	G	H	I	J	A	B	C	D	E	F	G	H	I	J	A	B	C	D	E	F	G	H	I	J	A	
C1	1								1												1											
C2	1								1												1											
C3	1	1							1												1											
C4	1	1							1												1											
C5																					1											
C6																					1											
C7																					1											
C8																					1											
...																																



At Different Levels of Granularities



Group at the upper level

	T1			T2			T3			
	A	B	C	A	B	C	A	B	C	A
C1	1				1				1	
C2	1				1				1	
C3	1				1				1	
C4	1				1				1	
C5	1				1				1	
C6	1				1				1	
C7	1				1				1	
C8	1				1				1	
...										

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Usefulness

- Personalization: Probabilistic Latent Semantic Analysis
- Efficiency: preload pages, site organization
- E-commerce: Ad placements



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PMSI Data

- Using data from the French hospital database (PMSI) to estimate **coronary thrombosis**
- PMSI is a coding system mandatory for hospital public service and private care facilities

Domicile patient status	
D 001	A.S.A.1
D 002	A.S.A.2
D 003	A.S.A.3
D 004	A.S.A.4

Anesthesia type and anesthesia duration	
No addition No excess of all these lines	
D 010	General anesthesia
D 011	General anesthesia with intubation
D 012	General anesthesia with blood transfusion
D 013	General anesthesia in Trendelenburg position

D 040	30 min	021 BE	D 039	5 h	250 BE
D 041	1 h	050 BE	D 050	5 h 30 min	275 BE
D 042	1 h 30 min	075 BE	D 051	6 h	300 BE
D 043	2 h	100 BE	D 052	6 h 30 min	325 BE
D 044	2 h 30 min	125 BE	D 053	7 h ...	350 BE

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Clusters

- Clusters are the different types of cares (main diagnosis)

Patient	t_0	t_1	t_2	t_3
P_1	I21	E14	I20	I70
P_2	I21	R07	I20	
P_3	I21	E14	I20	I70
P_4	I21	R07	I20	

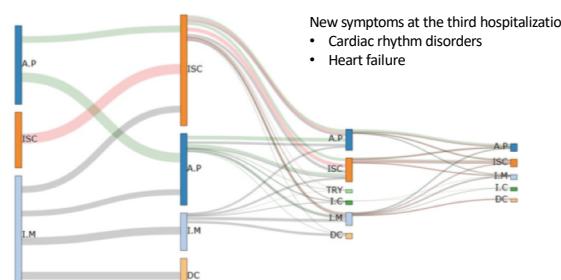
- From 2009 to 2014, all patients having coronary thrombosis as main diagnosis

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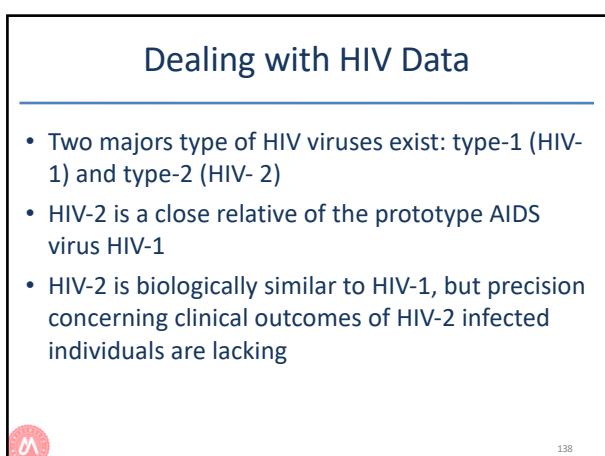
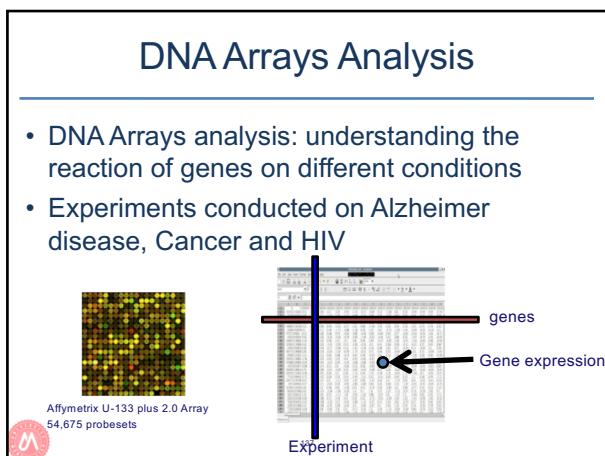
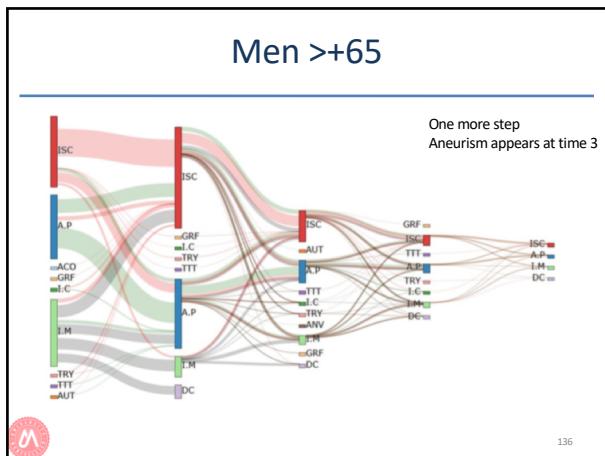
Women > +65

- New symptoms at the third hospitalization:
- Cardiac rhythm disorders
 - Heart failure



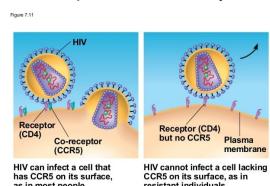
135





Co-receptor CXCR4 – CCR5

- HIV-1 cells invasion is enabled by the binding of envelope glycoproteins to the receptor CD4 and a co-receptor, principally CXCR4 or CCR5, according to the viral strain (X4 or R5, respectively).



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Experiments

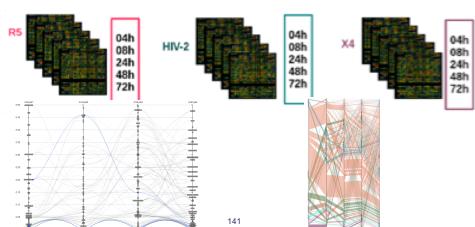
- Expression profile of about 19.000 human genes at 5 points timestamps after infection by one of 3 strains of HIV (HIV-2, X4, R5)

T _{db}		04h	08h	24h	48h	72h
Clusters	C _{db}	c ₁	c ₂	c ₃	c ₄	c ₅
Genes	gene ₁		1		1	1
	gene ₂		1		1	1
	gene ₃	1		1	1	1
	gene ₄	1		1	1	1

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Extracting patterns

- « Real unknown and interesting phenomena. Correlations between biological functions » dixit Biologist. Under investigation



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Trajectories for Tweets

- A tweet:
 - 140 characters
 - Tags (e.g. #saopaulo18, @user), RT (retweet)
 - Metatags (location, date, user-id, ...)
- Cluster of users
- Cluster of words



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Using Tweets

- Identification of patterns of retweets and to understand how information spreads over time in Twitter
- Tweetprofile a research platform for extracting, storing and analyzing the Portuguese Twittosphere for research and journalistic purposes

RetweetPatterns: detection of spatio-temporal patterns of retweets

Tony Rodrigues¹, Tiago Cunha¹, Dino Ienca², Pascal Poncelet³, and Carlos Soares¹



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Experiments

- A set of retweets extracted at the time of the protests in Brazil
- From June 2013 and July 2013 - 17083 tweets extracted from Twitter during a protests period in Brazil
- After a preprocessing : 260 retweets



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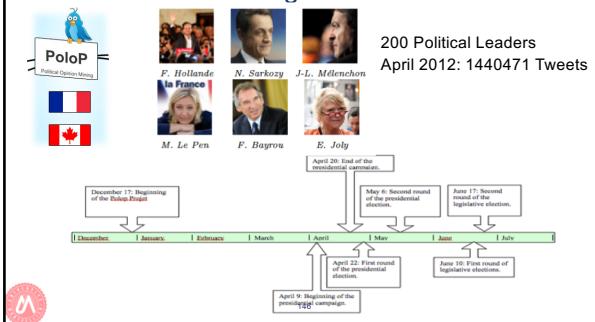
Results

- 18 closed swarms (84 retweets), 5 convoys, 5 moving clusters
- the majority of paths found are located in Rio de Janeiro and São Paulo



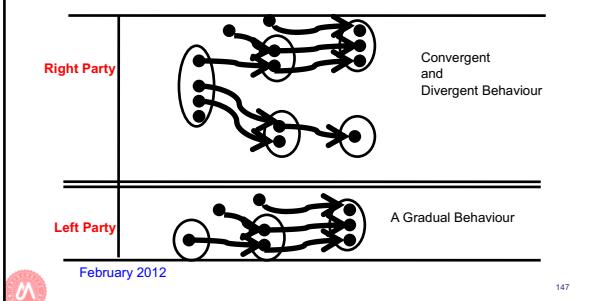
Tweets for Communities

- A set of users sharing the same interest



One trajectory

- "The Debate - The focus of the French election campaign suddenly shifts from the economy to racism and national identity" (07/02/2012)



One trajectory

- "Shootings in Toulouse and Montauban: The victims - Seven people have been killed and two wounded in serial gun attacks in south-western France" (3/2012)

Right Party

Left Party

Convergent and Divergent Behaviour

A Gradual Behaviour

March 2012

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A typical French trajectory

President
May 2012 – May 2017

1980 - 2007
Ségoënne Royal

2005 - 2014
Valérie Trierweiler

2013 -
Julie Gayet

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One trajectory

- "Courage to Olivier Falomi who has not been unworthy, who has battled alongside La Rochelle residents for so many years with unselfish commitment" Valérie Trierweiler, First Lady/Girlfriend of the President François Hollande

Right Party

Left Party

A Convoy or Closed Swarm Behaviour

A Gradual Behaviour

June 2012

Left Party

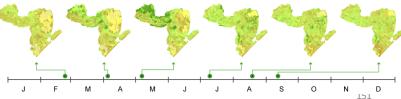
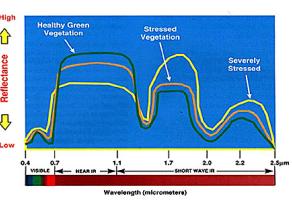
Valérie Trierweiler Ségoënne Royal Left Party

Julie Gayet 150

Satellite Remote Sensing Time Series

Remote sensing possibilities

- Spectral response of natural vegetation
 - Vegetation types
- Textural response
 - Vegetation structure (mapping physiognomic classes, e.g. shrubland and grassland)
- Temporal response
 - Vegetation structure dynamics



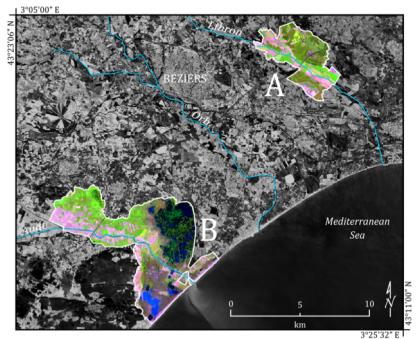
Motivations

- Automatically detect spatiotemporal evolutions (and their related dynamics)
 - how an entity (i.e. a lake, a saltmarsh area, a crop field) evolves along the time
- Provided useful information for natural habitats monitoring and mapping



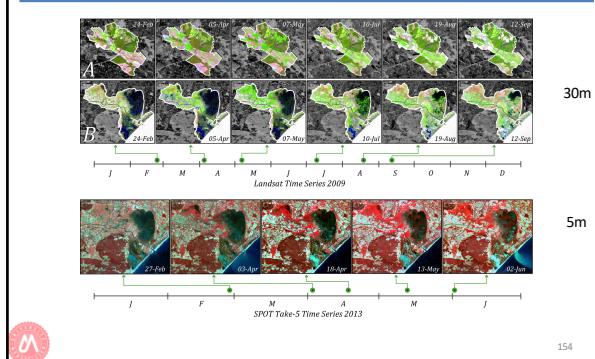
152

A – Libron Valley | B – Low Aude Plane

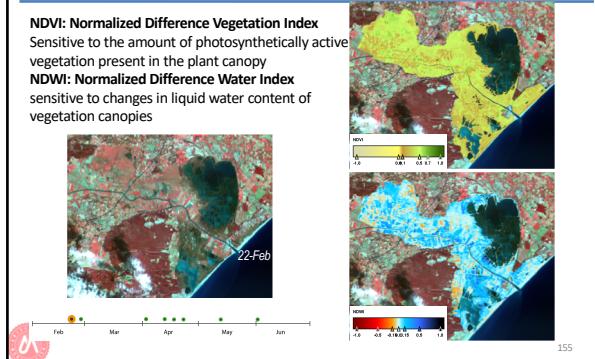


153

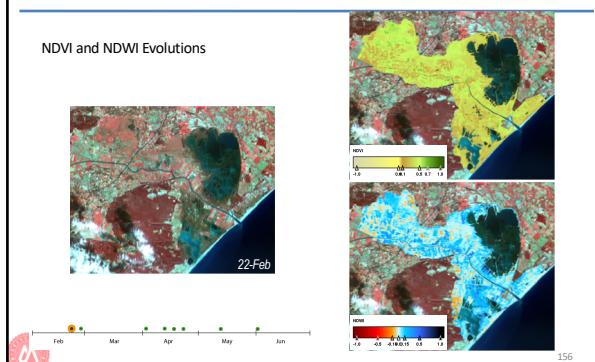
A – Libron Valley | B – Low Aude Plane



General Evolution of the Vegetation

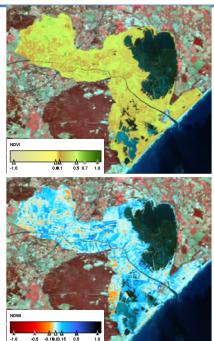


General Evolution of the Vegetation



General Evolution of the Vegetation

NDVI and NDWI Evolutions

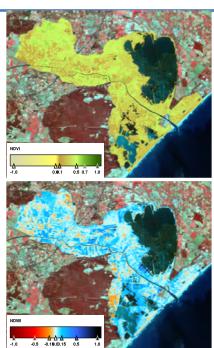


Feb Mar Apr May Jun

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General Evolution of the Vegetation

NDVI and NDWI Evolutions

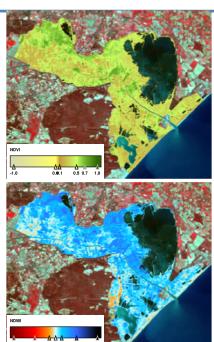


Feb Mar Apr May Jun

158

General Evolution of the Vegetation

NDVI and NDWI Evolutions



Feb Mar Apr May Jun

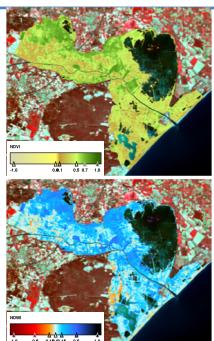
159

General Evolution of the Vegetation

NDVI and NDWI Evolutions



13-Apr
Feb Mar Apr May Jun



160

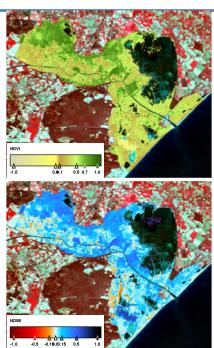


General Evolution of the Vegetation

NDVI and NDWI Evolutions



18-Apr
Feb Mar Apr May Jun



161

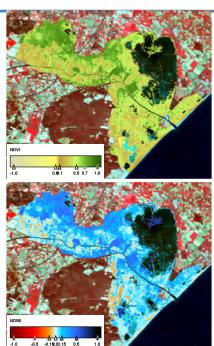


General Evolution of the Vegetation

NDVI and NDWI Evolutions



23-Apr
Feb Mar Apr May Jun

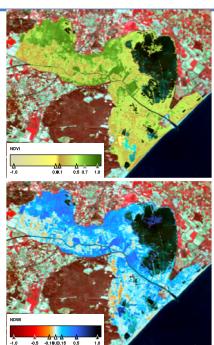


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General Evolution of the Vegetation

NDVI and NDWI Evolutions

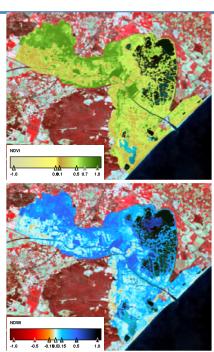


Feb Mar Apr May Jun

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General Evolution of the Vegetation

NDVI and NDWI Evolutions

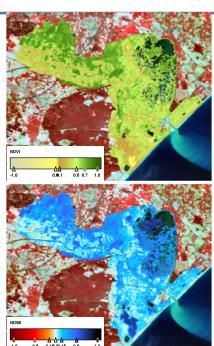


Feb Mar Apr May Jun

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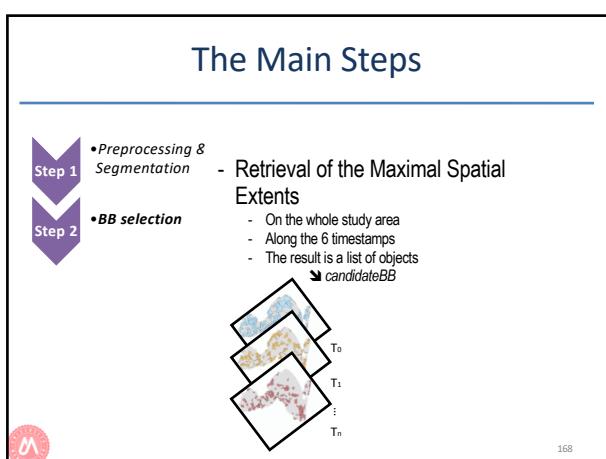
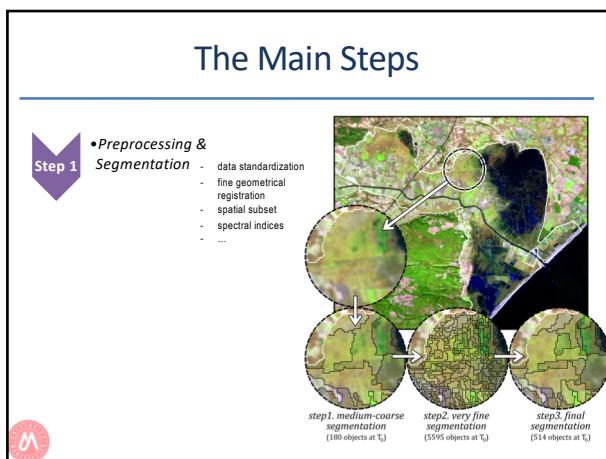
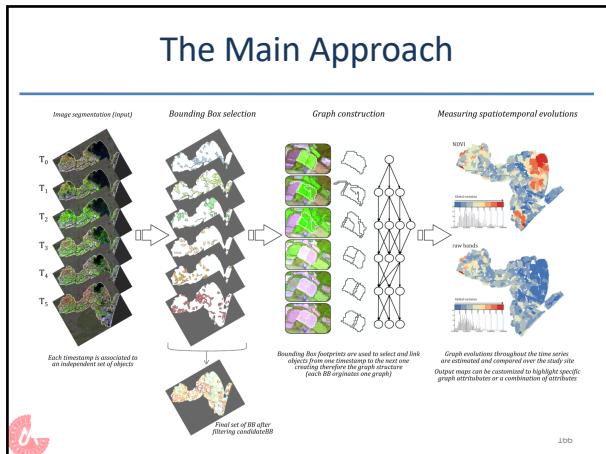
General Evolution of the Vegetation

NDVI and NDWI Evolutions

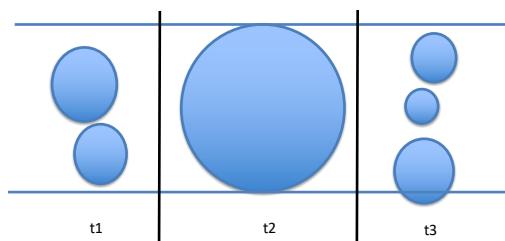


Feb Mar Apr May Jun

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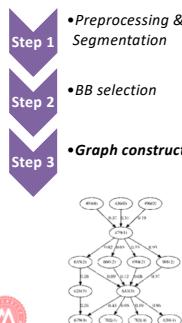
Selection of a Bounding Box



A temporary lake: At t2 it reaches its maximal spatial extent

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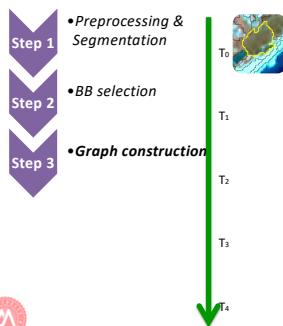
The Main Steps



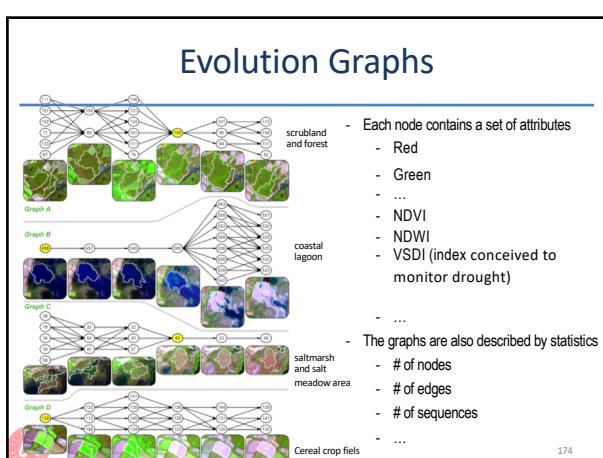
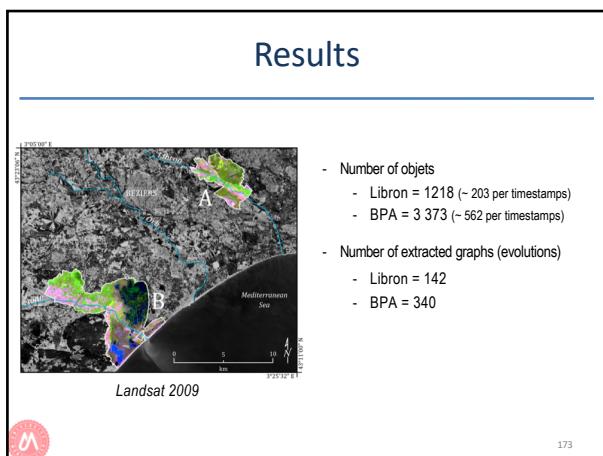
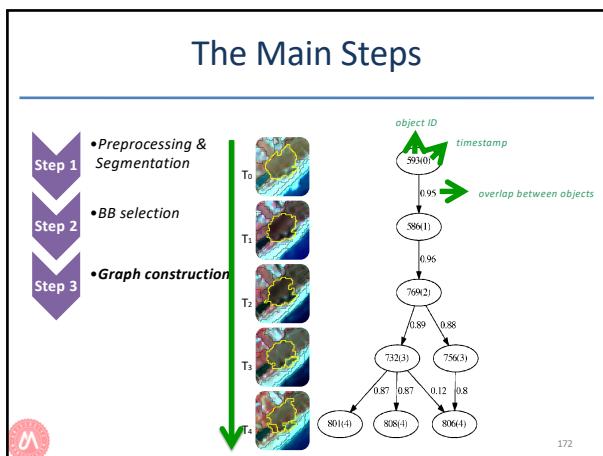
- Each BB is used to build an evolution graph
 - The objects of each graph are chosen following 2 conditions:
 - objet \cap BB \geq 25% of the object surface
 - objet \cap BB \geq 20% of the BB surface

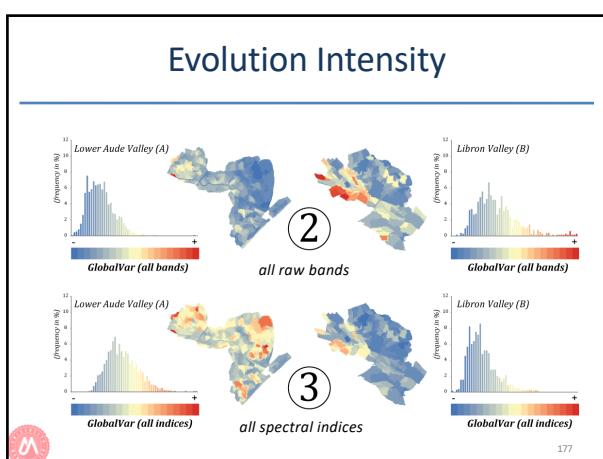
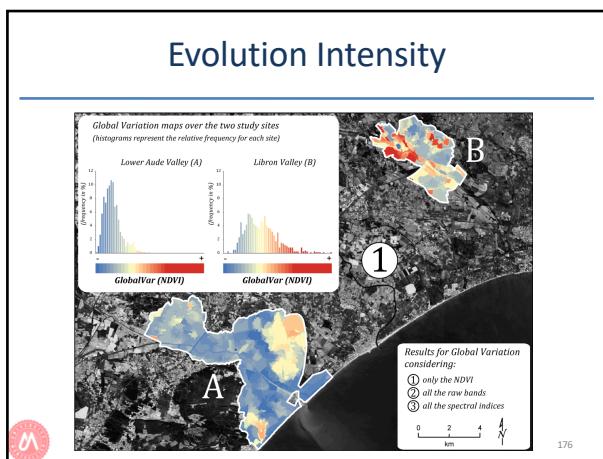
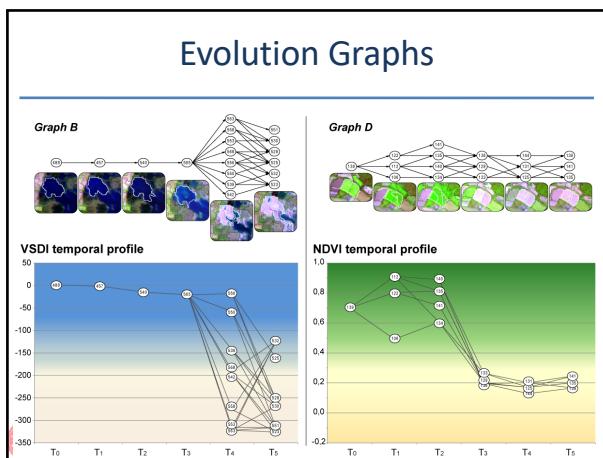
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The Main Steps



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Similar Behaviors

- Clustering approaches to find the region having the same behaviors
- At every timestamp in the graph, the set of attributes is available
- Considering the number of objects that may appear in a graph



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Outline

- A quick reminder on pattern discovery
- The different kinds of patterns from trajectory
- Towards a unified approach for extracting trajectories
- Deal with and without a spatial component?
- **A concrete illustration**
- Conclusion

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Now let's have a concrete example

jupyter TrajectoriesNoteBook Last Checkpoint: il y a 4 heures (autosaved)

This notebook is an example of applying getmove on real trajectories.

In [1] Installation

Running trajectories

```
import matplotlib.pyplot as plt
import matplotlib.cm as cm
from scipy.spatial import distance
import numpy as np
import datetime
from sklearn.cluster import DBSCAN
import pandas as pd
from geopy import geocoders
import json
import os
from geopy import geocoders
```



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Outline

- A quick reminder on pattern discovery
- The different kinds of patterns from trajectory
- Towards a unified approach for extracting trajectories
- Deal with and without a spatial component?
- A concrete illustration
- **Conclusion**



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Conclusions

- Trajectories are useful patterns for ...lots of applications
- They propose new kinds of patterns even when the spatial component is not present
- They have been really well studied and many approaches exist
- There are more and more applications



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Conclusions

- Considering the Pattern Mining issue:
 - Incremental (Objects)
 - Stream Mining
 - New measures for selecting the most interesting patterns
 - Outlier detection
 - Privacy
 - Classification/Clustering of trajectories
 - Interactive Mining
 - Considering the clustering during the process rather than before
 - ...



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Conclusions

- Big Data Issues:
 - Volume
 - Variety
 - Velocity
 - Veracity



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Special Thanks ...

- Jérôme Azé, Nicolas Bechet, Elnaz Bigdeli, Flavien Bouillot, Sandra Bringay, Fati Chen, Tiago Cunha, Jacques Fize, Fabio Gunter, Dino Ienco, Diana Inkpen, Stan Matwin, Jordi Nin, Phan Nhat-Hai, Jessica Pinaire, Yoann Pitarch, Tomy Rodrigues, Mathieu Roche, Arnaud Sallaberry, Carlos Soares, Maguelonne Teisseire, ...
- And many others



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Some Related Publications

- N. Phan, P. Poncelet and M. Teisseire. "All in One: Mining Multiple Movement Patterns". International Journal of Information Technology and Decision Making (IJITDM), June 2016, pp. 1-42
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• Questions ?



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