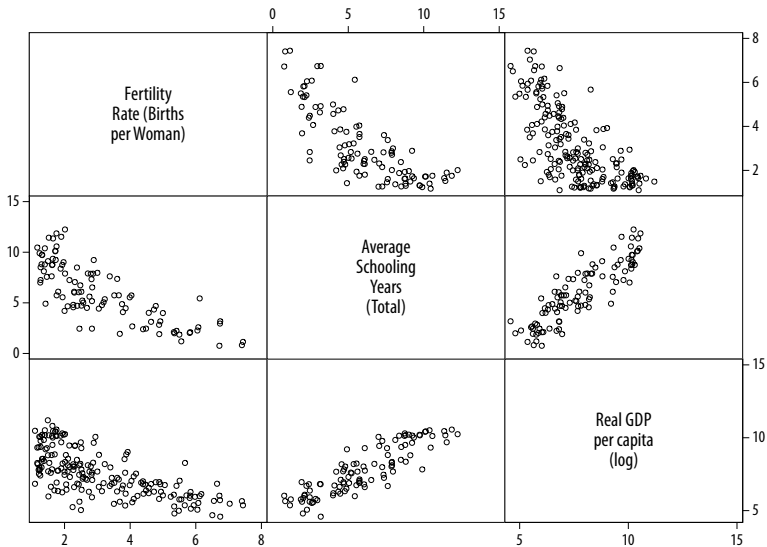


Linear regression

- 1 Multiple linear regression
- 2 Standardized coefficients
- 3 Regression dummies
- 4 Regression diagnostics
- 5 Final paper



Multiple linear regression

```
. reg births schooling log_gdpc
```

Source	SS	df	MS
Model	150.301883	2	75.1509417
Residual	70.475313	83	.849100157
Total	220.777196	85	2.59737878

Number of obs = 86
F(2, 83) = 88.51
Prob > F = 0.0000
R-squared = 0.6808
Adj R-squared = 0.6731
Root MSE = .92147

births	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
schooling	-.1976117	.0724595	-2.73	0.008	-.3417306	-.0534927
log_gdpc	-.4703416	.1324501	-3.55	0.001	-.7337796	-.2069036
_cons	7.950304	.6861182	11.59	0.000	6.585642	9.314965

Multiple linear regression

$$Y = \alpha + \beta_1 X_1 + \beta_2 X_2 + \dots + \beta_k X_k + \epsilon$$

Partial derivatives

Each coefficient is calculated by **holding all others constant**.

Least squares

The model is still optimized by minimizing the squared error terms.

Sanity check

The model is still assuming *linear, additive* relationships.

Logarithmic coefficients: see [UCLA mini-guide](#)

Linear-linear relationships: $Y = \alpha + \beta_1 X$

An increase of one unit of X is associated with an increase of β_1 units of Y .

Log-linear relationships: $\ln Y = \alpha + \beta_1 X$

An increase of one unit of X is associated with a $100 \times \beta_1\%$ increase in Y (true effect: $Y \times \exp(\beta_1)$).

Linear-log relationships: $Y = \alpha + \beta_1 \ln X$

A 1% increase in X is associated with a $0.01 \times \beta_1$ unit increase in Y (e.g. $\beta_1 \times \log(1.15)$ for +15% in X).

Log-log relationships: $\ln Y = \alpha + \beta_1 \ln X$

A 1% increase in X is associated with a $\beta_1\%$ increase in Y .

reg births schooling log_gdpc, beta

Each variable can be normalized to fit $\mathcal{D} \sim \mathcal{N}(0, 1)$, so that their **standardized coefficients** have comparable standard deviation units:

births	Coef.	Std. Err.	t	P> t	Beta
schooling	-.1976117	.0724595	-2.73	0.008	-.3686479
log_gdpc	-.4703416	.1324501	-3.55	0.001	-.4800156
_cons	7.950304	.6861182	11.59	0.000	.

(identical output for overall model fit omitted)

Sanity check

Interpret unstandardized coefficients; use standardization only for model comparisons.

Regression dummies and categorical predictors

Single coefficient of dummy X_3

$$Y = \alpha + \beta_1 X_1 + \beta_2 X_2 + \beta_3(0) + \epsilon$$

$$Y = \alpha + \beta_1 X_1 + \beta_2 X_2 + \beta_3(1) + \epsilon$$

The omitted category $X_3 = 0$ is called the **reference category** and is part of the **baseline model** $Y = \alpha$, for which all coefficients are null.

Example

$$Income = \alpha + \beta_1 \cdot \text{age} + \beta_2 \cdot \text{education} + 0 \cdot \text{male} \quad +\epsilon$$

$$Income = \alpha + \beta_1 \cdot \text{age} + \beta_2 \cdot \text{education} + 1 \cdot \text{female} \quad +\epsilon$$

reg births schooling log_gdpc i.region

Categorical variables can be used as **dummies**, i.e. binary recodes of each category that are tested against a **reference category** to provide regression coefficients for the net effect of each category:

births	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
schooling	-.0415563	.0639718	-0.65	0.518	-.1688888	.0857763
log_gdpc	-.742187	.1380037	-5.38	0.000	-1.016876	-.4674975
region						
2	-.6523485	.5803126	-1.12	0.264	-1.807432	.5027349
3	.3682404	.254364	1.45	0.152	-.1380585	.8745393
4	1.411177	.2486027	5.68	0.000	.9163457	1.906008
5	1.167491	.337383	3.46	0.001	.4959471	1.839035
_cons	8.315004	.8006456	10.39	0.000	6.721359	9.908649

(identical output for overall model fit omitted)

Regression diagnostics

Residuals

- `predict yhat`: fitted values
- `predict r, resid`: residuals
- `predict r, rsta`: standardized residuals

Use `rvfplot` for residuals-versus-fitted values plots.

Heteroskedasticity

When the residuals are not normally distributed, the model expresses **heterogeneous variance** (unreliable standard errors).

Examples: *UCLA Regression with Stata*, ch. 2

There are many more diagnostics on display there.

Regression diagnostics

Interaction terms

- Use `vif` to detect variables with $VIF > 10$
- Use `#` and `##` to capture interactions
- Use `c.` to interact continuous variables

(See also `avplot` and partial regression.)

Variance inflation

Variables that strongly interact induce **multicollinearity** ‘inside’ your model, making standard errors unreliable.

Examples: [UCLA Stata FAQ](#)

Search for “comparing coefficients across groups”.

Final paper

Univariate statistics

- Introduction
- Datasets
- Distributions
- Estimation

Assignment No. 1

Bivariate statistics

- Significance
- Crosstabs
- Correlation
- Linear regression

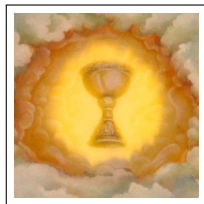
Assignment No. 2

corrected }
revised }
appended }

Statistical modelling

- Basics
- Extensions
- Diagnostics
- Conclusion

Final paper



Final paper

Essential instructions

- Review **paper template**: <http://goo.gl/7u8oa>
- Respect **paragraph limits** mentioned in the template
- Improve **formatting** (styles, citations, fonts. . .)

3-step guide

- 1 **Rewrite** from top to bottom
- 2 **Select** what you report
- 3 **Balance** evidence and analysis

Systematic interpretation

If you forget to interpret your output, you will be thrown into the gaping mouth of the sarlaac that inhabits the Great Pit of Carkoon on planet Tatooine ($p < 0.01$).

And kittens will get hurt.



Systematic references

If you forget to reference your sources, the hideous terror of Cthulhu will arise from the sunken city of R'lyeh to spread the abject curse of the Great Old Ones onto this world ($p < 0.01$).

And kittens will get hurt. Again.
Different ones.

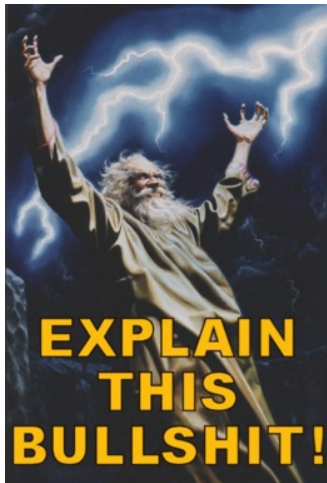


Systematic proofreading

If you forget to proofread your work, a gigantic hole might open in the earth under your feet, and you might burn in the flames of the monstrous Moloc'h for eternity ($p < 0.01$).

And your graders will get angry at their laptops.

All remaining kittens will be decimated without any sign of human mercifulness.



Thanks for your attention

Final paper

- Name your paper and do-file like Briatte_Petev_final
- Make sure to print your paper to a slick PDF
- Email with subject “SRQM: Final paper, *[your names]*”
- Do not forget to copy your partner on all emails

Readings

- *Stata Guide*, Sec. 11 and 13–16



**THIS
IS
STATA**

Congratulations, and thank you.

exit, clear