

# EC2101

## MICROECONOMIC ANALYSIS I

Semester 2 AY 2019/2020  
Dr. Zhang Yang

LECTURE 1

COURSE OVERVIEW

CONSTRAINED OPTIMIZATION

PREFERENCE



Part 1

# Course Overview

# Course Objectives

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- Master key concepts and principles in Microeconomic theory
- Develop a set of analytical tools
  - ▣ Using graphs, mathematics, and logic to make qualitative and quantitative analysis
- Prepare for more advanced modules

# What is Microeconomics?

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- Microeconomics studies how individual economic units make decisions
  - ▣ Individual economic units
    - consumers, households, workers, firms, etc.
  - ▣ Assuming individual economic units seek to maximize their objective function
  - ▣ When facing limited resources

# Basic Information

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- Lecture
  - ▣ L1: Thursday 2:00 pm – 4:00 pm, LT8
  - ▣ L2: Friday 2:00 pm – 4:00 pm, LT9
- Consultation hours
  - ▣ Wednesday 3:00 pm – 5:00 pm
  - ▣ Thursday 4:00 pm – 6:00 pm
  - ▣ Or by appointment
- Contact
  - ▣ AS2-04-36, 6516-6830, [zhangyang@nus.edu.sg](mailto:zhangyang@nus.edu.sg)

# Reading

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## □ Textbook

- ▣ Besanko and Braeutigam, *Microeconomics*, 5<sup>th</sup> edition (international student version), Wiley, 2015 (BB)
- ▣ The 4<sup>th</sup> edition of the book is also acceptable
- ▣ Solutions to textbook exercises
  - Will not be distributed

## □ Slides

- ▣ Available on LumiNUS every Wednesday by 2:00 pm

# Tentative Course Outline

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- Part 1 Consumer Theory
  - ▣ Week 1-4, BB: Chapter 3-5
- Part 2 Exchange (General Competitive Equilibrium)
  - ▣ Week 5-6, BB: Chapter 16 + additional reading on LumiNUS
- Part 3 Production and Costs
  - ▣ Week 8-10, BB: Chapter 6-8
- Part 4 Competitive Markets
  - ▣ Week 11-13, BB: Chapter 9-10



# EC2101 and EC1101E/EC1301

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- EC1101E/EC1301
  - ▣ Introductory level
  - ▣ Focus on knowing basic concepts
  - ▣ Limited mathematics
- EC2101
  - ▣ Intermediate level
  - ▣ Focus on understanding economic models
  - ▣ Uses calculus

# EC2101 and EC3101

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- Think of EC2101 and EC3101 as one big course
  - ▣ EC2101 covers first half
    - Consumer theory
    - Producer theory
    - Competitive markets
  - ▣ EC3101 covers second half
    - Advanced topics in consumer theory
    - Monopoly and oligopoly markets
    - Game theory
    - Uncertainty and asymmetric information

# Blended Learning

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- Blended learning means
  - ▣ Face-to-face lecturing + online learning
- Blended lectures
  - ▣ Lecture 1 (week 1, optional)
  - ▣ Lecture 3 (week 3)
  - ▣ Lecture 9 (week 10)
  - ▣ Lecture 12 (week 13)

# What are you supposed to do for a blended lecture?

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## Normal Lectures

- Come to class
- Work on tutorial questions
- Come to tutorial

## Blended Lectures

- *Watch the pre-lecture video*
  - ▣ *10-20 minutes*
- *Take the pre-lecture quiz*
- Come to class
  - ▣ *Participate in in-class exercises via Poll Everywhere*
- Work on tutorial questions
- Come to tutorial

# Other In-Class Activities

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- Fill in the blanks
  - ▣ There are some blanks in the lecture notes to be filled in during lecture
- Concept checks
  - ▣ A few questions will be given at the beginning/end of some lectures to gauge your understanding
  - ▣ Participate via Poll Everywhere

# Use of LumiNUS

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- Announcement
- Files
- Forum
- Gradebook
- Multimedia
  - ▣ Pre-lecture videos
- Quiz
  - ▣ Pre-lecture quizzes
- Web lectures
  - ▣ Webcasts

# Grading

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- Pre-Lecture LumiNUS Quiz 5%
- Homework 15%
- Participation (tutorial) 10%
- Midterm 25%
  - ▣ Closed-book
- Final 45%
  - ▣ Cumulative, closed-book

# Pre-Lecture LumiNUS Quiz

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- There are 3 graded quizzes
  - ▣ Quiz 1 is optional and not graded
  - ▣ Quiz 2 – 4 are graded
- Each quiz contains a few multiple choice questions
- The quizzes test your understanding of the pre-lecture videos
- Grading
  - ▣ 3 attempts are allowed for each quiz
  - ▣ Only the highest score will be recorded
  - ▣ No extension of deadline



# Homework

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- Two group homework
  - ▣ Homework 1 due 17 February at 2 pm
  - ▣ Homework 2 due 6 April at 2 pm
- Each group only needs to submit one copy
- Submit on time to my mailbox
- Late homework policy
  - ▣ 25% of marks will be deducted for each day past the due date

# Homework Groups

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- Why group homework?
  - ▣ Makes discussion legitimate
  - ▣ Forming studying groups is an effective way to learn
- Form a group of 2-3 with your classmates from the same tutorial
- If you really really do not want to work in a group
  - ▣ You have the option of doing individual homework
- Let your tutor know your choice and group members by tutorial 2 (week 4)
- Be a responsible group member!!!

# Tutorials and Practice Problems

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- Tutorials start from week 3
  - ▣ No tutorial in week 7 (midterm week)
- Practice problems will be assigned after each lecture
  - ▣ Starting from week 2
- Solutions to practice problems discussed in tutorials
  - ▣ Students present the solutions
  - ▣ Written solutions will be posted on LumiNUS
- Additional questions will be discussed if time permits

# Grading of Participation

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- Participation graded by tutorial presentations and general participation in tutorials
- Presentation (5%)
  - ▣ Each student presents once (only the first presentation will be graded)
  - ▣ Graded based on effort
    - Not on correctness
- General participation (5%)
  - ▣ Attendance
  - ▣ Participation in tutorial discussions
  - ▣ Volunteer to present more than once

# A Few Words on Presentations

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- Students volunteer for presentations
  - ▣ Your tutor may call someone to present if no one volunteers
- How to present?
  - ▣ Not the same as simply writing down your answer on the board
  - ▣ You need to explain!
  - ▣ When you present, you are the teacher and you are responsible for your classmates' learning

# Exams

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- Midterm
  - ▣ 3 March evening
  - ▣ Makeup midterm offered to students with conflicting schedules
    - 5 March and/or 6 March at regular lecture hours
    - Need to register for makeup midterm in advance
- Final
  - ▣ 28 April 9:00 am to 11:00 am
  - ▣ No makeup final will be offered

# Public Holiday and Rescheduling

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- 24 January (Friday)
  - ▣ Eve of Chinese New Year
  - ▣ No class after 2 pm
- 27 January (Monday)
  - ▣ Chinese New Year
  - ▣ W1-W6 to be rescheduled
- 10 April (Friday)
  - ▣ Good Friday
  - ▣ L2 to be rescheduled

# A Few More Things

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- Attendance of tutorials
  - ▣ Will be taken
  - ▣ Inform your tutor if you have to miss a tutorial and try to go for a makeup
- Past-year questions and questions from other sources
  - ▣ Will not be discussed

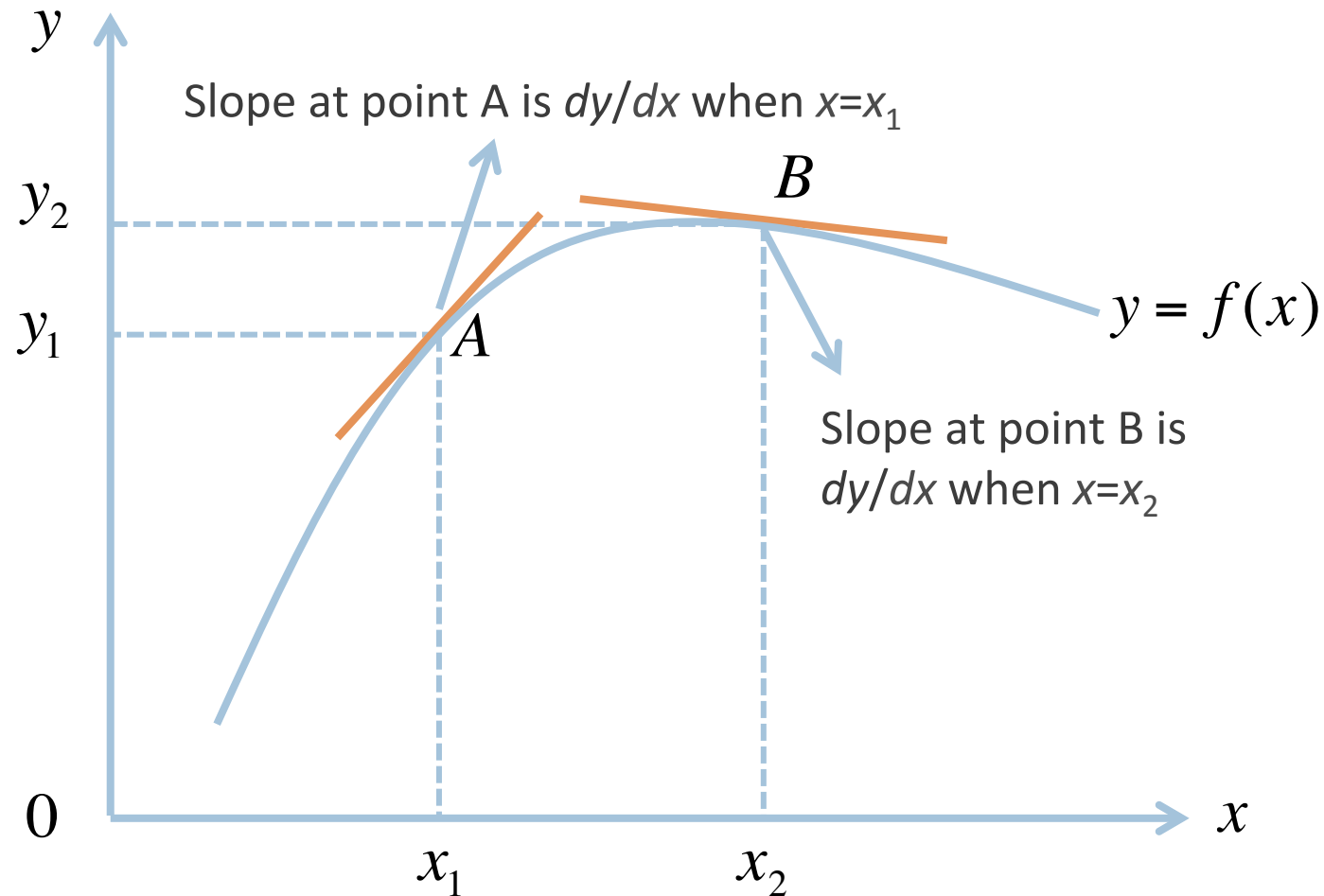


Part 2

# Constrained Optimization

# Review: Derivative and Slope

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Positive derivative: the curve is upward sloping

Negative derivative: the curve is downward sloping

# Unconstrained Optimization with One Variable

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- What is the maximum of the following function?

$$y = -x^2 + 2x + 10$$

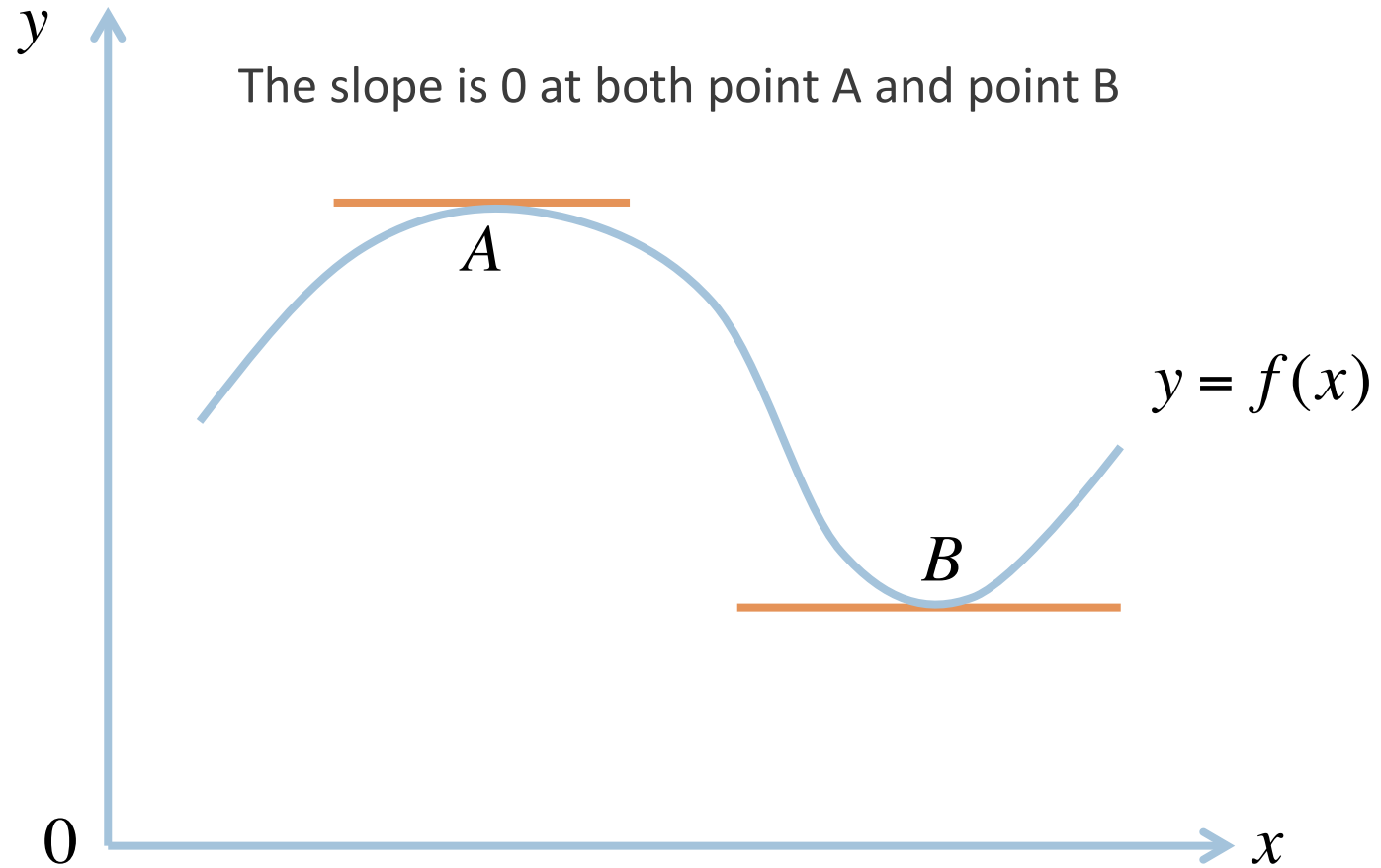
- At the maximum, the slope of the function must be 0 – *the first-order condition*

$$\frac{dy}{dx} = -2x + 2 = 0$$

- At the maximum,  $x=1$
- The maximum value of  $y$  is 11

# Maximum vs. Minimum

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# Second-Order Condition

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- At the maximum,

$$\frac{d^2 y}{dx^2} \leq 0$$

- Using our earlier example,

$$\frac{d^2 y}{dx^2} = \frac{d(-2x + 2)}{dx} = -2$$

- At the minimum,



# Unconstrained Optimization with Two Variables

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- Suppose you want to find the maximum of

$$f(x, y) = -x^2 + 2x - y^2 + 4y + 5$$

- Same idea – two first-order conditions



$$\frac{\partial f}{\partial x} = -2x + 2 = 0$$

$$\frac{\partial f}{\partial y} = -2y + 4 = 0$$

- The function reaches its maximum when  $x=1$  and  $y=2$ , and the maximum is 10

# Constrained Optimization

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- Suppose you still want to find the maximum of the same function
- However, now you need to satisfy another equation

$$x + y = 1$$

- This is a *constrained maximization* problem

- ▣ The *objective function* is

$$f(x, y) = -x^2 + 2x - y^2 + 4y + 5$$

- ▣ The *constraint* is

$$x + y = 1$$


# Lagrange Multiplier Method


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- We first rewrite the constraint as 

$$1 - x - y = 0$$

- We then construct the *Lagrangian function*

$$\Lambda(x, y, \lambda) = -x^2 + 2x - y^2 + 4y + 5 + \lambda(1 - x - y) \quad \text{$$

- The new unknown  $\lambda$  is the *Lagrange multiplier*
  - To find the solution to the constrained maximization problem, we just need to maximize the Lagrangian function
- 



# Lagrange Multiplier Method Cont'

33

- There are three first-order conditions,

$$\frac{\partial \Lambda}{\partial x} = -2x + 2 - \lambda = 0$$

$$\frac{\partial \Lambda}{\partial y} = -2y + 4 - \lambda = 0$$

$$\frac{\partial \Lambda}{\partial \lambda} = 1 - x - y = 0$$

- Solving for the three equations, we have

$$x = 0, \quad y = 1, \quad \lambda = 2$$

- The maximum value of the function is 8



# General Form of the Lagrange Multiplier Method

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- The constrained optimization problem is

$$\max_{x,y} f(x,y)$$



$$s.t. \quad g(x,y) = 0$$

- $f(x,y)$  is the objective function
  - $g(x,y)$  is the constraint
- The Lagrangian function is

$$\Lambda(x,y,\lambda) = f(x,y) + \lambda g(x,y)$$

# General Form of the Lagrange Multiplier Method Cont'

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- To find the maximum, we derive the first-order conditions

$$\frac{\partial \Lambda}{\partial x} = \frac{\partial f(x, y)}{\partial x} + \lambda \frac{\partial g(x, y)}{\partial x} = 0$$

$$\frac{\partial \Lambda}{\partial y} = \frac{\partial f(x, y)}{\partial y} + \lambda \frac{\partial g(x, y)}{\partial y} = 0$$

$$\frac{\partial \Lambda}{\partial \lambda} = g(x, y) = 0$$

- Use the three equations for the three unknowns

## Part 3

# Preference

# Key Questions in Consumer Theory

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- Consumer choice
  - ▣ How do consumers choose what to buy and how much to buy?
- Demand function
  - ▣ How do consumers' choices change with prices and income?
- Consumer welfare
  - ▣ How to measure the gain/loss to consumers when prices change?

# Consumer Choice: How do consumers make decisions?

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- Basic assumptions
  - ▣ Consumers are rational
    - Specifically, consumers maximize utility
  - ▣ Consumers face budget constraints
  - ▣ Consumers are fully informed
- What do consumers like?
  - ▣ Preference
- Prices and income
  - ▣ Budget constraint



# Preference

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- How do consumers rank two goods?
- Definition 1.1 A consumer (*strictly*) *prefers* A to B
  - ▣ If the consumer is more satisfied with A than with B
  - ▣ We use the notation  $A \succ B$
- Definition 1.2 A consumer is *indifferent* between A and B
  - ▣ If the consumer is equally satisfied with A or B
  - ▣ We use the notation  $A \approx B$
- Preference is not the same as choice
  - ▣ Preference does not change with prices or income



# Consumption Basket



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	Food	Clothing	All others
Basket 1	40 units	20 units	10 units
Basket 2	50 units	10 units	20 units
Basket 3	30 units	30 units	15 units

- For simplicity, assume a *consumption basket* consists of two goods
  - ▣ For example, food and clothing



# Fundamental Assumptions on Preference

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- Completeness 
  - ▣ For any two baskets  $A$  and  $B$
  - ▣ Either  $A \succ B$  
  - ▣ Or  $B \succ A$
  - ▣ Or  $A \approx B$
- Transitivity 
  - ▣ If  $A \succ B$  and  $B \succ C$ , then  $A \succ C$
  - ▣ Similarly, if  $A \succ B$  and  $B \approx C$  then  $A \succ C$

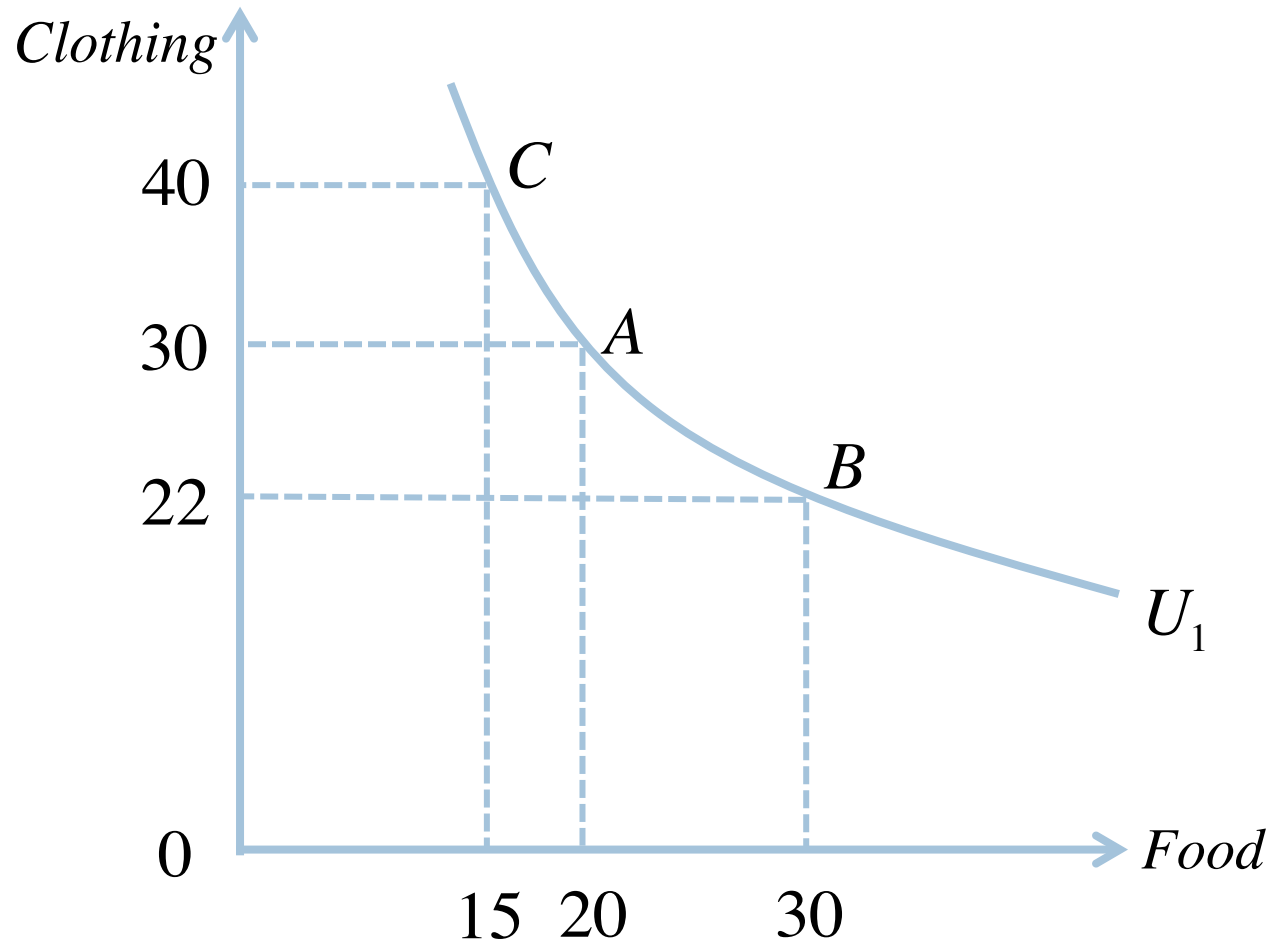
# How to represent preference in graph?

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- Suppose a consumer is indifferent between
  - ▣ A: 20 units of food + 30 units of clothing
  - ▣ B: 30 units of food + 22 units of clothing
  - ▣ C: 15 units of food + 40 units of clothing

# Indifference Curve

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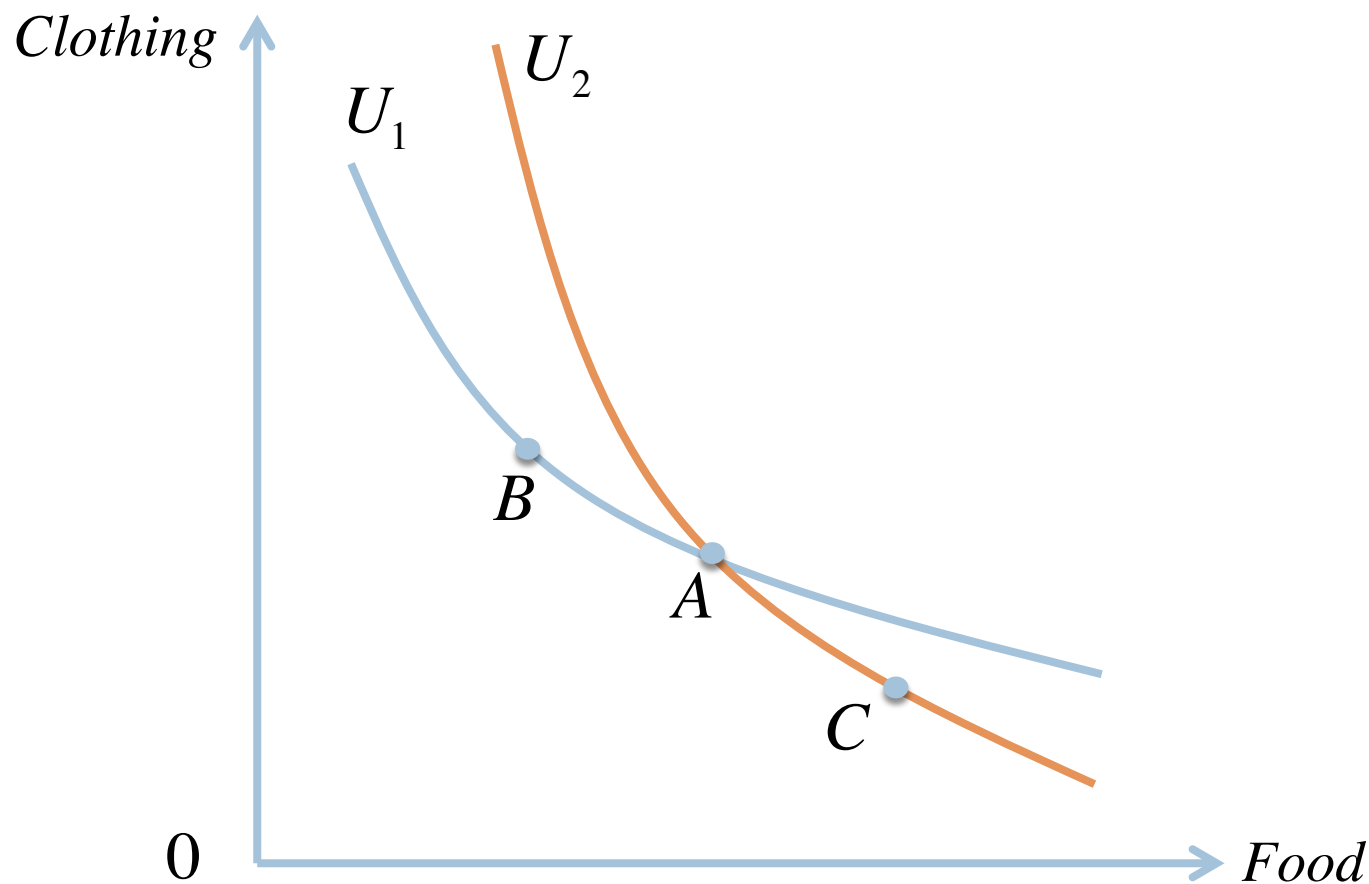


**Definition 1.3** An *indifference curve* connects all consumption baskets that give consumer the same level of satisfaction



# Indifference curves do not cross!

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Since  $A=B$  and  $A=C$   
By transitivity,  $B=C$

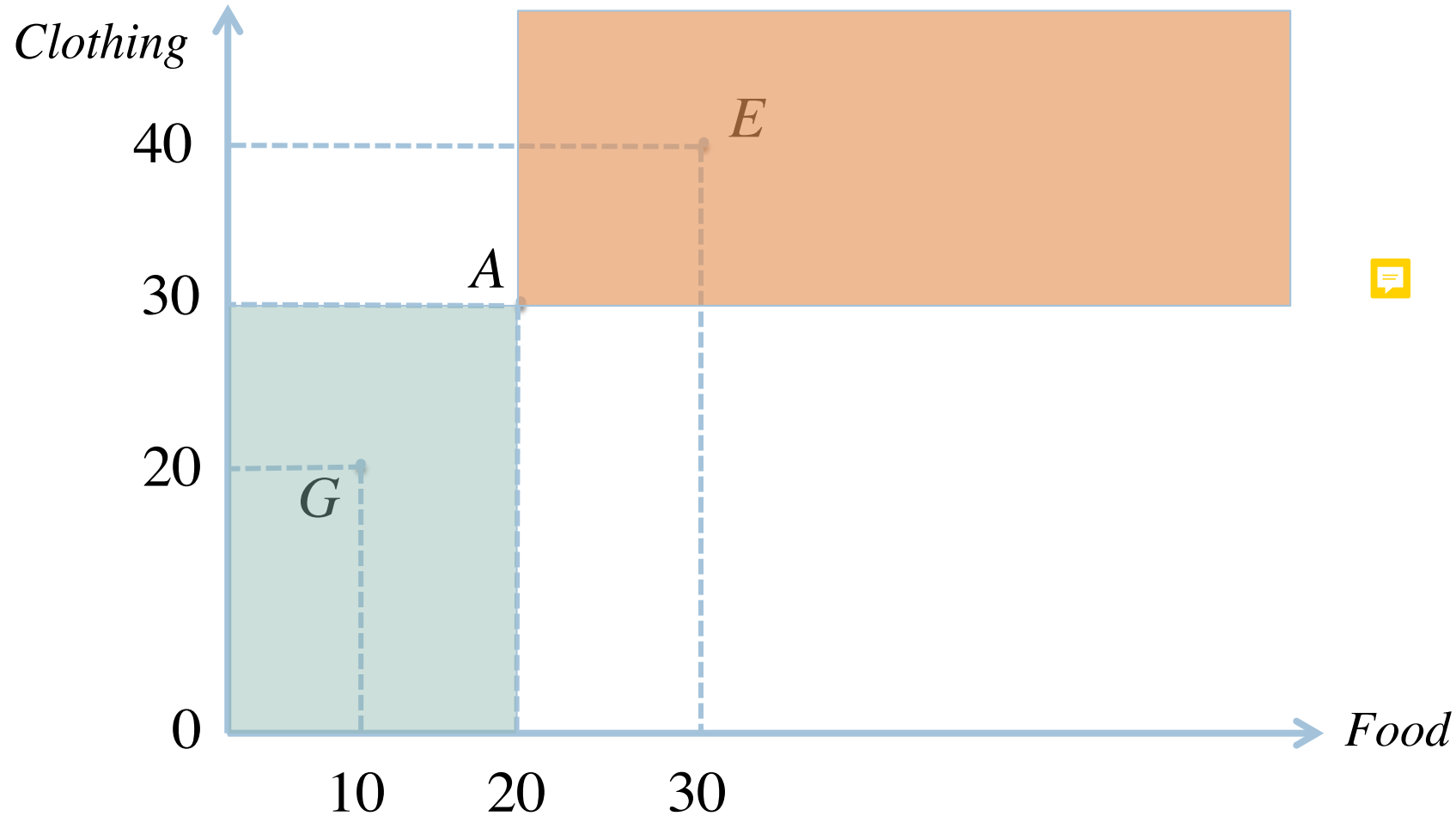
# Another Common Assumption on Preference

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- If “more is better” is satisfied for a good
  - ▣ Consumer likes the good
  - ▣ Consuming more increases satisfaction level
- For example, if “more is better” is satisfied for both food and clothing
  - ▣ 20 units of food + 30 units of clothing preferred to 19 units of food + 30 units of clothing
  - ▣ 20 units of food + 30 units of clothing preferred to 20 units of food + 26 units of clothing
  - ▣ 20 units of food + 30 units of clothing preferred to 18 units of food + 28 units of clothing

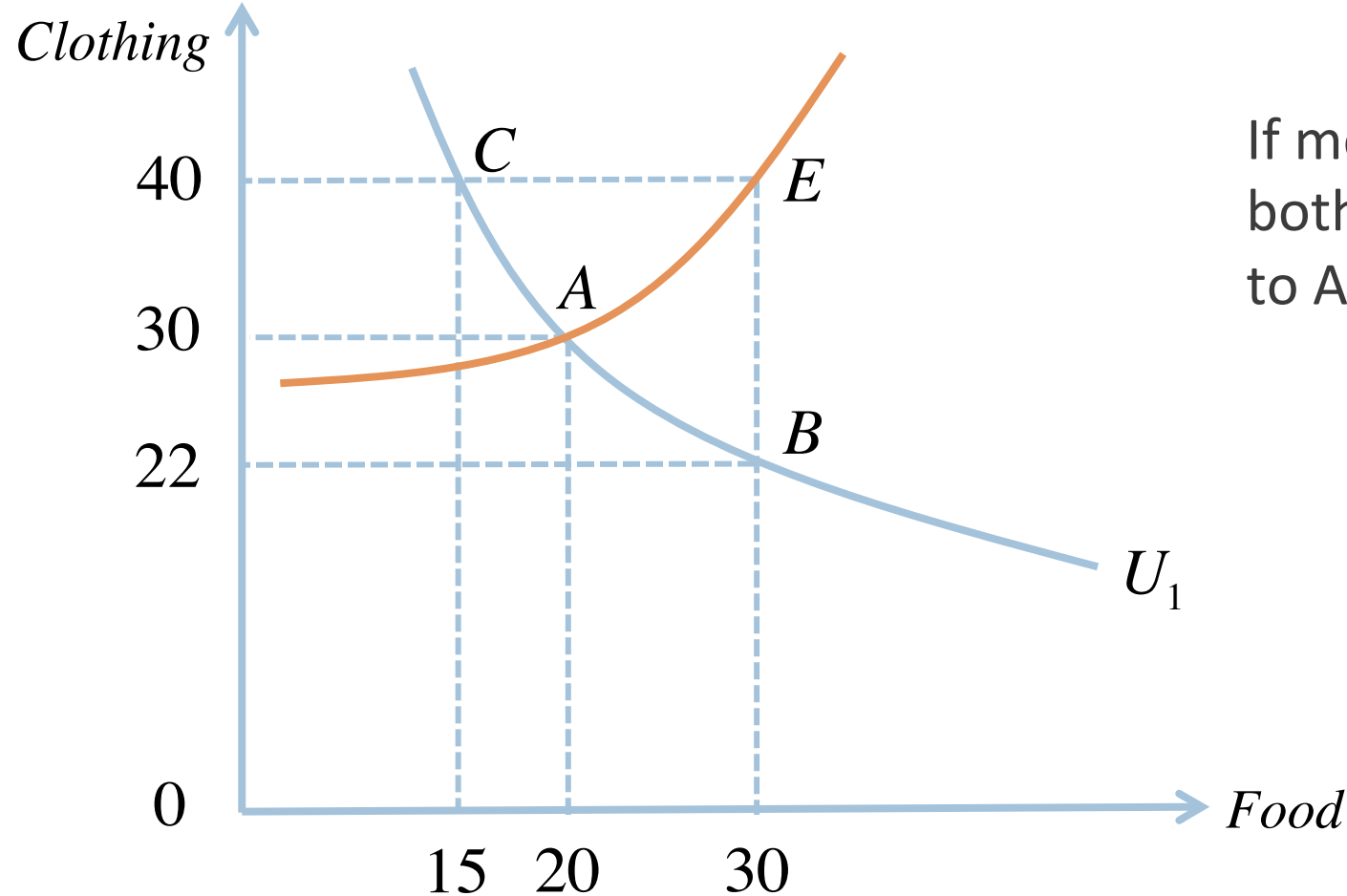
# Which baskets are preferred/less preferred to A?

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# Indifference Curves are Downward Sloping when Consumer Likes Both Goods

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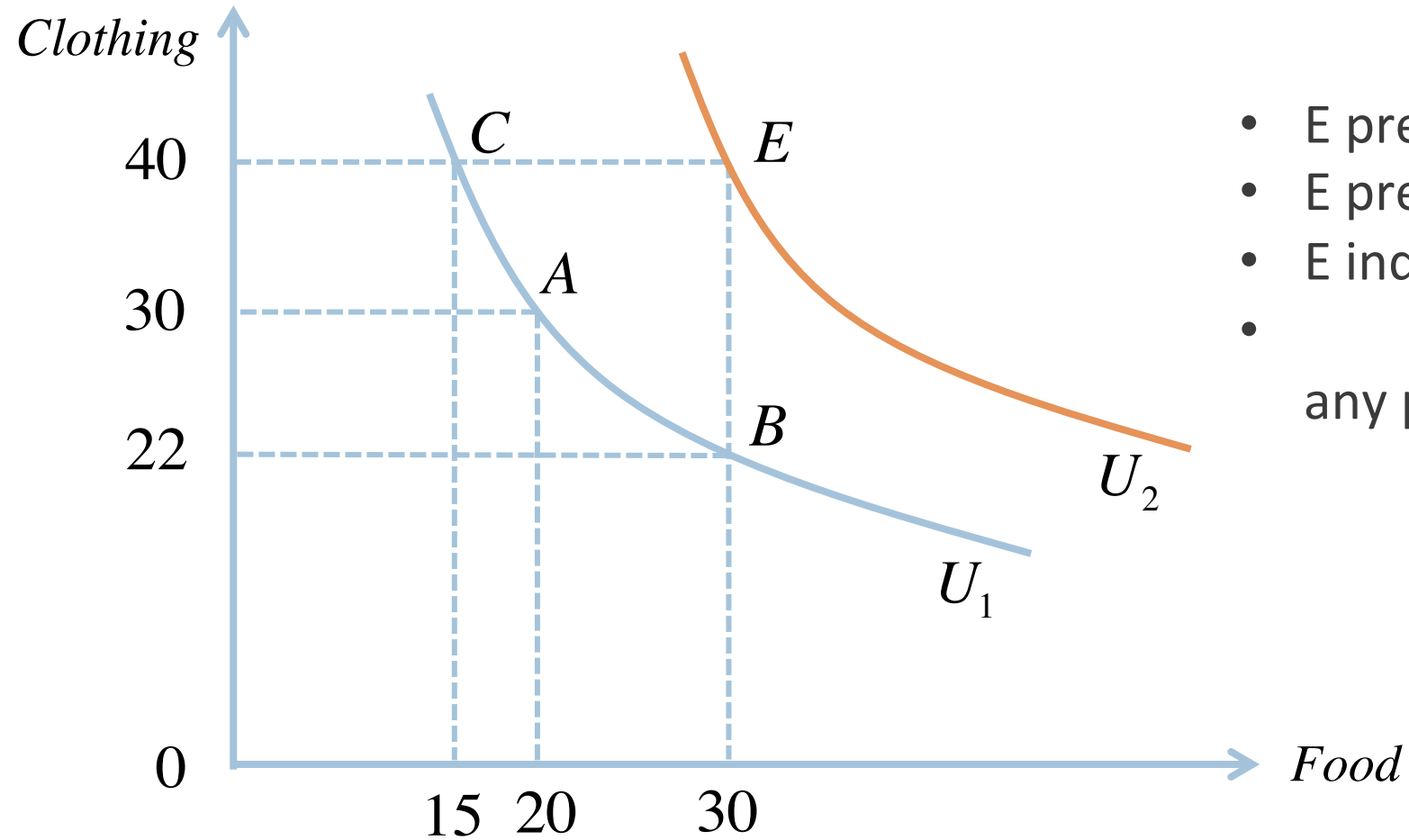




If more is better is satisfied for both goods, E should be preferred to A



# Direction of Preference when Consumer Likes Both Goods

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- E preferred to A
- E preferred to 
- E indifferent to any point on  $U_2$
-  preferred to any point on  $U_1$



# Summary on Three Assumptions

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- We always assume
  - ▣ Completeness
  - ▣ Transitivity
- “More is better” may be violated
  - ▣ E.g., Shin-chan hates “bell pepper” but likes “hamburger”
    - “More is better” not satisfied for bell pepper
    - More bell pepper, lower satisfaction

