

# 1 Introduction

One college:

Proof

$$\ell(f_i(x), 1) + \lambda c(x_z, x) \quad \text{Recourse function} \quad (1)$$

$$\ell(f_i(x), 1) = (1 - f_i(x))^2 \quad \text{Def. of binary cross-entropy} \quad (2)$$

$$(1 - f_i(x))^2 + \lambda c(x_z, x) \quad \text{Logistic function} \quad (3)$$

$$f_i(x) = \frac{1}{1 + e^{-w^T x}}$$

$$(1 - \frac{1}{1 + e^{-w^T x}})^2 + \lambda c(x_z, x) \quad \text{L1 Norm} \quad (4)$$

$$c(x_z, x) = \|x_z - x\|^2$$

$$(1 - \frac{1}{1 + e^{-w^T x}})^2 + \lambda \|x_z - x\|^2$$

$$-\frac{2w^T e^{-w^T x} \left(1 - \frac{1}{e^{-w^T x} + 1}\right)}{(e^{-w^T x} + 1)^2} - 2\lambda (x_z - x) \quad \text{1st derivative} \quad (5)$$

(6)

$$f'(x) = 2 \cdot \frac{-we^{w^T x}}{(1 + e^{w^T x})^2} \cdot (1 - \frac{1}{1 + e^{w^T x}})^2 + -2\lambda(x_z - x) \quad (7)$$

$$f''(x) = \frac{2 \left( \lambda e^{4w^T x} + (4\lambda - w^{2T}) e^{3w^T x} + (6\lambda + 2w^{2T}) e^{2w^T x} + 4\lambda e^{w^T x} + \lambda \right)}{(e^{w^T x} + 1)^4} \quad (8)$$

Two colleges:

$$\ell(f_i(x), 1) + \lambda c(x_z, x) \quad (9)$$

$$f(x) = 1 - \prod_{i=1}^n (1 - f_i(x)) \quad (10)$$

$$f_1(x) = (1 - \frac{1}{1 + e^{w^T x}})^2 \quad (11)$$

$$f_2(x) = (1 - \frac{1}{1 + e^{w^T x}})^2 \quad (12)$$

$$f(x) = 1 - \prod_{i=1}^n (1 - f_i(x)) \quad (13)$$

$$f(x) = 1 - [(1 - (1 - \frac{1}{1 + e^{w^T x}}))^2 \cdot (1 - (1 - \frac{1}{1 + e^{w^T x}}))^2] \quad (14)$$

## 2 Using flalign

Proof

$$\ell(f_i(x), 1) + \lambda c(x_z, x) \quad \text{Recourse function} \quad (15)$$

$$\ell(f_i(x), 1) = (1 - f_i(x))^2 \quad \text{Def. of binary cross-entropy} \quad (16)$$

$$(1 - f_i(x))^2 + \lambda c(x_z, x) \\ f_i(x) = \frac{1}{1 + e^{-w^T x}} \quad \text{Logistic function} \quad (17)$$

$$(1 - \frac{1}{1 + e^{-w^T x}})^2 + \lambda c(x_z, x) \\ c(x_z, x) = \|x_z - x\|^2 \quad \text{L1 Norm} \quad (18)$$

$$(1 - \frac{1}{1 + e^{-w^T x}})^2 + \lambda \|x_z - x\|^2 \\ - \frac{2w^T e^{-w^T x} \left(1 - \frac{1}{e^{-w^T x} + 1}\right)}{(e^{-w^T x} + 1)^2} - 2\lambda (x_z - x) \quad \text{1st derivative} \quad (19)$$

$$(20)$$