

Lecture 3: GWAS in Samples with Structure & Introduction to the REGENIE Software

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Introduction

- ▶ Genetic association studies are widely used for the identification of genes that influence complex traits.
- ▶ To date, hundreds of thousands of individuals have been included in genome-wide association studies (GWAS) for the mapping of both dichotomous and quantitative traits.
- ▶ Large-scale genomic studies often have high-dimensional data consisting of
 - ▶ Tens of thousands of individuals
 - ▶ Genotypes data on a million (or more!) SNPs for all individuals in the study
 - ▶ Many phenotypes of interest such as Height, BMI, HDL cholesterol, blood pressure, diabetes, etc.

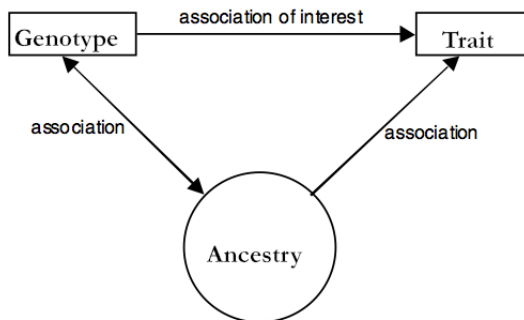
Introduction

- ▶ The vast majority of these studies have been conducted in populations of European ancestry
- ▶ Non-European populations have largely been underrepresented in genetic studies, despite often bearing a disproportionately high burden for some diseases.
- ▶ Recent genetic studies have investigated more diverse populations.

Confounding due to Ancestry

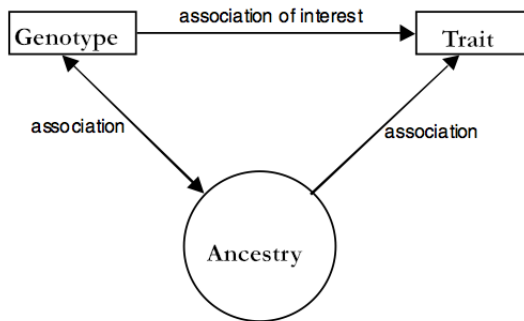
- ▶ The observations in association studies can be confounded by population structure
 - ▶ **Population structure**: the presence of subgroups in the population with ancestry differences
- ▶ Neglecting or not accounting for ancestry differences among sample individuals can lead to **false positive** or **spurious associations**!
- ▶ This is a serious concern for all genetic association studies.

Confounding due to Ancestry



In statistics, a **confounding variable** is an extraneous variable in a statistical model that correlates with both the dependent variable and the independent variable.

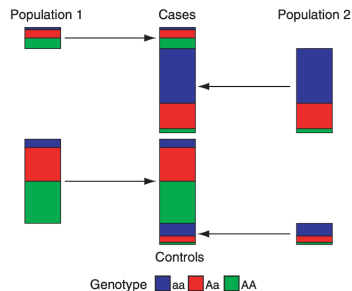
Confounding due to Ancestry



- Ethnic groups (and subgroups) often share distinct dietary habits and other lifestyle characteristics that leads to many traits of interest being correlated with ancestry and/or ethnicity.

Spurious Association

- ▶ Association test aims to compare of allele frequency between cases and controls.
- ▶ Consider a sample from 2 populations:
 - ▶ No differences in allele frequencies between cases/controls **within each population**
 - ▶ Large differences in allele frequencies **between populations**
 - ▶ **Population 2** is overrepresented among cases in the sample.
 ⇒ spurious association between disease and genetic marker



Marchini et al., Nature Genetics, 2004

Genomic Control

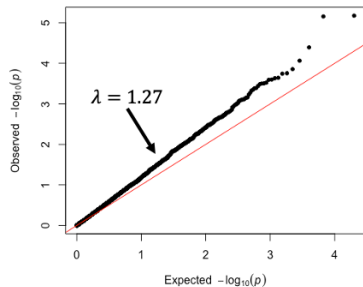
- ▶ Devlin and Roeder (1999) proposed correcting for substructure via a method called "genomic control."
- ▶ If there is no population structure, then **at unlinked variants** the test statistic $T \sim \chi_1^2$.
- ▶ If there is population structure, the statistic will deviate from a χ_1^2 distribution by an approximate constant factor $T \sim \lambda \chi_1^2$ which is estimated as

$$\lambda = \frac{\text{median}(T)}{\text{median}(\chi_1^2)} = \frac{\text{median}(T)}{.456}$$

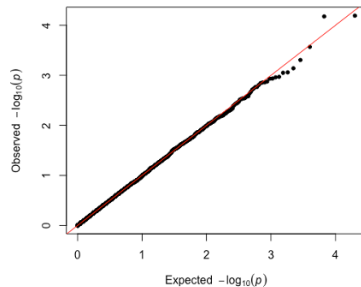
- ▶ It is then applied to the test statistic values at all markers:

$$\tilde{T}_j = \frac{T_j}{\lambda}$$

Genomic Control



Apply GC
 $\xrightarrow{T_j/\lambda}$



LD Score Regression

- ▶ In practice, λ is computed using all variants
- ▶ Polygenicity can cause $\lambda > 1$
 - ▶ Hard to separate confounding from polygenicity when $\lambda > 1$
- ▶ LD score regression separates these by regressing "LD scores" L_j on the test statistics

$$E[T_j] = Nh_g^2/M \cdot L_j + Na + 1$$

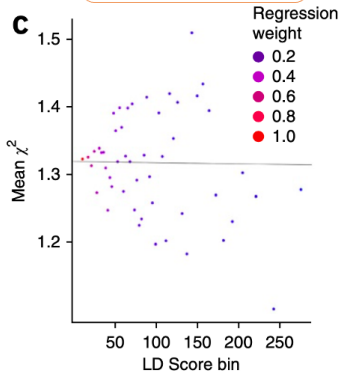
Slope \rightarrow captures polygenicity

Intercept \rightarrow captures confounding

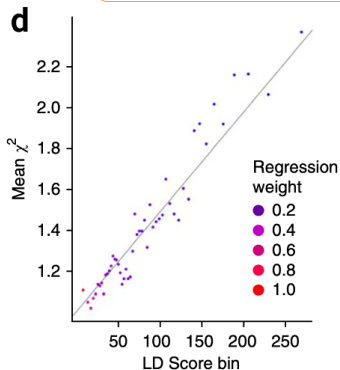
LD Score Regression

$$\lambda = 1.32$$

**Population structure
& no heritability**



**No Population structure
& with heritability**



Bulik-Sullivan, *Nature Genetics*, 2015

Correcting for Population Structure with PCA

- ▶ Principal Components Analysis (PCA) is the most widely used approach for identifying and adjusting for ancestry differences among sample individuals
- ▶ Consider the genetic relationship matrix $\hat{\Psi}$ discussed in the previous lecture with components $\hat{\psi}_{ij}$ for each pair of individuals as:

$$\hat{\psi}_{ij} = \frac{1}{M} \sum_{l=1}^M \frac{(G_{il} - 2\hat{p}_l)(X_{jl} - 2\hat{p}_l)}{\hat{p}_l(1 - \hat{p}_l)}$$

where $G_{il} = \{0, 1, 2\}$ is the genotype value and \hat{p}_l is a corresponding allele frequency estimate at marker l

Correcting for Population Structure with PCA

- ▶ Price et al. (2006) proposed correcting for structure in genetic association studies by applying PCA to $\hat{\Psi}$.
- ▶ They developed a method called EIGENSTRAT for association testing in structured populations where the top principal components (highest eigenvalues) are used as covariates in a linear regression model to correct for sample structure.

$$Y = \beta_0 + \beta_1 G + \beta_2 PC_1 + \beta_3 PC_2 + \beta_4 PC_3 + \cdots + \epsilon$$

$$H_0 : \beta_1 = 0 \text{ vs } H_a : \beta_1 \neq 0$$

Samples with Population Structure and Relatedness

- ▶ Relatedness (family structure or cryptic relatedness) in the sample can lead to spurious association in genetic association studies
- ▶ The EIGENSTRAT method was developed for unrelated samples with population structure
 - ▶ In the presence of relatedness, PCs may not fully capture this finer-scale structure
- ▶ Many genetic studies include relatedness & modeling it directly can lead to improvements in statistical power

Association Testing in Samples with Population Structure and Relatedness

- ▶ Linear mixed models (LMMs) have been demonstrated to be a flexible approach for association testing in structured samples. Consider the following model:

$$\mathbf{Y} = \mathbf{X}\boldsymbol{\beta} + \mathbf{G}_s\boldsymbol{\gamma} + \mathbf{g} + \boldsymbol{\epsilon}$$

- ▶ **Fixed effects:**

- ▶ \mathbf{X} is a $n \times (k + 1)$ matrix of covariates that includes an intercept
- ▶ $\boldsymbol{\beta}$ is the $(k + 1)$ -length vector of covariate effects
- ▶ $\boldsymbol{\gamma}$ is the (scalar) association parameter of interest, measuring the effect of genotype on phenotype

Linear Mixed Models for Genetic Association

$$\mathbf{Y} = \mathbf{X}\boldsymbol{\beta} + \mathbf{G}_s\boldsymbol{\gamma} + \mathbf{g} + \boldsymbol{\epsilon}$$

► Random effects:

- \mathbf{g} is a n -length vector of polygenic effects with $\mathbf{g} \sim N(\mathbf{0}, \sigma_g^2 \boldsymbol{\Psi})$
 - σ_g^2 represents additive genetic variance and $\boldsymbol{\Psi}$ is a $n \times n$ matrix of pairwise measures of genetic relatedness (e.g. kinship matrix, GRM)
 - \mathbf{g} should capture correlation between individuals due to genetic relatedness
- $\boldsymbol{\epsilon}$ is a n -length vector with $\boldsymbol{\epsilon} \sim N(\mathbf{0}, \sigma_e^2 \mathbf{I})$
 - σ_e^2 represents variance due to non-genetic effects assumed to be acting independently on individuals

LMM methods for Quantitative Traits

TECHNICAL REPORTS

nature
genetics

Variance component model to account for sample structure in genome-wide association studies

Hyun Min Kang^{1,2*}, Jae Hoon Sol^{3,4}, Susan K Service⁵, Noah A Zaitlen⁶, Sit-yee Kang⁴, Nelson B Freimer⁴, Chiara Sabatti² & Eleazar Eskin^{3,7}nature
genetics

TECHNICAL REPORTS

Genome-wide efficient mixed-model analysis for association studies

Xiang Zhou¹ & Matthew Stephens^{1,2}

BRIEF COMMUNICATIONS

FaST linear mixed models for genome-wide association studies

Christopher Lippert^{1,2}, Jennifer Langston^{3,4}, Ting Liu¹, Carl M Kadie¹, Robert I Davidson⁵ & David Buckner^{1,2}

the subset size (regardless of how many SNPs are tested) and (3) the RAM is used to densitize these variables, then FaST-LMM produces exactly the same results as a standard LMM but with a run time and memory footprint that is only linear in the cohort size. FaST-LMM also drastically increases the size of datasets that can be analyzed with LMMs and additionally reduces currently variable analysis run times.

Our FaST-LMM algorithm builds on the insight that the maximum likelihood for the restricted maximum likelihood (REML) of an LMM can be written as a function of just a single parameter, λ , the ratio of the genetic variance to the residual var-

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Rapid variance components-based method for whole-genome association analysis

Gulnara B Sotnikova¹, Tatiana I Axenovich¹, Nadezhda M Belongova¹, Cornelia M van Duijn² & Yuri S Aulchenko¹

OPEN ACCESS Freely available online

PLOS GENETICS

Polygenic Modeling with Bayesian Sparse Linear Mixed Models

Xiang Zhou^{1*}, Peter Carbonetto¹, Matthew Stephens^{1,2*}

1 Department of Human Genetics, University of Chicago, Chicago, Illinois, United States of America, 2 Department of Statistics, University of Chicago, Chicago, Illinois, United States of America

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Mixed linear model approach adapted for genome-wide association studies

Zhenzhen Zhang¹, Ethan Eskin², Chao-Qiang Lai³, Rory J Toddhunter⁴, Herment K Thwait⁵, Michael A Gore⁶, Peter J Broadhurst⁶, Jianming Ye¹, Deena K Aronoff¹, Jose M Ordovas^{1,6} & Edward S Buckler^{1,6}

LMMs: Two Step Procedure

- ▶ Many LMM methods use a two-step procedure for GWAS
- ▶ Step 1 considers a null model without the tested SNP of interest (i.e. $\gamma = 0$)

$$\mathbf{Y} = \mathbf{X}\beta + \mathbf{g} + \epsilon$$

- ▶ Obtain parameter estimates to get predictions for the polygenic effects \mathbf{g}
- ▶ Same for all variants tested so only performed once which reduces the computational burden

LMMs: Two Step Procedure

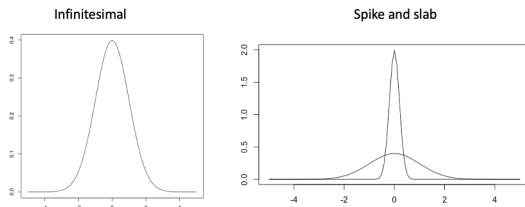
- ▶ In Step 2, association testing of SNP and phenotype ($H_0 : \gamma = 0$) is performed based on the model including the tested SNP

$$\mathbf{Y} = \mathbf{X}\beta + \mathbf{G}_s\gamma + \mathbf{g} + \epsilon$$

- ▶ A score test is performed using the null parameter estimates obtained from Step 1.
- ▶ Use Leave-One-Chromosome-Out (LOCO) scheme in Step 1 so polygenic term doesn't capture effects on tested chromosome (i.e. proximal contamination)

LMMs: Two Step Procedure

- ▶ Many methods differ mainly in Step 1 approach
 - ▶ Model used for the additive polygenic random effect term



- ▶ Algorithm used to obtain parameter estimates
 - ▶ Parameter estimates are obtained using various approaches (e.g. maximum likelihood, restricted maximum likelihood [REML],...)

LMMs on biobank scale data

- ▶ Largest biobanks have gathered data on 100,000s of individuals (e.g. UK Biobank at $N = 500,000$ individuals)
- ▶ Many LMM methods involved computationally expensive operations due to the $N \times N$ GRM

Table 1 Computational cost of EMMAX, FaST-LMM, GEMMA, GRAMMAR-Gamma and GCTA

Method	Building GRM	Variance components	Association statistics
EMMAX	$O(MN^2)$	$O(N^3)$	$O(MN^2)$
FaST-LMM ^a	$O(MN^2)$	$O(N^3)$	$O(MN^2)$
GEMMA	$O(MN^2)$	$O(N^3)$	$O(MN^2)$
GRAMMAR-Gamma	$O(MN^2)$	$O(N^3)$	$O(MN)$
GCTA	$O(MN^2)$	$O(N^3)$	$O(MN^2)$

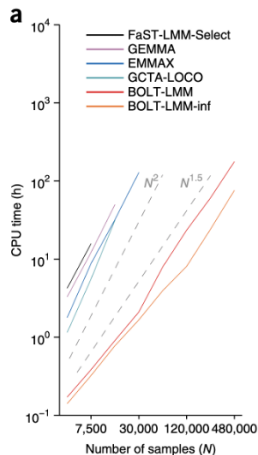
For each method, we list the computational cost of each step.

^aIf $M < N$, the computational cost of FaST-LMM can be reduced to $O(M^2N)$.

Yang et al., *Nature Genetics* 2014

LMMs on biobank scale data

- ▶ Loh et al. (2015) proposed BOLT-LMM which used very efficient algorithms (Variational Bayes) to reduce scaling to $\sim O(MN^{1.5})$ for Step 1 and could be applied to biobank-scale data
- ▶ Jiang et al. (2019) proposed fastGWA which made use of a sparse GRM leading to further improvements for Step 1 $\sim O(MN)$

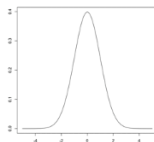


Loh et al., Nature Genetics 2015

LMMs & Whole Genome Regression

- LMMs are closely related to whole genome regression

$$\begin{array}{ccc}
 Y = W\beta + g + \epsilon & \Leftrightarrow & Y = W\beta + \sum_{l=1}^M G_l \theta_l + \epsilon \\
 \uparrow & & \uparrow \\
 N(0, \sigma_g^2 \Psi) & & N(0, \sigma_g^2 / M) \\
 \Psi = GG^T / M & & \\
 \text{GRM using } M \text{ variants} & &
 \end{array}$$



LMMs & Whole Genome Regression

- ▶ LMMs are closely related to whole genome regression

1 parameter

$$Y = W\beta + \textcolor{red}{g} + \epsilon$$



$$N(0, \textcolor{red}{\sigma_g^2} \Psi)$$

$$\Psi = \mathbf{G}\mathbf{G}^T / M$$

GRM using M variants



M parameters

$$Y = W\beta + \sum_{l=1}^M G_l \textcolor{red}{\theta}_l + \epsilon$$



$$N(0, \sigma_g^2 / M)$$

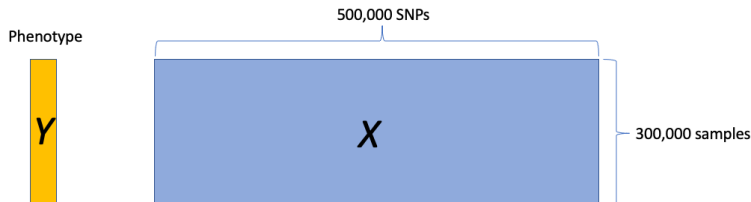
REGENIE: Whole Genome Regression

- ▶ Step 1: computationally efficient whole genome regression

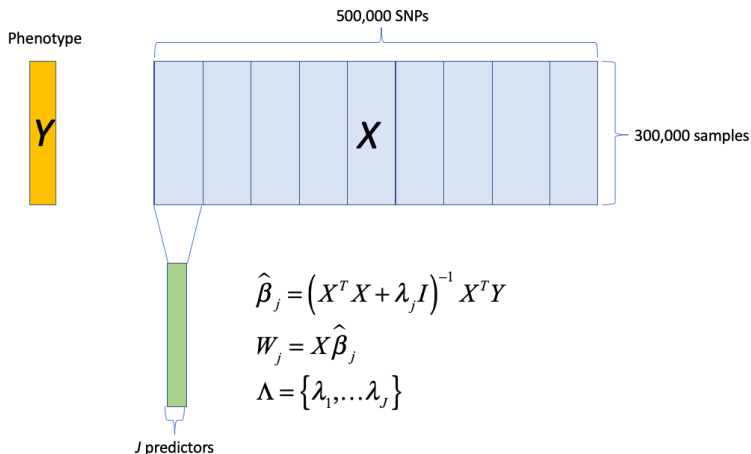
$$\mathbf{Y} = \mathbf{X}\boldsymbol{\beta} + \sum_{l=1}^M G_l \theta_l + \boldsymbol{\epsilon}$$

- ▶ M is usually $\sim 500,000$ SNPs across the genome
- ▶ REGENIE splits genetic data into blocks and run local regressions in each block to reduce computational burden

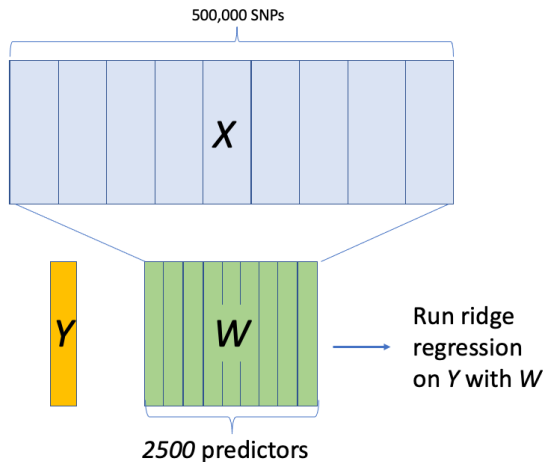
REGENIE: Whole Genome Regression



REGENIE: Whole Genome Regression



REGENIE: Whole Genome Regression



REGENIE: Whole Genome Regression

- ▶ Step 1: computationally efficient whole genome regression

$$\mathbf{Y} = \mathbf{X}\boldsymbol{\beta} + \sum_{l=1}^M G_l \theta_l + \epsilon$$

- ▶ Divide into two levels of regressions
 - ▶ Reads genetic data in blocks and within each block fits ridge regression (penalized linear regression)
 - ▶ Fit another round of ridge regression on all the block predictors
- ▶ Polygenic predictions ($\sum_{l=1}^M G_l \hat{\theta}_l$) capture population structure, relatedness as well as polygenicity

REGENIE: Whole Genome Regression

- ▶ Step 2: test the association parameter γ under the null hypothesis of $H_0 : \gamma = 0$.

$$\mathbf{Y} = \mathbf{X}\boldsymbol{\beta} + G_s\gamma + \sum_{l=1}^M G_l\hat{\theta}_l + \epsilon$$

- ▶ Test on millions of genetic variants (array/imputed/exome)
- ▶ Also works on binary traits where logistic regression is used instead of linear regression

<https://rgcgithub.github.io/regenie/>

References

- ▶ Devlin, B. & Roeder, K. Genomic Control for Association Studies. *Biometrics* **55**, 997-1004 (1999).
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- ▶ Price, A.L. et al. Principal components analysis corrects for stratification in genome-wide association studies. *Nature Genetics* **38**, 904-909 (2006).
- ▶ Yang, J., Zaitlen, N.A., Goddard, M.E., Visscher, P.M. & Price, A.L. Advantages and pitfalls in the application of mixed-model association methods. *Nature Genetics* **46**, 100-106 (2014).

References

- ▶ Loh, P.-R. et al. Efficient Bayesian mixed-model analysis increases association power in large cohorts. *Nature Genetics* **47**, 284-290 (2015).
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- ▶ Mbatchou, J. et al. Computationally efficient whole-genome regression for quantitative and binary traits. *Nature Genetics* **53**, 1097-1103 (2021).