

# **Differential gene regulation**

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Master Thesis in Biostatistics (STA495)

by

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# Preface

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October 2022

# Abstract

Single-cell RNA sequencing data has become more and more popular over the past few years. It allows answering biological questions that with bulk RNA sequencing could not be answered as cell-specific characteristics can be analyzed. In this thesis we investigate, in each cell cluster (e.g. cell type), how the relative abundance of spliced and unspliced reads varies between experimental conditions. Changes to these relative abundances are directly linked to gene regulation, therefore differences in these proportions are taken as a proxy for differences in gene regulation. Methods that are capable of detecting differences in relative abundance already exist (e.g. *BRIE2* and *eisaR*), however they neglect two sources of mapping uncertainty: i) multi-mapping reads across spliced and unspliced versions of a gene, and ii) reads compatible with multiple genes. Therefore, we propose a novel method, *DifferentialRegulation*, that tackles this issue and evaluate the performance of the existing methods (*BRIE2*, *DEXSeq* and *eisaR*) and our novel approach. For this we created two semi-simulated data sets from real mouse kidney single-cell RNA sequencing data to run the methods on. From the analysis we conclude that the two methods that account for mapping uncertainty (*DEXSeq* and *DifferentialRegulation*) have significantly higher TPR and better control of FDR than the methods that ignore mapping uncertainty. Additionally, we looked into stratified results based on gene abundance and observed that the performance of *DifferentialRegulation* is consistent across different levels of gene abundance, as well as robust in terms of FDR calibration. Lastly, we ran a computational benchmark on the mouse kidney data to evaluate the computational burden of each method.

# Chapter 1

## Introduction

### 1.1 RNA sequencing

RNA sequencing (RNA-seq) is a technology for detecting and quantifying the mRNA molecules of a biological sample ([Stark et al., 2019](#)). The invention of RNA-seq was a major breakthrough in the field of bioinformatics that replaced the use of microarray technology in the late 00's. In comparison to microarrays, RNA-seq allows for full sequencing of the whole transcriptome whereas microarrays only profile predefined transcripts through hybridization ([Rao et al., 2019](#)). Further, various protocols have since been derived from the standard RNA-seq protocol, e.g. single-cell RNA sequencing ([Stark et al., 2019](#)).

#### 1.1.1 Bulk RNA-seq

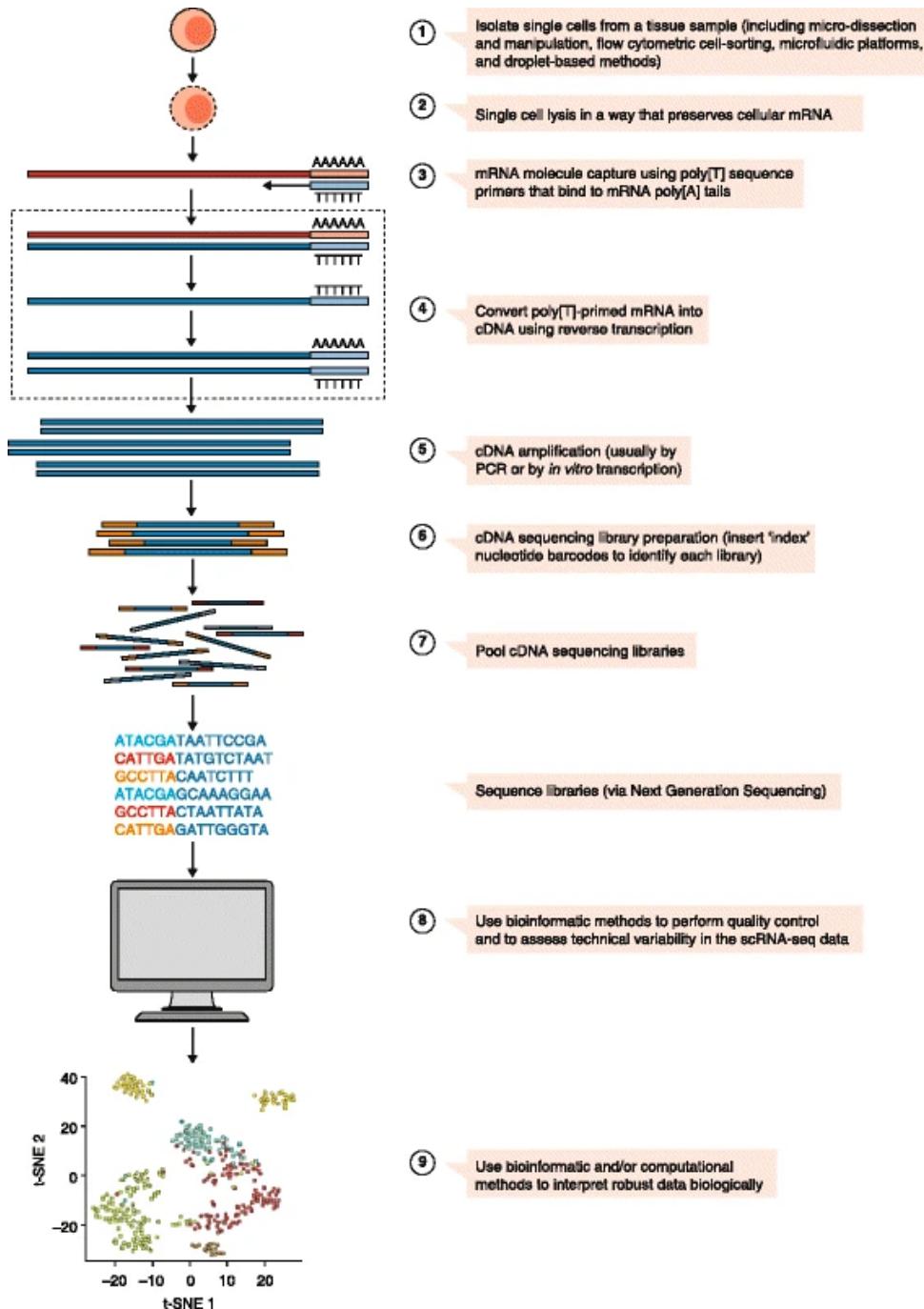
Bulk RNA sequencing allows detecting an aggregated signal across a mixture of cells. There are many applications for bulk RNA-seq. For example, it can be used to study the differences of expression profiles between tissues in healthy vs disease or across treatments ([Stark et al., 2019](#)). However, with bulk RNA-seq one can only estimate the average expression of each gene across a population of cells without regard for the differences between cell types. RNA-seq has several use cases. It can be used to study which genes are turned on in a cell and what their level of transcription is. This allows researchers to understand the biology of a cell at a deeper level. Further, RNA-seq allows the identification of variants and allele specific expression. It is also possible to study the patterns of alternative splicing, which are important to understand their contribution to cell differentiation and human disease.

#### 1.1.2 Single-cell RNA-seq

Single-cell RNA sequencing was developed to overcome some of the limitations of bulk RNA sequencing. With scRNA-seq it is possible to estimate the distribution of expression levels for each gene across a population of cells. This allows answering new biological questions where cell-specific characteristics are important. However, there are some caveats with scRNA-seq ([Haque et al., 2017](#)). scRNA-seq data in general is much more variable than bulk RNA-seq data due to both higher biological and technical variability at single-cell level ([Haque et al., 2017](#)). Figure 1.1 shows the typical workflow of a scRNA-seq experiment. Said workflow is broadly summarized by the following steps:

1. RNA extraction
2. Reverse transcription into cDNA
3. Adapted ligation

4. Amplification
5. Sequencing
6. Downstream analysis using bioinformatics tools



**Figure 1.1:** General workflow of single-cell RNA-sequencing experiments ([Haque et al., 2017](#))

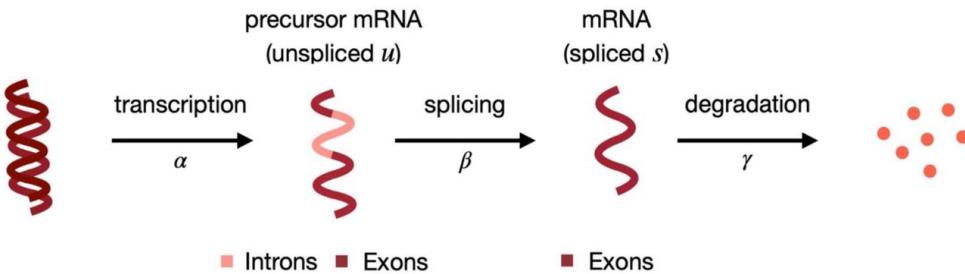
### 1.1.3 Quantification of single-cell RNA-seq data

scRNA-seq data has distinct characteristics that prevent it from being processed by widely used tools developed for bulk RNA-seq data ([He et al., 2022](#)). In general, quantification works by aligning the reads generated from the RNA-seq to the reference genome. There are several tools that allow to do that, notably: STAR ([Dobin et al., 2013](#)), kallisto | bustools ([Melsted et al., 2021](#)) and alevin ([Srivastava et al., 2019](#)). However, there is a difference between the first tool and the other two. STAR is an aligner, whereas the other two tools are mapping tools (pseudo-aligners). The difference between an full-aligner and a mapping tool is that the latter does not look for the exact location of the read, as a consequence pseudo-alignment is much faster than full-alignment. Here we focus on alevin-fry, and the method we have developed, which will be introduced later, has been built to work on the output of alevin-fry.

## 1.2 Objective

### 1.2.1 RNA velocity

We investigate spliced and unspliced reads from scRNA-seq data. During transcription, DNA is decoded into precursor messenger RNA (pre-mRNA). Pre-mRNA contains both coding (exons) and non-coding regions (introns). In a next step, introns are removed from the pre-mRNA which leaves only the mature mRNA. Figure 1.2 shows the process from DNA to mature mRNA, where  $\alpha$  is the transcription rate,  $\beta$  is the splicing rate and  $\gamma$  is the degradation rate.



**Figure 1.2:** The transcription process from DNA to mature mRNA ([Weiler et al., 2021](#))

It was assumed that there is a signal (RNA velocity) detectable in scRNA-seq data that could reveal the rate and direction of change of an entire transcriptome ([La Manno et al., 2018](#)). To quantify the relationship between the abundance of pre-mRNA and mature RNA, a simple system of ordinary differential equations was assumed (1.1): The solution of said system at equilibrium can then easily be estimated and used to explore the regulation of genes:

$$\begin{aligned} \frac{du}{dt} &= \alpha - \beta u \\ \frac{ds}{dt} &= \beta u - \gamma s \end{aligned} \tag{1.1}$$

The derivative of the spliced counts is then defined as the RNA velocity of cells. Thus, the balance of spliced and unspliced counts allows estimating whether a gene is up- or downregulated. If a larger fraction of unspliced counts are present than expected at equilibrium, a gene is likely upregulated. This is because within a short time interval, the newly spliced mRNA will exceed the amount of spliced mRNA which is degraded. Contrarily, if more spliced counts are present at equilibrium than expected, a gene is likely downregulated.

### 1.2.2 Differential regulation

The abundance of spliced and unspliced reads is directly linked to the regulation of genes and RNA velocities. Our idea is to examine how the abundance of spliced and unspliced counts changes between experimental conditions and biological replicates. We translate this intuition into the comparison of two experimental conditions, e.g. healthy vs. disease. Following the same intuitive rationale of RNA velocity, if a gene has a higher abundance of unspliced (spliced) counts in group A compared to group B, then this gene is likely being up-regulated (down-regulated) in group A compared to group B. Thus, we explore the differences in abundance of spliced and unspliced counts to study the differences in regulation between experimental conditions.

If the data contains multiple cell clusters (e.g. cell types), similarly to differential state analyses ([Crowell et al. \(2020\)](#) and [Tiberi et al. \(2021\)](#)) we will perform differential analyses in each cluster of cells, hence identifying cell-cluster/cell-type specific changes between conditions. The idea of performing differential analyses on the abundance of spliced and unspliced or exonic and intronic reads is not completely novel as there are at least two other methods that achieve that: *eisaR* and *BRIE2*.

### 1.2.3 Existing methods

**eisaR** ([Stadler et al., 2020](#)) is a R package implementation that allows for the split analysis between exons and introns. It allows one to measure changes in mature RNA and pre-mRNA across different experimental conditions. Ultimately, eisaR differential testing is based on edgeR ([Robinson et al., 2010](#)). edgeR is a R package that performs differential expression analyses between groups of samples. It implements statistical methods that are based on the negative binomial distribution as a model for count variability.

**BRIE2** ([Huang and Sanguinetti, 2021](#)) is a Bayesian hierarchical model that is implemented in Python and supports the analysis of splicing processes between spliced and unspliced RNA. There are two modes in which the tool can be used. First, the use of differential alternative splicing (DAS), where the aim is to quantify the proportions of alternative splicing isoforms. Second, the use of differential momentum genes (DMG), where the objective is to quantify the proportions of spliced and unspliced RNA in each gene and each cell. In this thesis we focus on the DMG mode as it performs differential testing on the relative abundance of spliced and unspliced reads.

Originally, eisaR and BRIE2 were developed to analyse all cells, but can easily be adapted to perform cell-type specific differential analyses.

### 1.2.4 Mapping uncertainty

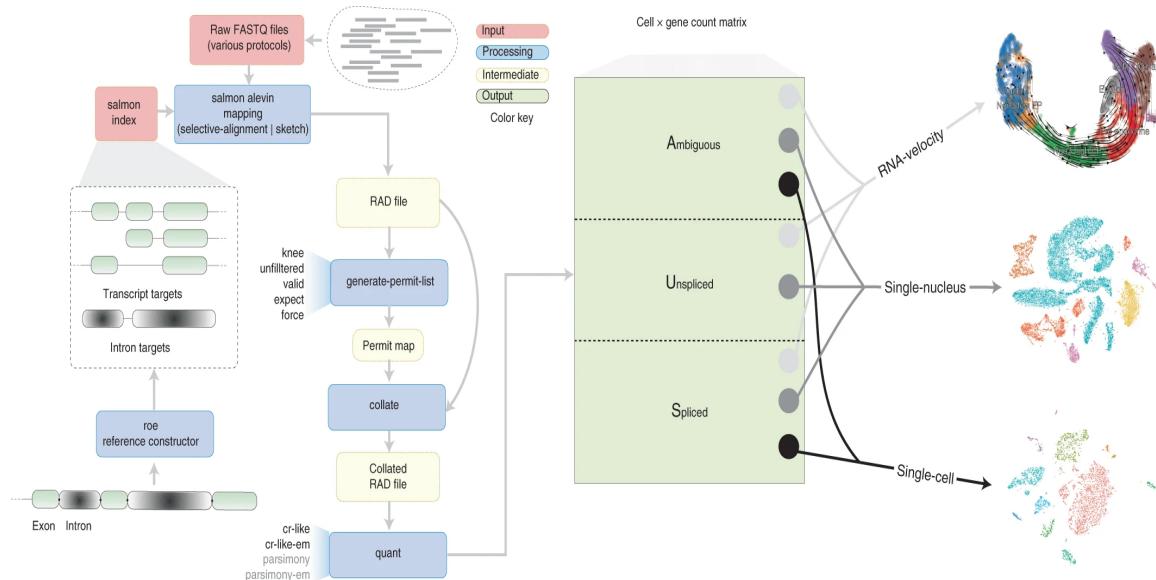
We can identify two main sources of mapping uncertainty concerning spliced and unspliced reads: i) multi-mapping reads across spliced and unspliced versions of a gene, and ii) reads compatible with multiple genes. In fact, it has been shown that many reads (5-40%) map to multiple genes ([Dharshini et al. \(2020\)](#), [McDermaid et al. \(2018\)](#)). In our real data analyses (see Section 3), we found approximately 20-30% of such multi-mapping reads across genes. We additionally found that a significant fraction of reads (6-19%) are compatible with both S and U versions of a gene. Therefore, the estimated spliced and unspliced counts carry a substantial amount of uncertainty, which should be accounted for in downstream analyses. However, both eisaR and BRIE2 use estimated spliced and unspliced counts and neglect the mapping uncertainty. In this thesis, we propose two approaches that account for said mapping uncertainties.

# Chapter 2

## Methods

### 2.1 Alignment and quantification with alevin-fry

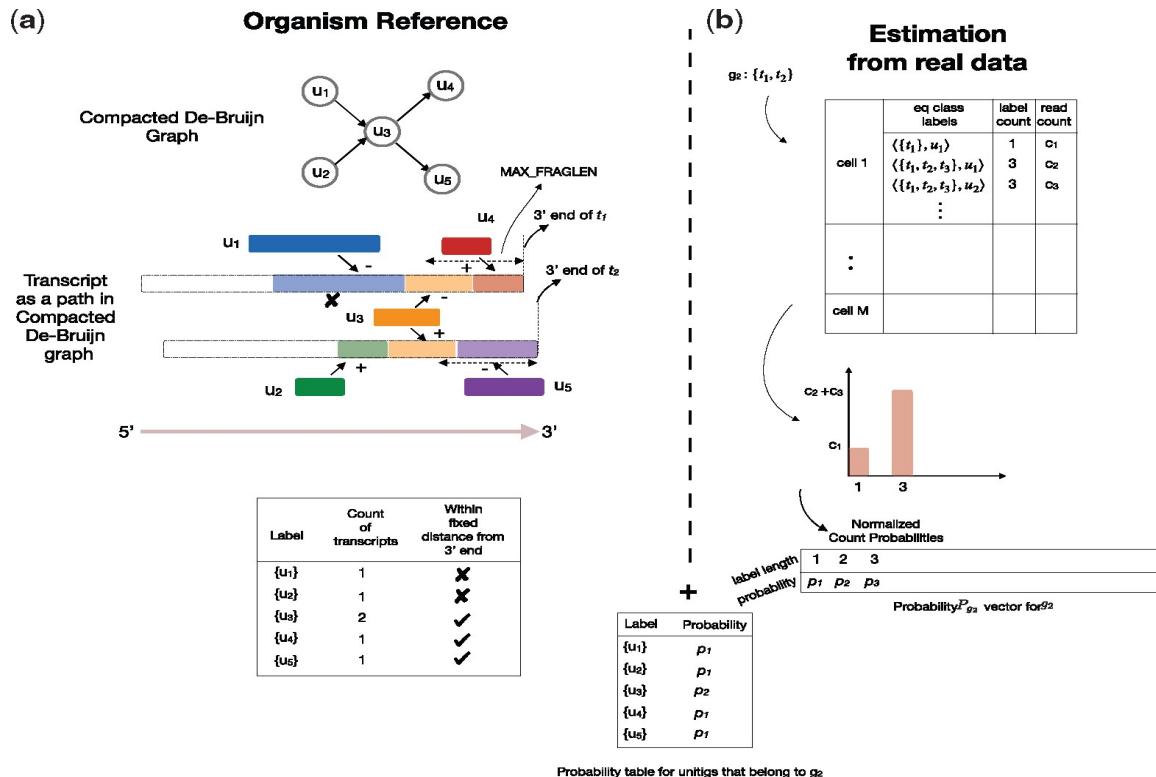
Alevin was developed to tackle the computational challenges that come with scRNA-seq data and to provide a tool that supports technologies other than 10x Genomics. Alevin works in two steps. First, it parses a read file which contains the cellular barcode and a unique molecule identifier to generate a frequency distribution of observed barcodes. Second, it maps the reads to the transcriptome and generates a cell-by-gene count matrix. Alevin-fry (He *et al.*, 2022) was designed to be the successor to alevin and achieves similar accuracy at significantly lower computational costs. It generates a permit list for cellular barcodes that will be quantified in subsequent steps. By using a multi-thread approach, alevin-fry filters and collates the mapping records for permitted cellular barcodes to produce a representation optimized for quantification (He *et al.*, 2022). We use alevin and alevin-fry for our analyses, in particular we focus on alevin-fry as it outputs unspliced, spliced and ambiguous (USA) counts and equivalence classes (EC) that are required by the approaches we propose (i.e. USA counts for *DEXSeq* and ECs for *DifferentialRegulation*).



**Figure 2.1:** Visualization of the *alevin-fry* pipeline from start to finish (He *et al.*, 2022)

## 2.2 Read-level simulation with minnow

*minnow* is a read level simulator for droplet based scRNA-seq data that accounts for important sequence-level characteristics and model effects (Sarkar *et al.*, 2019). It matches the gene-level ambiguity characteristics that are present in real scRNA-seq experiments. With *minnow* it is possible to demonstrate the effect of gene-level sequence ambiguity on accurate quantification, which is used in this thesis to simulate mapping uncertainty between spliced and unspliced counts. It achieves this by either simulating sequences from the underlying de-Bruijn graph of the reference transcriptome or from the reference transcriptome directly (Sarkar *et al.*, 2019). The *minnow* framework essentially works in three steps: (i) selection of transcript, (ii) simulation of cell barcode (CB) and unique molecular identifier (UMI) tagging and (iii) simulation of polymerase chain reaction (PCR), fragmentation and sequencing. PCR is a laboratory technique to rapidly produce millions of copies of a specific DNA segment (Garibyan and Avashia, 2013). First, *minnow* uses a gene-count matrix as input that provides an estimated number of distinct molecules corresponding to each gene and cell in the sample. *minnow* treats the normalized values of a particular cell as a multinomial distribution, then samples such molecules from that distribution (Sarkar *et al.*, 2019). Figure 2.2 illustrates the process from input to simulated reads. *Minnow* is used in this thesis to simulate at the read-level, which are afterwards aligned and quantified with *alevin-fry*. This leads to a realistic simulation, which incorporates multi-mapping uncertainty, whose modelling is the primary objective of this thesis.



**Figure 2.2:** Summary of the two possible pathways of *minnow* from start to simulated reads (Sarkar *et al.*, 2019)

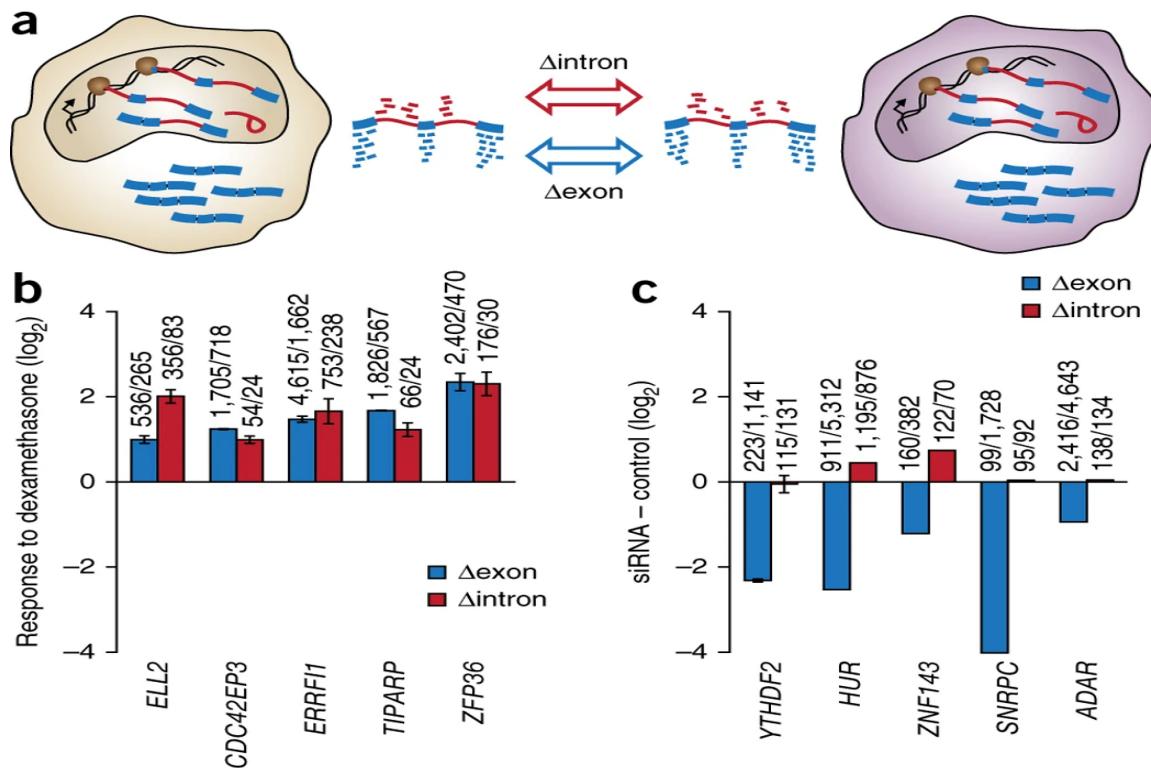
## 2.3 Differential methods

### 2.3.1 *eisaR*

Exon-intron split analysis (EISA) is a computational approach to measure mature RNA and pre-mRNA reads across different experimental conditions (Gaidatzis *et al.*, 2015). The method has been developed to detect changes in up- or down-regulated gene expression. *eisaR* works in multiple steps: first, both exonic and intronic counts are normalized to the mean library size and log-transformed with the addition of a pseudocount; second, genes with very low counts in either exons or introns are removed, such that there is a fixed set of quantifiable genes; third, the statistical analysis of the counts is conducted with the help of the *edgeR* framework (Robinson *et al.*, 2010). The *edgeR* framework is used to examine differential gene expression of replicated count data where the counts are modelled by a negative binomial distribution (2.1), where for the  $g$ -th gene and  $i$ -th sample:

$$Y_{gi} \sim NB(\text{mean} = M_i \rho_{gj}, \text{dispersion} = \phi_g) \quad (2.1)$$

where  $M_i$  is the library size (total counts) for  $i$ -th sample;  $\phi_g$  is the dispersion for the  $g$ -th gene and  $\rho_{gj}$  is the relative abundance of gene  $g$  in experimental group  $j$  which sample  $i$  belongs to and  $NB(a, b)$  denotes the negative binomial distribution with mean  $a$  and dispersion  $b$ .



**Figure 2.3:** Comparison of exonic and intronic changes for single genes under controlled transcriptional and post-transcriptional perturbations (Gaidatzis *et al.*, 2015)

### 2.3.2 *BRIE2*

*BRIE2* is a scalable computational method that regresses single-cell RNA-seq data against cell-level features (Huang and Sanguinetti, 2021). Unavoidable difficulty in the quantification arises from the fundamental ambiguity of the data, because a majority of reads cannot be mapped

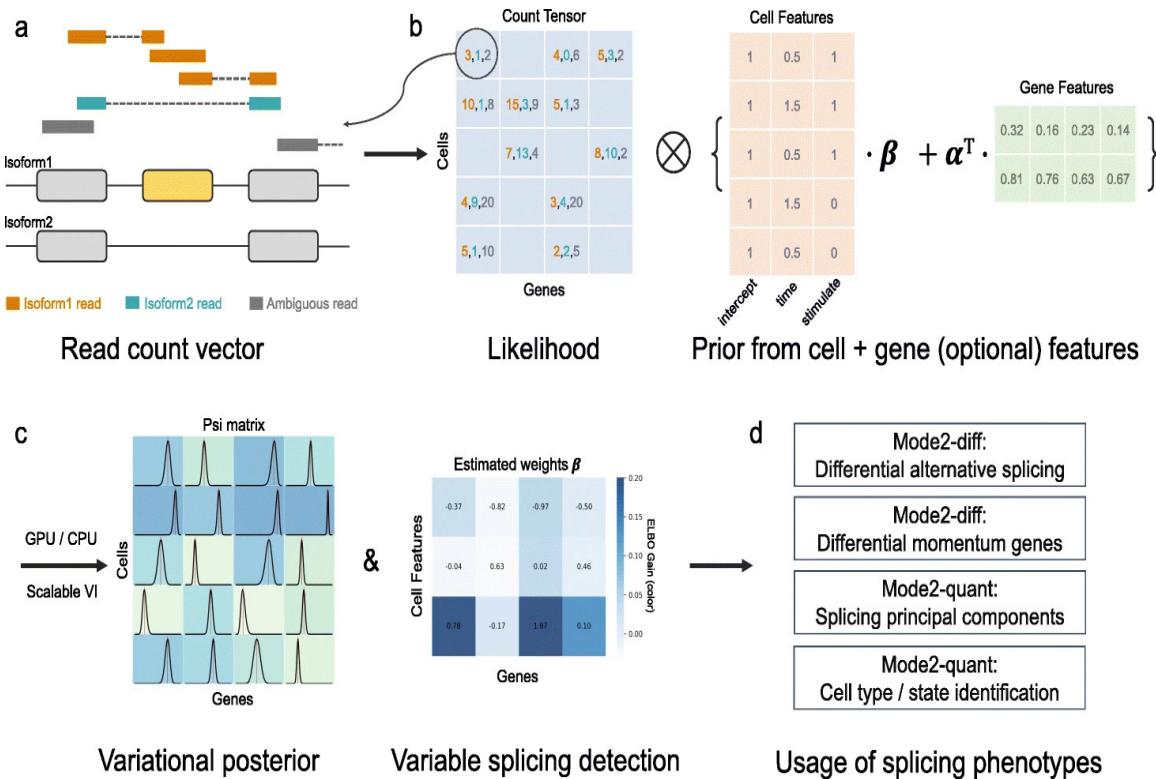
unambiguously to a single isoform. *BRIE1* tackled this issue by regressing percentage of spliced-in (PSI) values through a Bayesian regression approach. However, *BRIE1* is not well suited to quantify differential splicing across cell types because sequence features are usually the same between individual cells (Huang and Sanguinetti, 2021). *BRIE2* again starts from a latent regression framework, however, it differs from *BRIE1* in two important ways: first, it augments the set of regressor features by including cell-specific information e.g. cell type; second, the added complexity considerably increases the computational cost. Therefore, because of its elevated computational complexity, *BRIE2* was developed to be used in conjunction with advanced software e.g. Tensorflow and graphics processing units (GPUs), which significantly increases computational acceleration. Figure 2.4 summarizes the process from input to output in the *BRIE2* pipeline.

Equations (2.2) and (2.3) are the two posterior distributions where  $t$  denotes all cell features except feature  $t$ . In our case we only have one cell feature which is the group allocation, as we run *BRIE2* on all cell types individually. The two posterior distributions represent the two models - Model 0 with no effects and Model 1 with significant effects:

$$M_0 : p_g^{(0)} = \prod_{c=1}^M p(s_{c,g}|z_{c,g})N(z_{c,g}|y_{c,t} \cdot 0 + y_{c,t}^\top \beta_{g,t}, \sigma_g^2) \quad (2.2)$$

$$M_1 : p_g^{(1)} = \prod_{c=1}^M p(s_{c,g}|z_{c,g})N(z_{c,g}|y_{c,t} \cdot \beta_{g,t} + y_{c,t}^\top \beta_{g,t}, \sigma_g^2) \quad (2.3)$$

where  $N(z_{c,g}|y_{c,t} \cdot \beta_{g,t} + y_{c,t}^\top \beta_{g,t})$  denotes the normal distribution with mean



**Figure 2.4:** Summary of the estimation process of *BRIE2* (Huang and Sanguinetti, 2021)

### 2.3.3 *DEXSeq*

*DEXSeq* (Anders *et al.*, 2012) is a statistical method originally proposed to test for differential exon usage in RNA-seq data, which has been widely adopted in other contexts too, such as differential transcript usage (Love *et al.*, 2018). The model is based on the negative binomial distribution and allows for covariates such as batch effects to be taken into account to offer reliable control of false discoveries (Anders *et al.*, 2012). In its original implementation *DEXSeq* inputs how many reads map to each exon, but the method has also been used on transcript level counts [(Love *et al.*, 2018), (Tiberi and Robinson, 2020)]. Equation (2.4) shows that the read counts follow a negative binomial distribution where  $\alpha$  is the dispersion parameter. Further, a generalized linear model is used to predict the mean via a log-linear link, where for gene  $i$ , exon  $l$  and sample  $j$ :

$$K_{ijl} \sim \text{NB}(\text{mean} = s_j \mu_{ijl}, \text{dispersion} = \alpha_{il}) \quad (2.4)$$

$$\log(\mu_{ijl}) = \beta_i^G + \beta_{il}^E + \beta_{i\rho_j}^C + \beta_{i\rho_j l}^{EC} \quad (2.5)$$

where  $\text{NB}(a, b)$  denotes the negative binomial distribution with mean  $a$  and dispersion  $b$ ,  $\alpha_{il}$  is the dispersion parameter;  $s_j$  is the size factor for the  $j$ -th sample;  $\mu_{ijl}$  is the expected value of the concentration of cDNA fragments of the  $l$ -th exon of  $i$ -th gene in sample  $j$ ;  $\rho_j$  is the group sample  $j$  belongs to;  $\beta_i^G$  is the baseline expression strength of gene  $i$ ;  $\beta_{il}^E$  is the coefficient for the  $l$ -th exon in gene  $i$ ;  $\beta_{i\rho_j}^C$  is the coefficient for the group  $\rho_j$  in gene  $i$ ;  $\beta_{i\rho_j l}^{EC}$  is the exon-condition interaction term for condition  $\rho_j$  and exon  $l$  in gene  $i$ .

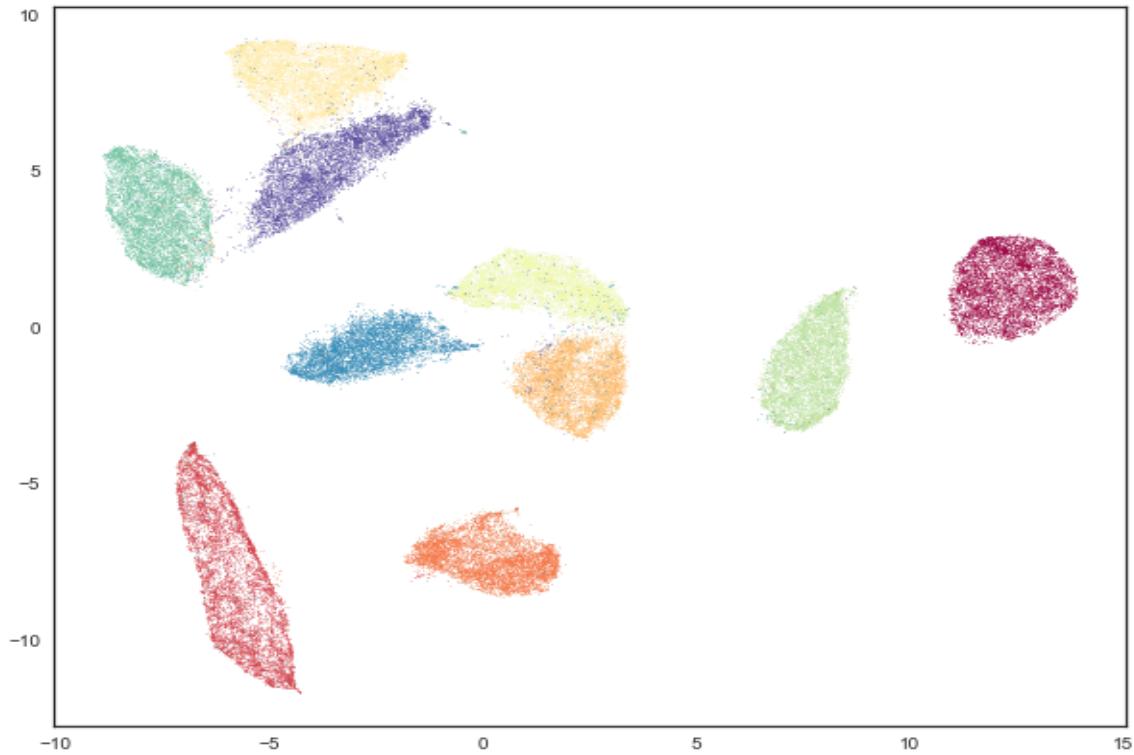
The dispersion parameter allows to model over-dispersed data (i.e. higher variance than mean). Here, we propose to use *DEXSeq* on estimated USA counts, and perform a differential usage test between experimental conditions. Therefore, for every gene, exons are replaced by the spliced, unspliced and ambiguous versions of the gene. This models ambiguous reads separately from spliced and unspliced or exonic and intronic, thus eliminating one of the main sources of mapping uncertainty. However, the uncertainty related to reads mapping to multiple genes is still neglected by this approach. To address both sources of mapping uncertainty we propose a novel method, developed by Simone Tiberi (Tiberi, 2022).

### 2.3.4 *DifferentialRegulation*

## 2.4 Analysis of results

### 2.4.1 Unifold Manifold Approximation and Projection (UMAP)

Unifold Manifold Approximation and Projection (UMAP) is a dimension reduction technique that can be used to visualize data from a high-dimensional space into a low-dimensional space (McInnes *et al.*, 1802). UMAP is implemented on the following three assumptions about the data: first, the data is uniformly distributed on the Riemannian manifold (Lee, 2018); second, the Riemannian metric is locally constant (Lee, 2018); third, the manifold is locally connected. Essentially, UMAP constructs a high dimensional graph representation of the data and then tries to fit a low-dimensional graph that is as structurally similar as possible (McInnes *et al.*, 1802). In this thesis UMAP is used to assess how cells cluster i.e. based on their cell type or to which sample they belong. This knowledge is important, for example to evaluate whether there are structural differences between samples, although the samples are biological replicates. Figure 2.5 shows the clustered digits of the famous MNIST data set which consists of 28x28 pixel grayscale images of handwritten digits (0 through 9) (Deng, 2012). Each digit is described by a 784 dimensional vector which hereby was reduced to a two-dimensional representation by applying UMAP.



**Figure 2.5:** Example of a UMAP representation of high dimensional data into two dimensions highlighting the data clusters (Sainburg *et al.*, 2021)

#### 2.4.2 Classification measurements

The true positive rate (TPR), false positive rate (FPR), and false discovery rate (FDR) are defined as:

$$\text{TPR} = \frac{|\text{TP}|}{|\text{TP} + \text{FN}|} \quad (2.6)$$

$$\text{FPR} = \frac{|\text{FP}|}{|\text{FP} + \text{TN}|} \quad (2.7)$$

$$\text{FDR} = \frac{|\text{FP}|}{|\text{TP} + \text{FP}|} \quad (2.8)$$

where TP, TN, FP, and FN indicate the sets of true positive, true negative, false positive, and false negative elements, respectively. TP are the number of elements that were correctly identified as the positive outcome. Similarly, TN are the number of elements that were correctly identified as the negative outcome. FP are those elements that were identified as the positive outcome, however they should have been identified as negative. In statistics, FP is usually referred to as Type 1 error. Similarly, FN are the elements that were incorrectly identified as negative - also referred to as Type 2 error in the realms of statistics. Figure 2.6 illustrates the meaning of these measurements quite clearly. The TPR (true positive rate) also referred to as sensitivity, measures the proportion of positive elements that were correctly identified - often alluded to as statistical power (2.6). The FPR (false positive rate) measures the proportion of negative outcomes that are identified as positive (2.7). On the other hand, FDR (false discovery rate) measures the expected proportion of false positive among all positive predictions (2.8).

		True Class	
		Positive	Negative
Predicted Class	Positive	TP	FP
	Negative	FN	TN

**Figure 2.6:** Confusion matrix reporting the performance of a binary classification problem ([Mohajon, 2020](#))

#### 2.4.3 ROC curve

The ROC curve is a performance measurement that is used for classification problems - in this case whether a gene is differently regulated or not. Essentially, the ROC curve plots the TPR (y-axis) against the FPR (x-axis). ROC curves above the diagonal indicate better performance than blind random guessing, denoted by the diagonal line. ROC curves are one of the performance evaluation methods used in this thesis.

#### 2.4.4 TPR v. FDR curves

Similar to the ROC curve the TPR v. FDR curve is used to assess performance in classification problems. It plots the TPR (y-axis) against the FDR (x-axis). In addition, one often plots the actual which was observed for some theoretical thresholds - usually 1, 5 and 10%. FDR values are essentially adjusted p-values which can be calculated in various ways from raw p-values. Arguably, the most popular one being the Benjamini-Hochberg correction ([Benjamini and Hochberg, 1995](#)). All the methods considered in this thesis, provide FDR adjusted p-values obtained via Benjamini-Hochberg correction.

When the observed FDR is lower than or equal to the specified threshold, the method controls for the FDR. However, if the observed FDR is greater than the threshold the method does not control for the FDR and there is an inflation of false positive predictions. In this thesis, the methods are evaluated by an adjusted p-value.

# Chapter 3

## Results

### 3.1 Exploratory Data Analysis

#### 3.1.1 Mouse kidney cells

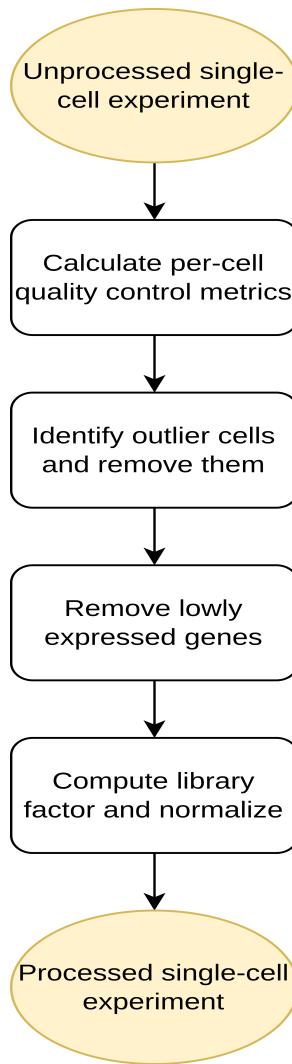
The first data set stems from a paper that investigates potential cellular targets of kidney disease in mice ([Park et al., 2018](#)). The authors isolated and sequenced a total of 57'979 cells from whole kidney cell suspensions (one kidney per mouse) derived from seven healthy male mice using droplet-based single-cell RNA sequencing. The samples were labelled as: normal1, normal2, normal3, normal4, Ksp-cre-GFP, Scl-cre-GFP and Pod-cre-GFP. For our work, we decided to use the raw data from the four samples that were labelled as normal to ensure the biological reproducibility between the samples.

We used the *alevin-fry* pipeline to quantify the raw single-cell RNA sequencing data for further use in the R programming environment. Quality control is a crucial stage in data pre-processing as low-quality libraries can contribute to misleading results in downstream analyses ([Amezquita et al., 2020](#)). Therefore, we filtered lowly abundant genes and low-quality cells to mitigate said problems to improve interpretability of the results.

To identify low-quality cells, cell-specific QC metrics were calculated with the *perCellQC-Metrics* function from the *scater* R package ([McCarthy et al., 2017](#)). These metrics include the total number of expressed genes, the overall count across all genes, and the fraction of counts assigned to control genes such as mitochondrial genes. By setting a specific threshold on per-cell QC metrics, high-quality cells can be retained. In our setting, outliers are defined as cells with library sizes more than two median absolute deviations away from the median library size. Figure 3.1 summarizes the process from unprocessed to processed single-cell experiment.

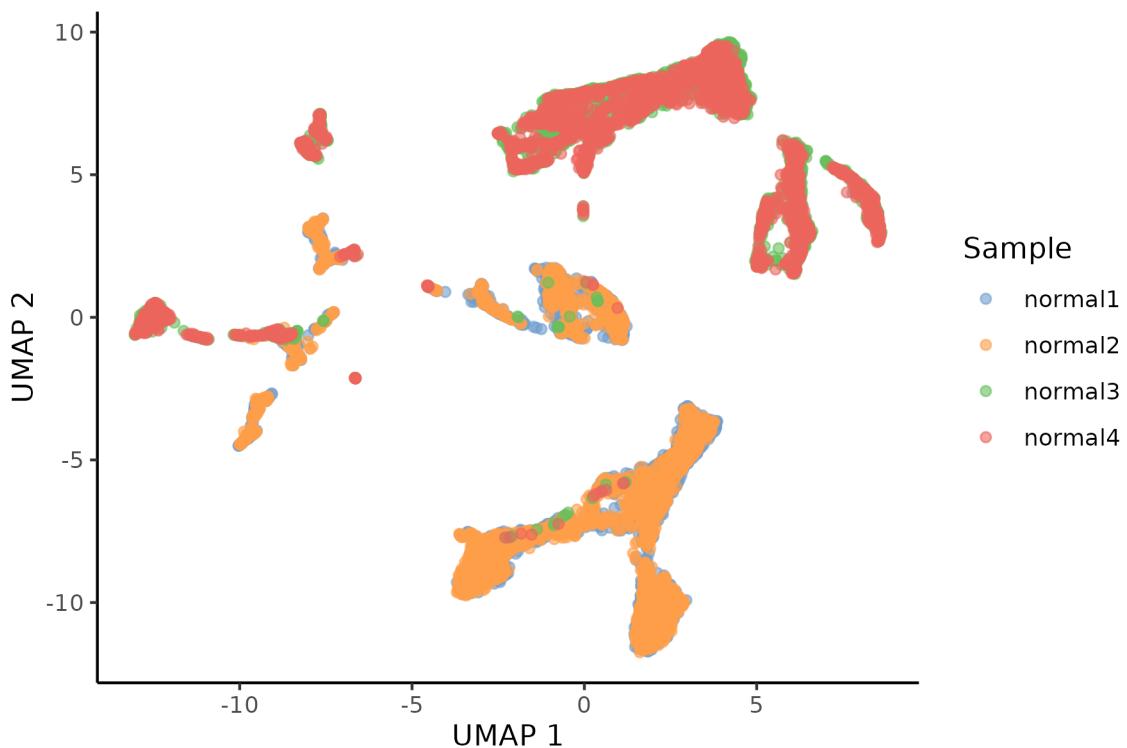
After filtering, the data set consists of 23'543 cells and 18'537 genes. Next, we used the *singleR* function from the *singleR* R package ([Aran et al., 2019](#)) for cell-type annotation. Cell-type annotation is important to determine what biological state is represented by cell clusters which helps the interpretability of the results and their implications ([Amezquita et al., 2020](#)). *singleR* is a method that assigns labels based on the reference samples with the highest Spearman rank correlation while only using marker genes between pairs of labels to focus on the relevant differences between cell types ([Aran et al., 2019](#)). Figure 3.2 shows the UMAP of the cells coloured by their respective sample id. From Figure 3.2 one can observe that the projection of the cells is very similar across the samples. Further, Figure 3.3 also illustrates that cells from the same cell-type cluster together, as one would expect.

Figure 3.4 shows that the annotated cells were largely classified as either: Adipocytes, Epithelial cells and Hepatocytes. Additionally, one can observe that those three cell types are approximately evenly distributed across the four samples. For further analyses we focus on those cell types to investigate the performance of existing methods for the detection of differentially expressed genes and design our own simulation study.

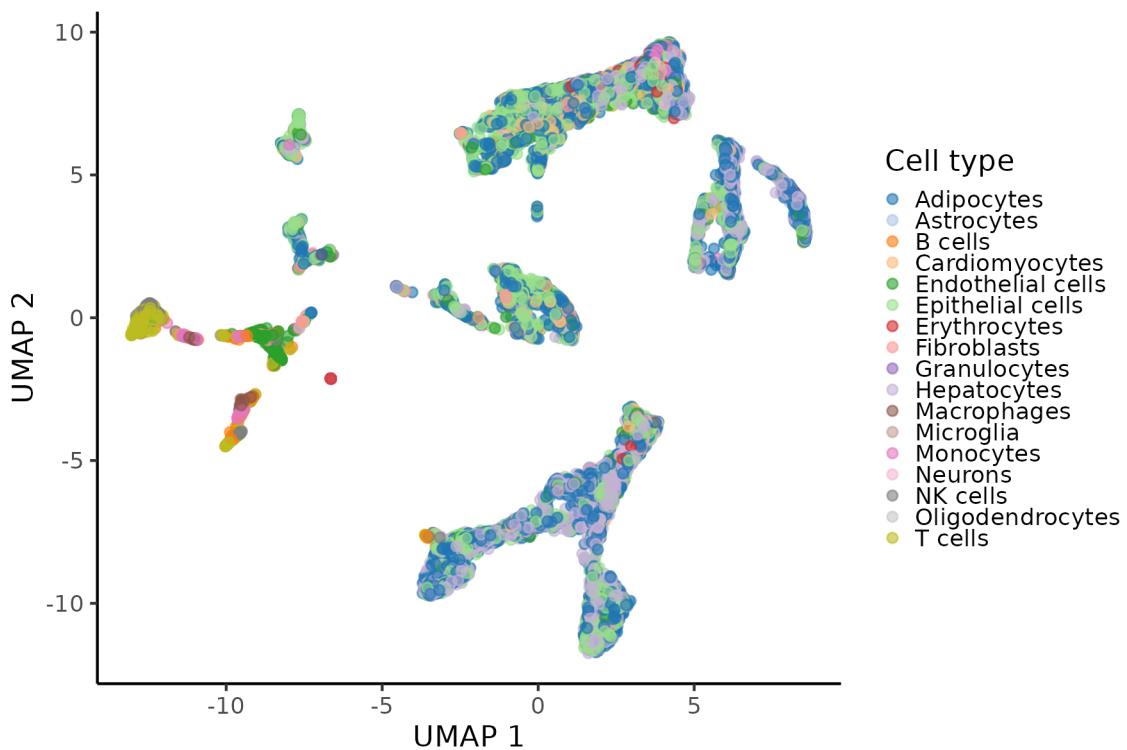


**Figure 3.1:** Quality control process from unprocessed, raw to processed, filtered single-cell experiment

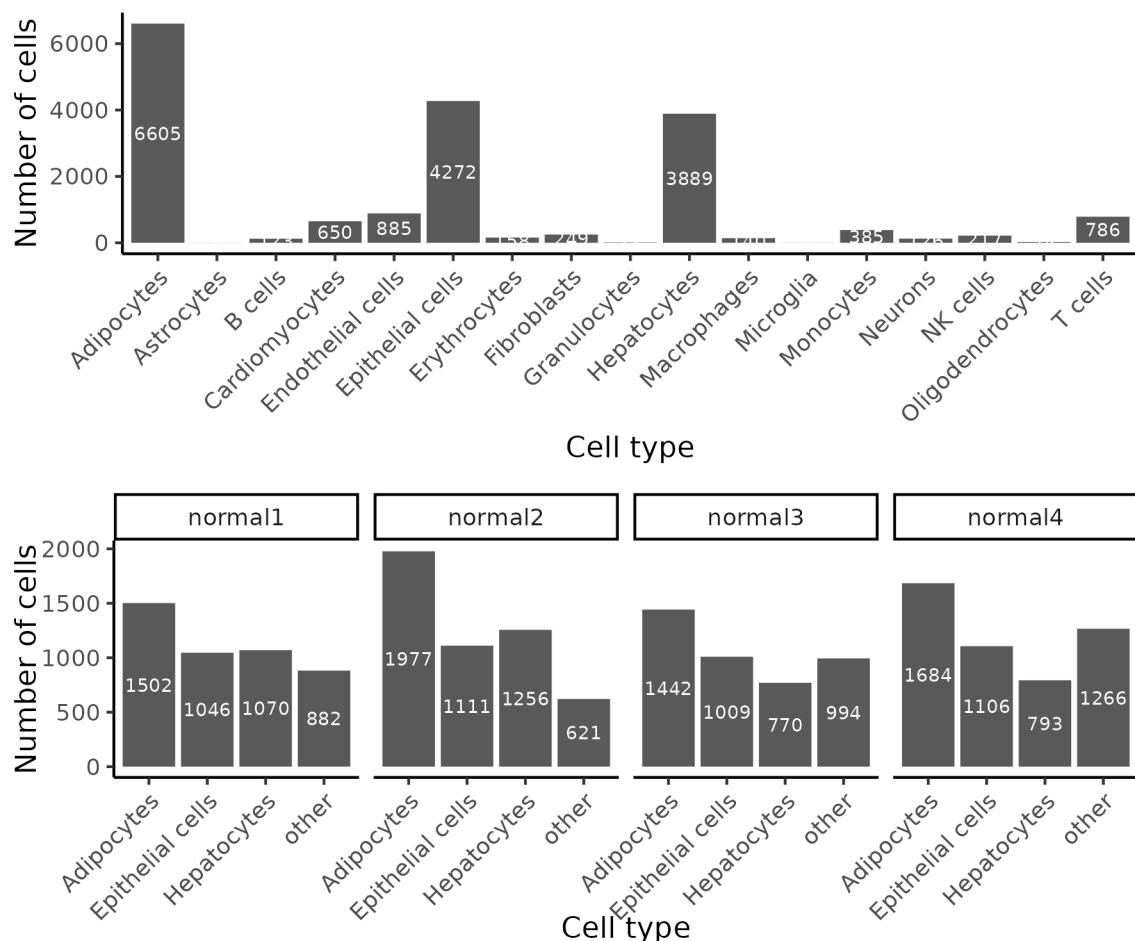
After QC filtering and cell type annotation we investigated the RNA velocities for each sample. Initially, we expected similar patterns with changing trajectories. First, we explored the proportions of spliced and unspliced counts in each sample. Figures 3.5 to 3.8 show that the abundance of spliced counts is very high in comparison to unspliced counts. In samples 3 and 4 the abundance of unspliced counts approximately half, compared to samples 1 and 2. After exploring the velocity plots there were no clear patterns that were consistent between the biological replicates as shown in Figures 3.9 to 3.12. We initially thought that we could relate differentially regulated genes to differential velocity between experimental conditions. However, this does not seem possible. We therefore concluded that our discoveries (i.e. differences in the relative abundance of US or USA reads), cannot be taken as a proxy for "differential velocity". Although, the ideas of differential regulation and differential velocity are connected (i.e. RNA velocities are calculated on US estimated reads), we decided to keep the two concepts separate, and interpret our discoveries as differential regulated genes only.



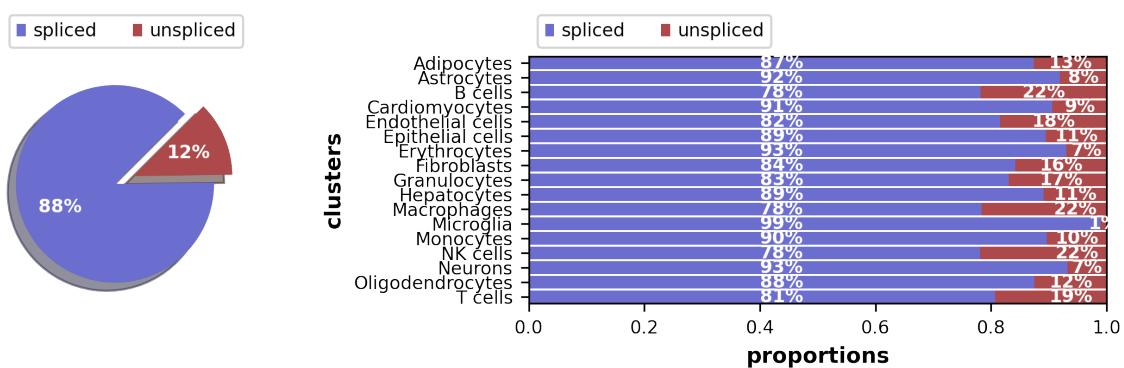
**Figure 3.2:** UMAP representation of the mouse kidney cells coloured by sample id



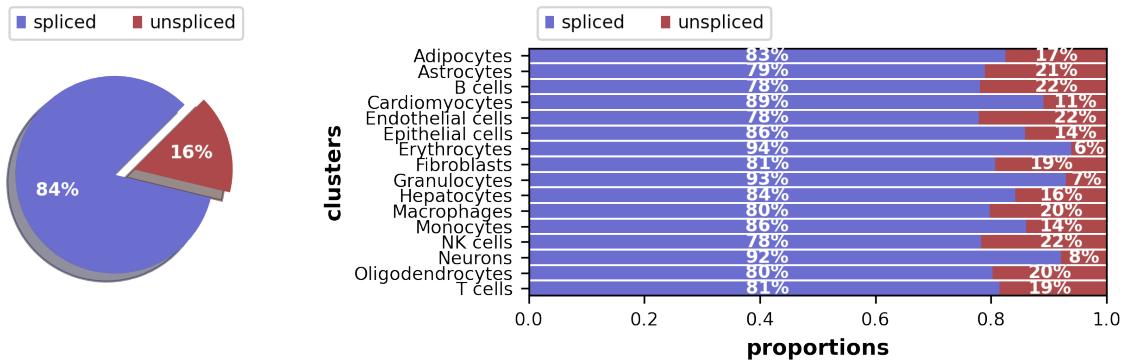
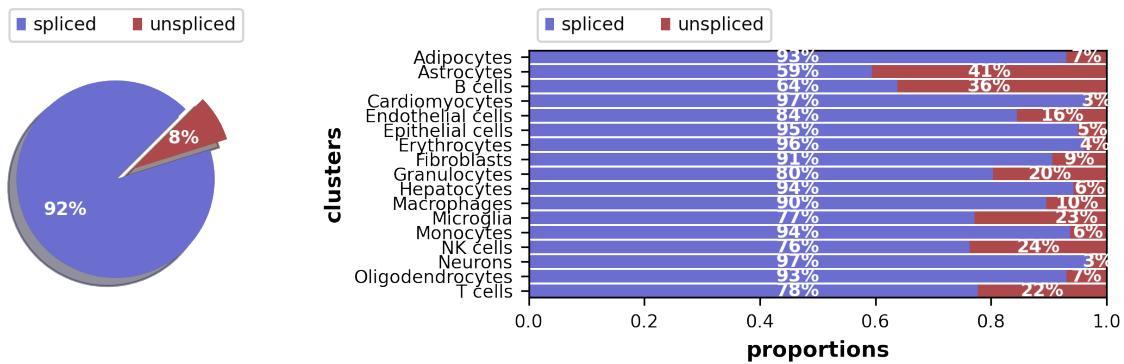
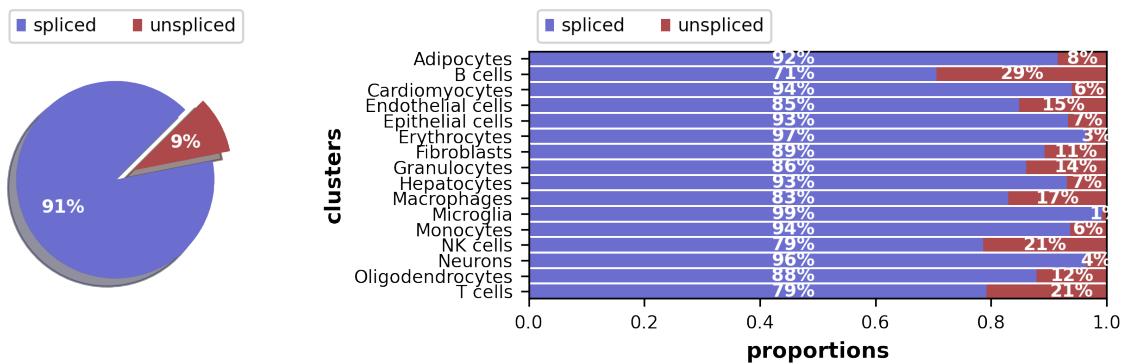
**Figure 3.3:** UMAP representation of the mouse kidney cells coloured by cell type

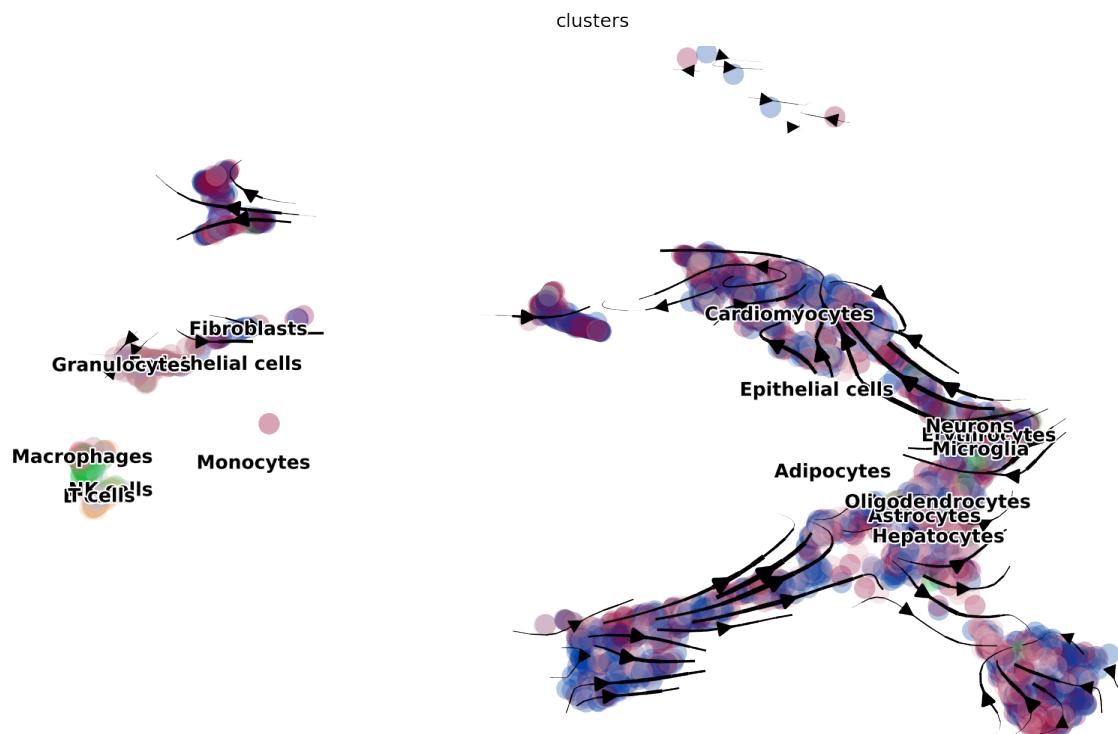


**Figure 3.4:** Frequency distribution of the cell types after quality control



**Figure 3.5:** Abundance of spliced and unspliced counts in sample normal1

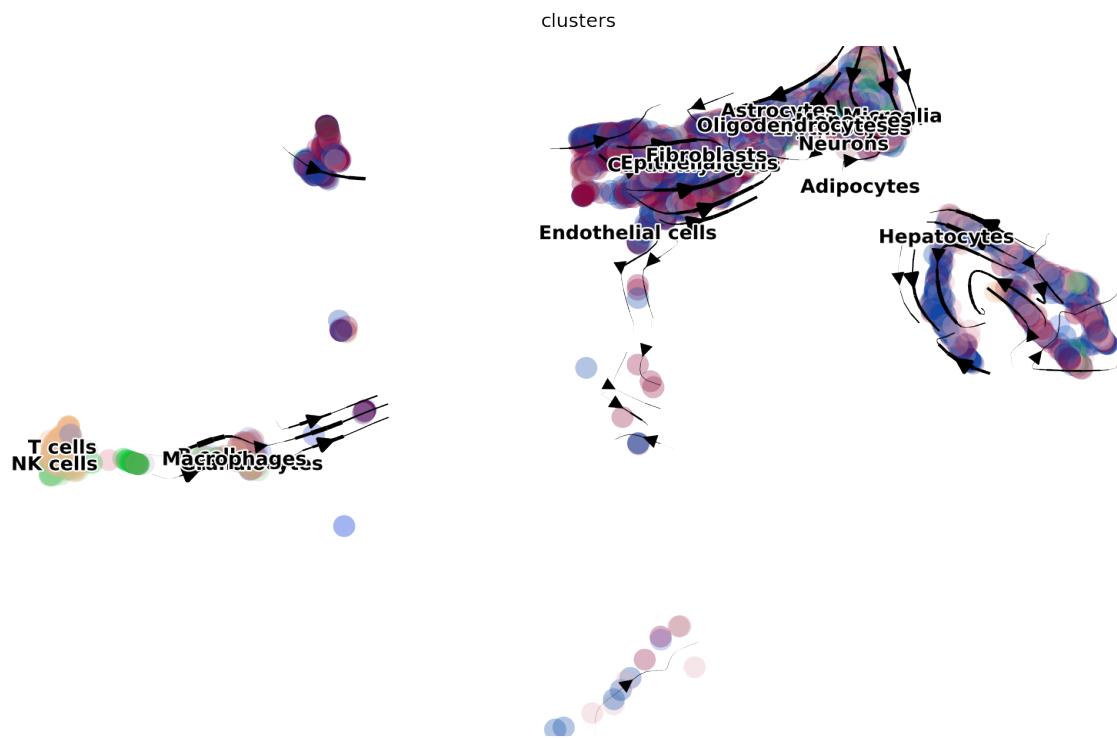
**Figure 3.6:** Abundance of spliced and unspliced counts in sample normal2**Figure 3.7:** Abundance of spliced and unspliced counts in sample normal3**Figure 3.8:** Abundance of spliced and unspliced counts in sample normal4



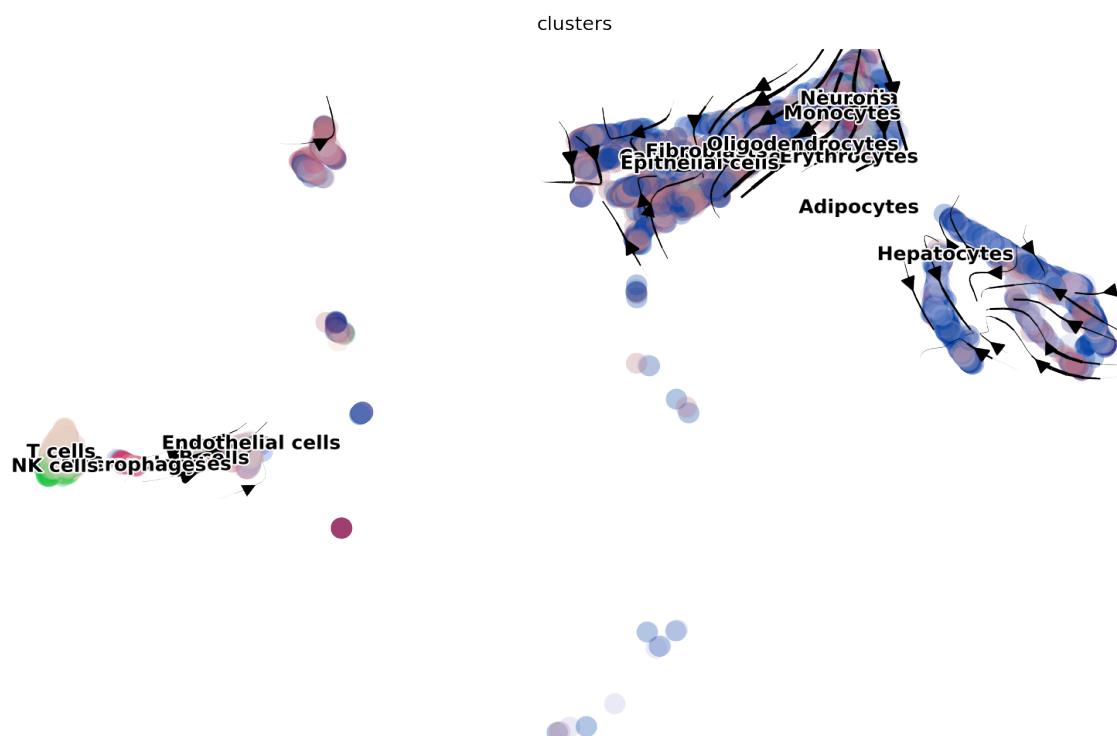
**Figure 3.9:** Dynamical model showing RNA velocity of sample normal1



**Figure 3.10:** Dynamical model showing RNA velocity of sample normal2



**Figure 3.11:** Dynamical model showing RNA velocity of sample normal3



**Figure 3.12:** Dynamical model showing RNA velocity of sample normal4

## 3.2 Simulation study

### 3.2.1 Simulation strategy

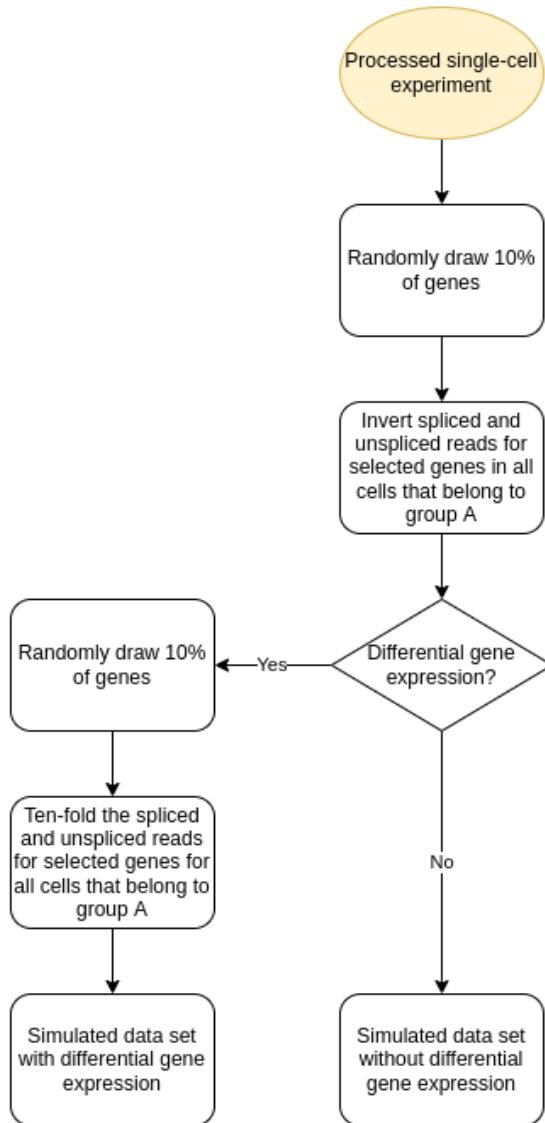
We designed two simulations: i) one where we simulated differentially regulated (DR) genes only and ii) one where we simulated both DR and differentially gene expression (DGE). In the second simulation, DGE was added as a nuisance effect that makes DR detection more challenging. Below, we first describe how to simulate DR effects, and then illustrate how DGE was added in the second simulation. Initially, the simulation strategy was to invert the spliced and unspliced counts for 10% of genes for all cells that belong to an arbitrary group A. The group allocation was made based up on the consideration of the UMAP from Figure 3.2 where it is visible that samples tend cluster in pairs: 1 with 2, and 3 with 4. Therefore, the group allocation of  $Group_A = (sample_1, sample_3)$  and  $Group_B = (sample_2, sample_4)$  was chosen to obtain a homogeneous representation of the groups. The set of genes, whose counts were to be inverted, was randomly drawn by a sampling algorithm without replacement (hypergeometric distribution). There are many different ways to introduce a differential effect, however nailing down on inverting the spliced and unspliced counts seemed like a neat way to achieve this without actually modifying the originally estimated counts. This procedure was done separately for each cell type, so that differential genes are not the same across cell types. Additionally, in the second simulation only, DGE was introduced in 10% of genes in all cells that belong to said arbitrary group A. In order to introduce DGE, we additionally multiply the counts by 10 (ten-fold gene expression) for 10% randomly drawn genes in group A. Again, the set of genes was randomly drawn by the same sampling algorithm as before.

Starting from a real data set as an anchor data set, then artificially introducing a differential effect, we essentially created two semi-simulated data sets. Compared to full simulations, semi-simulated approaches have the advantage of having a realistic structure, because it was indeed taken from real data. The genes and cells that were subject to change were stored as ground truth for further evaluation in the downstream analyses. Figure 3.13 illustrates the simulation process from the original mouse kidney data set to two simulated data sets.

The goal of this thesis was to determine how well the aforementioned methods perform on detecting differentially regulated genes on read-level simulated data sets and the effect of multi-mapping uncertainty. To achieve this two groups of methods were postulated as *eisaR* and *BRIE2* cannot take into account ambiguous reads. For this reason the classification performance of *eisaR* and *BRIE2* are compared with each other with the help of ROC and TPR v. FDR curves. As *alevin-fry* allows the estimation of ambiguous counts as well as spliced and unspliced, it was possible to assign the ambiguous counts to both spliced and unspliced counts (50-50 split) so that *eisaR* and *BRIE2* can be applied. We settled to assign 50% of ambiguous count to spliced and the other 50% to unspliced because other methods, such as *alevin*, also use this approach. In a similar manner, *DEXSeq* and our own method *DifferentialRegulation* were used to detect differentially regulated genes. However, in this case the ambiguous counts were used as an additional information. As a next step, *minnow* was used to introduce mapping uncertainty into the simulated data sets. The simulated matrix of US counts was provided to *minnow* to simulate scRNA-seq data at the read-level, which was then aligned and quantified with *alevin-fry*. In order to assess the impact of multi-mapping uncertainty, we fit *eisaR* and *BRIE2* (the only methods that require US counts), to the original US simulated matrix (i.e. the input of *minnow*), and to the US counts estimated from *alevin-fry* (after running *minnow*). The two analyses are shown in the next two sections, 3.2.2 and 3.2.3.

### 3.2.2 Simulation without mapping uncertainty

As a first step, we looked at the results from the naive simulation for both data sets with and without DGE. Figures 3.14 and 3.15 show that both *eisaR* and *BRIE2* perform quite well



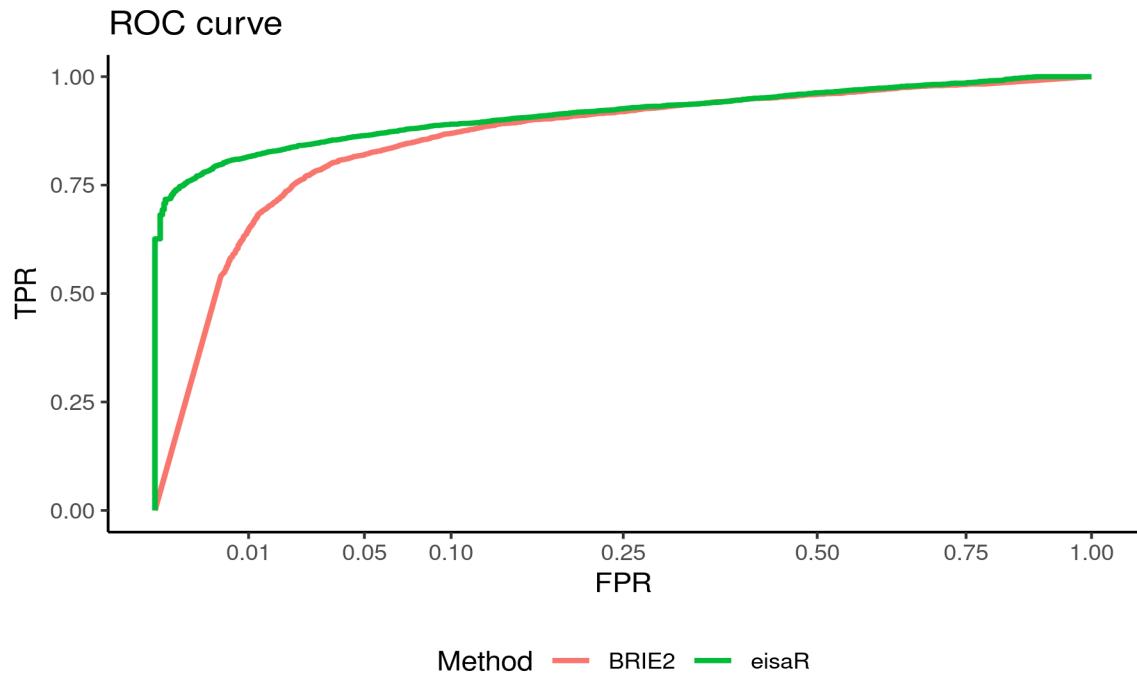
**Figure 3.13:** Simulation process from original mouse data set to simulated data sets

in detecting differential genes. *eisaR* has a slightly higher TPR as shown in the ROC curve. Although, both methods have a similar performance pattern in the ROC curve, the TPR v. FDR plot looks quite different between the two methods. From Figures 3.16 and 3.17 it is shown that *eisaR* is well calibrated for FDR, whereas *BRIE2* is not.

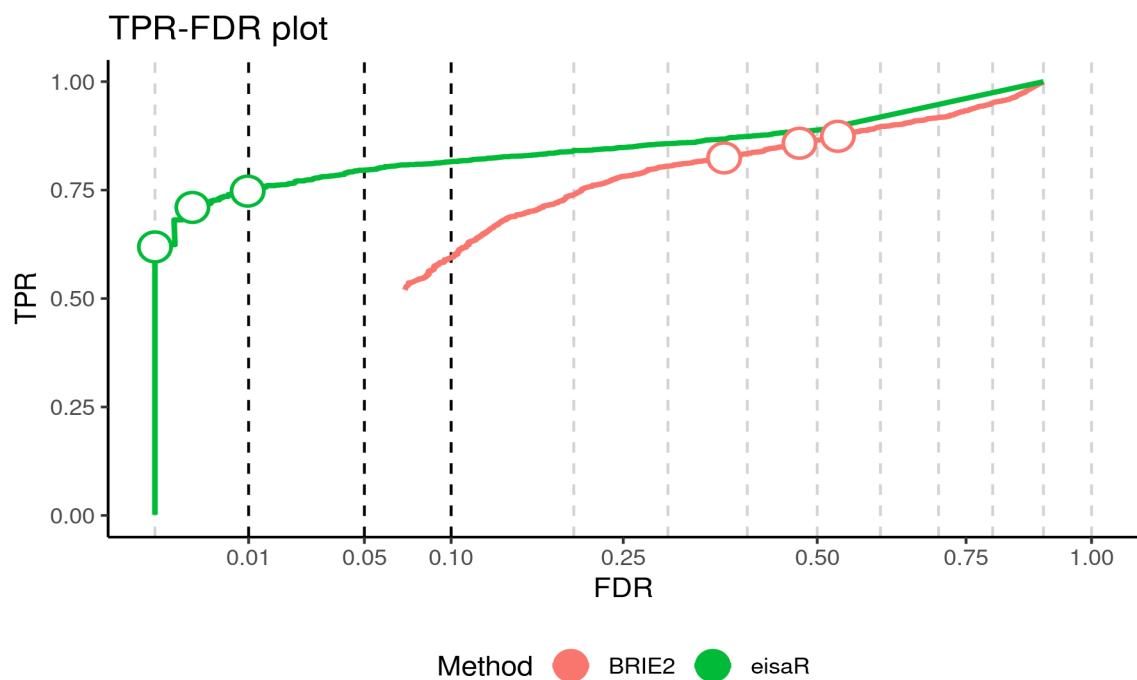
After introducing DGE in the second data set performance drops quite substantially as shown in Figure 3.16. TPR is almost halved in both methods as it is shown in the ROC curve of Figure 3.16. However, *eisaR* is still well calibrated for FDR. Similar to the data set without DGE, *BRIE2* is not well calibrated for FDR. It seems that both methods are heavily affected by the introduction of DGE as performance dropped to almost half. However, we introduced a very strong effect - 10 fold change - therefore, it is to be expected that performance drops. Nevertheless, we wanted to investigate how the performance changes in an extreme scenario, hence the strong effect size.

From this naive simulation we concluded that *BRIE2* has inflated FDR in both cases - with and without DGE. On the other hand, *eisaR* was well calibrated for FDR in both cases. However, TPR decreases by almost half after introducing DGE. In the next step, we use *minnow* to

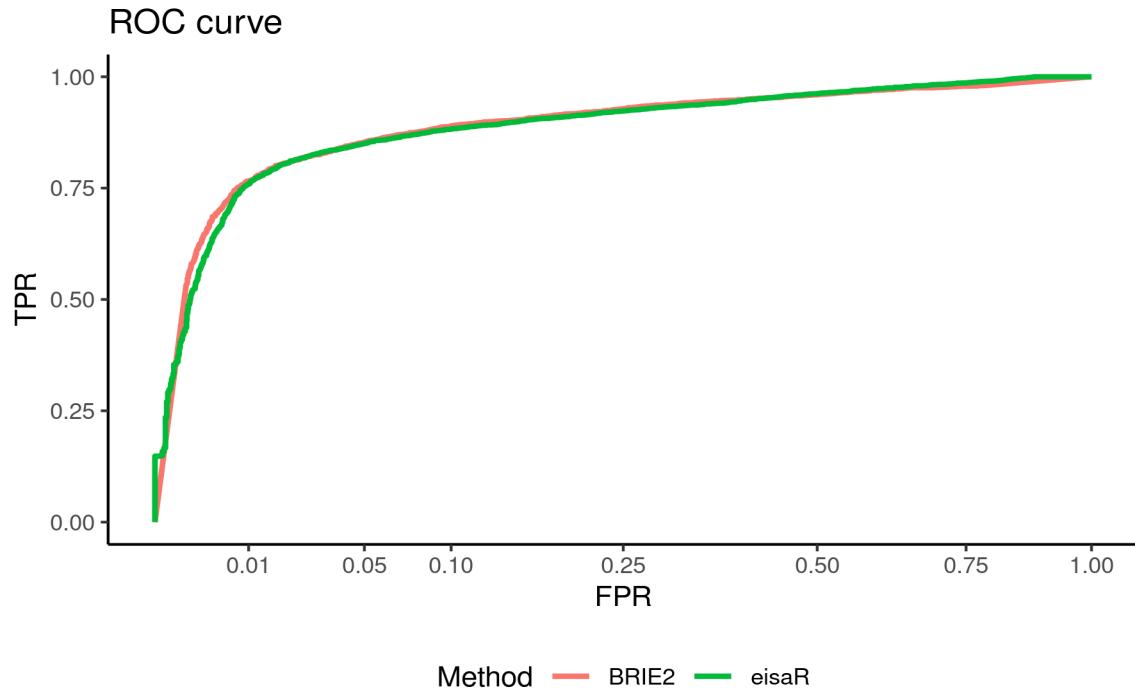
introduce multi-mapping uncertainty in to both data sets to make the simulation more realistic. It is to be expected that performance will further decrease after the introduction of multi-mapping uncertainty.



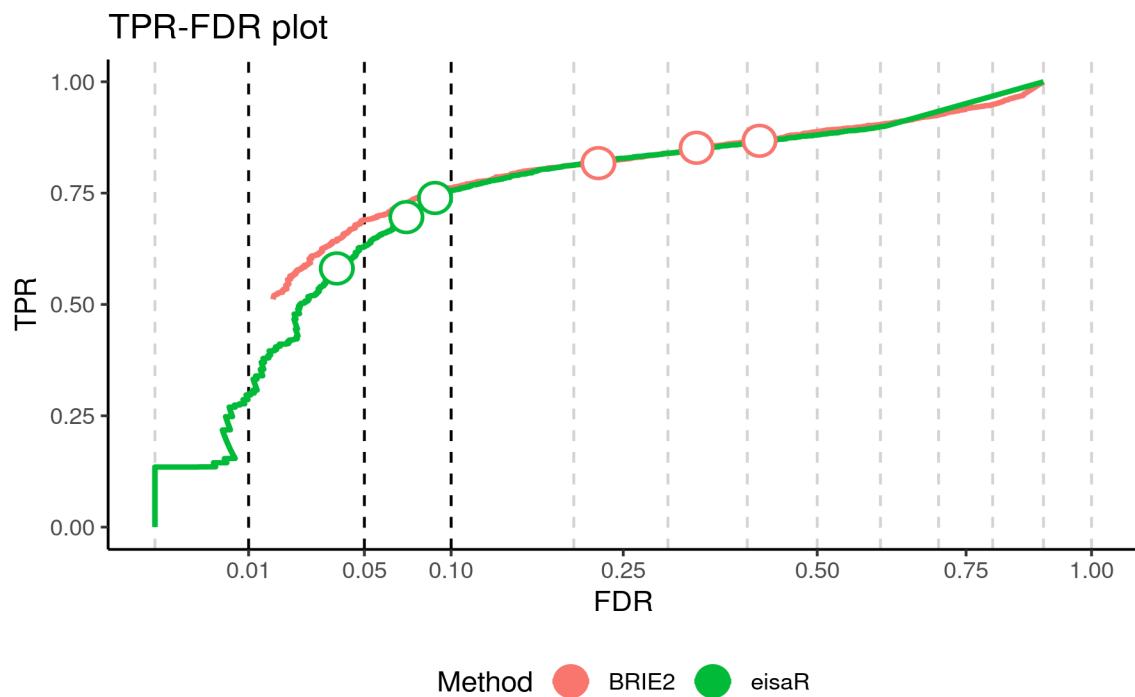
**Figure 3.14:** ROC curve of *BRIE2* and *eisaR* in the initial simulation without DGE



**Figure 3.15:** TPR v. FDR plot of *BRIE2* and *eisaR* in the initial simulation without DGE



**Figure 3.16:** ROC curve of *BRIE2* and *eisaR* in the initial simulation with DGE



**Figure 3.17:** TPR v. FDR plot of *BRIE2* and *eisaR* in the initial simulation with DGE

### 3.2.3 Simulation with mapping uncertainty

As a next step, multi-mapping uncertainty was introduced in to the two simulated data sets. First, *minnow* was used to simulate new reads from the previously simulated data sets. Second, we used *alevin-fry* to align the generated read files to the reference genome and for quantification of the reads. The newly generated data sets were then run on the aforementioned methods to identify differential genes.

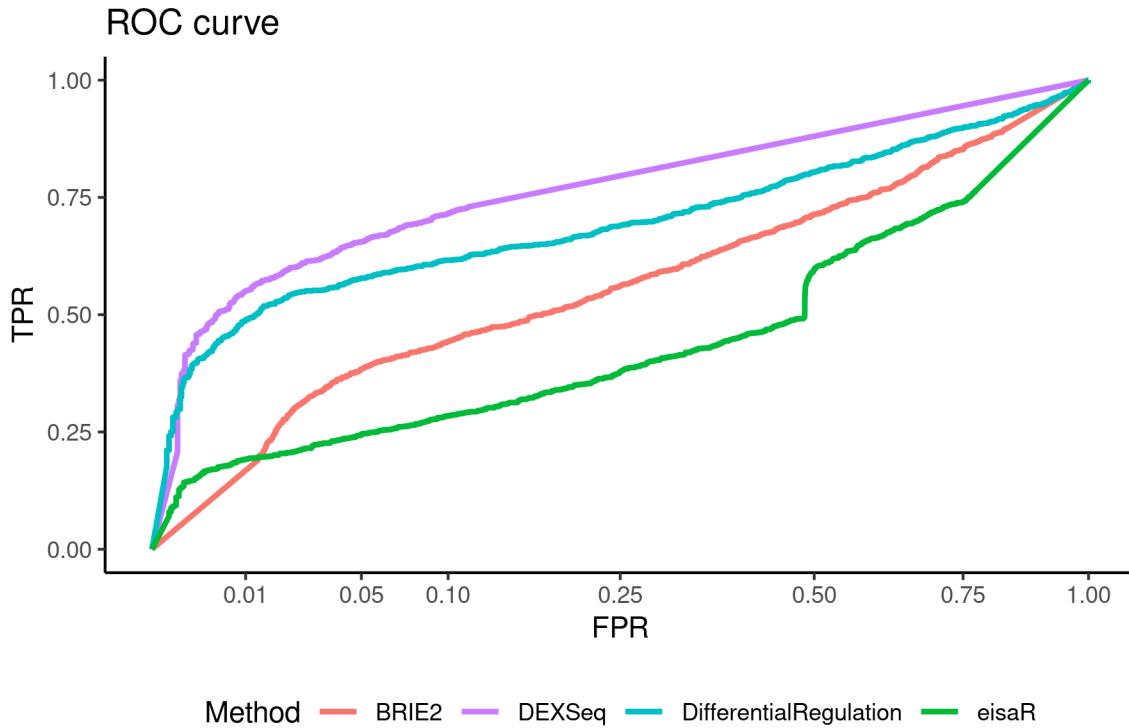
Figure 3.18 shows the performance of all four methods without DGE. For visualization purposes we decided to omit results where spliced and unspliced counts are very similar because it is very hard to detect a differential effect. Therefore, only results are plotted where there is a minimum difference of 0.2 between spliced and unspliced counts. From the ROC curve we observe that *DEXSeq* and *DifferentialRegulation* have a similar TPR, although *DEXSeq* perform slightly better. Both *BRIE2* and *eisaR* have a lower TPR than the other two methods. From Figure 3.19 we observe that again *DEXSeq* and *DifferentialRegulation* have a similar performance profile. However, *DifferentialRegulation* controls better for FDR than *DEXSeq*. Contrarily to before, *eisaR* controls quite well for FDR, however has half the TPR compared *DEXSeq* and *DifferentialRegulation*. On the other hand, *BRIE2* does not control well for FDR as there is strong inflation.

In the next step, we investigated how the performance changes after introduction of DGE into the data set. Figure 3.20 shows the ROC curve for all four methods. From the Figure we observe that the difference in TPR between *DEXSeq* and *DifferentialRegulation* is smaller than before. On the other hand, the performance based on TPR is approximately the same as before for *BRIE2* and *eisaR*. From Figure 3.21 it is shown that *DifferentialRegulation* still controls well for FDR, whereas the other three methods do not. The introduction of DGE as a nuisance parameter seems to affect the performance of *DEXSeq* and *eisaR* quite substantially in terms of FDR calibration as FDR is almost doubled to before. The FDR calibration for *BRIE2* was not affected by DGE, although it was not well calibrated to begin with.

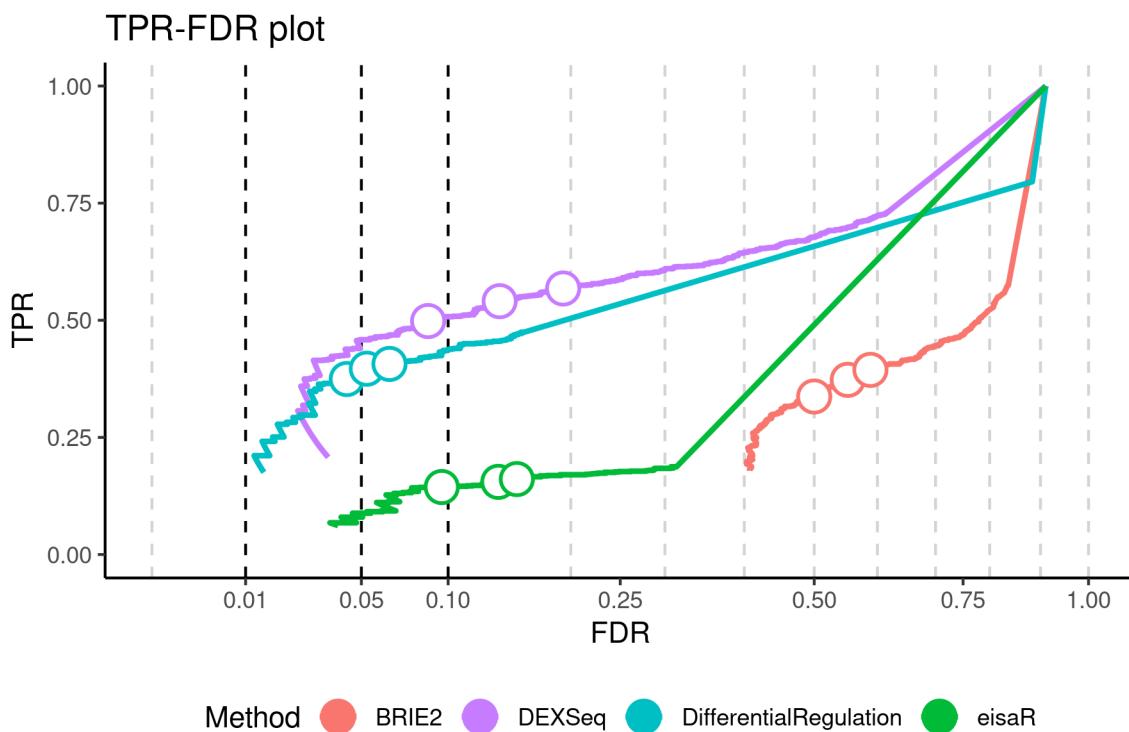
Furthermore, in order to assess how overall gene abundance affects results, we stratified the previous results by gene expression and evaluated performance, separately, for lowly, medium and highly abundant genes. This is achieved by separating results according to overall gene abundance into 3 groups, based on the quantiles of levels 1/3 and 2/3; in particular, lowly abundant genes have abundance below the first quantile (of level 1/3), moderately expressed genes have expression between the two quantiles, while highly abundant genes have expression above the second quantile (of level 2/3).

Figures 3.22 to 3.27 show the results stratified by the level of gene abundance. The Figures show that performance is consistent across gene abundance levels for *DifferentialRegulation*. TPR increases only marginally, which is expected as more data usually implies higher statistical power and FDR is also stable across gene abundance levels. Overall, *DifferentialRegulation* is not substantially impacted by gene abundance. For *DEXSeq* TPR and FDR are both increasing as gene abundance gets higher. This effect is even larger for the simulation with DGE. For *BRIE2* there is a significant increase of TPR from low to highly abundant genes, however, the FDR is badly calibrated. With *eisaR* there is a marginal increase of TPR, whereas FDR is only slightly inflated without DGE. On the other hand, FDR is strongly inflated with DGE as gene abundance rises.

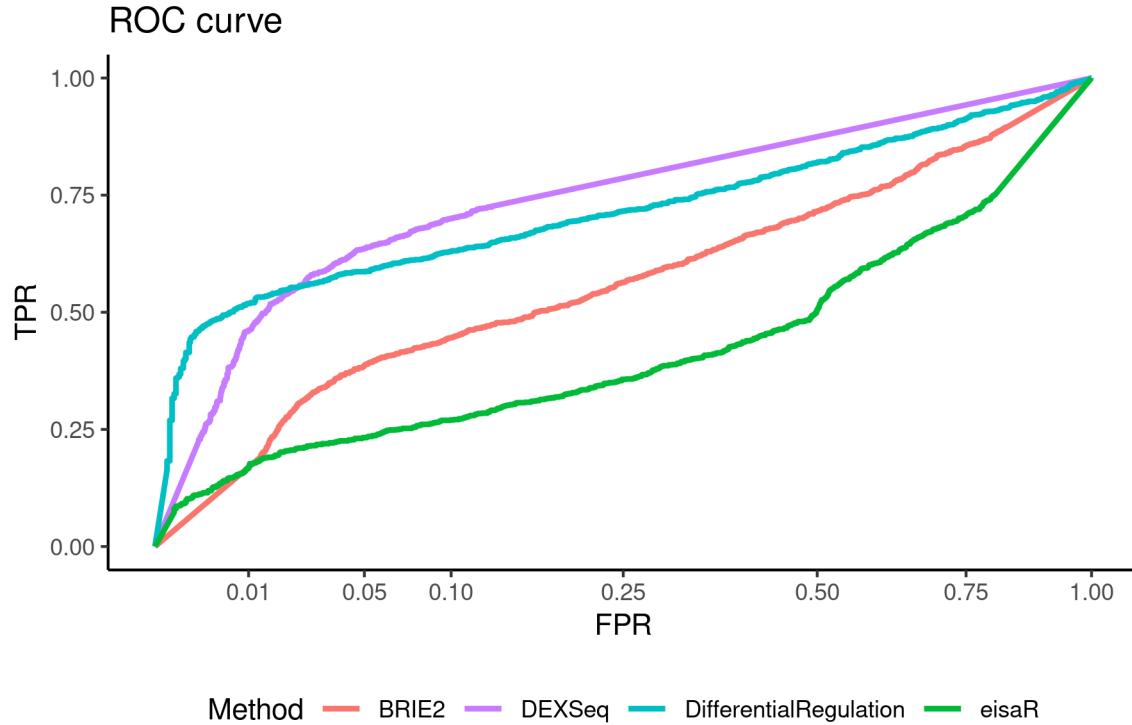
In this part we investigated how robust the methods are to gene abundance with and without DGE. We conclude that the performance of *BRIE2* is low in all cases. *eisaR* has a low TPR but FDR is generally well calibrated without DGE. *DEXSeq* has good TPR and mild inflation of FDR without DGE, however, there is a strong increase in FDR with DGE. Generally, TPR is increasing with gene abundance, however FDR is increasing as well. On the other hand, *DifferentialRegulation* is the only method with good TPR and well calibrated FDR with and without DGE across all levels of gene abundance.



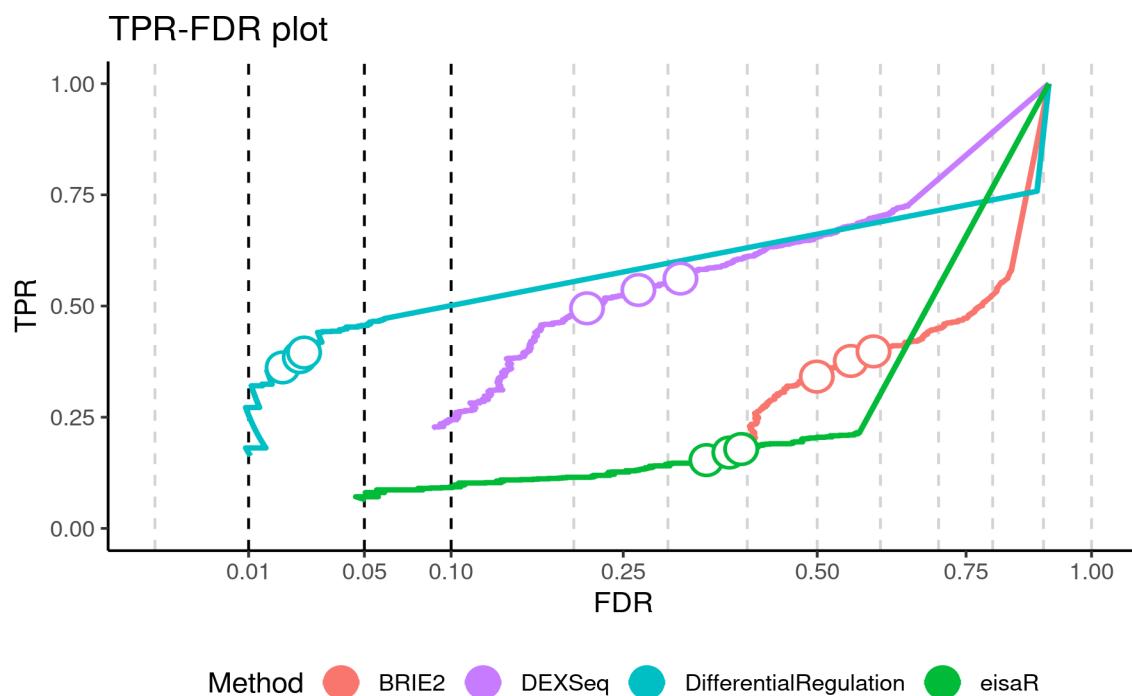
**Figure 3.18:** ROC curve of *BRIE2*, *DEXSeq*, *DifferentialRegulation* and *eisaR* in the sophisticated simulation without DGE



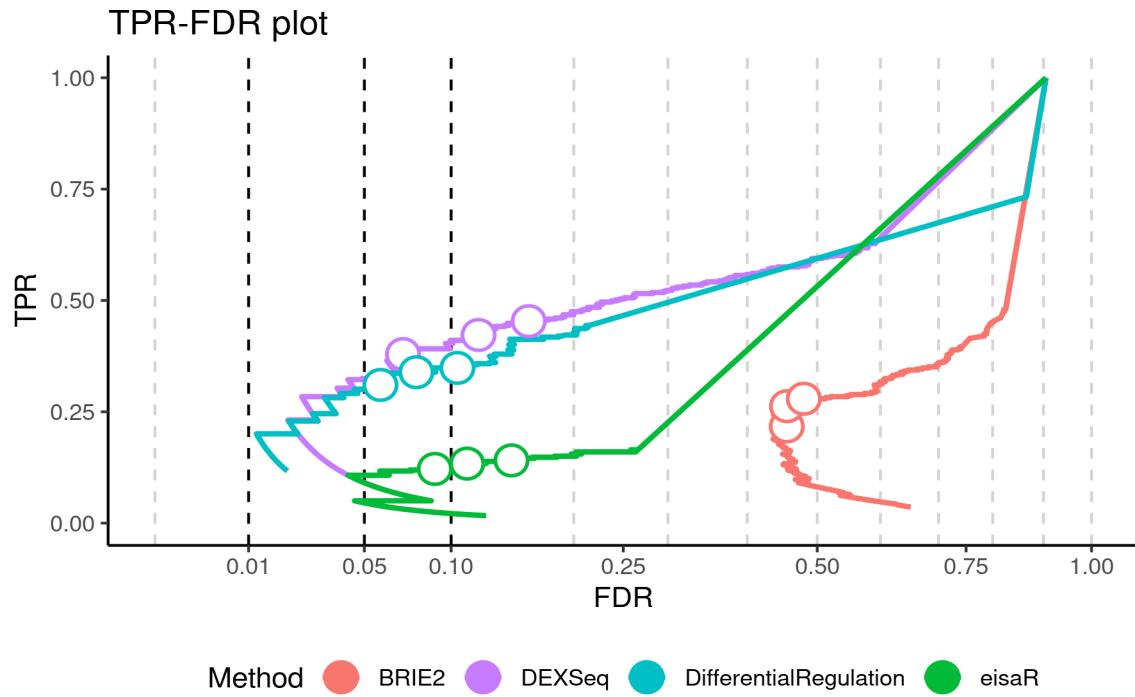
**Figure 3.19:** TPR v. FDR plot of *BRIE2*, *DEXSeq*, *DifferentialRegulation* and *eisaR* in the sophisticated simulation without DGE



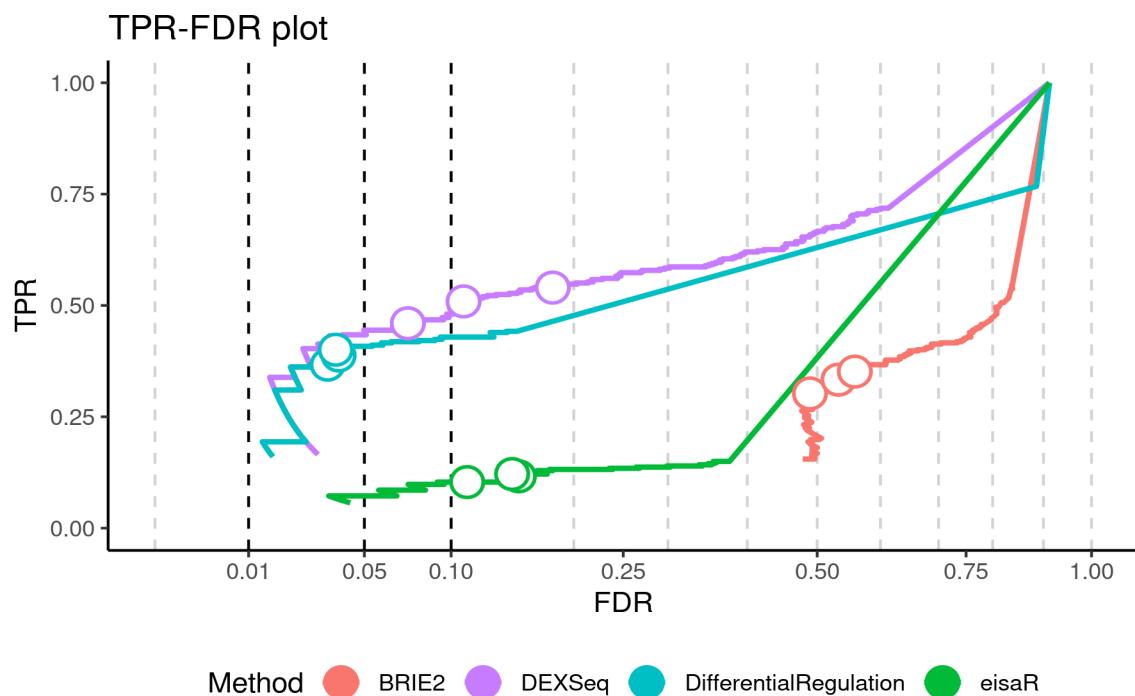
**Figure 3.20:** ROC curve of *BRIE2*, *DEXSeq*, *DifferentialRegulation* and *eisaR* in the sophisticated simulation with DGE



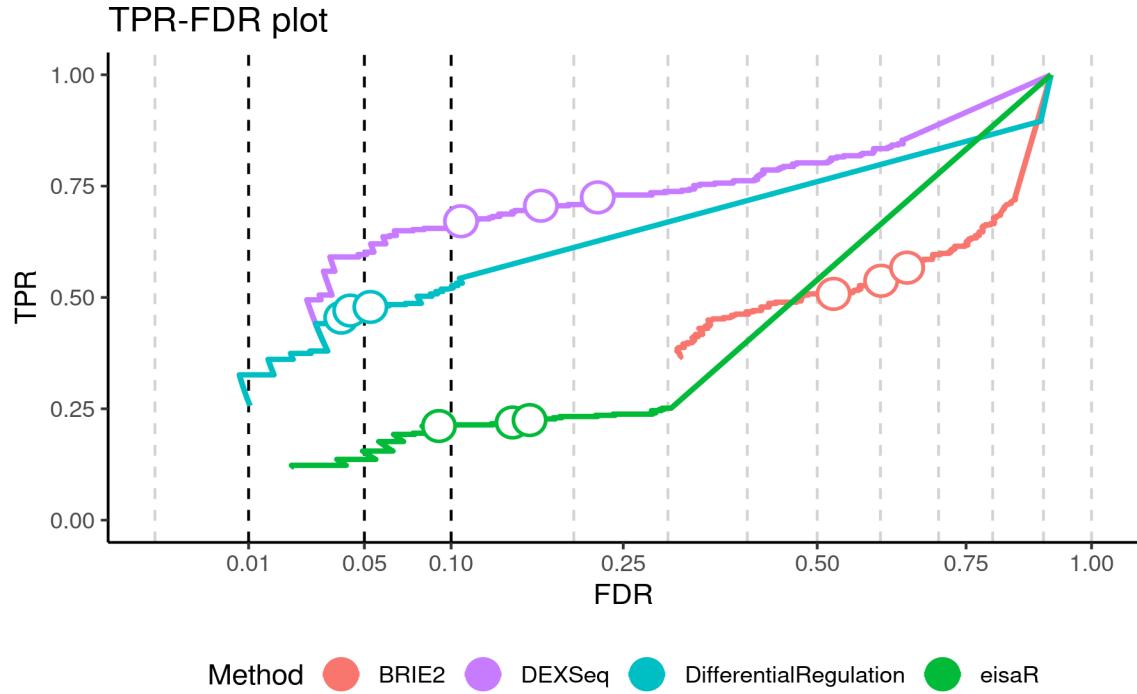
**Figure 3.21:** TPR v. FDR plot of *BRIE2*, *DEXSeq*, *eisaR* and *DifferentialRegulation* in the sophisticated simulation with DGE



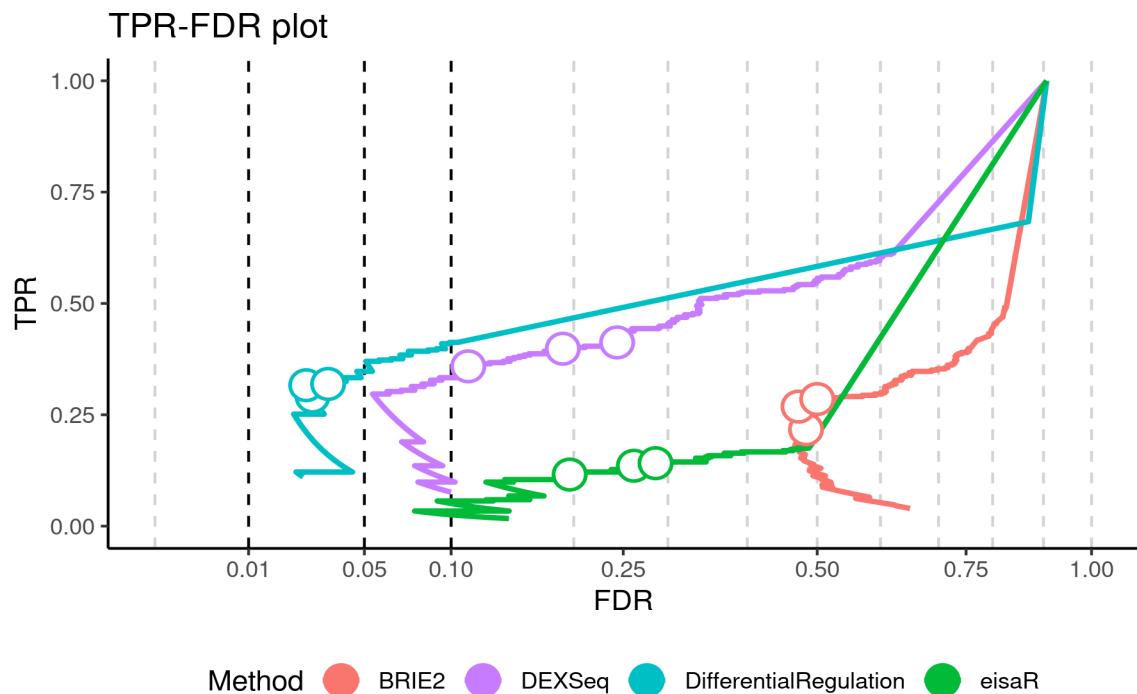
**Figure 3.22:** TPR v. FDR plot of *BRIE2*, *DEXSeq*, *DifferentialRegulation* and *eisaR* in the sophisticated simulation for the lowly expressed genes in the stratified analysis



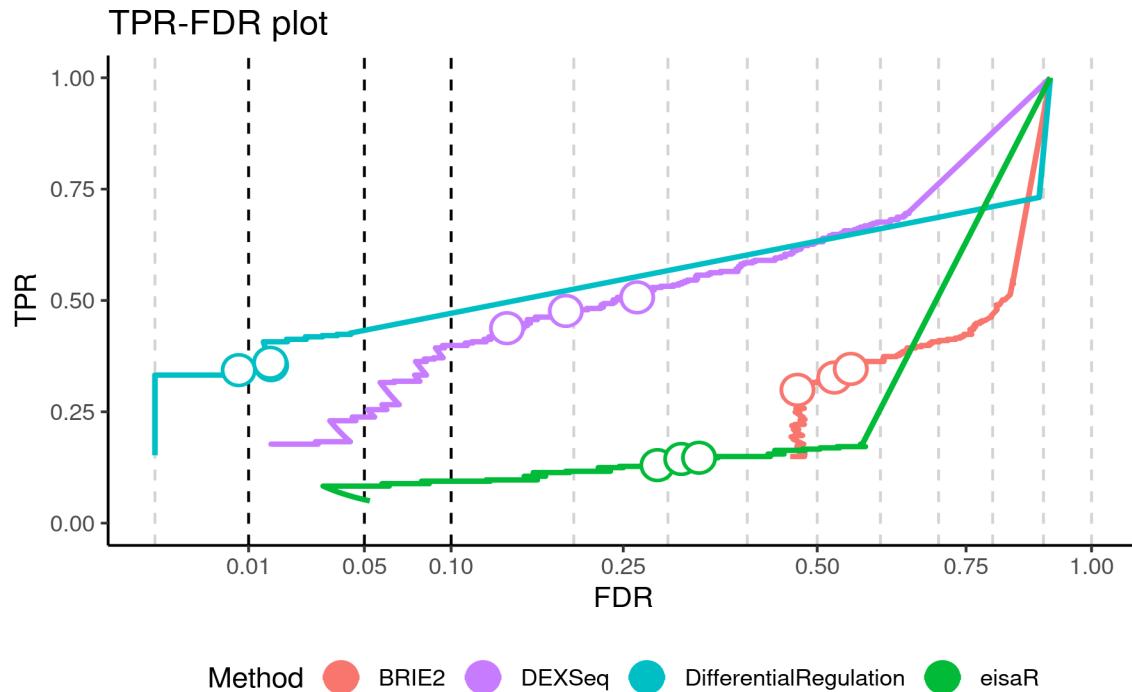
**Figure 3.23:** TPR v. FDR plot of *BRIE2*, *DEXSeq*, *DifferentialRegulation* and *eisaR* in the sophisticated simulation for the moderately expressed genes in the stratified analysis



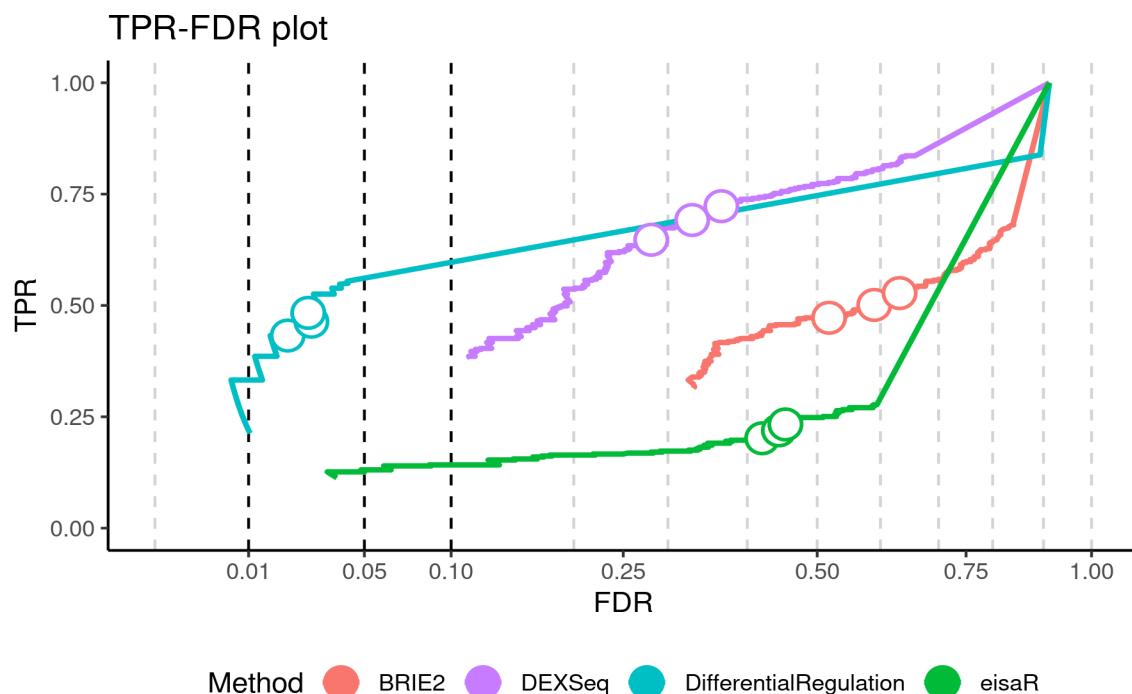
**Figure 3.24:** TPR v. FDR plot of *BRIE2*, *DEXSeq*, *DifferentialRegulation* and *eisaR* in the sophisticated simulation for the highly expressed genes in the stratified analysis



**Figure 3.25:** TPR v. FDR plot of *BRIE2*, *DEXSeq*, *DifferentialRegulation* and *eisaR* in the sophisticated simulation for the lowly expressed genes in the stratified analysis with DGE



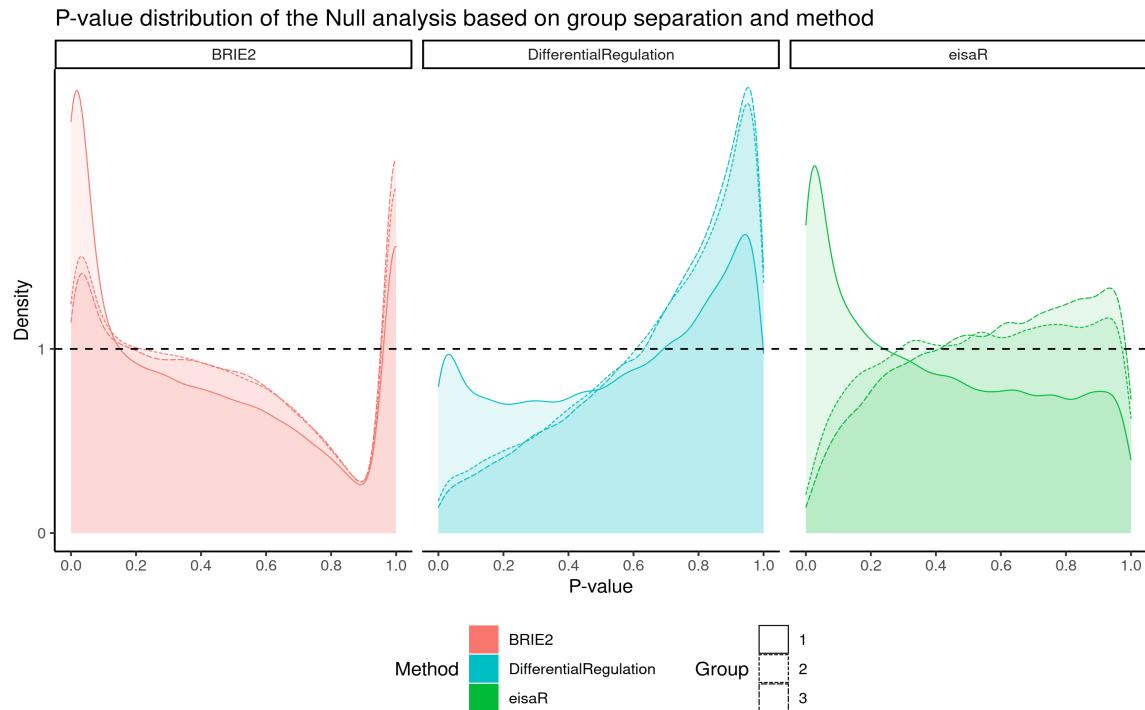
**Figure 3.26:** TPR v. FDR plot of *BRIE2*, *DEXSeq*, *DifferentialRegulation* and *eisaR* in the sophisticated simulation for the moderately expressed genes in the stratified analysis with DGE



**Figure 3.27:** TPR v. FDR plot of *BRIE2*, *DEXSeq*, *DifferentialRegulation* and *eisaR* in the sophisticated simulation for the highly expressed genes in the stratified analysis with DGE

### 3.3 Null analysis on the mouse kidney data

As a last step, a Null analysis was conducted on the original mouse kidney data set to evaluate the methods of on a real world data set. For that, all three possible group allocations were considered. Under the Null hypothesis  $H_0$  the p-values would be uniformly distributed between zero and one, because all samples belong to the same experiment condition (i.e. normal). In particular, we were interested in checking for false positive detections which are indicated by inflated p-values towards zero. Figure 3.28 shows that the p-values are slightly inflated for the first group separation, which leads to a marginal separation between groups, as visible from the UMAP 3.2. Further, from Figure 3.28 it is shown that for *DifferentialRegulation* FPs are never inflated. However, p-values are inflated towards one, hence *DifferentialRegulation* is more conservative as compared to the other methods. *eisaR* is only inflated for the first group separation, but overall approximately uniformly distributed. On the other hand, *BRIE2* demonstrates inflated FPs for all three group separations, which is also consistent with the results from the simulation study. *DEXSeq* was not evaluated for p-value distribution as it does not provide raw p-values at gene-level, whereas the other methods do.



**Figure 3.28:** P-value distribution of the methods based on the three possible group separations

Further, we looked into the performance of the models based on the proportion of p-values and FDR values smaller or equal than the conventional significance levels of 10%, 5% and 1%. From Table 3.1 it is shown that *BRIE2* does not control the p-values particularly well as the values are inflated for all three levels. On the other hand, both *DifferentialRegulation* and *eisaR* do not have inflated p-values, whereas *DifferentialRegulation* is a bit more conservative than *eisaR*. Table 3.2 paints a similar picture as *BRIE2* produces by far larger values than the other methods including *DEXSeq*. With FDR values one would usually want the values to be as small as possible. From that convention one can observe that *DifferentialRegulation* controls the FDR better than both *DEXSeq* and *eisaR*, whereas the latter two methods perform approximately equally as good.

**Table 3.1:** Proportion of p-values smaller than the proposed significance levels 10%, 5% and 1%

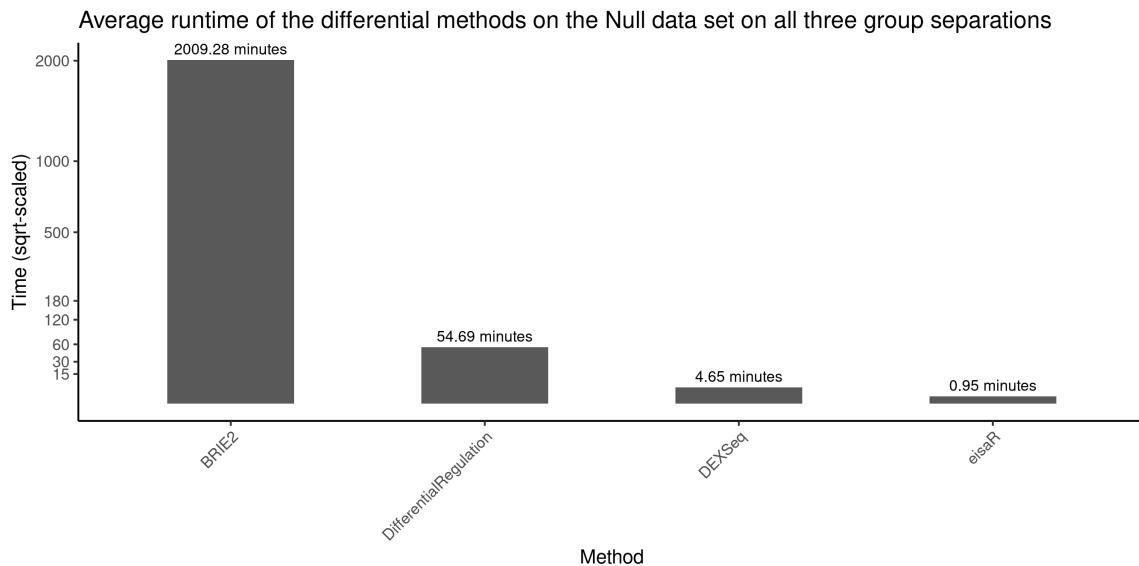
	10%	5%	1%
BRIE2	0.215	0.155	0.083
DifferentialRegulation	0.059	0.035	0.014
eisaR	0.108	0.065	0.026

**Table 3.2:** Proportion of FDR values smaller than the proposed significance levels 10%, 5% and 1%

	10%	5%	1%
BRIE2	0.080	0.061	0.038
DEXSeq	0.016	0.012	0.006
DifferentialRegulation	0.006	0.005	0.003
eisaR	0.017	0.010	0.004

### 3.4 Computational benchmark

Ultimately, we compared the computational burden of the differential methods excluding alignment and quantification. Alignment and quantification were excluded from the benchmark as all methods use the same input generated from *alevin-fry*, therefore including it would be redundant. The computational benchmark was run on the Null data and averaged across all three possible group separations. All methods were provided three cores on the same machine (internal server) to run the benchmark. However, *BRIE2* uses all cores available on a machine and *eisaR* only runs on one core. Figure 3.29 illustrates the average runtime of each differential method in minutes on a square root scaled axis, as there is a large difference in absolute runtime between the methods. From the Figure it is shown that *BRIE2* ran the longest - roughly 2000 minutes. However, we did not run *BRIE2* on a GPU, which is its intended use. The other three methods finished within a few minutes with *DifferentialRegulation* taking the longest and *eisaR* taking the shortest.



**Figure 3.29:** Runtime of the differential methods on the Null data averaged across all three possible group separations

## 3.5 Data availability

### Kidney mouse cells

The raw data can be downloaded from NCBI GEO (accession number GSE107585).

<https://www.ncbi.nlm.nih.gov/geo/query/acc.cgi?acc=GSE107585>

## 3.6 Code availability

All code for data preprocessing and analysis associated with the thesis is available at <https://github.com/joelmeili/DifferentialRegulation>.

# Chapter 4

## Discussion

### 4.1 Conclusion

In this thesis we investigate, how the relative abundance of spliced and unspliced reads differs between experimental conditions. Changes to these relative abundances are directly linked to gene regulation and methods that are capable of detecting differences already exist (e.g. *BRIE2* and *eisaR*). However, these methods do not account for multi-mapping uncertainty, thus we propose two solutions: i) *DEXSeq* and ii) our novel approach *DifferentialRegulation*. We investigated the performance of all methods on two semi-simulated data sets. The semi-simulated data sets were created by the use of real single-cell RNA sequencing data with four biological replicates. After alignment and quantification we applied quality control measures to the data. In a first step, we introduced an arbitrary differential effect to a subset of genes and cells by inverting the counts of spliced and unspliced reads. Further, we added DGE to a second subset of genes and cells as an additional nuisance parameter. Multi-mapping uncertainty was considered next to make the semi-simulated data sets more realistic. This was achieved by using the *minnow* pipeline where we used the two semi-simulated data sets as input. Again *alevin-fry* was used for alignment and quantification of the reads - such that we have estimated spliced, unspliced and ambiguous count matrices. We then analysed the performance of *BRIE2*, *eisaR*, *DEXSeq* and *DifferentialRegulation* in detecting the differential genes by comparing ROC and TPR v. FDR curves. From this analysis we found that *DifferentialRegulation* controls the FDR well for both data sets in comparison to the other three methods. Additionally, we examined the results stratified by gene abundance levels. We showed that for *DifferentialRegulation* TPR was consistent across gene abundance levels. Furthermore, we demonstrate that FDR is well calibrated for all levels of gene abundance with and without DGE. Next, we did a Null analysis on the original data set where we compared the distribution of p-values for all three possible group separations. We found that *BRIE2* had inflated p-values for all three group separations, whereas *DifferentialRegulation* had no inflated p-values at all. From the Null analysis it was also shown that *DifferentialRegulation* seems to be conservative as there was a tendency for inflation towards one. Ultimately, we ran a computational benchmark on the Null data where we applied all four methods on all three possible group separations and averaged the runtime. From the computational benchmark it was shown that the better performance of *DifferentialRegulation* comes with a longer runtime, however, there is also the possibility to run the method without equivalence classes, which is slightly less accurate however much faster.

From the previous analyses, we show that *DifferentialRegulation* had overall better results than the other methods, however, there are also some caveats to the method, for example, *DifferentialRegulation* cannot deal with additional covariates e.g. batch effects, whereas *BRIE2* and *DEXSeq* can.

## 4.2 Outlook

*DifferentialRegulation* has already been published on the Bioconductor project, which is an open source software that promotes reproducible analysis of data from emerging biological assays. Further, it is planned to extend the use case of *DifferentialRegulation* from only scRNA-seq data to bulk RNA-seq data, which allows deeper analysis on the transcript level. Ultimately, the work of this thesis is part of a future paper which needs some additional analyses on different data sets and some changes to the simulation algorithm.

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