

**Modern Algebra (Math 6302)**  
**Fall 2024, Final Exam**  
**\*\*skeleton version – not the actual exam\*\***

*For full credit, complete all problems, show your work, and justify your answers.*

- (1) Something which requires you to know and use the class equation for a group acting on itself by conjugation (see lectures 9 and 10).
- (2) Construct a non-Abelian group of order \*\*\*\*\*.
- (3) Something about prime ideals in commutative rings (from lecture notes).
- (4) Something about PIDs (from lecture notes).
- (5) Explicit construction of a finite field of a certain order.
- (6) Let  $R$  be **\*\*(some ring)\*\*** and let  $I \subseteq R$  be **\*\*(some ideal)\*\***.
  - (a) Find a complete set of distinct representatives for  $R/I$ .
  - (b) Prove **\*\*(something about  $R/I$ )\*\***.