

Technical University of Munich

# Development of a Destination Choice Model for Ontario

by

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A thesis submitted in partial fulfillment for the  
degree of Master of Science

in the  
Chair of Modeling Spatial Mobility  
Department of Civil, Geo and Environmental Engineering

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# Declaration of Authorship

I, Joseph Molloy, declare that this thesis titled, 'Development of a Destination Choice Model for Ontario' and the work presented in it are my own. I confirm that:

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- Where any part of this thesis has previously been submitted for a degree or any other qualification at this University or any other institution, this has been clearly stated.
- Where I have consulted the published work of others, this is always clearly attributed.
- Where I have quoted from the work of others, the source is always given. With the exception of such quotations, this thesis is entirely my own work.
- I have acknowledged all main sources of help.
- Where the thesis is based on work done by myself jointly with others, I have made clear exactly what was done by others and what I have contributed myself.

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Technical University of Munich

# *Abstract*

Chair of Modeling Spatial Mobility

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The Thesis Abstract is written here (and usually kept to just this page). The page is kept centered vertically so can expand into the blank space above the title too...

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# Abbreviations

**LAH** List Abbreviations **Here**

# Chapter 1

## Introduction

Long distance travel.....

The ability to travel long distances, for leisure, business or personal reasons, depends on enormous amounts of infrastructure such as highways, airports and railways. Such infrastructure is expensive, and can take decades, and billions of dollars, from the concept to implementation. It is also very hard to alter after it is put in place. Should a rail line or highway be built? Where should it start and end? What capacity is needed? These questions are hard to answer, precisely because they are questions about the future, and involve the collective impacts of the mobility behaviors of millions of unique individuals. To investigate these questions, transport planners need to be able to observe, visualize, understand and forecast where, why and how people travel.

### 1.1 Behavioral Models

Travel behavior is based on a series of choices; if they travel, where they travel to, and how they make the journey. Each individual takes different factors into account in their decision making process. How someone chooses to travel depends not just on concrete facts such as the location of the workplace and auto ownership, but also the daily weather, their schedule, personal preference of different transport modes and even just their current mood.

Since we cannot hope to replicate the decision making process of every individual exactly, particularly in the response to future changes in their environment, we use behavioral models to simplify, define and quantify human behavior and its impacts. We can either consider the population as a whole (aggregate modeling), or predict the choice of each

individual (disaggregate modeling). The respective benefits of the two approaches are discussed more in section 2.

Where the disaggregate modeling of human behaviour involves making a choice between alternatives, such as a destinations for a journey, or transport mode, discrete choice models can be used. In such scenarios, only one alternative can be selected. A person cannot travel to two places at the exact same time. Discrete choice models calculate the probability that an individual chooses a particular alternative. It is then assumed that each individual will choose the alternative that provides the highest utility. The resulting model can only be probabilistic in nature as in practice, complete information on the individual and the alternatives is lacking. Although the individual choice may not be exact, when the model is applied over a whole sample population, the results become reasonable.

## 1.2 Foundations of transport modeling

When modeling mobility behaviour, we seek to answer 5 key questions; if people travel and where they travel from, where they travel to, how they travel, and what route they take on the journey. These questions form the 4 steps of the traditional transport model. The four step model has been standard in transport modelling practice since the 1960's (Dios Ortúzar, Willumsen, et al. 1994).

The classic 4 step model works as an aggregate process. In trip generation, a trip vector listing of the number of trips from each origin is constructed. In the second step, trip distribution, an OD matrix is calculated, which can be constrained by the number of expected incoming trips at each destination, or by attributes of the destination, such as population. In the third step, the mode share (of auto, bus, train) for each OD pair is calculated. Finally, a route assignment is performed to allocate these trips to the transport network.

Advances in modeling techniques and computing have made fully disaggregate models based on the 4-step method feasible for large scale models. A list of trips is generated using a sample population and statistical model. A destination, mode and route are then predicted and assigned to each trip. For a large model, this can require the generation, storing, and processing of tens of millions of individual trips. Feedback loops are also often included to consider the inter-related influences of each step, such as the effect of congestion. Numerous researchers have found that mode choice influences destination choice, and there are two common approaches that can be taken to account for this. The logsum of the mode choice model is included as a parameter in destination choice

(Jonnalagadda et al. 2001; Mishra et al. 2011) or a combined destination-mode-choice model is calculated (Newman and Bernardin Jr 2010; Adler and Ben-Akiva 1976; Boyce et al. 1983)

### 1.3 Big data in transport modeling

Big data is the topic-du-jour in the fields of data analysis and transport modelling. There is no clear delineation between ‘normal data’ and ‘big data’. However, it has come to be defined by the four v’s: volume, velocity, variety and veracity (Beyer and Laney 2012). It is these characteristics that make it attractive as a data source for transportation modeling, particularly volume and veracity. Traditional transport models still rely on travel surveys and census data. Even comprehensive travel surveys such as the TSRC in Canada often have a sample size of only around 50,000 records per year, and there is no standard survey methodology or output. On the other hand, big data sources can track the movements of millions of individuals (volume), providing unprecedented spatial and temporal accuracy (veracity). Furthermore, the format of many common big data sources, such as cell phone records and geotagged social media interactions are standard, reducing the effort needed to define models around the data available. In some recent examples, GPS data is increasingly being incorporated into various transport models. Some examples include for destination choice (Schönfelder et al. 2006; Pan et al. 2006) and route assignment (Broach, Dill, and Gliebe 2012; Menghini et al. 2010).

While there has been a “virtual explosion of data availability”, as predicted by many, including Nagel and Axhausen (2001), Horni and Axhausen (2012) note that the collection of big data such as GPS and GSM data “is generally associated with privacy, cost and technical issues”. These challenges go against the ideal of general models that are flexible and transferable (Patriksson 2015). None the less, big data undoubtedly has a role to play in the future of transport modeling. Erath (2015) suggests further research into probabilistic models based on big data, and the blending of big data with data from travel diaries would be useful.

## Chapter 2

# Literature Review

Also known as Intercity models, long-distance transport models were first proposed in the 1960s, with two of the earliest being developed in the United States and Canada respectively (Canadian Transport Commission [1971](#)). These models were comparatively basic, with the demand component of the model only incorporating zonal population and income as attraction measures, and trip time, cost and convenience as impedance measures. More recent demand models include attributes such as auto ownership and household size.

Long-distance models are commonly defined to contain trips of certain length or longer, as opposed to the much more common urban model. TRB's NCHRP Report 735 notes that current state-wide models and travel surveys in the United States have used a range of thresholds to define long-distance trip-making, "either 50, 75, or 100 miles as the minimum threshold for trips to be considered long-distance." (Schiffer [2012](#))

According to Miller ([2004](#)), a distinct class of intercity travel demand models exist, which have unique characteristics when compared to urban models. "An intercity travel demand model is designed to forecast travel demand between two or more urban areas ... rather than travel within a given urban region". He also highlights two main features of such models. Firstly, he argues that an intercity travel demand model should apply to a well-defined travel corridor, containing a small number of major cities. Secondly he suggests that such models are almost always designed to model the impact of new travel modes such as high speed rail, or other policy initiatives.

Miller also notes that while urban models and methods are well documented in open literature, and applied in published policy analysis, intercity models are often the intellectual property of the consultants involved. The models are infrequently published in the scientific literature, and the travel data on private travel modes is often closely

guarded, meaning that the models are often hard to replicate, if they are published. It follows that “intercity travel demand models tend to be a less attractive/feasible application area for academic researchers than the more data-rich urban field.” (Miller 2004)

## 2.1 Aggregate Intercity Transport Models

Until the 1980s, intercity transport models were exclusively designed as aggregate models, which distributed trips between origin-destination pairs and modes using the gravity model proposed by (Casey 1955). However, as early as 1962, the deficiencies in this approach were identified by numerous researchers (1962; 1962). In 1967, (Wilson 1967) first proved the theoretical validity of the gravity model, following two decades of its use in practice. These theoretical foundations encouraged further use of the gravity model in the development of transport demand models.

## 2.2 Discrete Destination Choice Models

Despite their widespread acceptance and use in practice, the aggregate gravity model has some fundamental flaws as a modelling methodology. As an alternative, McFadden (1973); Ben-Akiva (1974) proposed the use of the logit model as a disaggregate method to model travel demand. McFadden, in his pioneering paper, noted that “When the model of choice behaviour under examination depends on unobserved characteristics in the population, the testable implications of the individual choice model are obscured.” (McFadden 1973)

Further research focused on the use of disaggregate models for the trip distribution step of the classic four step model. These came to be known as destination choice models, the focus of this thesis. A thorough investigation of the suitability of discrete choice models as opposed to aggregate methods for transportation modelling was conducted by Spear (1977). Spear noted that the

- Individual choice models are more data efficient than conventional (i.e. gravity) models.
- They can utilize the variation in socio-economic data much better, avoiding ecological fallacies.
- The probabilistic nature of the dependent variable allows for the modeling of interdependent choices, such as mode choice and trip chaining decisions.

Since then, the application of disaggregate models in transport demand modelling has been continually refined, with important research done in both modelling destination choice and mode choice in this manner. Daly (1982) focused on representing the attractiveness of a destination, in a destination choice model, while further work was done by Ben-Akiva (1974) and Anas (1983) in defining the structure and application of such models. Train (2009) comments that “discrete choice models cannot be calibrated using a simple curve fitting, as since the dependent variable, as a probability cannot be observed”. Instead, maximum likelihood estimation is used. Since the utility of every alternative must be calculated, this technique was prohibitive before the advent of modern computers for large scale problems. This may go some way to explaining the persistent popularity of aggregate models, due to their simplified computational requirements.

In chapter 9 of *Discrete Choice Analysis*, Akiva and Lerman (1985) present a comprehensive discussion of destination choice models. They note that “destination choice is characterized by a very large number of alternatives”, and that the selection of resolution of the choice set is a very important consideration. They further discuss the challenge of data availability for destination attractiveness. Since the attractiveness of data is not always available at a destination level, “the alternatives in a destination choice model must be based on aggregate alternatives”. Even with the modern GPS and social data available to the modern modeler, this is clearly still an issue. This is an important point that Ben-Akiva and Lerman make, that while destination choice models can model the decisions of individual travelers, they still need to rely on some level of aggregation for modeling the utility of each destination.

Discrete choice models have been repeatedly shown to provide better results than aggregate methods when modeling travel behavior (1984; 2013) compared the gravity model and multinomial logit destination choice model when integrated into a model for Maryland. They found that the destination choice model performed much better than the gravity model for a state-wide travel demand model.

## 2.3 Trip Chaining

Adler and Ben-Akiva (1979) were one of the first to model the inter-dependencies between links in a trip chain. They defined a theoretical and empirical model of trip chaining behavior to do so, based on utility theory, and accounting for the tradeoffs involved in multi-step chain trips. They, like most researchers in the area, focus on daily travel patterns within urban models. However, they note that “It is important that the determinants of non-work travel patterns that include multiple-sojourn tours

be better understood”. To do this, they model the utility to a given household of a particular travel pattern as a function of scheduling convenience, activity duration, income, destination attributes and socio-economic characteristics of the household. One of the significant advantages of a disaggregate destination model is the ability to model tours. Due to the nature of the data, trip chaining commonly isn’t included in long distance travel models. Moeckel, Fussell, and Donnelly (2015) considered its inclusion, however the proportion of multi-link trips was found to be too small, and the trip lengths between stops were not recorded in the National Household Travel Survey (NHTS) data they used.

Kitamura (1984) incorporated trip chaining directly into an analysis of destination choice. He used an approach called Prospective Utility that “represents the expected utility of the visit to that zone and also those visits that may be made”. In essence, this theory postulates that with two destinations A and B of equal utility, opportunity B will be more attractive than A to a trip maker when it is surrounded by destinations supporting other opportunities that the trip maker wishes to pursue.

## 2.4 Recent Intercity Transport Models

(Outwater et al. 2010) developed a state-wide model to model high speed rail. They combined both stated and revealed preference data in their attributes. For destination choice, they looked at destination attraction, employment and household characteristics, the region and area type, trip purpose, distance class, and party size. While not a combined destination-mode choice model, they combine some network data to calculate auto and non-auto accessibility, for peak and off-peak respectively. Destination was estimated using a simple multinomial logit model. The authors also note that their modeling shows “that an individual may value different trip characteristics for different distance-categories of travel”. They also modeled the area type of a zone, as one of rural, suburban or urban. Interaction terms were also created between zones, under the assumption that urban to urban trips are much more common.

More recently, models are also being designed on a larger, more ambitious scale. One such example is the new national model of long-distance travel in the United States (Outwater et al. 2015). This model focuses includes multiple advancements on previous models, including modeling at an individual household level, a high level of spatial detail for destination choice, and the vertical integration of all 4 steps of the classical model. Unlike activity based models, it uses a temporal resolution of months and weeks, not days, and jointly predicts destination and mode choice together.



## 2.5 Mnlogit R Package

In this thesis, the R package *mnlogit* (Hasan, Zhiyu, and Mahani 2014) is used to estimate the multinomial model of destination choice. This package provides improvements over the classic *mlogit* package, by reducing computer memory usage to allow for more model parameters. It also performs the maximum likelihood estimation in parallel for significant decrease in estimation runtime.

### 2.5.1 Data format

The model input must be provided in a long format. The format of the input can be described as followed: Let  $S$  be the set of input trips, and  $R$  be the total choice set of possible destination alternatives.

For each trip  $s \in S$ , an arbitrary choice set  $R_s$  is required, where

$$R_s = \{a | R_s \subseteq R \wedge \exists t \in S : destination(t) = a\}$$

The model input is then constructed by adding a row for each trip  $s$  and alternative  $a \in R_s$ , giving a total number of rows  $\sum_{s \in S} |R_s|$  for the model input. A boolean column is also added that indicates whether a particular choice was chosen for that trip or not.

### 2.5.2 Formula Specification

The *mnlogit* package accepts model formulas structured using the R formula package. A mlogit formula consists of 4 parts:  $choice \sim Y|X|Z$ , where  $X, Y, Z$  are as followed:

- Choice: the LHS of the equation, the column that indicates if an alternative was chosen or not.
- $X$ : Individual  $i$  specific variables with alternative  $k$  specific coefficients  $\vec{X}_i \vec{\beta}_k$ .
- $Y$ : Alternative specific variables with alternative independent coefficients  $\vec{Y}_i k \vec{\alpha}$ .
- $Z$ : Alternative specific variables with alternative specific coefficients  $\vec{Z}_i k \vec{\gamma}_k$ .

In the context of destination choice, individual variables are those such as income, gender and education level that pertain to the traveler. A coefficient must be estimated for every destination, as the value of the individual vary does not vary across the choice set for each trip, only between trips. Alternative specific variables can have coefficients

independent or dependent of the choice set. The coefficient only needs to be dependent on the alternative  $Z$  when the parameter has a different meaning across the choice set. This is more commonly used in mode choice modeling; for example, the calculation of cost might vary between car and train journeys.

Parts of the equation can also be excluded by specifying 0 or  $-1$  in the respective section. Intersects can also be removed by adding  $+0$  to the in the same way. The estimation will return an error if the equation cannot be solved, and the most common reason for this is high multi-colinearity between parameters specified in the model.

## 2.6 Location based social networks

The ubiquity of mobile GPS transceivers, especially in the smart phone market, has enabled a new category of social networks, called location based social networks (LBSN), which associate social networking data with a geo-referenced location. Different social networks have taken advantage of this opportunity in different ways. Facebook enables a user to mark themselves as safe during a natural disaster, flicker can show a map of where your images were taken, and google maps can provide accurate travel times by identifying areas of congestion.

Most location based social networks, such as facebook, tripadvisor and foursquare enable users to 'checkin' to a 'venue', such as a shop, tourist attraction or airport, and provide tips, ratings and reviews. When these services are used by millions of people around the world, in different countries and cities, a enourmous amount of data is collected, which can be used in a multitude of ways to explore mobility patterns.

Lindqvist et al. (2011) looked at how and why people use location sharing services such as foursquare, and discussed how users manage their privacy when using such services. (Cheng et al. 2011) collected 22 million checkins across 220,000 users to quantitatively assess human mobility patterns. 53% of their checkins came from foursquare, highlighting the dominance of foursquare in the LSBN space. They sampled location sharing status updates from the public Twitter feed, identifying users with geo-referenced tweets, and then collected the most recent 2000 geo-labeled tweets.

Noulas et al. (2012) used foursquare data to design gravity model based on Stouffer's theory of intervening opportunities. They found that while no universal law exists between mobility and distance, a universal behavior in all cities when measured with their rank-distance variable exists. Regarding the potential applications of LBSNs in future research, they note that the scale of data collected by foursquare provides the means to analyse and compare mobility patterns in different parts of the world, surpassing

cultural, geographical and political borders. They also warn “there may be a strong demographic bias in the community of Foursquare users”, before noting that “it is encouraging that the analysis and models developed in the context of the present work demonstrate strong similarities across multiple urban centers and different countries.”

Abdulazim et al. (2015) introduces a framework for inferring activity travel given nearby land use information gathered from LSBNs. Their results suggest that daily activity travel can be automatically inferred from LSBN data, and they present a generic method for acquiring land use data from LSBN services such as foursquare. The authors also present a case study for the greater Toronto and Hamilton area, Ontario, Canada, a subset of the study area for this thesis. S A et al. (2015) investigated the potential for cell phone and foursquare data to replace the use of Travel Surveys in calculating and Origin Destination Demand matrix. They found that The cell phone and Foursquare data were consistent with OD pairs expected to have higher trip volumes, but that some differences existed. Jin et al. (2014) proposed a doubly constrained gravity model based on LBSNs. They were able to achieve significant reductions in O-D estimation errors caused by sampling bias when compared to a singly constrained model.

## 2.7 Objectives

Disaggregate models provide clear advantages over aggregate methods in modelling trip distribution. While aggregate methods still hold sway in the modelling of long distance travel, due to the availability of data and more powerful computers, the modelling of destination choice using logit models is becoming more popular. Destination choice models provide more flexibility in attribute selection, and more efficient use of data. Most models include the basic socio-economic variables and a description of zone attractiveness.

It is often difficult or simply not appropriate to take a model that has been designed for another geographical region and apply it in study area of concern. Firstly, the data available for the study area will most likely be different to those available for other study areas. The data may provide more variables that weren't available to modellers working on other regions, or be more restricted, forcing the modeler to be creative in designing parameters that can represent the travel behavior in the region. Secondly, it is very difficult to design accurate models that work effectively when transposed to new study areas. This is due not just to obvious geographical differences, but variations in policy and culture that are difficult to reflect in a destination choice model. If every possible parameter reflecting was added to the model, not only would it be computationally infeasible, but there would be a high risk of overfitting in the model. The fact that the destination choice models already presented in the literature are individually unique

supports this notion that modelling is both a science and an art, and that there is no “one size fits all” model.

For these reasons, the design of a destination choice model for Ontario in itself reflects a new contribution to the field. The field of transport modelling is advanced every time the process of a designing a new model is performed. Future researchers can then look at the body of previous models, and use statistical analysis, their experience and intuition to select variables that best suit the requirements and use cases for which their model will be designed.

The second contribution of this thesis is the application of LSBNs to improve the utility modelling of destination choice. While work has been done on investigating mobility patterns, and the generation of OD matrices using LSBNs, their application to disaggregate models in transport has not been considered. This thesis will explore how foursquare check-in data can be used in the calculation of destination utility, and whether it can effectively replace other socio-economic variables such as employment. This is a significant contribution, as socio-economic data is not always available, especially at the high modelling resolutions made possible by the advances in microsimulation and computing technologies. check-ins data also provides an opportunity to model important traits of destination utility, such as the presence of national parks, that are not reflected in standard socio-economic variables.

## Chapter 3

# Data Acquisition and Analysis

### 3.1 Travel Survey of Residents of Canada

#### 3.1.1 Introduction

The Transport Survey of Residents of Canada (TSRC) is a monthly, cross-sectional survey collected by Statistic Canada to measure the volume, characteristics and economic impact of domestic travel. The survey provides a large quarterly sample of performed trips within Canada, along with socio-economic data and the activities and expenditures performed on each trip. Results are released yearly, with the data available at a monthly temporal resolution.

The TSRC was designed to measure the size and economic impacts of Canada's domestic tourism industry. It was first performed in 2005, and replaces the Canadian Travel Survey. In 2011, the survey was redesigned to bring the questionnaire more in line with the World Tourism Organisation guidelines, and align the recorded activities with the International Travel Survey (ITS).

The TSRC acts as the main data source for the estimation and calibration of the destination choice model presented by this Thesis. Hence, this section provides an overview of the aspects of the TSRC and its design that relate to the development of a destination choice model. In particular, the methodology behind the survey is discussed, and the relevant variables and weightings available in the resultant microdata are highlighted.

### 3.1.2 Method

The survey is performed as a voluntary supplement to the compulsory Labour Force Survey (LFS). The LFS is a mandatory household survey of around 54,000 households to measure employment, and has a 90% response rate. The LFS sample consists of the entire civilian, non-institutionalized population over 15 years of age. A sub-sample of these households is selected to answer the TSRC, excluding residents of the Yukon, the Northwest Territories and Nunavut and people living on Native Reserves. A respondent is randomly selected from the household and asked to complete the travel survey. The survey is a computer-assisted telephone interview (CATI) available in both of Canada's official languages, English and French. 15 minutes are allocated for each respondent, with as many trips being collected as possible in that time.

### 3.1.3 Data

#### 3.1.3.1 Spatial Resolution

All spatial data points, namely those for home location, trip origins and destinations and stopovers are provided in the microdata at three resolutions, Province or Territory, Census Division, and Census Metropolitan Agglomeration (CMA). Canada is made up of ten provinces and three territories, the largest of which is Ontario, the focus of this thesis.

Census Divisions are the next largest geographical area in Canada. Census Divisions represent groups of neighboring municipalities combined to aid regional planning and the provision of common services. After the provinces and territories, they are the most stable spatial unit. They were last modified for the 2011 census, and therefore are consistent between each TSRC dataset since the revised version was introduced. In most provinces and territories, these census divisions are defined in legislation, however in Newfoundland and Labrador, Manitoba, Saskatchewan, Alberta, Yukon, Northwest Territories and Nunavut, provincial or territorial law does not provide for these administrative geographic areas. In these cases, the census divisions are allocated by Statistics Canada.

Census sub-divisions are the next smallest geographical area, representing individual municipalities. These are recorded as part of the survey, however are not available in the TSRC microdata. The finest level of aggregation available is that of the Census Metropolitan Areas (CMA) and Census Agglomerations (CA). CMAs and CAs represent certain clustered areas of population around an urban core. More specifically, to be defined as a CMA, an area must have a total population of at least 100,000, with half

of those living in the core urban area. CAs, which related to CMAs but require a core population of only 10,000, are not recorded in the TSRC data.

Since CMAs do not topographically cover the whole Canadian study area, but only identify particular dense urban areas, census divisions are the most detailed resolution available for consistent use when working with the TSRC data. CMAs are only recorded for 51.5% of trip origins, and 48.3% of trip destinations. However, CMA's can be used to better allocate trips to transport zones in urban areas, as discussed in section 3.3.1.

### 3.1.3.2 Error Detection and Imputation

The computer-assisted nature of the survey allows for real-time error detection and consistency checking during the interview process. One example is that the program will inform the interviewer if the number of nights recorded for a trip does not match the number of nights recorded in various types of accommodations. Dont Know and Refused are also valid options for many questions, to prevent false answers been recorded. Sanity checks against extreme values are also performed, and the coding of geographical areas is mostly performed automatically.

Two forms of imputation are performed for the survey, for trip details and expenditure amounts respectively. Since the survey only allows 15 minutes for the recording of trip details, the details of non-selected trips are imputed from other trips recorded for that resident. This imputation process is multi-staged, and is performed per respondent. A donor pool of trips is selected that are similar to the non-selected trip. A distance function is then used to select the closest donor-trip to the recipient, and the detailed variables (activities, expenditures, etc) are copied over to the recipient trip.

### 3.1.3.3 Weighting

The weighting of records is particularly important when working with survey data. They allow the researcher to scale up the results for a sample to build an accurate representation of population, taking into account under- and over- represented groups within the survey. In total, four weightings are provided for the TSRC, with two relating to trip variables: full-sample person weights first-month person weights person-trip weights trip weights

As the TSRC sample is based on the LFS survey, person weights are applied from the LFS and recalibrated to reflect subsampling, non-response, and known control groups.

After the 2011 redesign, respondents are asked about same-day trips that ended in the previous month, but overnight trips that ended in the previous two months. This means that effectively only half the sample is asked about same-day trips. To account for this, two weights are provided for each person record. A first month weight, that can be used for any person variable, and a second "full sample" weight that can be applied to person characteristics and overnight travel variables.

The person-trip weight, used to estimate trip volume, is then calculated by accommodating for identical trips, declared and reported trips, missing data and non-response. These weights are treated for outliers and recall bias. In calculating the person-trip weight, the person weight is also multiplied by the number of identical trips that this trip represents. The person-trip weight (WTEP) can be used against all socio-economic characteristics, as well all trip and visit variables, excluding expenditures. Trip weight (WTTP) is then calculated by dividing the number of household members that went on the trip, is only used to calculate expenditures, and as such is not relevant to the model design.

#### 3.1.4 Microfile Format

The results from the TSRC are provided as yearly collections, separated into individual files for persons, trips and visits. The survey results are provided as fixed width delimited .dat files. A code book and data dictionaries are provided to decode the values stored in each line. The schema for encoded variables such as province are consistent across files and years (i.e. Ontario is always coded as 35), meaning that once read from the correct position on a line, values don't need to be decoded before being compared with each other.

Each person record is associated with one or more trips. Not all persons recorded in the person microdata necessarily have a trip recorded for a particular time period, as the survey records the travel behavior of both travelers and non-travelers.

Each recorded trip record has at least two associated visit records, or more if intermediate overnight stops were recorded. Visits are classified into two types, origins or destination/airport. Each Trip has one origin visit record, and at least one destination record. Where the main mode of travel for the trip is "Air", two or more airports are specified as visit records, along with the 3-digit airport code for the respective Canadian airport. The survey codebook notes that these airport records may be adjusted to protect respondent privacy.



## **Trip Datafile**

Trips covered by the TSRC include same-day trips of more than 40km and overnight trips with at least one night in Canada. Domestic same-day and overnight trips are recorded in full. International trips with no nights in Canada are not recorded in the TSRC. For trips with an overnight destination, but some nights in Canada, only the domestic portion of the trip is recorded, with the point of departure from Canada recorded in the MDxxx variables for trip destination. The TR\_D11 variable records the number of times this trip was performed in the reference month, and must be taken into account when estimating trip frequencies.

Socio-economic variables for the traveler are recorded for each trip record; namely age, gender, education level, employment status and income. The number of household members who participated on the trip is also recorded.

Trip purpose is recorded at two categorical levels. In the first, purposes are split into four options:

- Holidays, leisure or recreation
- Visit friends or relatives
- Business - All business and work related trips, except routine travel which is a regular part of the job
- Other - All trips for other reasons except regular household chores

## **Visit Datafile**

The visit data file provides a stops performed on each trip, which can be linked to the relevant trip by the Public Use Microdata File Number (PUMFID) and the Trip Identification Number (TRIPID). Each trip has at least two visits associated with it, an origin and a destination visit, differentiated by the VISRECFL variable. The AIRFLAG variable is used to identify visit records that refer to an airport entry or exit.

If a location is visited twice during a single trip, only one visit is recorded for that location. The visits are not guaranteed to be recorded in the chronological order of visitation, even though the visits are collected in chronological order during the survey process. This lack of order prevents the modeling of trip chaining from the TSRC visit records.

### 3.1.5 Season of Travel

Canada has starkly contrasting seasons which influence travel choices of residents. The TSRC provides the month of travel for each trip, and these are aggregated into two seasons, designed to highlight the impact of winter conditions on long distance travel behavior. For this thesis, the months from November to March are considered winter, with the rest as summer. With this classification, summer covers 7 out of 12 months of year, or 58.4%. Table 3.1 shows how leisure and visit trip counts occur disproportionately in the summer months. The  $P$  value indicates the probability that this result is not by chance.

TABLE 3.1: Seasonal split of TSRC trips

	Summer	Winter	Summer %	P
Business	11,750	8,641	57.62%	0.02
Leisure	52,639	19,774	72.69%	1.00
Visit	61,630	39,856	60.73%	1.00

It is self explanatory that destination choice should depend on seasonal factors. The example of winter sports is a prime example. Winter sports is an activity that people willing travel long distances for. In 2014, TSRC respondents reported participating in winter sports in 4% of overnight trips, and 2% of same day trips. These trips naturally only occur in the winter months, at certain destinations.

## 3.2 Filtering of Trip Records

For the model input, the TSRC trip records from 2011 to 2014 were collated together, giving 220,512 trip records. Not all these trips were relevant to the estimation of the destination choice model. Firstly, records were removed where:

- Either an origin or destination is not stated
- The trip purpose is not leisure, visit or business
- A distance is not recorded
- The mode is recorded as air and the destination and origin airports are identical

The TSRC trip files provide trip records not just for Ontario, but for all of Canada. However, as a model for Ontario, we are only concerned with the following categories of trips that influence travel in Ontario:

- Internal trips within Ontario - Internal (II)
- Trips entering Ontario - Incoming (EI)
- Trips leaving Ontario - Outgoing (IE)
- Trips that cross Ontario - External (EE)

Any trips that didn't fit one of these categories are also excluded from the trip dataset used to estimate the destination choice model. Internal, incoming and outgoing trips don't need to be filtered, and all trips in these categories remain in the trip set. External trips, on the other hand, are filtered to remove trips that don't cross Ontario. Excluding such external trips is important to make sure that the estimated model reflects the behavior of travel in Ontario, which could be different to the behaviors in other provinces.

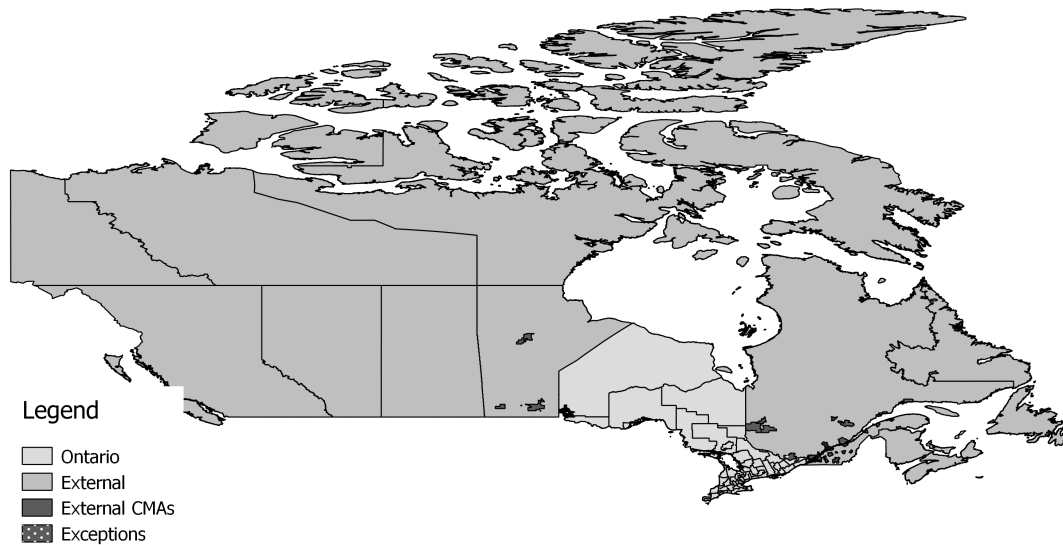


FIGURE 3.1: Dividing external zones into east and west

The unique geography of the Canadian provinces greatly restricts the number of external origin-destination pairs that need to be considered when excluding unwanted external trips. Ontario acts as land bridge between the eastern and western parts of Canada, see figure 3.1, dividing the external zones into two groups, east and west. Trips originating in the east and arriving in west have to pass through Ontario, and vice versa. For trips within a group, this is not true. Hence all trips that don't go between east and west

can be removed. There are two zones which are the exception to this, zones 85 and 117 in western Quebec. Journeys between these zones and other zones in Quebec may pass through Ontario. For example, figure 3.2 illustrates a journey from Gatiéau, Quebec to Montreal Airport. a car journey takes around 2 hours when passing through Ontario, and 2 hours and 30 minutes otherwise. It is hence likely that travellers will chose the route passing through Ontario. Trips between these two exception zones and all other zones in Quebec are therefore retained.

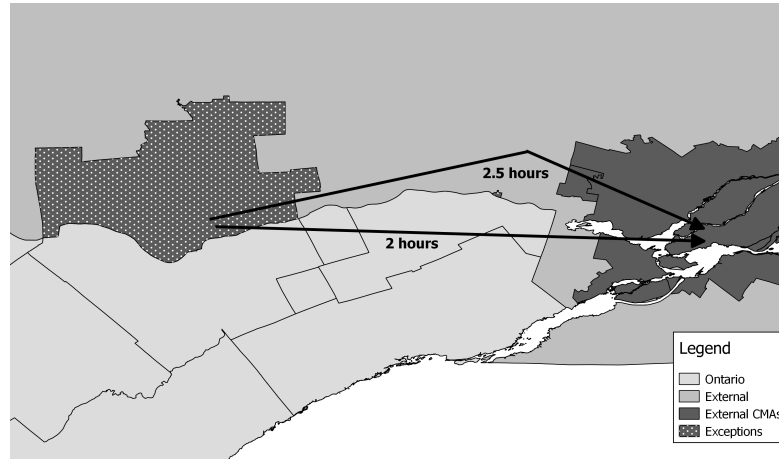


FIGURE 3.2: An example of an external origin-destination pair that passes through Ontario

Figure 3.3 illustrates how our the trip distribution of the estimated trips fits the observed distribution much better after undesired external trips are removed. In total 69,328 individual trip records remain from the TSRC dataset for model estimation, representing 40,177,841 weighted trips.

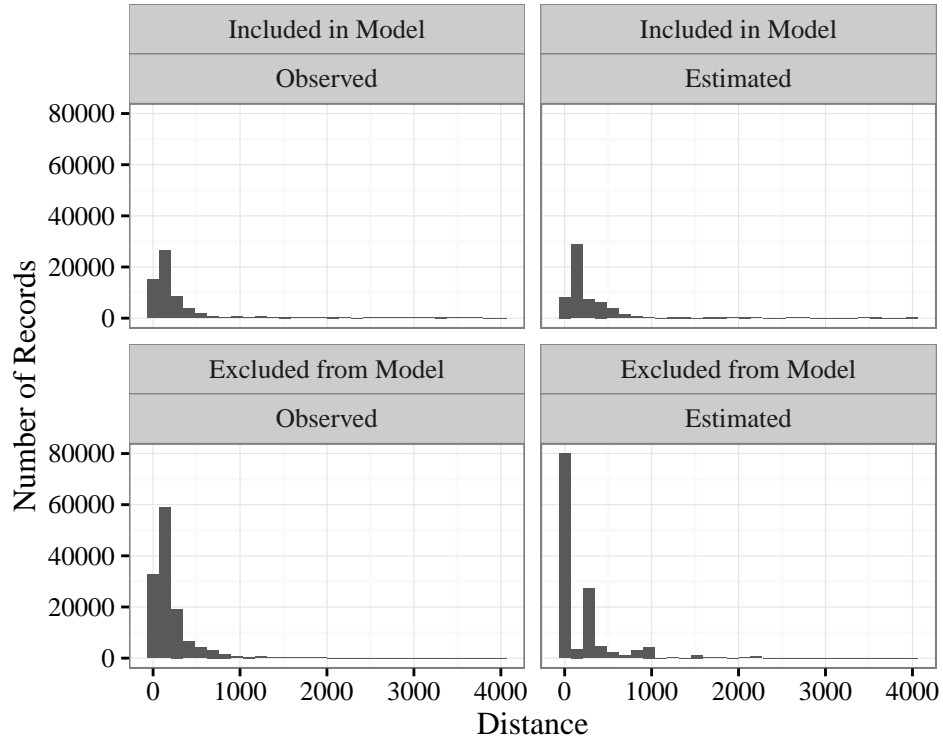


FIGURE 3.3: Estimated vs. Observed Trip Distance

### 3.3 Zone System

To avoid confusion throughout the rest of this thesis, the reader should be aware that there are two zone systems considered in the following chapter.

- **TAZs**, or traffic analysis zones, are the zones provided for the project, representing the proposed final spatial resolution of the transport model.
- **Zones**, are the zones representing the destinations in the destination choice model, referred to collectively as the *zone system* in the remainder of this thesis.

This chapter discusses the definition of the choice set of alternatives for the destination choice model. Numerous factors need to be considered when designing the choice set. Firstly, The sample size of the data available to estimate the model coefficients is an important restraint. With a small sample set relative to the size of the destination choiceset, not enough records are available to calculate the parameter coefficients with high confidence. Hence, the size of the choiceset needs to be considered carefully. Large destinations choice sets also lead to very long computation times when estimating the model coefficients. A balance needs to be found between the detail represented in the choice set, and the computability and validity of the coefficients.

For this particular destination choice model, a zone system was already provided, consisting of 6671 Traffic Analysis Zones (TAZ). The TAZs can be grouped into 4 categories; 6495 internal zones for Ontario, 48 and 121 external zones representing the rest of Canada and North America respectively, and 7 zones for remaining world-wide destinations. As this thesis is only concerned with domestic travel within Canada, only the internal zones for Ontario, and 48 external zones covering the other provinces of Canada are considered. The external zones are taken directly from the TAZs as TSRC origins and destinations are directly translatable to the external TAZs.

The Internal TAZs within Ontario are allocated using a gradual raster based zone approach, based on the method developed by Moeckel and Donnelly (2015). The 6495 generated TAZs vary in size from  $0.879km^2$  to  $3600km^2$ , with smaller cells defined for more populous areas, and larger cells for regional areas. The gradual zone system is designed on the premise that it is desirable to have larger zones in rural areas where there is less population, and hence, less activity. This method reduces the number of TAZs, and hence, the complexity of the model, while only removing detail where it is least required.

Unfortunately, the TSRC trip origins and destinations are only recorded at the resolution of CMAs and CDs, which are much broader than the raster based TAZs created for Ontario. For this thesis, a zone system is designed based on the TSRC spatial resolution for the design and estimation of the destination choice model. The allocation of trips origins and destinations to TAZs will be performed at a later stage in the transport model, and is outside the scope of this thesis. The proposed method is discussed further in section 5.3.

### 3.3.1 Defining a zone system for Ontario based on the TSRC data

As discussed in 3.1.3, provinces and census divisions cover the national study area completely. Hence as a first step, the zones are defined by the census divisions comprising Ontario, of which there are 49. However, the TAZs are much smaller than their encompassing CDs, even in rural areas. When the zone system is defined purely using the Census Divisions within Ontario, over 50% of Census Divisions have more than 75 TAZs, with a large spread of values (see figure 3.4).

Although CMAs are defined only for selected urban areas of Canada, they can be considered alongside the CDs when allocating zones to improve the spatial resolution of the zone system. The concept of a CMA aligns closely with the objective behind the gradual raster cell size of the provided zone system for Ontario. CMAs identify areas of denser population around an urban core that may be of particular significance to geographers

and modelers. By simply including CMAs as zones in the aggregated zoning model, the number of zones is increased to 57, allowing trip origins and destinations in urban areas to be more accurately assigned during disaggregation to TAZs. As seen in figure 3.4, the lower number of average TAZs per zone indicates an improved zone system.

However, there is still further detail to be extracted from the combination of CDs and CMAs. The previous approach creates a large outlier that consists of over 2000 TAZs. This outlier corresponds to the CMA of Toronto, the most populous in Ontario, a very large generator and attractor of trips. In 2014, Toronto represented 13.4% and 10% of trip origins and destinations respectively. The disaggregation of trip origins and destinations between 2000 child TAZs would undoubtedly affect the overall quality of the model.

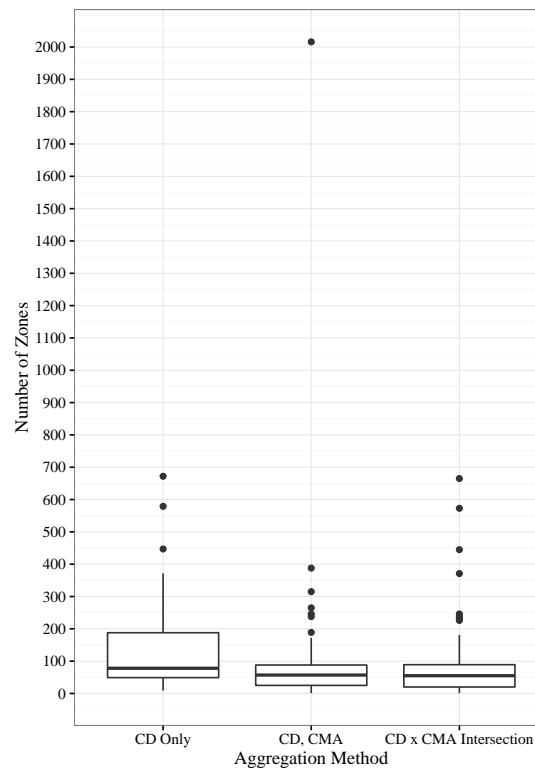


FIGURE 3.4: Different methods of aggregating internal zones to match the TSRC spatial resolution.

This outlier was not present when only the CDs were considered as destination alternatives. Since CMAs often overlap multiple CDs, rather than simply including CMAs and CDs independently, the union of the CDs and CMAs can be taken to fully reflect the number of destination choices available in the TSRC data. This results in 69 zones for Ontario, a 41% increase over the simplest approach that only considers CDs.

Figure 3.4 illustrates the difference between these methods. When only Census Divisions are used, a significant number of CDs have a large number of assigned TAZs. When the

CMAs are considered, the results are clearly better. A lower average number of TAZs per aggregate zone will give improved results when trips origins and destinations are disaggregated. Taking the intersection of CDs and CMAs has little effect on most zones, but still improves the overall result in a very significant way. The CMA of Toronto overlaps with 7 separate CDs, and can with this method be divided into seven smaller zones.

This third method has another advantage. The a distinction between urban and rural areas is now encoded into the zone system. This will be important in the estimation process as 51.5% of trips in the filtered TSRC survey originated in a CMA, and 48.3% had destination recorded as a CMA. Not only is it clear that urban areas are important drivers of long distance travel, but that, interestingly, CMAs are more likely to be origins than destinations.

### 3.4 Aggregating Zonal Data

All the data on distances, population and employment was provided at the TAZ level. This data was aggregated to the zone system using the following approach. The TAZs themselves were assigned to the zone which intersected their centroid. Where the centroid of the TAZ didn't intersect any zones, the first intersecting zone was used. When the TAZ did not intersect with any part of the Canadian census boundaries at all, it was assigned manually to the nearest zone using GIS software.

Socio-economic variables, namely population and employment, were aggregated from the TAZ level to the zone system using a simple summation.

The aggregation of the distance skim matrix was more involved. The matrix, in OMX format (Stabler et al. 2014), contained the auto travel times between all TAZs. It was calculated without congestion using the Canadian road network. Intra-zonal travel times were not included. To aggregate the skim matrix to the zone system used in the destination choice model, the distance  $d$  between each child OD pair was weighted by the multiplied populations  $p$  of the origin and destination.

$$d_{ij} = \frac{\sum_{k \in i, l \in j} d_{kl} \cdot p_k \cdot p_l}{\sum_{k \in i, l \in j} p_k \cdot p_l}$$



## 3.5 Foursquare

Trip distribution models that consider only population and employment have a significant flaw. They fail to account for points of interest (POI), such as National Parks that attract large numbers of people, yet exist in areas of low population and employment. Discrete choice modeling provides the opportunity to incorporate parameters that reflect these drivers of travel demand.

Leisure travel is a particular case where socioeconomic metrics don't always reflect the attractiveness of a destination. Areas such as lakes, national parks and ski resorts are popular long distance recreational destinations in the summer and winter respectively, yet have small populations and employment. Simma, Schlich, and Axhausen (2001) developed a destination choice model for leisure travel in Switzerland that considered many variables of destination attractiveness such as the number of swimming pools, ski area qualities and land use attributes. They found that while

The TSRC microfile records the activities performed on each recorded trip and destination visited during a trip. When aggregated by trip destination, these activities give an indication of which zones provide particular attractions such as national parks or ski areas. The number of trips with each recorded activity can also be used to identify the importance of a particular activity for each zone. However, there are two key problems with this approach:

- When implementing of the model, The spatial resolution of the TSRC microfile means that the location where an activity was performed can only be determined at a zone level. Another data source is still needed to identify key points of interest such as hospitals and tourist attractions to predict trip destinations at the TAZ level.
- As a domestic survey, the TSRC doesn't cover the US, meaning a different method would need to be used to identify key attractions across the border.

In this section, we describe how the collection and processing of foursquare check-in data was performed in order to build destination utility variables.

### 3.5.1 Foursquare Venue Search API

Foursquare collects a wealth of data, on where and when users check-in. Users and their behavior can be tracked over time using twitter as a proxy, however the time-frame for

this thesis made this method unfeasible. Instead, the public venue API was used, which is much more limited in its scope, only providing a cross-sectional dataset of POIs within the search area. For a search area and criteria, the API returns a list of venues in JSON format. Each venue record provides the following relevant information:

- Name
- Venue category
- Geo-referenced location
- Number of unique visitors
- Number of total check-ins

Each request is limited to roughly 1 square degree of longitude and latitude in search area, and only the top 50 venues for that search are returned. A limit of 5000 requests per hour is also enforced. Search results are returned based on the popularity of the venues. How the rank of returned venues is determined by foursquare is not specified.

The API does not return check-in counts by date, so it can only be used to generate a total metric of activity for each venue, up to the time of the search. For the forecasting of trips to individual venues, this would present a significant obstacle. In this thesis, however, the foursquare metrics are only used for identifying the intensity of activity in zones that may not be reflected in socioeconomic variables. Check-in counts also can not be filtered by origin country or state. This capability would, in a larger model, also allow us to identify U.S. destinations that are commonly visited by Canadian travelers, as opposed to all users of foursquare.

### 3.5.2 Demographic Bias

While the use of social networks is becoming more ubiquitous throughout the general population, LSBNs such as foursquare still have a particular user demographic, which should be taken into account when working with social network based data. The data retrieved from the foursquare API does not provide any demographic information that can be used to weight the retrieved data.

In this thesis, the potential impact of bias is minimized, as only the intensity of activity for each category in a zone is measured as a variable. There is also no stratification of these variables by age, gender or education level in the model estimation. Such stratification would cause concerns with demographic bias, for example with older groups

of travelers. One concern is that certain venue categories could be under-represented in the data, such as aged care services, or those where a check-in might be taboo such as a place of worship. This is considered by grouping venues into broad categories, which are then considered as model parameters.

### 3.5.3 Methodology

To collect the venue data from the Foursquare API, the following procedure was followed:

1. A developer account was set up which allowed access to the API. The maximum search area allowed is smaller than most external zones, so a search grid of 1 degree raster cells was generated for the study area.
2. Using the activities specified in the TSRC as a reference, a selection of potentially important venue categories was curated (see table 3.2).
3. Each category was mapped to at most 5 main foursquare venue categories, on which the search was performed. This is necessary to exclude venue categories such as “States & Municipalities”.
4. A python script was written to query the foursquare API for each raster cell and category, returning the top 50 venues, while adhering to the rate limit of 5000 requests per hour. Calls to the api had to be structured as:

```
https://api.foursquare.com/v2/venues/search?intent=browse
&limit=50&sw={sw}&ne={nw}& categoryId={categories}
```

where

- sw, ne are the bottom-left and top-right corners of the search area
  - categories is a comma separated list of venue ids.
5. Unique venues were then stored in the PostGIS database, and each tagged with the zone to which it geographically belongs.
  6. Two attributes were then calculated for each zone and category; the number of venues of that category in the zone, and the number of check-ins for each category and zone.

The foursquare API provides data at a higher spatial resolution than the TSRC microfile, but without the temporal detail. In table 3.2, the number of venues and check-ins per category are presented. In total, 34,041 unique venues and 7,981,458 check-ins were collected for the different categories.

TABLE 3.2: foursquare venue categories

Search Category	Venue Categories					Venues	Check-ins
Medical	Dentist's Office	Doctor's Office	Hospital	Medical Center	Veterinarian	6,294	586,082
	Ski Area	Ski Chairlift	Ski Chalet	Ski Lodge	Ski Trail	1,048	203,266
Airport	Airport	Airport Gate	Airport Lounge	Airport Terminal	Plane	1,882	1,919,050
Hotel	Bed & Breakfast	Hostel	Hotel	Motel	Resort	7,268	1,502,248
Nightlife	Bar	Brewery	Dive Bar	Pub	Sports Bar	5,900	1,936,153
Outdoors	National Park	Campground	Nature Preserve	Other Great Outdoors	Scenic Lookout	7,262	709,274
Sightseeing	Art Gallery	Historic Site	Museum	Theme Park	Scenic Lookout	4,387	1,125,385
Total						34,041	7,981,458

## Chapter 4

# Gravity Model

As discussed in section 2, the Gravity model is still the standard approach to estimating OD trip distribution matrices. Its simplicity and low computational complexity makes it attractive to modelers. In modeling, it is always a good idea to develop the simplest model first. Firstly, it may be good enough, and a more complex model not required. Secondly, the errors in simpler models can aid the development of more complicated models. As such, this model will be used as a baseline to compare the destination choice models presented in section 5.

### 4.1 Design

The gravity model is singly constrained on the origin, with the size of each zone being the sum of population and employment. The gravity model was implemented in Java, and is specified as followed:

$$T_{ij} = \frac{A_j \cdot e^{-\alpha \cdot d_{ij}}}{\sum_j A_j \cdot e^{-\alpha \cdot d_{ij}}} \cdot P_i$$

Where

$T_{ij}$  is the number of trips between zones  $i, j$ .

$P_i$  is the number of trips produced in origin zone  $i$ .

$A_j$  is the attraction at destination zone  $j$ .

$\alpha$  is the impedance factor, calibrated with the average trip distance.

$d_{ij}$  is the distance between zones  $i, j$ .

## 4.2 Model Strata

It is common practice to design a transport model that is in reality, a collection of separate models for heterogeneous groups of travelers, and trips. The most common attribute to categorize by is trip purpose. The categories recorded for each trip by the TSRC, our sample of trip records is split into 4 categories, Business, Visit, Leisure and Other, of which only the first three are used. In figure 4.1, the number of trips for each category by year in the TSRC is shown. A model is then estimated for each trip purpose, and the results of the model strata combined into the final model. Each purpose, when multiple years are combined in one dataset, has a suitably large sample size to support model estimation.

TABLE 4.1: Sample size by trip purpose

	2011	2012	2013	2014	Total
Business	1,798	1,640	1,449	1,341	6,228
Leisure	5,939	5,878	5,515	5,577	2,2909
Visit	9,057	8,777	7,962	7,618	3,3414
Total	18,694	18,016	1,6547	16,071	6,9328

## 4.3 Calibration

A separate model was created for each trip purpose, and calibrated to match the expected average trip distance  $\bar{d}$ , calculated from the trip distances recorded in the TSRC, to within 1%. The results of the calibration are presented in table 4.2. The average observed trip distance is  $\bar{d}$ , the average predicted trip distance  $d$ , and the impedance factor  $k$ . As measurements of model accuracy, the model correlation ( $r^2$ ), root mean square error (RMSE) and normalized root mean square error (NRMSE) are provided.

TABLE 4.2: Gravity Model calibration

Model	Trips	$\bar{d}$	$d$	$\alpha$	$r^2$	RMSE	NRMSE
Business	34,229.43	244	243.20	0.0013	0.42	53.45	0.94
Leisure	83,357.94	149	148.13	0.0035	0.36	100.72	1.03
Visit	129,843.18	163	164.77	0.0030	0.52	103.65	0.93

## 4.4 Results

Figure 4.1 presents an residuals plot, with the number of observed trips on the x axis, and difference between the observed and predicted on the y axis. While the three purposes cannot be compared with each other in the graph, due to the differing sample sizes, it is clear that all three models have serious errors, and are almost unusable. The predicted values should fall roughly above and below the dotted line. There is a definite pattern in the observed data, indicating that important OD pairs, ones with large numbers of trips, are strongly underestimated. The numerous OD pairs with small numbers of trips dominate the calibration to the observed average trip distance. However, this comes at the expense of model accuracy for large, important connections.

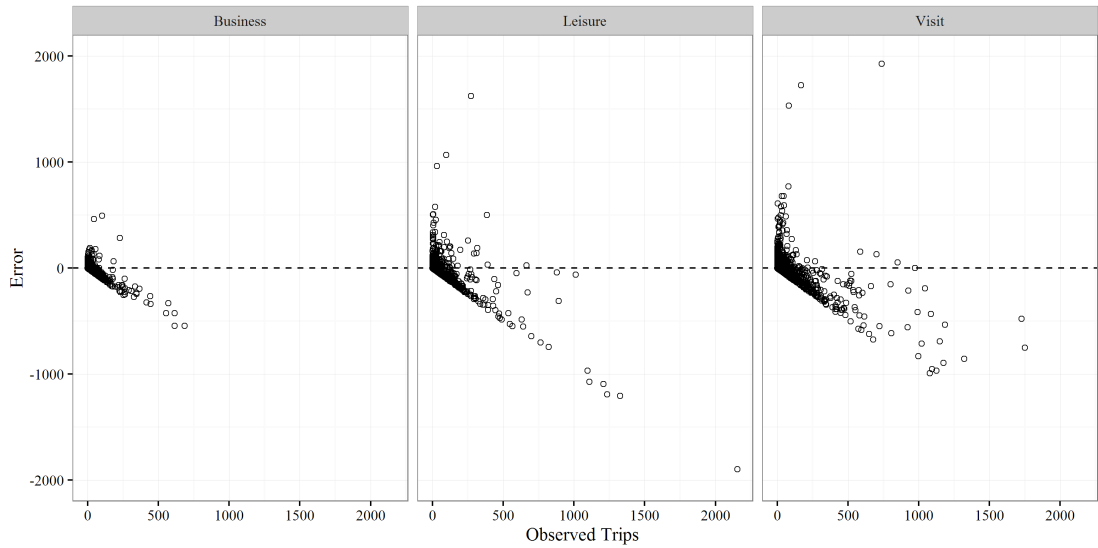


FIGURE 4.1: Gravity model errors by observed trip count for OD pairs by trip purpose

Figure 4.2 gives a better indication of how the model fits these important zones. On the x axis is the absolute error  $|x - E(x)|$ , and on the y axis, a variant of the relative error, which we call maximum relative error is plotted.

$$\frac{|x - E(x)|}{\min(x, E(x))}$$

In the standard relative error  $\frac{|x - E(x)|}{E(x)}$ , only one term,  $E(x)$  is present in the denominator, meaning that large underestimations produce very small relative errors, reducing the visibility of such errors in the chart. In contrast, the maximum relative error treats overestimations and underestimations equally. For this model, it is also more useful than the error plot in figure 4.1, as the error Large y values are only of concern when the x value, namely absolute error, is also large.

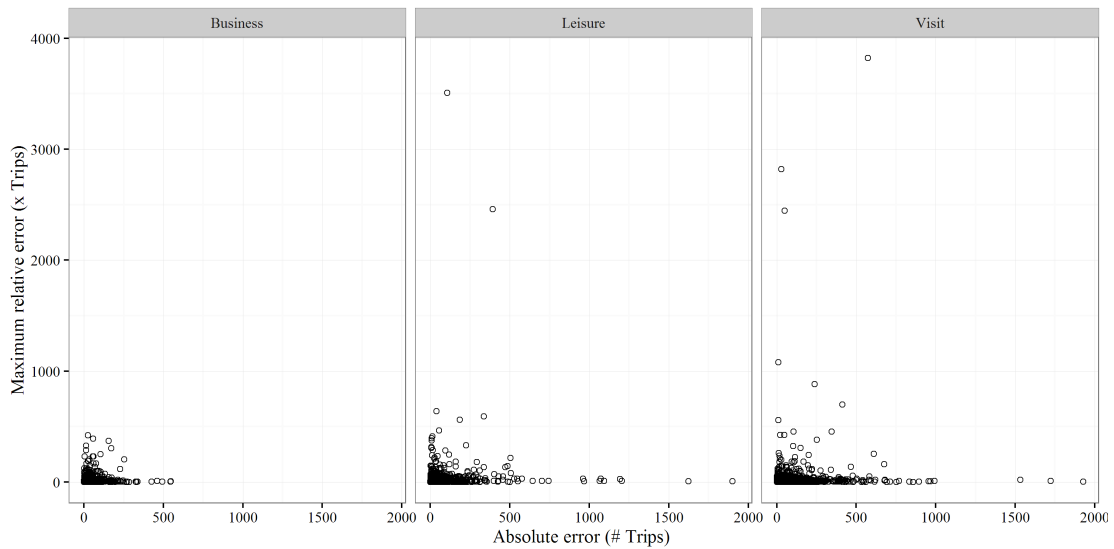


FIGURE 4.2: Maximum relative error chart for OD pairs by trip purpose

Large outliers are present for all three trip purposes in figure 4.2. A clear weakness of the gravity model can be seen by further examining some of these outliers for the leisure purpose. The number of leisure trips originating from zones in the Toronto region to tourist destinations such as Niagara Falls and Muskoka are strongly underestimated. By its nature, the gravity model is limited in how well it can model such zone interactions, as it only takes into account one attraction factor and one impedance factor.

The propensity for leisure travelers to visit destinations with tourist attractions is clearly determined by factors other than the population and employment of the destination. The multinomial logit model of destination choice discussed in the next section adds such factors, and explores how they can be modeled.



## Chapter 5

# Destination Choice Model

### 5.1 Introduction

As mentioned multiple times in this thesis already, discrete choice models are much more powerful than gravity models. However, this power comes at the cost of additional complexity, both in their set-up, estimation and application. A destination choice model gives the probability that the traveller  $i$  will choose alternative  $j$ .

$$P_{ni} = \frac{e^{\beta x_{ni}}}{\sum_{k=1}^K e^{\beta x_{nk}}}$$

where

$$x_{nk} = \{\beta_{nk}^1, \dots, \beta_{nk}^K\} \text{ and } \{w_1, \dots, w_K\}$$

$K$  = is the total number of alternatives

These  $\beta$ , the coefficients of the model, need to be calibrated using some optimisation function. In this thesis, this is done using Maximum Likelihood Estimation, through the `mnlogit` package described in section 2.5. The probabilities provided by an estimated model for each alternative and individual can then be used in a weighted selection of a destination for that individual. Furthermore, a trip distribution matrix can be created by summing the probabilities over the trip sample for each OD pair. This allows the model to directly be compared with aggregate models.

Firstly, the data must be transformed into the correct input structure, this process was also described in section 2.5. The next step is estimation. The estimation of a discrete

choice model for destination choice is much more involved than the construction of a gravity model, since modeler has almost infinite possible permutations of variables at his or her disposal. Divining the best variables is part art, part science. Some variables may be statistically significant, while adding little useful explanatory power to the model. Others may only be significant when paired with certain other variables. Rather than just present a final model, this next section elaborates on the model development process, covering the estimation, validation and implementation stages.

## 5.2 Estimation

In this section, the evolution of a destination choice model is presented. In *m1*, a simple model based on the gravity model is presented. *m2* and *m3* add further interaction variables between origin and destinations. *m4* and *m5* explore the potential of LSBN data to improve destination choice models when incorporated into the calculation of destination utility.

### 5.2.1 Socioeconomic Variables

For the first model, the same inputs as for the gravity model are used, namely the exponential of distance  $e^{-d_{ij}}$ , and the combined population  $p$  and employment  $emp$ .

The distance factor for each trip purpose was adjusted by the impedance factor  $k$  estimated for the respective gravity model (see chapter 4). This approach significantly improves the model, and provides a quick way to calibrate the distance coefficient without requiring the design of a more complicated GEV models.

Metropolitan areas are not homogeneous in land use patterns. There exists residential areas and central business districts to which people may choose to travel. However, at the spatial resolution of our zone system these differences are hidden, resulting in a very high correlation between population and employment across the destination choice set of 98.95%. Therefore as with the gravity model, population and employment are summed together. This value is then log transformed, to account for the long tail in the distribution (see figure A.1 in the appendix. In order to simplify the further model equations, we assign a new variable for each destination

$$civic_j = \log(p_j + emp_j)$$

The resulting model  $m1$ , is defined by the utility  $u$  of destination  $j$  for a traveler in origin  $i$ :

$$u_{ij} = \beta_1 e^{-\alpha \cdot d_{ij}} + \beta_2 civic_j$$

where  $\beta_n$  are the coefficients to be estimated by the `mnlogit` package.

The employment data is classified by NAICS category, and models were tested that considered different combinations of employment categories. This investigation found that filtering the categories of employment did not improve the model. The individual employment categories were also not considered separately as unique variables, as they were highly inter-correlated (see table A.2 in appendix (CITE)).

TABLE 5.1:  $m1$  model coefficients

Parameter	Visit		Leisure		Business	
$e^{-\alpha \cdot d_{ij}}$	4.29	***	3.86	***	4.21	***
$civic_j$	0.51	***	0.35	***	0.76	***

The parameters of this model  $m1$  (see table 5.1) are encouraging. All the signs are as expected, and differences in the coefficients across trip purposes are evident. A leisure trip is less likely to go towards areas of civic importance than visits or business, and the trip distance is naturally less important for business travelers. For each trip purpose, the basic multinomial logit model already performs better than the gravity model, as evident in the higher correlation and lower RMSE values in table 5.8.

### 5.2.2 Origin-Destination Interactions

In this section, the model is extended to reflect the relationship between the origin and destination that might affect the choice of destination. Model  $m2$  is specified by the utility function

$$u_{ij} = \beta_1 e^{-\alpha \cdot d_{ij}} + \beta_2 civic_j + \beta_3 language_{ij} + \beta_4 mm_{ij} + \beta_5 rm_{ij}$$

where

$$language_{ij} = language(i) \neq language(j)$$

$$mm_{ij} = metro(i) \wedge metro(j)$$

$$rm_{ij} = !metro(i) \wedge metro(j)$$

The variable  $language_{ij}$  reflects if the traveler is traveling to a zone where the main spoken language is different, namely somewhere in Quebec, where the main spoken language is French. Potentially, travelers may be more likely to choose a destination where the same language is spoken.  $mm_{ij}$  and  $rm_{ij}$  are designed to model the tendency to travel towards metropolitan areas. A zone is classified as metro when it is part of a CMA, and rural otherwise. There are 4 possible combinations of the metropolitan flag for origin and destination pairs, however, only two were selected for inclusion in the model. The flag that identifies trips leaving metropolitan areas towards rural areas,  $mr_{ij}$ , results in an unsolvable model, and all other combinations, other than the one selected,  $\beta_4 mm_{ij} + \beta_5 rm_{ij}$ , also result in unsolvable models.

The use of these two parameters add small improvements to the model, as can be seen in the lower AIC. The RMSE is almost the same between the models. Table 5.2 presents the estimated parameters for this model. The new parameters vary strongly between trip purposes.  $mm_{ij}$  works well for each trip purpose, with visit and leisure trips more likely to leave metropolitan areas, and business travel more likely to be inter metropolitan. However, language and  $rm_{ij}$  do not work as well. They are not statistically significant for visit trips, and the coefficient value is at least an order of magnitude smaller than for the other trip purposes. Business dealings normally require a common language, and hence it is not surprising to see a negative coefficient for language in this category, however the language coefficient for leisure is hard to justify. Finally,  $rm_{ij}$  is not significant for two trip purposes, despite working well for leisure trips.

TABLE 5.2:  $m2$  model coefficients

Parameter	Visit		Leisure		Business	
$e^{-\alpha d_{ij}}$	4.35	***	4.57	***	3.81	***
$civic_j$	0.52	***	0.48	***	0.73	***
$language_{ij}$	0.05	*	0.58	***	-0.44	***
$mm_{ij}$	-0.10	***	-0.99	***	0.55	***
$rm_{ij}$	0.06	*	-0.39	***	-0.09	.

Comparing figures 4.1 and 5.1, many outliers have been significantly brought back towards the origin, indicating an improvement in the model. However, there are still some significant outliers, with a sample of the largest in table A.1 in the appendix. These outliers fall into two categories:

- Overestimation of intra-zonal trips within metropolitan zones such as Toronto.

- Underestimation of leisure and visit trips from metropolitan centers to tourist attractions such as Niagara Falls.

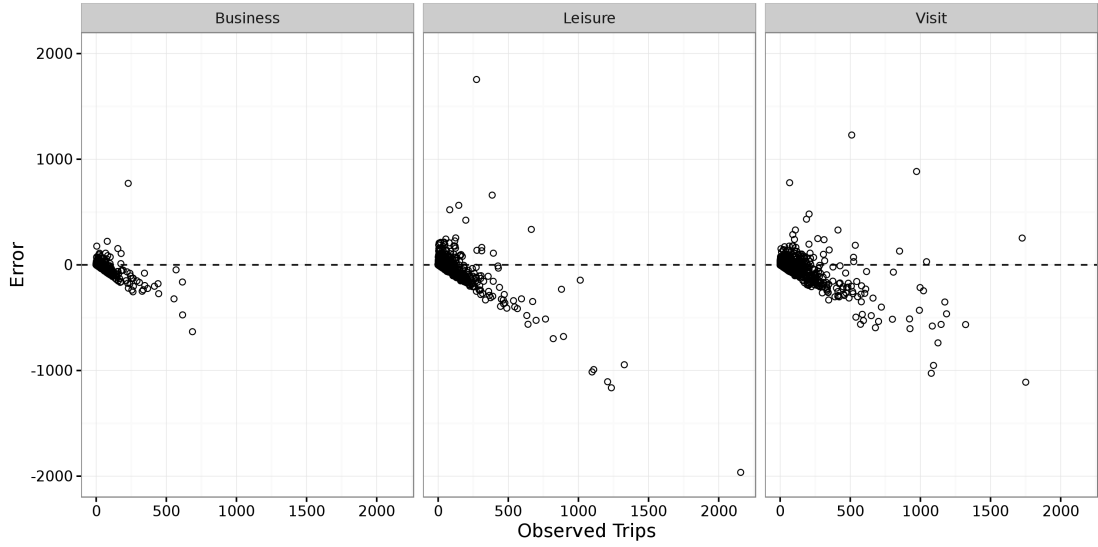


FIGURE 5.1:  $m2$  model errors by observed trip count for OD pairs by trip purpose

The large intra-zonal trip counts occur in small metropolitan zones, while in rural zones, intrazonal trip counts are underestimated (See figure A.3 in the appendix. Since we want to penalize intra-zonal travel in the metropolitan zones, but allow it in larger rural zones,  $mm_{ij}$  is replaced with three new variables:

$$intrametro_{ij} = \begin{cases} 1, & \text{if } metro(i) \wedge i = j \\ 0, & \text{otherwise} \end{cases}$$

$$intermetro_{ij} = \begin{cases} 1 & \text{if } metro(i) \wedge metro(j) \wedge i \neq j \\ 0, & \text{otherwise} \end{cases}$$

$$intrarural_{ij} = \begin{cases} 1 & \text{if } !metro(i) \wedge i = j \\ 0, & \text{otherwise} \end{cases}$$

The first variable  $intrametro_{ij}$  identifies trips within the same zone, where that zone is a metropolitan zone. This allows the model to reflect the propensity of a traveler to leave a metropolitan zone when they travel. The second,  $intermetro_{ij}$  is 1 when the traveler is traveling from one metropolitan zone to another. This may be a common choice for business travelers, but less likely for recreational trips. The third variable,  $intrarural_{ij}$  allows the model to consider that in larger, rural zones, there are more likely to be

sufficient opportunities within the zone, and that the distances to reach other zones are more significant. However, its inclusion significantly improves the model results, and as presented in 5.3, it has a strong influence, particularly for business travel.

The other zone interaction variables  $language_{ij}$  and  $rm_{ij}$  are removed in this iteration. They weren't suitable in the previous model, and the significance of their coefficients did not improve in this iteration when combined with the new variables  $intrametro_{ij}$ ,  $intrametro_{ij}$  and  $intrarural_{ij}$ .

The parameters for the  $m3$  model are showing in table 5.3. They are all significant, with the three new variables having differing magnitudes and signs, that each make logical sense for the different purposes. Business shows a strong preference for traveling to other metropolitan areas, as expected. Leisure travel is also very strongly influenced by metropolitan connections, but with a negative sign. This replicates the observed explanatory power of the  $rm_{ij}$  variable for leisure travel in  $m2$ , while also working for visit and business trips as well.

TABLE 5.3:  $m3$  model coefficients

Parameter	Visit			Leisure			Business		
$e^{-\alpha \cdot d_{ij}}$	4.83	***		4.75	***		4.19	***	
$civic_j$	0.57	***		0.52	***		0.76	***	
$intermetro_{ij}$	-0.08	***		-0.87	***		0.56	***	
$intrametro_{ij}$	-1.68	***		-2.56	***		-0.89	***	
$intrarural_{ij}$	0.39	***		0.85	***		1.66	***	

In table 5.8 we can see significant improvements throughout the model iterations across all metrics. In figure B.1, we can also see visually the significant improvements over the gravity model. The errors on OD pairs with small numbers of observed trips are drastically reduced, particularly for visit trips. The trend to under-estimate OD pairs with large numbers of observed trips is still evident (see figure B.1), and this problem is tackled in the next section.

### 5.2.3 Incorporating LBSN Data

The traditional socio-economic variables don't reflect why people travel to a particular destination. People don't travel to a location purely because many people live there, but because there are opportunities to perform certain activities in that location. Population and employment act as proxy variables for some of these opportunities, but not all.

This section incorporates data from LSBNs to improve the destination choice model, particularly for leisure trips.

The TSRC data show that activities such as skiing and visiting national parks are commonly performed on long distance trips. Areas where these outdoor activities are performed often have a low population and employment, while still providing attractive features to the traveler.

The collection and processing of LSBN data from foursquare was covered in section 3.5. To summarize briefly, the venues were collected into the following categories for each destination:

- Medical
- Ski Area
- Airport
- Hotel
- Sightseeing
- Nightlife
- Outdoors

Different multinomial logit models utilizing the foursquare data were created, to explore the suitability of different categories, and whether they had different explanatory effects for different trip purposes. For each destination, two metrics were available for representing destination attractiveness; the number of venues, and the total number of checkins across all venues. It was found that the best approach involved taking the natural log of the check-in count for each category. This gave the highest level of significance, as it corrected for the long right-hand tail present in the checkin counts for each category.

Certain categories were found to be significant for particular trip purposes. For example, the outdoor category was only significant for leisure trips, and the Medical category was only significant for visit trips. As would be reasonably expected, the number of hotel checkins was a significant variable across all trip purposes for long distance travel.

After exploring different combinations of the foursquare categories as parameters in the model, a model was settled on that was simple, yet powerful, using the most effective categories. The following categories were included in the model; Hotels, Sightseeing, Medical, Outdoors and Skiing.

The main objective of including foursquare data was to investigate how the modeling of leisure destination choice can be improved. To this end, The common summer leisure activity, outdoor recreation, and the classic winter activity, skiing, were represented through categories containing the types of venues commonly visited to perform these activities. Hence, two variables were added only for the leisure model strata. One for

outdoor venues, and one for skiing areas. These two variables were found to be significant only when they were estimated for trips occurring in the season in which their respective activities are normally performed.

In model  $m3$ , it was observed that leisure trips to the zone containing Niagara Falls were underestimated by 85%. This particular important case was additionally controlled for by the addition of an extra variable using the sightseeing category, that is only considered for trips of the leisure purpose to the Niagara zone. The sightseeing category was also evaluated across all trip purposes as its own variable.

The foursquare variables were included into the multinomial logit model as the following.

$$\begin{aligned}
 medical_j &= (purpose == "visit") \cdot \log(medical_j) \\
 hotel_j &= \log(hotel_j) \\
 sightseeing_j &= \log(sightseeing_j) \\
 naigara_j &= (purpose == "leisure") \cdot (j == "niagara") \cdot \log(sightseeing_j) \\
 outdoors_j &= (purpose == "leisure") \cdot (season == "summer") \cdot \log(outdoors_j) \\
 skiing_j &= (purpose == "leisure") \cdot (season == "winter") \cdot \log(skiing_j)
 \end{aligned}$$

Below, two models are presented that apply foursquare data,  $m4$  and  $m5$ .  $m4$  illustrates the explanatory power of the foursquare data alone, by excluding the classic measure of attraction. For practical purposes, such a model is unfeasible, as population and employment are important variables for predicting the impact of socioeconomic changes on travel patterns. However, even on its own, the foursquare data still performs equivalently to the  $m3$  model for business and visit trips, and significantly better for leisure trips (see table 5.8).

We can see that the popularity of hotels and sightseeing venues is particularly important for leisure travel. Business conferences are often located in areas of tourist significance, as a way of promoting the event, supporting the large coefficient for sightseeing in the business category. The presence of medical facilities is also strongly influential on attractiveness of visit trip destinations.



TABLE 5.4:  $m4$  model coefficients

Parameter	Visit		Leisure		Business	
$e^{-\alpha \cdot d_{ij}}$	4.41	***	4.11	***	4.43	***
$hotel_j$	0.09	***	0.21	***	0.20	***
$sightseeing_j$	0.08	***	0.02	***	0.24	***
$niagara_j$			0.12	***		
$outdoors_j$			0.04	***		
$skiing_j$			0.09	***		
$medical_j$	0.16	***				

$m5$  re-includes all the variables from  $m3$ . In this model,  $intermetro_{ij}$  and  $intrametro_{ij}$  were found to be no longer significant for the visit trip purpose, and were therefore excluded for this model strata. They were retained for both leisure and business trips. The combination of  $m3$  and  $m4$  to form  $m5$  gives the best model so far, with noticeably higher correlation and lower normalized RMSE for both business and leisure trips. The AIC metric also improves dramatically, even despite the increased number of parameters. The value of the foursquare variables, except for sightseeing, remain consistent after the addition of the the variables from model  $m3$ . The signs and magnitude of the variables from  $m3$  also change little.

TABLE 5.5:  $m5$  model coefficients

Parameter	Visit		Leisure		Business	
$e^{-\alpha \cdot d_{ij}}$	5.00	***	5.35	***	4.37	***
$civic_j$	0.21	***	-0.15	***	0.36	***
$intermetro_{ij}$			-0.81	***	0.72	***
$intrametro_{ij}$	-1.75	***	-2.88	***	-0.87	***
$intrarural_{ij}$	0.24	***	0.58	***	1.51	***
$hotel_j$	0.11	***	0.27	***	0.17	***
$sightseeing_j$	0.04	***	0.13	***	0.08	***
$niagara_j$			0.13	***		
$outdoors_j$			0.03	***		
$skiing_j$			0.10	***		
$medical_j$	0.07	***				

Overall, this model performs better across all trip purposes than the  $m3$  model without variables based on foursquare data. Particularly noticeable is the large improvement

across all metrics for leisure travel. Figure 5.2 shows impact of the foursquare variables for leisure travel. While it is hard to see the impacts for smaller OD pairs, the graph does illustrate how the errors for major outliers have been reduced.

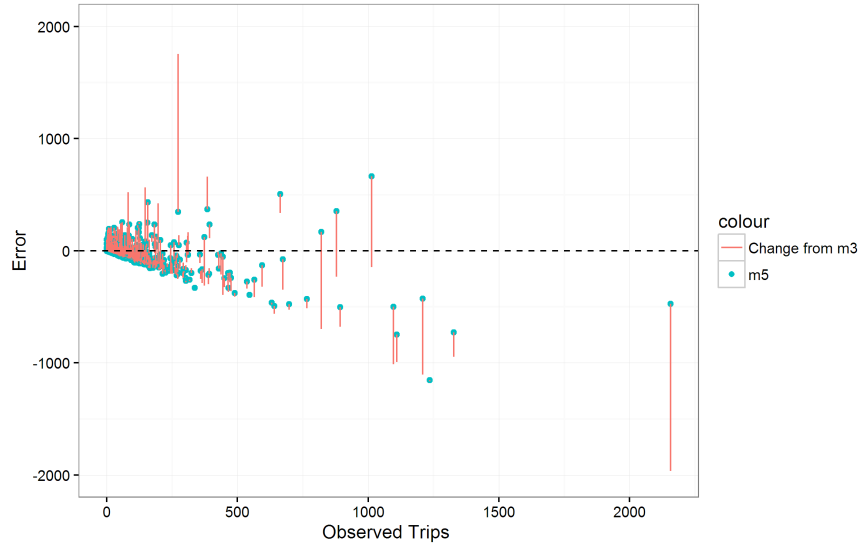


FIGURE 5.2: Effect of adding foursquare variables to model  $m3$  on leisure trips

#### 5.2.4 Income Strata

Sociodemographic factors, such as income are important explanatory variables (Kitamura, Mokhtarian, and Laidet 1997). Since income is a characteristic of the individual, it doesn't vary between alternatives. However the income of the traveler may influence his or her perception of the utility of each alternative. Including income as a variable in the destination choice model requires at a minimum, one separate coefficient for each of the 117 alternatives. Since the income is stored as an ordinal variable, realistically, a dummy variable for each income category would be required. Tried in the model, this resulted in significant coefficients for some zones, but not others, with no appreciable pattern. This approach was discarded due to the lack of overall significance, and large number of coefficients required.

An alternative approach is to strata the destination choice model by income categories. This approach was tried with numerous permutations. First with the 4 individual categories, secondly, with two categories: low income (1,2) and high income(3,4), and third, with the income categories grouped as 1,2,3 and 4. Table 5.6 shows the parameters of the models for the groupings of 1,2 and 3,4 against the non-strata model. A visual inspection shows that the parameters are mostly consistent between the models. The *distance* variable does show variation between the two strata, but other variables are mostly consistent across the strata. Where a coefficient is different between the strata,

such as *intermetro* for visit travel for the low income strata, it is no longer significant. In all scenarios, the performance of the models with income strata, according to the  $r^2$  and  $NRMSE$  metrics, is almost identical compared to the non-strata model (see table 5.7). Although there are surely model permutations where variables based on income are more significant, based on the lack of difference between the strata coefficients, income was not included in this destination choice model.

TABLE 5.6: Income-strata model coefficients (high &amp; low income groupings)

Income-strata	Visit				Leisure				Business			
	low		high		low		high		low		high	
$e^{-\alpha \cdot d_{ij}}$	5.23	***	4.83	***	5.41	***	5.39	***	5.95	***	3.87	***
$civic_j$	0.23	***	0.23	***	-0.17	***	-0.14	***	0.31	***	0.4	***
$intermetro_{ij}$	0		-0.11	***	-0.68	***	-0.91	***	0.83	***	0.71	***
$intrametro_{ij}$	-1.66	***	-2.29	***	-2.62	***	-3	***	-1.49	***	-1	***
$intrarural_{ij}$	0.25	***	0.07		0.51	***	0.47	***	1.57	***	1.38	***
$hotel_j$	0.1	***	0.13	***	0.28	***	0.25	***	0.23	***	0.18	***
$sightseeing_j$	0.06	***	0.01		0.15	***	0.14	***	0.02		0.08	***
$niagara_j$					0.13	***	0.13	***				
$outdoors_j$					0		0.04	***				
$skiing_j$					0.09	***	0.1	***				
$medical_j$	0.02	.	0.12	***								

TABLE 5.7: Income-strata model results

Model	<i>m5</i>	<i>income-strata</i>
$r^2$		
Business	0.77	0.78
Leisure	0.80	0.80
Visit	0.82	0.81
NRMSE (%)		
Business	0.66	0.65
Leisure	0.61	0.60
Visit	0.59	0.59

### 5.2.5 Refinement after considering trip length

A distribution of the trip lengths produced by the model was used to evaluate the accuracy of the estimated MNL model. The observed average trip length is different

to those in the gravity model, as for the gravity model, the recorded distances from the TSRC were used. For the Destination Choice model, the length of each trip was calculated using the zonal skim matrix.

Figure 5.3 shows an excellent fit to the observed data, however, the average trip length of 214.84 km is low. The general shape of the distribution also an overestimation of shorter trips. To compensate for this, the logarithm of distance was added as a parameter. With the second distance term, the average trip distance of the overall predicted model was reduced to 3.1% of the observed average trip length. Including the logarithm of distance also slightly improves the accuracy across trip purposes, most noticeably for visitation trips. This model is presented as the final estimated model *m6*. With so little difference in the overall average trip length between the observed and predicted models, no further calibration is needed.

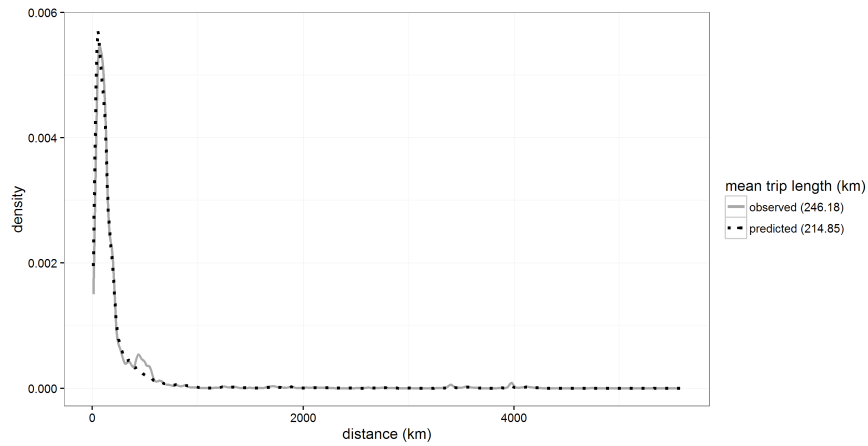


FIGURE 5.3: Trip length distribution of model *m5*

### 5.2.6 Estimation Results

Table 5.8 contains various statistical measures that measure the iterative improvements throughout the model estimation process. An increase in the loglikelihood indicates a higher probability that the model reflects the reality, assuming that the input data remains the same.  $r^2$  is the correlation between the predicted and observed trip counts for each OD pair. Likewise, RMSE, or root mean square error another measure of the differences between predicted and observed values. In this case, lower is better. Finally, the NRMSE is an alternative measure of the RMSE, normalized by the standard deviation of the observed trip counts. This last measure allows for a better comparison of model performance between trip purposes, as they have different sample sizes in the observed data.

TABLE 5.8: Comparison of model iterations

Model	<i>m0</i>	<i>m1</i>	<i>m2</i>	<i>m3</i>	<i>m4</i>	<i>m5</i>	<i>m6</i>
# Coefficients	1	2	4	5	7	11	
<b>Loglikelihood</b>							
Business		- 21,053	- 20,930	- 20,596	-21,071	-20,288	-20,091
Leisure		- 86,054	- 84,705	- 83,663	-81,192	-78,038	-77,808
Visit		- 117,463	- 117,441	- 115,666	-116,862	-114,557	-113,189
<b>AIC</b>							
Business		42,110	41,870	41,201	42,148	40,590	40,195
Leisure		172,113	169,420	167,337	162,396	156,095	155,638
Visit		234,931	234,893	231,342	233,731	229,128	226,393
<b><math>r^2</math></b>							
Business	0.43	0.62	0.62	0.73	0.56	0.77	0.77
Leisure	0.36	0.47	0.49	0.56	0.63	0.80	0.82
Visit	0.52	0.69	0.69	0.80	0.65	0.82	0.84
<b>RMSE</b>							
Business	53.45	45.95	45.75	39.53	49.76	37.26	36.98
Leisure	100.72	90.05	88.85	82.29	79.66	59.61	58.68
Visit	103.65	87.32	87.34	69.07	94.23	65.95	61.35
<b>NRMSE (%)</b>							
Business	0.94	0.81	0.80	0.70	0.88	0.66	0.65
Leisure	1.03	0.92	0.91	0.84	0.81	0.61	0.60
Visit	0.93	0.78	0.78	0.62	0.85	0.59	0.55

### 5.3 Implementation

The Destination Choice model described in this thesis was designed as a component of a larger long distance model for the Ministry of Transportation, Ontario. This long distance model is being developed in the JAVA programming language as a traditional 4-step model.

In the trip generation phase, a list of trips without destinations is generated for a synthetic population of households and persons. These trips are then passed into the destination choice model, which assigns a destination for each trip. For each trip the destination choice model is run, returning a predicted destination for that trip. The algorithm

works as followed, with step 2 being performed across the list of trips in parallel.

1. A Destination Choice Model is initialized with the following:
  - Coefficients for each model strata
  - Destination zones and their attributes
  - The distance matrix between zones
2. For each trip:
  - (a) Calculate the utility  $u_j$  for each destination  $j$ , using the relevant stored coefficients.
  - (b) calculate the denominator of the logit equation  $q = \sum_{j=1}^J e^{u_j}$
  - (c) Calculate the probability of each destination  $j$ ,  $P(j) = e^{u_j}/q$
  - (d) Choose a destination based on the probabilities using an *EnumeratedDistribution* from the Apache commons math library
 

```
return new EnumeratedDistribution<>(probabilities).sample();
```
  - (e) store the destination in the trip object

## 5.4 Calibration

The model was calibrated against the original input data to the estimation

## 5.5 Sensitivity Analysis - Case study of a new Ski Resort

This section presents a hypothetical application of the developed destination choice model. For any large scale land use planning or development, it is important to model the impacts that such development will have on the transport network. As an example of this, a hypothetical scenario of the development of a large new ski resort is presented. Such resorts not only provide infrastructure for skiing and other snow-based activities, but require the development of multiple new hotels, employee housing, and retail infrastructure. In the winter months, ski resorts can generate significant demands on the transport network, and this needs to be taken account when considering such a development.

In the hypothetical scenario, a new resort is proposed for the highlands area north of Toronto (see figure ??). The higher elevation ensures good snowfall, and the elevation

difference makes for exciting riders for snow sports enthusiasts. Two sites are being considered, one to the west of the range, and one to the east, closer to Ottawa. While this resort can naturally not be the size of mega resorts in British Columbia or Alberta, its development is expected to bring similar numbers of visitors as other resorts in Ontario. Two average sized hotels will also be built at the base of the resort to accommodate guests. In the summer, the resort will attract visitors by providing mountain biking facilities and hiking. Additional housing for 400 new residents will be required to support 300 jobs.

This somewhat contrived scenario assumes that other policy and development considerations, such as site location and transport access have all been dealt with. The design of the scenario presents the opportunity to investigate the sensitivity of the variables based on the foursquare data. The variables concerned are hotels, skiing and outdoor. The impact of the new development is estimated through adjusting these variables for the zone in which the development will take place. The foursquare POI database developed in section ?? was used to estimate adjustments for each of the categories. Taking all venues in Ontario, the average number of checkins per venue for each search category was calculated. The following adjustments are made for the respective zones, and their values are displayed in table 5.9.

- Skiing: The average number of checkins for ski areas
- Hotel: Twice the average number of checkins for hotels
- Outdoor: The average number of checkins per outdoor venue

TABLE 5.9: Inputs for sensitivity analysis scenario

Parameter	Old Value	Adjustment	New Value	Increase %
$civic_{ij}$	42216	700	42916	
$hotel_j$	1393	8304	9697	
$outdoors_j$	1	3389	3390	
$skiing_j$ 40	3550		3590	

## 5.6 Remaining implementation work

This thesis presents an operational destination choice model for domestic travel to and from Ontario. The U.S.-Ontario border is an important source of incoming trips to Ontario, and external trips that pass through to other parts of Canada. Further work

is needed to extend the model to include firstly continental travel to the United States, and then also intercontinental travel. The Canadian International Travel Survey (ITS) provides trip records that can be used to estimate such a model, although it does not include socioeconomic data for travelers.

For a fully functional transport model, the trip ends of the completely specified trips will have to be allocated to the higher resolution TAZs before route assignment can take place. This can happen before or after mode choice. Train (2009) discusses the issue of geographical aggregation, specifically in regards to destination choice in chapter 3 of *Discrete Choice Methods with Simulation*. “to specify a destination choice model that is not sensitive to the level of zonal aggregation, representative utility needs to be specified with parameters inside a log operation.” As all parameters that actually represent destination utility (population and employment, and foursquare categorical variables) have been transformed with a logarithmic function, The model should be insensitive to the resolution of the zone system, and the estimated coefficients transferable to a an choice set of alternatives based on the TAZs of the larger transport model.



## Chapter 6

# Discussion

In this section, a discussion of the results is presented, and framed in the context of other work in the field. Firstly, a brief overview of the different models is presented. Chapter 5.2 on estimation explores the models in more detail. The importance and relevance of the work is then discussed. Finally, the limitations of the work are presented and areas where future work is required are detailed.

### 6.1 Overview of results

In the estimation process, it was found that the output from the calibrated gravity model was unrealistic to the point of being almost unusable. The correlation of between 0.36 and 0.52 across trip purposes was very low. The calibrated impedance coefficients from the gravity model were retained to build a simple discrete choice model incorporating distance, population and employment. Essentially using the same variables as the gravity model, this first destination choice model performed significantly better across all trip purposes. Further models, incorporating interactions between the origin and destination, such as metropolitan/regional connections further improved the model results. Not all interactions were found to be significant. In particular, the barrier between English and French speaking parts of Canada had only a limited impact.

The next iteration improved the estimation of intra-zonal trips in smaller metropolitan zones. It was discovered that to properly account for intra-zonal behavior, separate parameters were needed for rural and metropolitan origins. The coefficients for these two parameters were of opposite sign, logically indicating that intra-zonal long distance travel is more likely in larger rural zones, but unlikely in metropolitan zones that are barely large enough to support an internal long distance trip. The accuracy of the

model for leisure trips was noticeably weaker than for the other two models, and it was hypothesized that better modeling of the destination attractiveness for leisure activities would improve the results.

The LBSN based models demonstrated how venue checkin data from foursquare could be incorporated into a destination choice model. As hypothesized, the foursquare data dramatically improved the estimation of leisure trips. It also performed well for visit and business trips. Even with all other variables excluded except for distance, the model ( $m_4$ ) performed comparably to the basic  $m_1$  model. When the foursquare data was combined with the variables from previous iterations, a very agreeable model was produced.

Scenario Analysis

## 6.2 contributions

This thesis provides multiple contributions to the field. As a completed and calibrated domestic destination choice model, it presents a significant amount of work towards a completed long distance transport model for Ontario. The superior performance of the destination choice models over the gravity model validates the work of others in this area (Mishra et al. 2013), and adds further weight to the argument that such disaggregate methods, despite the additional effort required, result in better transport models (Sbayti and Roden 2010; Lemp, McWethy, and Kockelman 2007). Bhatta and Larsen (2011) found that the inclusion of intra-zonal trips is important in model estimation, and the investigations in this paper into origin-destination interactions highlight some novel ways to adjust for these in long distance modeling.

Big data already presents both exciting opportunities, and daunting challenges to transportation modeling. It is predicted that by 2020, 6.1 billion people will be owning and using a smartphone (International Settlements 2016). With GPS already standard on mobile devices, data is already being collected, in real time and at an unprecedented spatial resolution, that tracks individuals as they travel and interact with their environment. People are also choosing to share more about their behavior, and foursquare is just one example of a platform that enables this. The results of the estimation process and sensitivity analysis in this thesis show how even a limited application of such data can dramatically improve destination choice models for leisure travel. The capability to model many aspects of destination attractiveness is particularly useful for leisure travel.

Traditional mobility surveys such as the TSRC still have an important role to play in transportation modeling. They track the same individuals over time, and provide the socioeconomic characteristics of the individual, which have been repeatedly shown to be important determinants of travel behavior (Pas 1984; Hanson 1982). However, they also have shortcomings; they normally rely on the recall ability of the participant, and are limited in both their spatial and temporal resolutions. The TSRC data exhibited this second shortcoming, which influenced the decisions around spatial resolution in the destination choice model. Most sources of big data collect information from the individual in real time (GPS, GPRS), or rely on location tracking services to verify the checkin (foursquare) to an accuracy of meters.

While a higher spatial resolution in the observed trip records would allow for a more detailed destination choice model, it would require a more detailed consideration of another issue, the choice set selection. With only 69 destinations, as used in thesis, it is not essential to restrict the choice set for an individual. However, should the number of alternatives be very large, the choice set presented to each individual needs to be reduced for each individual. Realistically, an individual is not capable of evaluating thousands of possible alternatives when selecting a destination. And any model that assumes this would be unrealistic. In particular, Ben-Akiva and Lerman (1985) found that the size and selection of the choice set impacts the model performance.

The venue data for each zone essentially acts as database of the points of interest (POI) at a particular destination. POI data is available from many sources, such as Open Street Maps. However, LBSNs such as foursquare take this POI database one step further, by measuring the popularity of each POI. In the case of foursquare, as discussed in section ??, when summed together, checkins measure the intensity of activity at each POI. A measure of importance was clearly beneficial in the model. Not all POIs are equal. Hotels are of different sizes, some national parks are more visited than others. Of course, the importance of each POI can be measured based on attributes such as the number of hotel beds or recorded visitors per year. However, the data collection required is prohibitive, particularly for a large scale model. LBSN data provides an fast way of estimating the importance of POIs, and in turn, destination utility.

### 6.3 Limitations and future work

One of the benefits of designing a model based on traditional socioeconomic variables is the ability to run the model for future years and model the impacts of demographic change. This is difficult for the foursquare checkin counts. Not only is it hard to predict the how the popularity of certain venues will grow or decline in future years, but the

quantity of checkins depends on uptake of the foursquare platform. Further study of the demographics of foursquare users and their distribution in relation to the population. Foursquare data also has thematic limitations in its applicability to destination choice modeling. In study on why people use foursquare, Lindqvist et al. (2011) found that “participants expressed reluctance to check-in at home, work, and other places that one might expect them to be at”. This suggests that there are limits to how effectively foursquare can model travel behavior. A potential alternative would be to use foursquare or a similar LBSN as a POI database, and use GPS traces to identify the intensity of activity at these locations, thereby avoiding the selective reporting behavior evident in foursquare usage.

The incorporation of foursquare data into a discrete choice model just touches the surface of what is possible with big data. Many dimensions to the data which were not explored in this thesis, particularly the temporal aspect. Through public services such as twitter, Panel data can be collected by associating checkins over time with an individual. (CITE) used such a method to identify mobility patterns. In future work utilizing more detailed foursquare data, checkins could be filtered for those performed by residents of Canada, or grouped by season to further improve the modeling of different trip purposes.

## Chapter 7

## Conclusions

## Appendix A

### Further data analysis

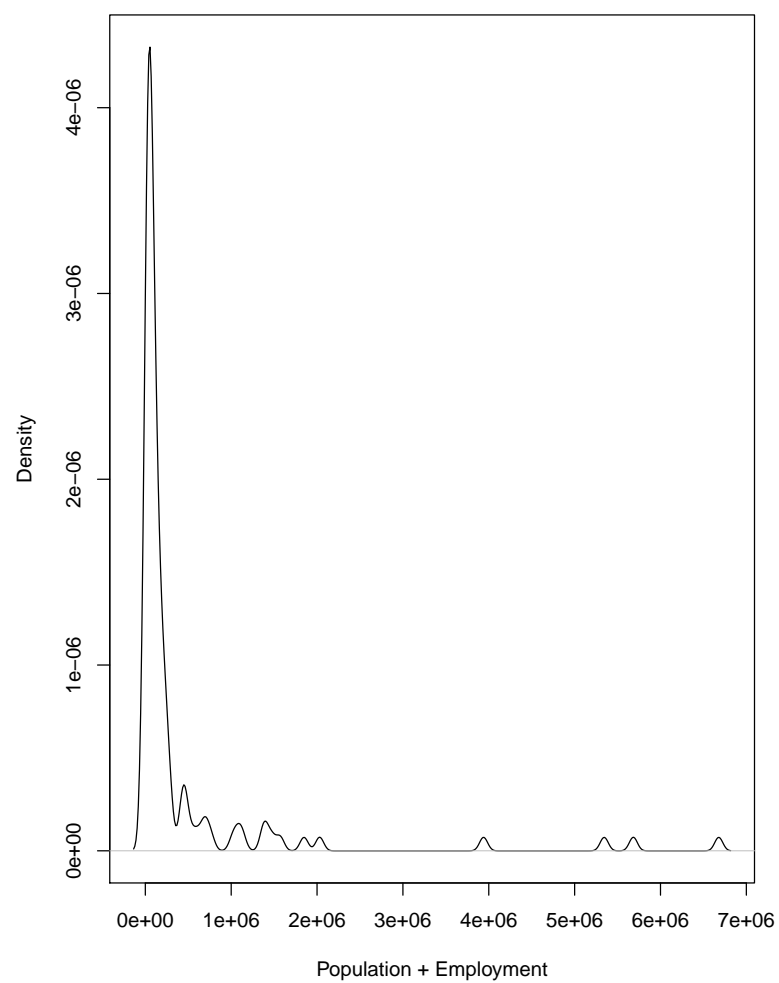


FIGURE A.1: Long tail and right skew of (population + employment) for each destination

	Population	Total Employment	Goods Industry	Service Industry	Professional	Employment & Health	Arts & Entertainment	Leisure & Hospitality
Population	<b>1</b>	<b>0.99</b>	<b>0.94</b>	<b>0.98</b>	<b>0.93</b>	<b>0.99</b>	<b>0.92</b>	<b>0.96</b>
Total Employment	<b>0.99</b>	<b>1</b>	<b>0.96</b>	<b>0.99</b>	<b>0.95</b>	<b>0.99</b>	<b>0.95</b>	<b>0.98</b>
Goods Industry	<b>0.94</b>	<b>0.96</b>	<b>1</b>	<b>0.92</b>	<b>0.84</b>	<b>0.94</b>	<b>0.91</b>	<b>0.94</b>
Service Industry	<b>0.98</b>	<b>0.99</b>	<b>0.92</b>	<b>1</b>	<b>0.98</b>	<b>0.98</b>	<b>0.94</b>	<b>0.97</b>
Professional	<b>0.93</b>	<b>0.95</b>	<b>0.84</b>	<b>0.98</b>	<b>1</b>	<b>0.94</b>	<b>0.91</b>	<b>0.93</b>
Employment & Health	<b>0.99</b>	<b>0.99</b>	<b>0.94</b>	<b>0.98</b>	<b>0.94</b>	<b>1</b>	<b>0.92</b>	<b>0.97</b>
Arts & Entertainment	<b>0.92</b>	<b>0.95</b>	<b>0.91</b>	<b>0.94</b>	<b>0.91</b>	<b>0.92</b>	<b>1</b>	<b>0.99</b>
Leisure & Hospitality	<b>0.96</b>	<b>0.98</b>	<b>0.94</b>	<b>0.97</b>	<b>0.93</b>	<b>0.97</b>	<b>0.99</b>	<b>1</b>

FIGURE A.2: High correlation between population, employment, and various employment categories across destinations

TABLE A.1:  $m2$  Results.  
Toronto: zones 20-22, Niagara: zone 30

	Origin	Destination	Type	Predicted	Observed	Absolute Error	Max Rel. Error
1	21	30	II	877.21	3695.07	2817.86	3.21
2	85	72	EE	123.67	2407.73	2284.06	18.47
3	21	20	II	4507.84	2251.48	2256.36	1.00
4	21	22	II	4844.63	2680.21	2164.42	0.81
5	36	21	II	1346.76	3085.23	1738.46	1.29
6	103	4	EI	541.86	2061.78	1519.92	2.80
7	103	21	EI	198.15	1529.83	1331.68	6.72
8	21	53	II	821.51	2115.53	1294.01	1.58
9	64	64	II	209.47	1423.02	1213.55	5.79
10	21	54	II	215.05	1346.02	1130.97	5.26
11	20	30	II	261.47	1365.27	1103.80	4.22
12	22	30	II	352.63	1420.03	1067.40	3.03
13	30	30	II	157.40	1178.94	1021.54	6.49
14	21	52	II	804.06	1818.06	1014.00	1.26
15	21	4	II	264.90	1238.33	973.43	3.67
16	29	21	II	1165.79	2124.10	958.31	0.82
17	29	30	II	428.45	1353.10	924.65	2.16
18	4	21	II	403.14	1318.43	915.28	2.27
19	47	21	II	631.84	1535.96	904.12	1.43
20	4	85	IE	1660.31	809.08	851.23	1.05

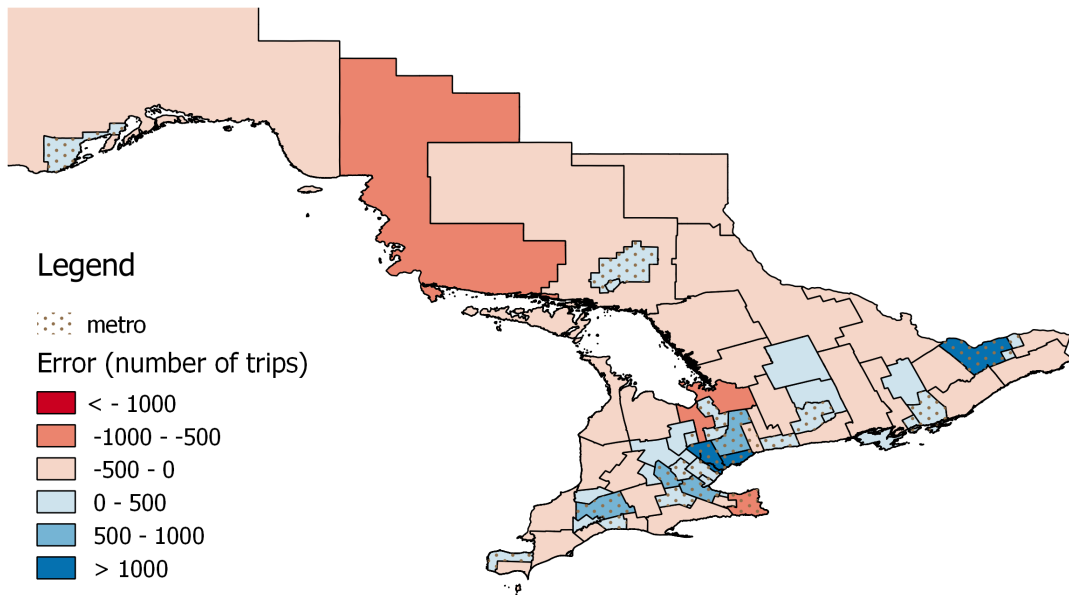


FIGURE A.3: Intrazonal errors produced by the  $m2$  model



## Appendix B

### Further model results

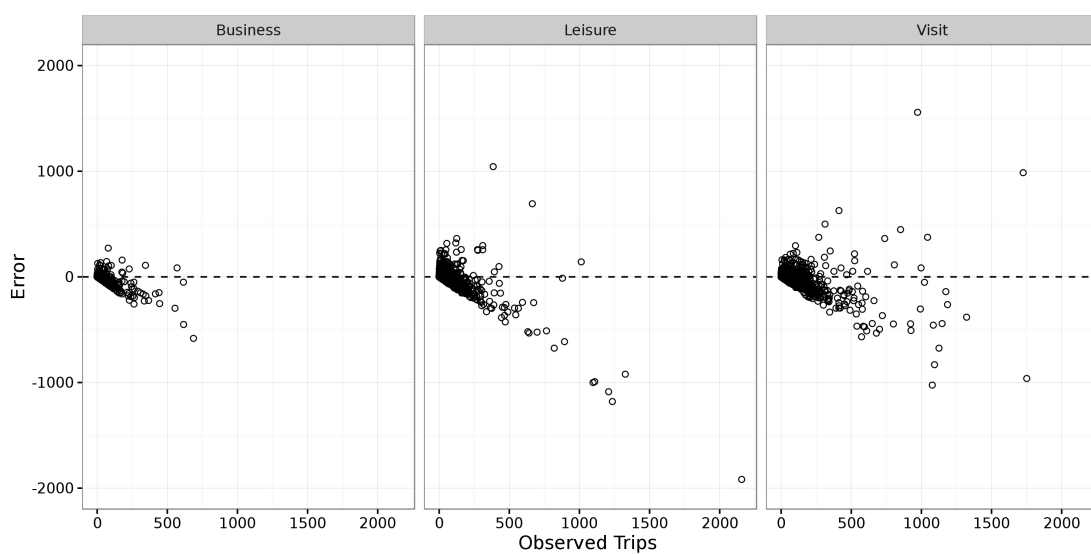


FIGURE B.1:  $m3$  model errors by observed trip count for OD pairs by trip purpose

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