NATIONAL UNIVERSITY OF SINGAPORE

CS1101S — PROGRAMMING METHODOLOGY

(AY2019/2020 SEMESTER 1)

MIDTERM ASSESSMENT (ADAPTED TO AY2021 IN 9/2020)

Time Allowed: 1 Hour 45 Minutes

INSTRUCTIONS

- 1. This assessment paper contains SIX (6) questions and comprises EIGHTEEN (18) printed pages, including this page.
- 2. The full score of this paper is **75 marks**.
- 3. This is a **CLOSED BOOK** assessment, but you are allowed to bring in one A4 sheet of notes (handwritten or printed on both sides).
- 4. Answer **ALL** questions **within the space provided** in this booklet.
- 5. Where programs are required, write them in the **Source §2** language.
- 6. Write legibly with a pen or pencil. Untidiness will be penalized.
- 7. Do not tear off any pages from this booklet.
- 8. Write your **Student Number** below **using a pen**. Do not write your name.
- 9. Also write down your **Studio Group Number** in the provided box, if you can remember it.

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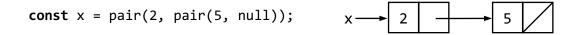
This portion is for examiner's use only

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Question 1: Box-and-Pointer Diagrams [10 marks]

Draw the box-and-pointer diagram for the value of x after the evaluation of each of the following programs. Clearly show where x is pointing to.

For example, the following program results in the following diagram on the right:



1A. [2 marks]

```
const x = pair(pair(null, pair(4, null)), 5);
```

1B. [2 marks]

```
const q = list(6);
const x = list(q, pair(6, null), q);
```

1C. [3 marks]

const ys = list(4, 5, 6);
const x = map(x => ys, ys);

1D. [3 marks]

Question 2: List Processing [19 marks]

2A. [4 marks]

THIS QUESTION IS OBSOLETE IN AY2020/21.

2B. [5 marks]

THIS QUESTION IS OBSOLETE IN AY2020/21.

2C. [5 marks]

Complete the last_comes_first function, which takes as argument a *non-empty list* xs, and returns a list that results from removing the last element from xs and adding it as the first element of the result list.

Examples:

```
last_comes_first(list(2));  // returns List(2)
last_comes_first(list(2,5,3,4,5)); // returns List(5,2,5,3,4)
```

```
function last_comes_first(xs) {
```

2D. [5 marks]

The fib_list function takes as argument an integer $N \ge 2$ and returns a list containing the first N Fibonacci numbers, arranged in *ascending order*.

Examples:

```
fib_list(2); // returns list(0, 1)
fib_list(7); // returns list(0, 1, 1, 2, 3, 5, 8)
```

Complete the following implementation of fib_list, which must give rise to an **iterative process** and its runtime should have an order of growth of $\Theta(N)$.

```
function fib_list(N) {
```

Question 3: Orders of Growth [8 marks]

3A. [3 marks]

Assume a resource function r(n). Indicate true or false for each of the following:

(i) [1 mark] r(n) has order of growth $\Theta(r(n))$.

Circle one: True / False

(ii) [1 mark] r(n) has order of growth O(r(n)).

Circle one: True / False

(iii) [1 mark] r(n) has order of growth $\Omega(r(n))$.

Circle one: True / False

3B. [2 marks]

Assume a resource function r(n) and another function g(n) such that r(n) has order of growth $\Theta(g(n))$. Indicate true or false for each of the following:

(i) [1 mark] r(n) has order of growth O(g(n)).

Circle one: True / False

(ii) [1 mark] r(n) has order of growth $\Omega(g(n))$.

Circle one: True / False

3C. [3 marks]

Assume a resource function r(n) with order of growth $\Theta(n \log n)$. An example would be the runtime for merge sort. Indicate true or false for each of the following:

(i) [1 mark] r(n) has order of growth $\Theta(n^2)$.

Circle one: True / False

(ii) [1 mark] r(n) has order of growth $\Omega(n^2)$.

Circle one: True / False

(iii) [1 mark] r(n) has order of growth $O(n^2)$.

Circle one: True / False

Question 4: Active Lists [13 marks]

An *active list* is a function that takes an integer number and returns an empty list or a list of length 1. It can be used as an alternative representation of a list, where it takes as argument an element's position in the active list, and returns that element in a list of length 1. Note that the first element in an active list is at position 0.

The function make_active_list takes a list as its argument and returns an active list that represents the input list.

Example:

```
const alist = make_active_list(list(8, 3, 5));
alist(-1); // returns null
alist(0); // returns list(8)
alist(1); // returns list(3)
alist(2); // returns list(5)
alist(3); // returns null
```

Note that when the argument passed to alist is negative, or is greater than or equal to the length of the input list to make_active_list, the function alist should return an empty list.

4A. [3 marks]

Write the function act_length that takes as argument an active list as, and returns the length of the active list.

Example:

```
const as = make_active_list(list());
const bs = make_active_list(list(8, 3, 5));
act_length(as); // returns 0
act_length(bs); // returns 3
```

```
function act_length(as) {
```

4B. [5 marks]

Write the function act_append that takes as arguments two active lists, as and bs, and returns an active list that results from appending bs to as.

Example:

```
const as = make_active_list(list(11, 22));
const bs = make_active_list(list(33, 44, 55));
const cs = act_append(as, bs);
act_length(cs); // returns 5
list(cs(0), cs(1), cs(2), cs(3), cs(4));
    // returns list(list(11), list(22), list(33), list(44), list(55))
```

Your implementation may make use of the act_length function from the preceding task.

```
function act_append(as, bs) {

}
```

4C. [5 marks]

Write the function sum that takes as arguments an active list as and a function f, and returns the sum of f(x) for every element x of the input active list. We assume that all elements of the input active list are numbers.

Example:

```
const as = make_active_list(list(1, 2, 3));
sum(as, x => x * x); // returns 14 (1*1 + 2*2 + 3*3)
```

Your implementation may use the act_length function, and must make use of at least one of the three functions: accumulate, map, filter, in a meaningful way, to produce the result.

```
function sum(as, f) {

}
```

Question 5: Binary Arithmetic Expressions [11 marks]

A *Binary Arithmetic Expression (BAE)* is either a *number* or the expression ($\langle bae \rangle \langle op \rangle \langle bae \rangle$), where each $\langle bae \rangle$ is a BAE and $\langle op \rangle$ is the binary operator + or *. The followings are examples of BAEs:

- 123
 (56+23)
 ((2+5)*100)
- BAEs are arithmetic expressions that we are all familiar with, except that in BAEs, a pair of parentheses is always used to surround every binary arithmetic operation. As a result, we do not

We represent BAEs in Source in the following way: a BAE is either a *number* or a list that has 3 elements where the first element is a BAE, the second element is a string "+" or "*", and the third element is a BAE. The first and third elements are the left and right operands of the binary arithmetic operation, respectively. For example, the BAE ((2 + 5) * 100) has the following representation in Source: list(list(2, "+", 5), "*", 100).

5A. [5 marks]

Write a function eval_BAE that takes as argument a BAE bae, and evaluates it to a single numeric value.

Example:

```
const bae1 = 123;
eval_BAE(bae1); // returns 123
const bae2 = list( list(2, "+", 5), "*", 100 );
eval_BAE(bae2); // returns 700
```

need to be concerned with operator precedence and associativity.

```
function eval_BAE(bae) {
```

5B. [6 marks]

Write a function negate_BAE that takes as argument a BAE bae, and returns a BAE whose value is the negation of bae. The result BAE must have the same number of "+" and "*" as the original.

Example:

```
function negate_BAE(bae) {
```

Question 6: Functions [14 marks]

6A. [6 marks]

Consider the following two functions:

```
const twice = f => (x => f(f(x)));
const thrice = f => (x => f(f(f(x))));
```

What is the result of each of the following statements?

```
(i) [2 \text{ marks}] (twice(x => 2 * x))(1);
```

```
(ii) [2 marks] (thrice(twice(x => 2 * x)))(1);
```

```
(iii) [2 marks] ((thrice(twice))(x => 2 * x))(1);
```

6B. [4 marks]

What is the result of evaluating the following program?

```
function mystery(f, x) {
    return x === 0
        ? f(x)
        : mystery(x => f(x + 1), x - 1);
}
mystery(x => 7 * x, 8);
```

6C. [4 marks]				
THIS QUESTION IS OBSOLETE IN AY2020/21.				
—— END OF QUESTIONS ——				

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Appendix

The following **list processing** functions are supported in Source §2:

- pair(x, y): Makes a pair from x and y.
- is pair(x): Returns true if x is a pair and false otherwise.
- head(x): Returns the head (first component) of the pair x.
- tail(x): Returns the tail (second component) of the pair x.
- is_null(xs): Returns true if xs is the empty list, and false otherwise.
- is_list(x): Returns true if x is a list as defined in the lectures, and false otherwise. Iterative process; time: O(n), space: O(1), where n is the length of the chain of tail operations that can be applied to x.
- list(x1, x2,..., xn): Returns a list with n elements. The first element is x1, the second x2, etc. Iterative process; time: O(n), space: O(n), since the constructed list data structure consists of n pairs, each of which takes up a constant amount of space.
- equal(x, y): Returns true if x and y have the same structure with respect to pair, and the same numbers, boolean values, functions or empty list at corresponding leave positions (places that are not themselves pairs), and false otherwise; time, space: O(n), where n is the number of pairs in x.
- length(xs): Returns the length of the list xs. Iterative process; time: O(n), space: O(1), where n is the length of xs.
- map(f, xs): Returns a list that results from list xs by element-wise application of f. Recursive process; time: O(n), space: O(n), where n is the length of xs.
- build_list(n, f): Makes a list with n elements by applying the unary function f to the numbers 0 to n 1. Recursive process; time: O(n), space: O(n).
- for_each(f, xs): Applies f to every element of the list xs, and then returns true. Iterative process; time: O(n), space: O(1), where n is the length of xs.
- list_to_string(xs): Returns a string that represents list xs using the text-based box-and-pointer notation [...].
- reverse(xs): Returns list xs in reverse order. Iterative process; time: O(n), space: O(n), where n is the length of xs. The process is iterative, but consumes space O(n) because of the result list.
- append(xs, ys): Returns a list that results from appending the list ys to the list xs. Recursive process; time: O(n), space: O(n), where n is the length of xs.
- member(x, xs): Returns first postfix sublist whose head is identical to x (===); returns null if the element does not occur in the list. Iterative process; time: O(n), space: O(1), where n is the length of xs.
- remove(x, xs): Returns a list that results from xs by removing the first item from xs that is identical (===) to x. Recursive process; time: O(n), space: O(n), where n is the length of xs.
- remove_all(x, xs): Returns a list that results from xs by removing all items from xs that are identical (===) to x. Recursive process; time: O(n), space: O(n), where n is the length of xs.
- filter(pred, xs): Returns a list that contains only those elements for which the one argument function pred returns true. Recursive process; time: O(n), space: O(n), where n is the length of xs.
- enum_list(start, end): Returns a list that enumerates numbers starting from start using a step size of 1, until the number exceeds (>) end. Recursive process; time: O(n), space: O(n), where n is the length of xs. For example, enum_list(2, 5) returns the list list(2, 3, 4, 5).
- list_ref(xs, n): Returns the element of list xs at position n, where the first element has index 0. Iterative process; time: O(n), space: O(1), where n is the length of xs.

• accumulate(op, initial, xs): Applies binary function op to the elements of xs from right-to-left order, first applying op to the last element and the value initial, resulting in r_1 , then to the second-last element and r_1 , resulting in r_2 , etc, and finally to the first element and r_{n-1} , where n is the length of the list. Thus, accumulate(op, zero, list(1,2,3)) results in op(1, op(2, op(3, zero))). Recursive process; time: O(n), space: O(n), where n is the length of xs, assuming op takes constant time.

Some other functions supported in Source §2:

- is_boolean(x): Returns true if x is a boolean value, and false otherwise.
- is_number(x): Returns true if x is a number, and false otherwise.
- is_string(x): Returns true if x is a string, and false otherwise.

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