NATIONAL UNIVERSITY OF SINGAPORE

SCHOOL OF COMPUTING

MIDTERM QUIZ

ADAPTED TO SOURCE 2021 IN 9/2020

Semester 1 AY2015/2016

CS1101S — PROGRAMMING METHODOLOGY

30 September 2015 Time Allowed: 1 Hour 35 Minutes

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Matriculation No.:					

Instructions (please read carefully):

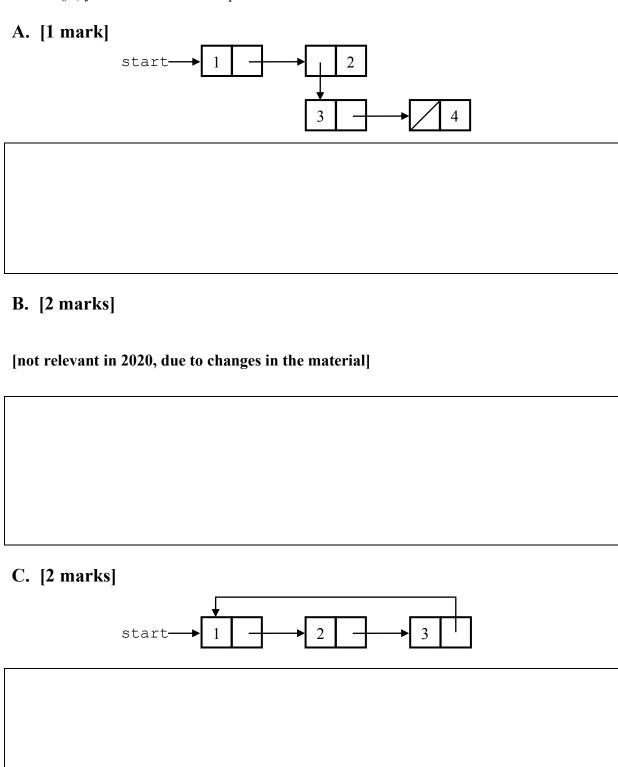
- 1. Write down your **matriculation number** on the **question paper**. DO NOT WRITE YOUR NAME ON THE QUESTION SET!
- 2. Write down your Avenger's name in the box provided above.
- 3. This is an **open-sheet quiz**. You are allowed to bring one A4 sheet of notes (written or printed on both sides).
- 4. This paper comprises **5 questions** and **EIGHTEEN (18)** printed pages.
- 5. The maximum score of this quiz is **60 marks**. The weight of each question is given in square brackets beside the question number.
- 6. All questions must be answered correctly for the maximum score to be attained.
- 7. All questions must be answered in the space provided in the question paper; no extra sheets will be accepted as answers.
- 8. The pages marked "scratch paper" in the question paper may be used as scratch paper.
- 9. You are allowed to use pencils or pens, as you like (no red color, please).
- 10. Write legibly; **UNTIDINESS will be penalized**.

GOOD LUCK!

Q #	1	2	3	4	5	Σ
MAX	5	15	13	12	15	60
SC						

Question 1: Boxes and Pointers [5 marks]

Write a Source §2 program that produces exactly the pairs shown in each of the following box-and-pointer diagrams. At the end of the execution of your program, the name start must refer to the pair as shown in the diagram. If the structure cannot be constructed using Source §2, you must answer "not possible."



Question 2: Lists and Trees [15 marks]

A. [3 marks] Sharing Pairs

[not relevant in 2020, due to changes in the material]

B. [4 marks] Lists of Numbers

A list of numbers is null or a pair whose head is a number and whose tail is a list of numbers. For example,

```
const list of num = list(1, 4, 5, 3);
```

Write a function is_list_of_numbers such that is_list_of_numbers (x) returns true if x is a list of numbers and false in all other cases. Your function is not supposed to give rise to an error, regardless of the argument value.

You get the maximum 4 marks only if you *do not* use any of the functions filter, map and accumulate in your correct solution, otherwise you get at most 2 marks.

```
function is_list_of_numbers(x) {
```

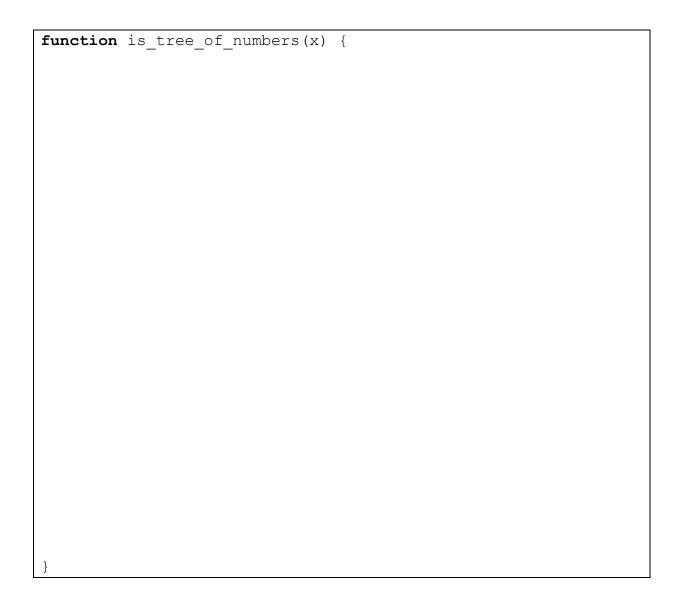
C. [5 marks] Trees of Numbers

A tree of numbers is a list whose elements are numbers or trees of numbers. For example,

```
const tree of num = list(list(1, list(2,3)), 4, 5, list(6, 7));
```

Write a function is_tree_of_numbers such that is_tree_of_numbers (x) returns true if x is a tree of numbers and false in all other cases. Your function is not supposed to give rise to an error, regardless of the argument value.

You get 5 marks if you use at least one of the functions filter, map and accumulate in a correct and meaningful way, and 3 marks for any other correct solution.



D. [3 marks] my_filter

Write a Source $\S 2$ function my_filter that behaves like the built-in function filter, but you must implement it using the accumulate function.

```
function my_filter(pred, xs) {

// Property of the content of
```

Question 3: Processing Digital Images [13 marks]

A grayscale 2D digital image is a rectangular table of pixel brightness values. Here, we represent a digital image as a list of lists of numbers. For example, the digital image

1	2	3	4
5	6	7	8
9	10	11	12

is represented as

```
list(list(1, 2, 3, 4), list(5, 6, 7, 8), list(9, 10, 11, 12));
```

The top-most row of the image is row 0, and the row number increases from top to bottom. The left-most column of the image is column 0, and the column number increases from left to right.

A. [6 marks] make_image

Write a function make_image that takes two *positive* integers rows and columns as the first and second arguments, respectively, and a function func as the third argument, such that make_image returns an image with rows rows and columns columns, and each pixel at row r and column c has the value func (r, c).

```
function make_image(rows, columns, func) {
```

B. [2 marks] flip_image_vertically

Write a function flip_image_vertically that takes an image as the only argument, and returns an image that is the vertical flip of the input image. For example, the vertical flip of the digital image

Ī	1	2	3	4
ſ	5	6	7	8
ſ	9	10	11	12

is the digital image

9	10	11	12
5	6	7	8
1	2	3	4

```
function flip_image_vertically(image) {

// Property of the state of the state
```

C. [2 marks] flip_image_horizontally

Write a function flip_image_horizontally that takes an image as the only argument, and returns an image that is the horizontal flip of the input image. For example, the horizontal flip of the digital image

1	2	3	4
5	6	7	8
9	10	11	12

is the digital image

4	3	2	1
8	7	6	5
12	11	10	9

```
function flip_image_horizontally(image) {

// Property of the property of
```

D. [3 marks] rotate_image_180

Write a function rotate_image_180 that takes an image as the only argument, and returns an image that is equal to the input image rotated 180 degrees.

```
function rotate_image_180(image) {
```

Question 4: Exhausting Time and Space [12 marks]

According to the substitution model of execution, a process can be said to *exhaust all time resources* if it keeps evaluating sub-expressions and never reaches any result value.

A process can be said to exhaust all space resources if it keeps growing while it evaluates sub-expressions, i.e. for any natural number n, it will reach the size n (in the number of sub-expressions) during evaluation.

Example:

```
function loop(x) {return loop(x);}
loop(0);
```

This program exhausts all time resources, but not all space resources.

Example:

```
function loop2(x) {return loop2(loop2(x));}
loop2(0);
```

This program exhausts all time resources and all space resources.

Consider the following programs and indicate whether they exhaust all time resources and whether they exhaust all space resources. You are awarded 1 mark for each correct answer, 0 mark for no answer, and -½ mark for an incorrect answer. The minimum total marks for the entire Question 4 will be kept at 0.

A. [2 marks]

```
(x \Rightarrow x)(x \Rightarrow x);
```

Exhausts all time resources? (Yes/No):

Exhausts all space resources? (Yes/No):

B. [2 marks]

```
(x \Rightarrow x(x))(x \Rightarrow x);
```

Exhausts all time resources? (Yes/No):

Exhausts all space resources? (Yes/No):

C. [2 marks]

$$(x => x(x))(x => x(x));$$

Exhausts all time resources? (Yes/No):

Exhausts all space resources? (Yes/No):

D. [2 marks]

$$(x => x(x)(x))(x => x(x));$$

Exhausts all time resources? (Yes/No):

Exhausts all space resources? (Yes/No):

E. [2 marks]

$$(x => x(x(x)))(x => x(x));$$

Exhausts all time resources? (Yes/No):

Exhausts all space resources? (Yes/No):

F. [2 marks]

$$(x => x(x))(x => x(x(x)));$$

Exhausts all time resources? (Yes/No):

Exhausts all space resources? (Yes/No):

Question 5: Combinations and Permutations [15 marks]

A. [8 marks] Checking Permutations

[6 marks] Write a function are_permutation that takes two lists of numbers xs1 and xs2 as the first and second arguments, respectively, and returns true if xs1 and xs2 are permutations of each other. Note that xs1 and xs2 are allowed to have duplicate numbers.

For example,

- are_permutation(list(1, 2, 2, 5, 4), list(4, 2, 5, 1, 2)) returns true;
- are_permutation(list(1, 2, 2, 5, 4), list(1, 5, 5, 2, 4)) returns false.

<pre>function are_permutation(xs1,</pre>	xs2) {
}	

[2 marks] Let the length of xs1 and xs2 be m and n, respectively. What would be the order of growth of runtime of are_permutation, in Θ notation, with respect to m and n? (No need for explanation.)

B. [7 marks] k-Combinations

A *k-combination* of a set *S* is a subset of *k* elements of *S*.

Write a function combinations that takes a list of n distinct numbers xs as the first argument and an integer k as the second argument, and returns a list containing all the k-combinations of the numbers in xs. Each k-combination is represented as a list of k numbers. We can assume $0 \le k \le n$.

```
For example, combinations (list (1, 2, 3, 4), 2) returns list (list (1, 2), list (1, 3), list (1, 4), list (2, 3), list (2, 4), list (3, 4)).
```

Note that the numbers within each k-combination can be in any order, and the k-combinations within the returned list can be in any order too.

function	combinations(xs,	K)	{	
}				

— END OF QUESTIONS —

Appendix

List Support

Source §2 supports the following list processing functions:

- pair (x, y): Makes a pair from x and y.
- is pair (x): Returns true if x is a pair and false otherwise.
- head (x): Returns the head (first component) of the pair x.
- tail (x): Returns the tail (second component) of the pair x.
- is null(xs): Returns true if xs is the empty list, and false otherwise.
- is_list(x): Returns true if x is a list as defined in the lectures, and false otherwise. Iterative process; time: O(n), space: O(1), where n is the length of the chain of tail operations that can be applied to x.
- list (x1, x2,..., xn): Returns a list with n elements. The first element is x1, the second x2, etc.
- length (xs): Returns the length of the list xs. Iterative process; time: O(n), space: O(1), where n is the length of xs.
- map (f, xs): Returns a list that results from list xs by element-wise application of f. Recursive process; time: O(n), space: O(n), where n is the length of xs.
- build_list(n, f): Makes a list with n elements by applying the unary function f to the numbers 0 to n 1. Recursive process; time: O(n), space: O(n).
- for_each(f, xs): Applies f to every element of the list xs, and then returns true. Iterative process; time: O(n), space: O(1), where n is the length of xs.
- list_to_string(xs): Returns a string that represents list xs using the box-and-pointer notation [...].
- reverse (xs): Returns list xs in reverse order. Iterative process; time: O(n), space: O(n), where n is the length of xs. The process is iterative, but consumes space O(n) because of the result list.
- append (xs, ys): Returns a list that results from appending the list ys to the list xs. Recursive process; time: O(n), space: O(n), where n is the length of xs.
- member (x, xs): Returns first postfix sublist whose head is identical to x (===); returns null if the element does not occur in the list. Iterative process; time: O(n), space: O(1), where n is the length of xs.

- remove (x, xs): Returns a list that results from xs by removing the first item from xs that is identical (===) to x. Recursive process; time: O(n), space: O(n), where n is the length of xs.
- remove_all(x, xs): Returns a list that results from xs by removing all items from xs that are identical (===) to x. Recursive process; time: O(n), space: O(n), where n is the length of xs.
- filter (pred, xs): Returns a list that contains only those elements for which the one argument function pred returns true. Recursive process; time: O(n), space: O(n), where n is the length of xs.
- enum_list(start, end): Returns a list that enumerates numbers starting from start using a step size of 1, until the number exceeds (>) end. Recursive process; time: O(n), space: O(n), where n is the length of xs. For example, enum_list(2, 5) returns the list list(2, 3, 4, 5).
- list_ref(xs, n): Returns the element of list xs at position n, where the first element has index 0. Iterative process; time: O(n), space: O(1), where n is the length of xs.
- accumulate (op, initial, xs): Applies binary function op to the elements of xs from right-to-left order, first applying op to the last element and the value initial, resulting in r_1 , then to the second-last element and r_1 , resulting in r_2 , etc., and finally to the first element and r_{n-1} , where n is the length of the list. Thus, accumulate (op, zero, list(1,2,3)) results in op(1, op(2, op(3, zero))). Recursive process; time: O(n), space: O(n), where n is the length of xs, assuming op takes constant time.

Miscellaneous Functions

• is number (x): Returns true if x is a number, and false otherwise.