Page 2 states:

We can relate the body and inertial frame by a rotation matrix *R* which goes from the body frame to the inertial frame. This matrix is derived by using the ZYZ Euler angle conventions and successively "undoing" the yaw, pitch, and roll.

$$R = \begin{bmatrix} c_{\phi}c_{\psi} - c_{\theta}s_{\phi}s_{\psi} & -c_{\psi}s_{\phi} - c_{\phi}c_{\theta}s_{\psi} & s_{\theta}s_{\psi} \\ c_{\theta}c_{\psi}s_{\phi} + c_{\phi}s_{\psi} & c_{\phi}c_{\theta}c_{\psi} - s_{\phi}s_{\psi} & -c_{\psi}s_{\theta} \\ s_{\phi}s_{\theta} & c_{\phi}s_{\theta} & c_{\theta} \end{bmatrix}$$

For a given vector \vec{v} in the body frame, the corresponding vector is given by $R\vec{v}$ in the inertial frame.

Unfortunately there is a mistake here. The rotation matrix as a function of roll, pitch, yaw angles is actually derived from rotating around 3 different axes e. g. XYZ (not rotating around 2 axes ZYZ). The final formula, if we make the following association:

```
Roll -\varphi — X-axis
Pitch — \theta — Y-axis
Yaw — \psi — Z-axis
```

is given by

$$R = \begin{bmatrix} \cos\psi\cos\theta & \cos\psi\sin\varphi\sin\theta - \cos\varphi\sin\psi & \sin\varphi\sin\psi + \cos\varphi\cos\psi\sin\theta \\ \cos\theta\sin\psi & \cos\varphi\cos\psi + \sin\varphi\sin\psi\sin\theta & \cos\varphi\sin\psi\sin\theta - \cos\theta\sin\varphi \\ -\sin\theta & \cos\theta\sin\varphi & \cos\varphi\cos\theta \end{bmatrix}$$

This formula can be derived from elementary rotations around X,Y,Z axes. The derivations can be easily obtained with Matlab's symbolic toolbox:

Also, see https://en.wikipedia.org/wiki/Rotation_matrix