



## Week 4

# Machine Learning and Big Data - DATA622

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CUNY School of Professional Studies

# Textbooks

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- We are introducing 2 new textbooks to supplement our primary textbook (PMLiR)
- The Elements of Statistical Learning
  - In the notes, "ESL" refers to the book "The Elements of Statistical Learning"
  - You should have from the prerequisite courses.
  - You can buy it [here](#)
  - [Book](#) is available for free as a PDF [here](#) (author's site [here](#))
- An Introduction to Statistical Learning
  - In the notes, "ISLR" refers to the book "An Introduction to Statistical Learning"
  - You should have from the prerequisite courses.
  - You can buy it [here](#)
  - Book is available for free as a PDF [here](#) (author's site [here](#))

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# Naïve Bayes

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**Classification using Bayes Theorem.**

# Bayes Theorem

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## LIKELIHOOD

The probability of "B" being True, given "A" is True

## PRIOR

The probability "A" being True. This is the knowledge.

$$P(A|B) = \frac{P(B|A).P(A)}{P(B)}$$

## POSTERIOR

The probability of "A" being True, given "B" is True

## MARGINALIZATION

The probability "B" being True.

# Naïve Bayes: Example

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Predicting whether you should play golf

Outlook	Temp	Humidity	Windy	Play Golf
Rainy	Hot	High	False	No
Rainy	Hot	High	True	No
Overcast	Hot	High	False	Yes
Sunny	Mild	High	False	Yes
Sunny	Cool	Normal	False	Yes
Sunny	Cool	Normal	True	No
Overcast	Cool	Normal	True	Yes
Rainy	Mild	High	False	No
Rainy	Cool	Normal	False	Yes
Sunny	Mild	Normal	False	Yes
Rainy	Mild	Normal	True	Yes
Overcast	Mild	High	True	Yes
Overcast	Hot	Normal	False	Yes
Sunny	Mild	High	True	No

# Naïve Bayes: Example

Let's look at the data:

Frequency Table		Play Golf	
		Yes	No
Outlook	Sunny	3	2
	Overcast	4	0
	Rainy	2	3

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Likelihood Table		Play Golf		
		Yes	No	
Outlook	Sunny	3/9	2/5	5/14
	Overcast	4/9	0/5	4/14
	Rainy	2/9	3/5	5/14
		9/14	5/14	

$$P(x | c) = P(\text{Sunny} | \text{Yes}) = 3 / 9 = 0.33$$

$$P(c) = P(\text{Yes}) = 9 / 14 = 0.64$$

$$P(x) = P(\text{Sunny}) = 5 / 14 = 0.36$$

Posterior Probability:

$$P(c | x) = P(\text{Yes} | \text{Sunny}) = 0.33 \times 0.64 \div 0.36 = 0.60$$

# Naïve Bayes: Example

Frequency Table

		Play Golf	
		Yes	No
Outlook	Sunny	3	2
	Overcast	4	0
	Rainy	2	3



Likelihood Table

		Play Golf	
		Yes	No
Outlook	Sunny	3/9	2/5
	Overcast	4/9	0/5
	Rainy	2/9	3/5

		Play Golf	
		Yes	No
Humidity	High	3	4
	Normal	6	1



		Play Golf	
		Yes	No
Humidity	High	3/9	4/5
	Normal	6/9	1/5

		Play Golf	
		Yes	No
Temp.	Hot	2	2
	Mild	4	2
	Cool	3	1



		Play Golf	
		Yes	No
Temp.	Hot	2/9	2/5
	Mild	4/9	2/5
	Cool	3/9	1/5

		Play Golf	
		Yes	No
Windy	False	6	2
	True	3	3



		Play Golf	
		Yes	No
Windy	False	6/9	2/5
	True	3/9	3/5

Source: Saed Sayad

# Naïve Bayes: Example

Will I play golf in the following example?

Outlook	Temp	Humidity	Windy	Play
Rainy	Cool	High	True	?

$$P(Yes | X) = P(Rainy | Yes) \times P(Cool | Yes) \times P(High | Yes) \times P(True | Yes) \times P(Yes)$$

$$P(Yes | X) = 2/9 \times 3/9 \times 3/9 \times 3/9 \times 9/14 = 0.00529 \rightarrow 0.2 = \frac{0.00529}{0.02057 + 0.00529}$$

$$P(No | X) = P(Rainy | No) \times P(Cool | No) \times P(High | No) \times P(True | No) \times P(No)$$

$$P(No | X) = 3/5 \times 1/5 \times 4/5 \times 3/5 \times 5/14 = 0.02057 \rightarrow 0.8 = \frac{0.02057}{0.02057 + 0.00529}$$



# Naïve Bayes: Strengths and Weaknesses

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- Strengths:
  - Simplicity and computational efficiency.
  - It does a great job handling categorical features directly, without any preprocessing.
  - Outperforms more sophisticated classifiers when working with a large number of predictors
  - It handles noisy and missing data pretty well.
- Weaknesses:
  - Needs a sizable amount of data
  - It is naïve: assumption of independence between inputs & classes
  - Doesn't work well for datasets with a large number of continuous features
  - It assumes that all features within a class are not only independent but are equally important

# Naïve Bayes: Use-cases

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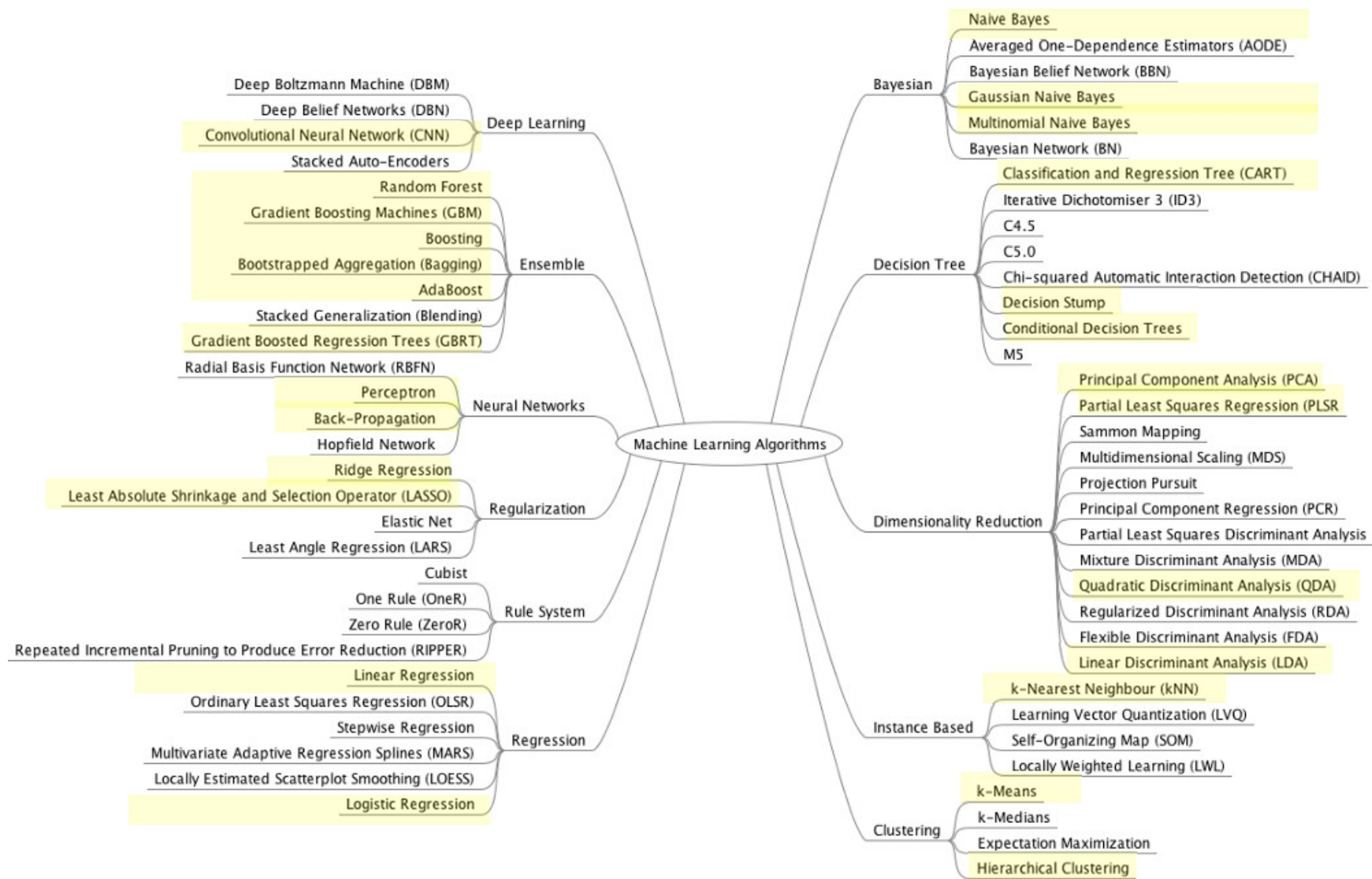
- Spam detection
- Sentiment analysis (news articles)
- Document classification
- Many classification problems...

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# Landscape of algorithms

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**We will cover many of the algorithms listed**



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# No free lunch Theorem

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**Bias-free learning is futile**

# TANSTAAFL

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- There ain't no such thing as a free lunch
- No-Free-Lunch Theorem states:
  - No single classifier works the best for all possible problems
  - We need to make assumptions to generalize (we need bias)



Source: <https://medium.com/@LeonFedden/the-no-free-lunch-theorem-62ae2c3ed10c>

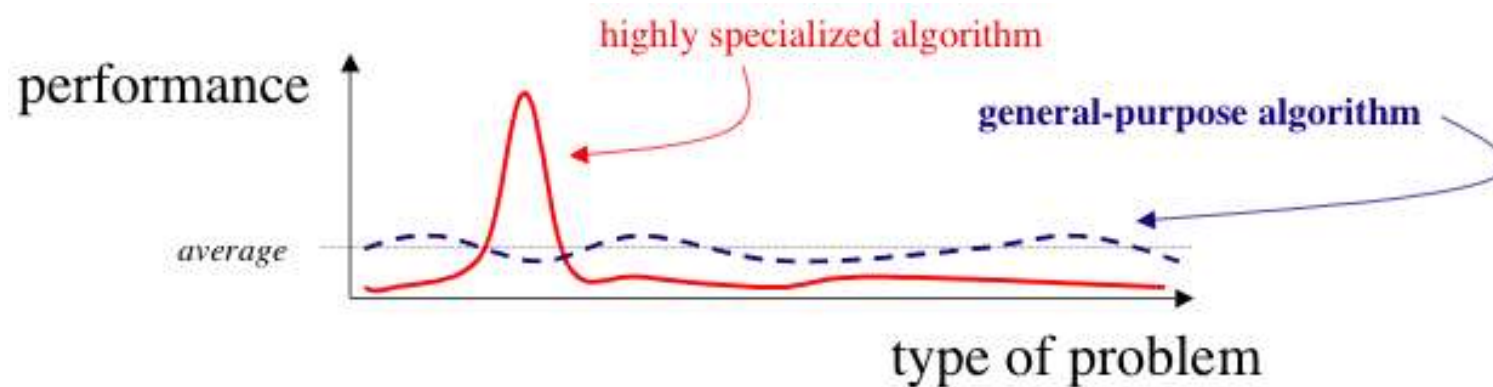
# TANSTAAFL

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Theorem:

*The average performance of any pair of algorithms across all possible problems is identical.*

If an algorithm achieves superior results on some problems, then it must pay with inferiority on the other problems



Source: <https://medium.com/@LeonFedden/the-no-free-lunch-theorem-62ae2c3ed10c>