

Type-Level Programming 101

The Subspace of Scala

Joe Barnes

Follow along at <http://172.30.7.195:8080>

Powered by



Joe Barnes

@joescii

prose :: and :: conz

Primarily Java from 2004-2013

Started Scala late 2012

Started Scala at Mentor Graphics late 2013

Lift committer in July 2014

So... Type programming...

What do *you* know about *that*, Joe??

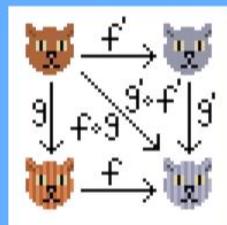
Not much...

So... Type programming...
What do you know about *the*

I've made zero contributions to shapeless

Not much...

Also no contributions to Cats



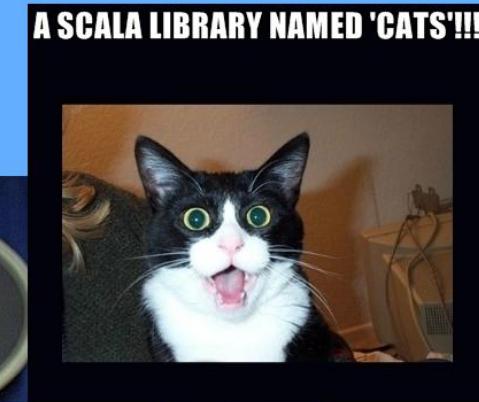
Type-Level Programming 101

The Subspace of Scala

Joe Barnes

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Although I have contributed plenty of cat memes!

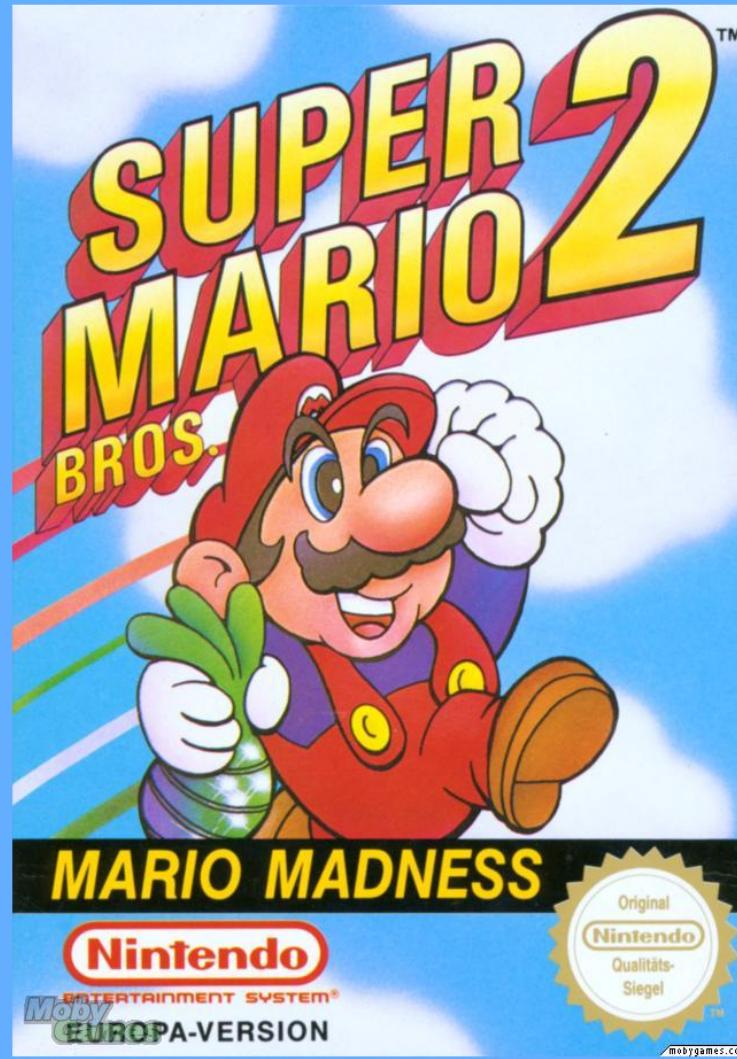


laimarily Java from 2004-2015
arted Scala late 2012
rted Scala at Mentor Graphics late 2
it committer in July 2014

sealed
case of
case of

I'm not here to share expertise on the subject,
but rather my *Aha!* moment.

Programming in Scala is like...





Normal value programming



A flask of type programming!

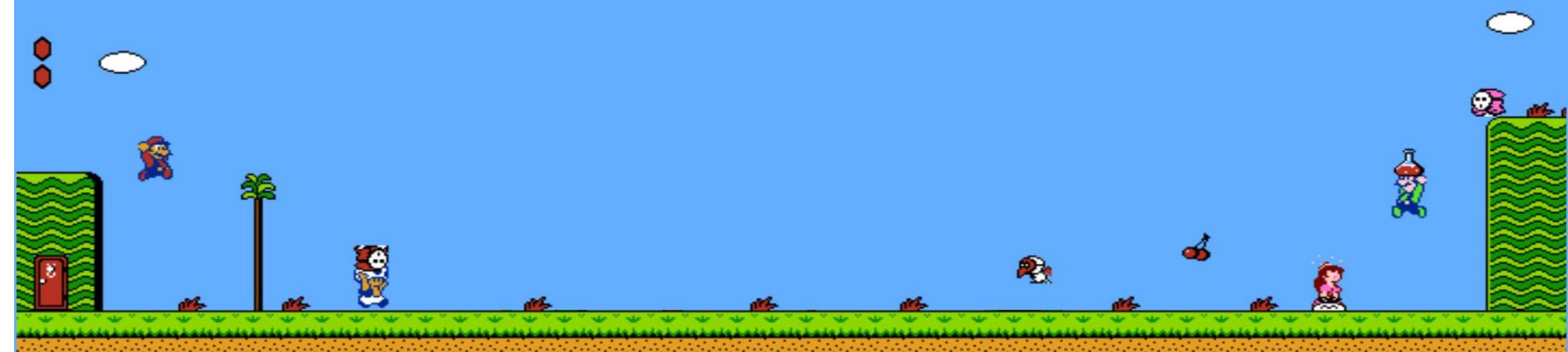


Where does this go?



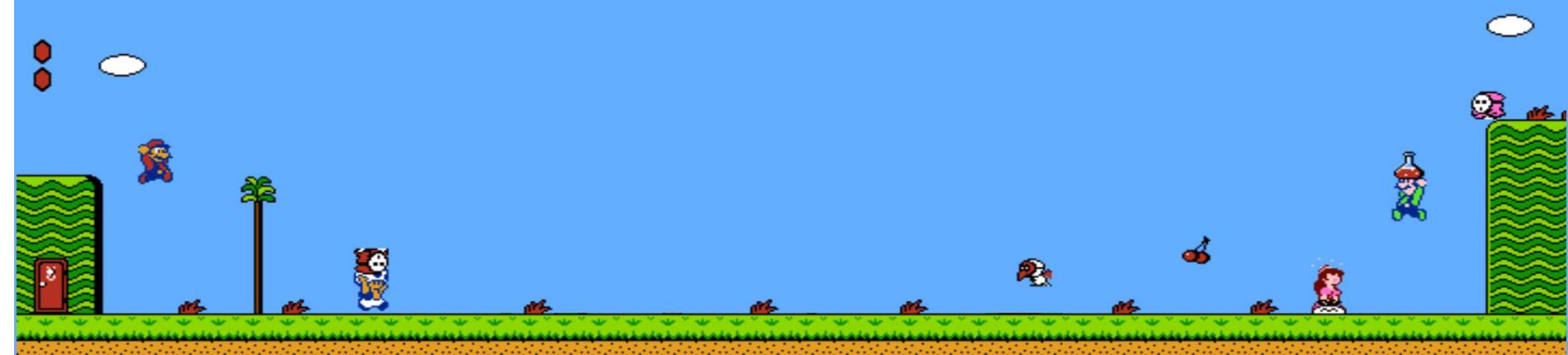
SUBSPACE!

```
val num = 1 + 2 + 3
```



```
val num = 1 + 2 + 3
```

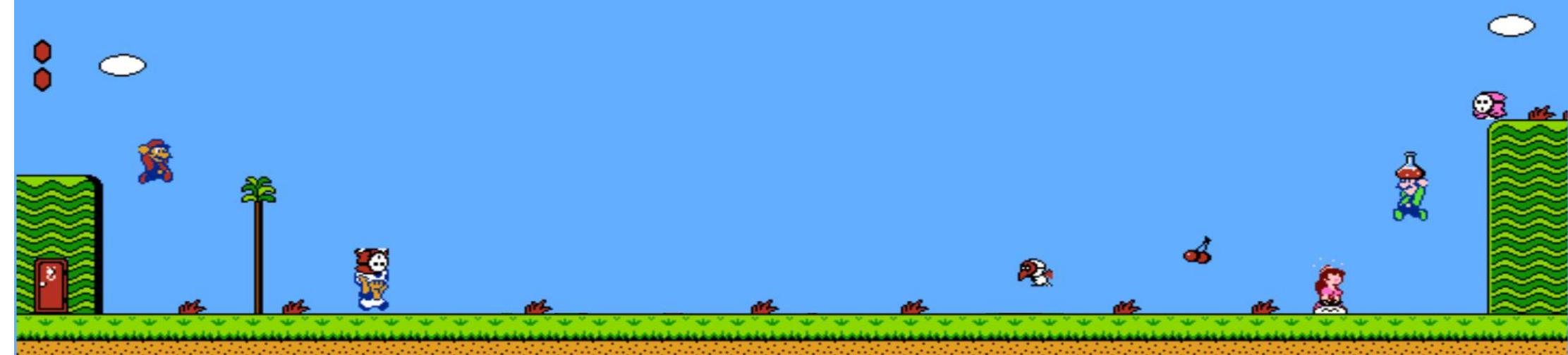
```
lazy val str = "a"+"b"+"c"
```



```
val num = 1 + 2 + 3
```

```
lazy val str = "a"+"b"+"c"
```

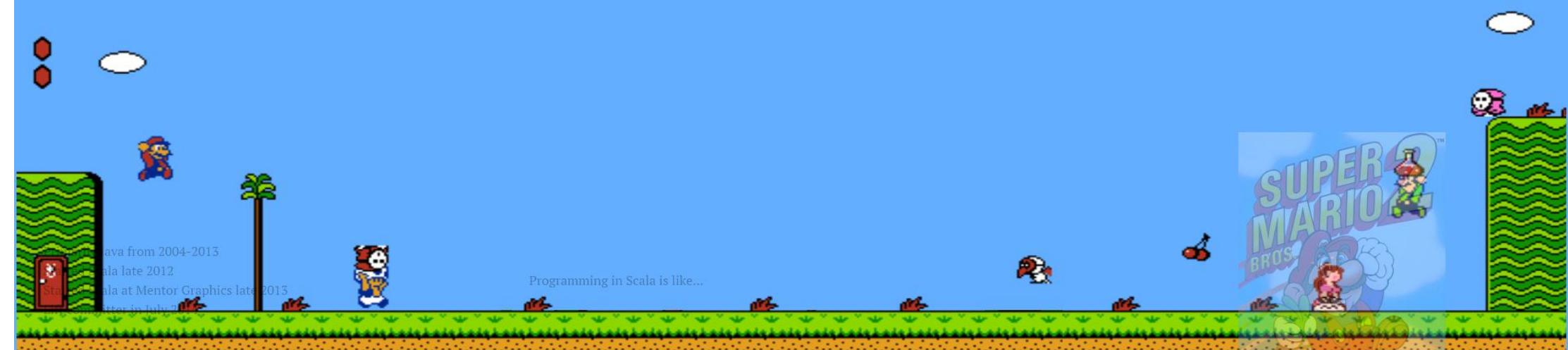
```
def now = new java.util.Date
```



```
type MyMap = Map[Int, String]
```



Let's compare values to types with the simplest domain ever

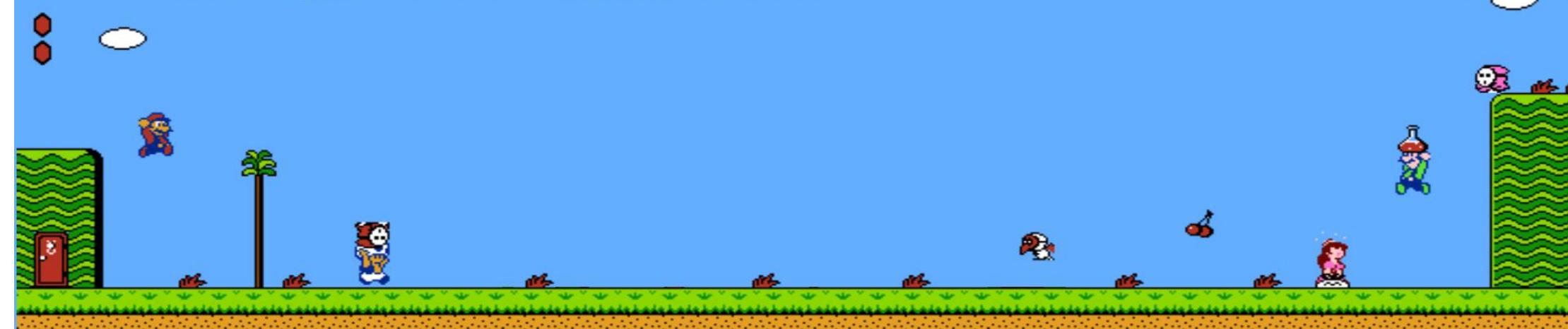


java from 2004-2013
scala late 2012
scala at Mentor Graphics late 2013
after in July 2014

Programming in Scala is like...

```
sealed trait BoolVal  
case object TrueVal extends BoolVal  
case object FalseVal extends BoolVal
```

```
sealed trait BoolTy  
sealed trait TrueTy  
sealed trait FalseTy
```





```
sealed trait BoolVal {  
    def not:BoolVal  
    def or(that:BoolVal):BoolVal  
}
```

```
sealed trait BoolType {  
    type Not <: BoolType  
    type Or[That <: BoolType] <:
```



```
case object TrueVal extends BoolVal {  
    override val not = FalseVal  
    override def or(that:BoolVal) = TrueVal  
}  
}
```

```
sealed trait TrueType extends BoolType {  
    override type Not = FalseType  
    override type Or[That <: BoolType] = TrueType  
}  
}
```

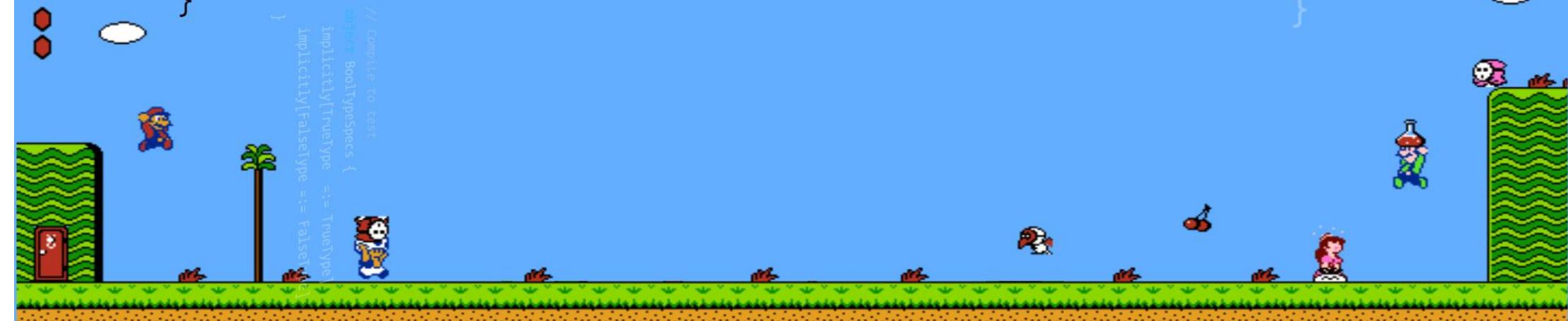
```
case object FalseVal extends BoolVal {  
    override val not = TrueVal  
    override def or(that:BoolVal) = that
```

```
}
```

```
// Compile to test  
object BoolTypeSpecs {  
    implicitly[TrueType] =:= TrueType  
    implicitly[FalseType] =:= FalseType
```

```
sealed trait F  
    override type T  
    override type U
```

```
}
```



```
sealed trait BoolType
sealed trait TrueType extends BoolType
sealed trait FalseType extends BoolType
```



oe Barnes
@joesci
prose :: and :: conz

Primarily Java from 2004-2013
Started Scala late 2012
Started Scala at Mentor Graphics late 2013
Lift committer in July 2014

Programming in Scala is like...

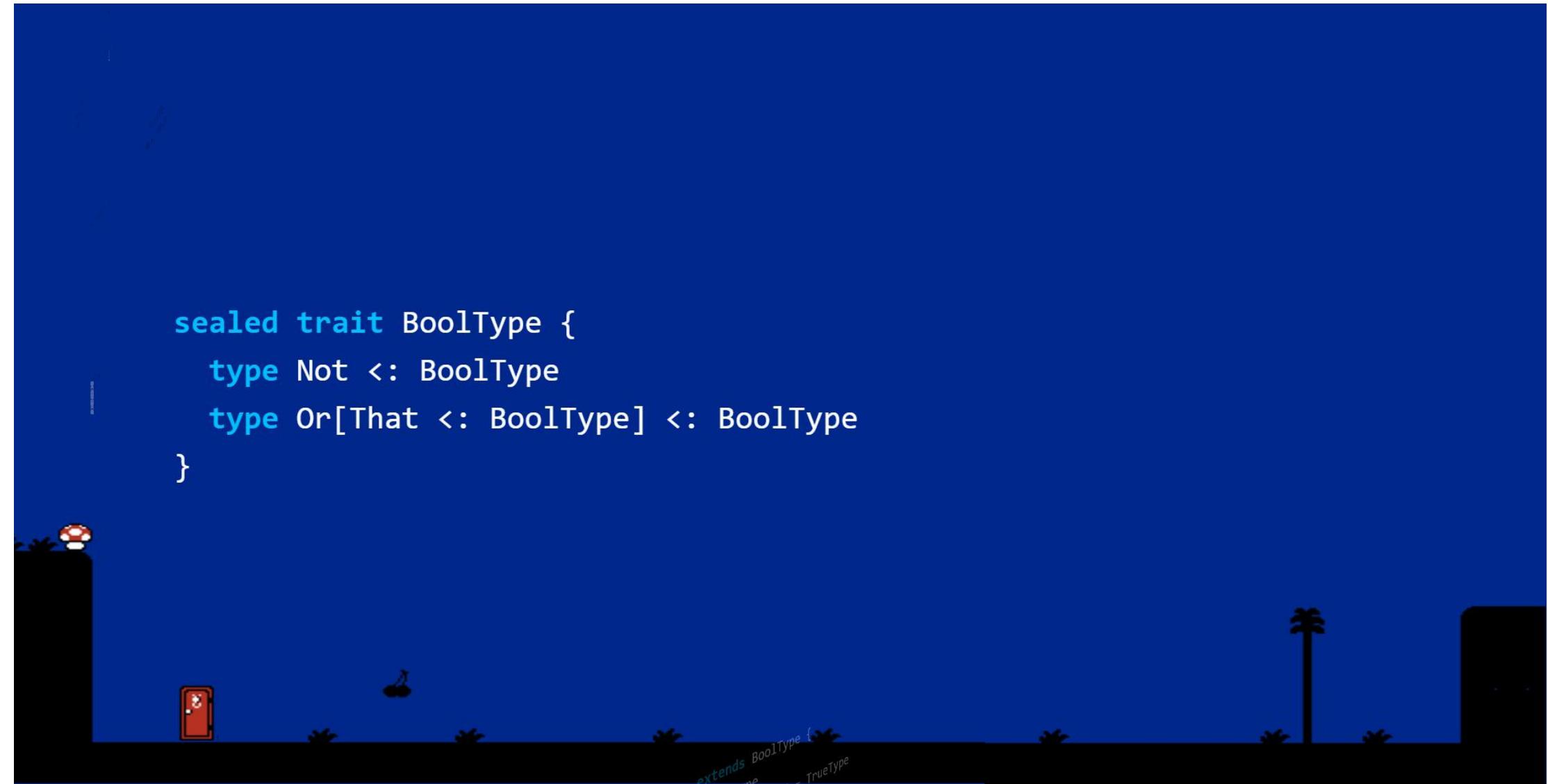


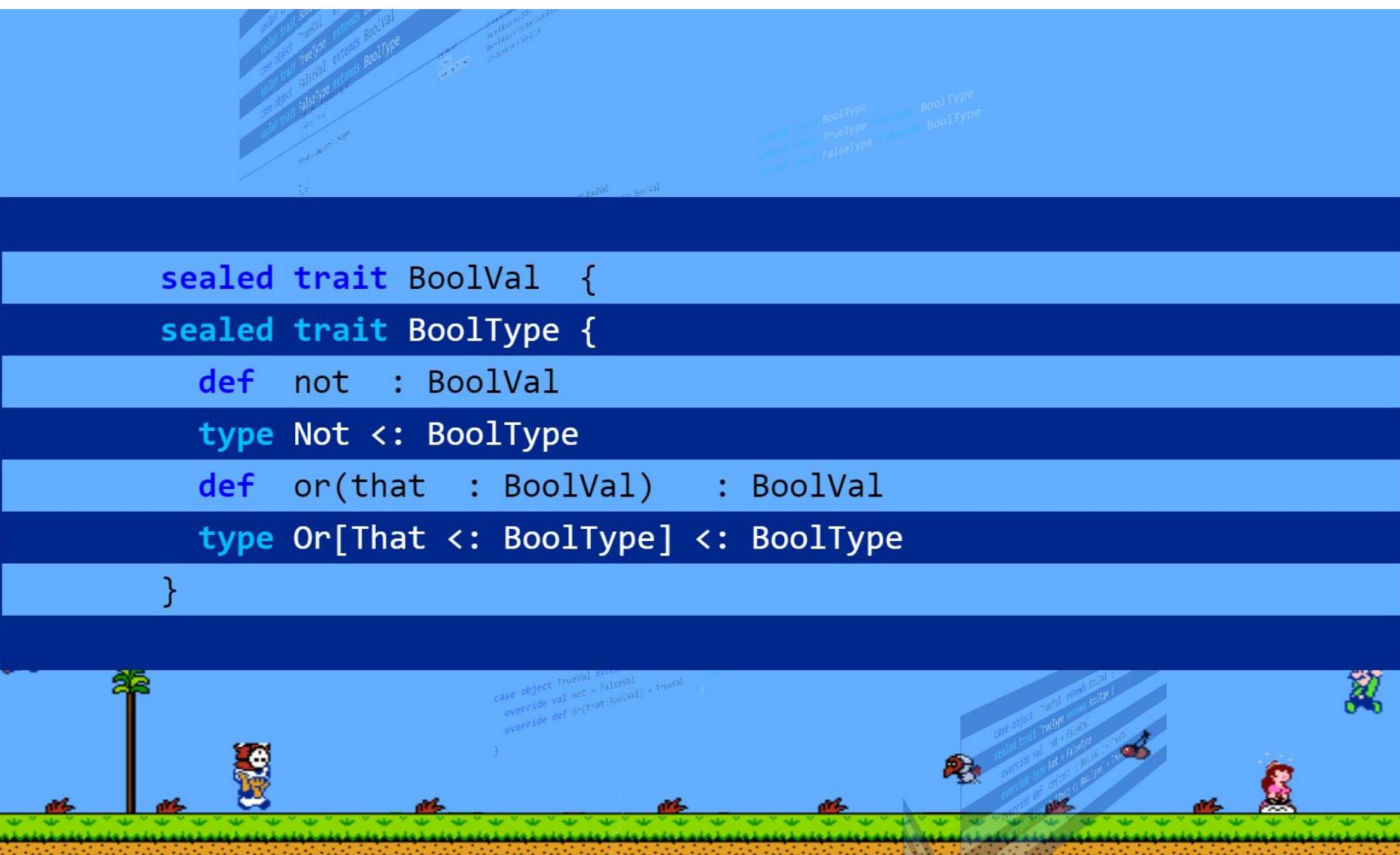
```
sealed trait BoolVal
sealed trait BoolType
case object TrueVal extends BoolVal
sealed trait TrueType extends BoolType
case object FalseVal extends BoolVal
sealed trait FalseType extends BoolType
```

BoolType {
 Not <: BoolType
 andThat <: BoolType
}



```
sealed trait BoolType {  
    type Not <: BoolType  
    type Or[That <: BoolType] <: BoolType  
}  
  
object TrueType extends BoolType {
```





```
sealed trait TrueType extends BoolType {  
    override type Not = FalseType  
    override type Or[That <: BoolType] = TrueType  
}
```

TrueType {

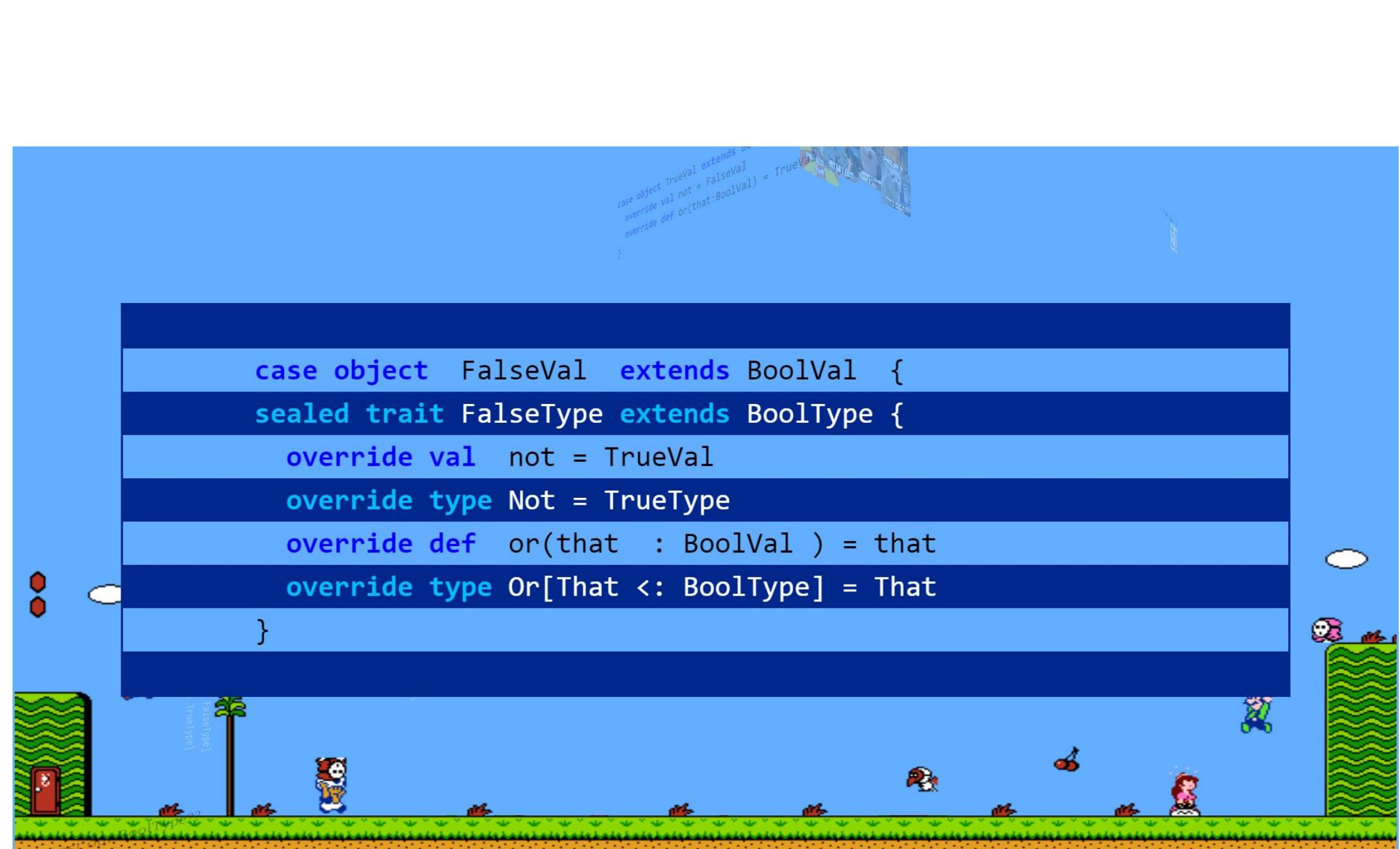
```
case object TrueVal extends BoolVal {  
  sealed trait TrueType extends BoolType {  
    override val not = FalseVal  
    override type Not = FalseType  
    override def or(that : BoolVal) = TrueVal  
    override type Or[That <: BoolType] = TrueType  
  }  
}
```

```
sealed trait FalseType extends BoolType {  
  override val not = TrueType  
  override type Not = TrueType  
  override def or(that : BoolType) = that  
}
```

```
sealed trait FalseType extends BoolType {  
    override type Not = TrueType  
    override type Or[That <: BoolType] = That  
}
```



```
case object FalseVal extends BoolVal {  
    sealed trait FalseType extends BoolType {  
        override val not = TrueVal  
        override type Not = TrueType  
        override def or(that : BoolVal) = that  
        override type Or[That <: BoolType] = That  
    }  
}
```

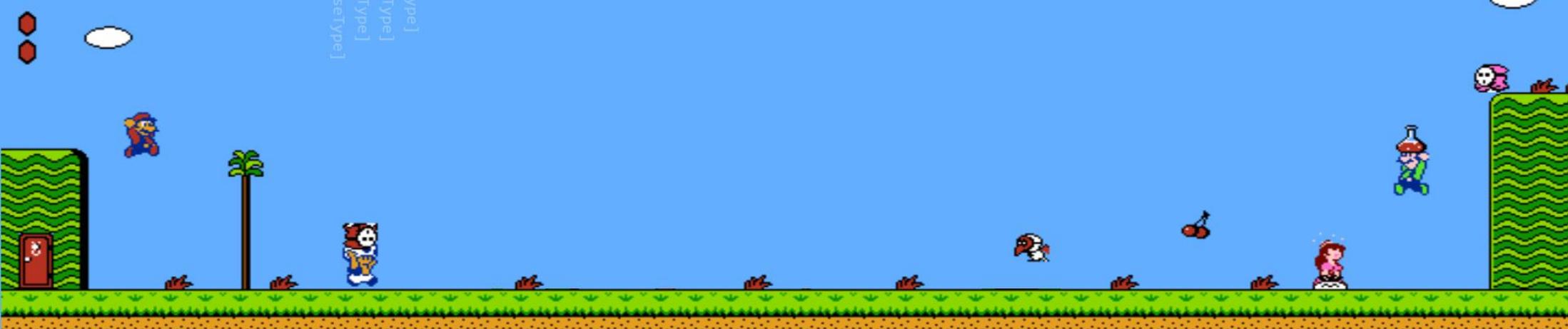


But how can we test our BoolType??

```
// Compile to test
object BoolTypeSpecs {
    implicitly[TrueType ==:= TrueType]
    implicitly[FalseType ==:= FalseType]
}

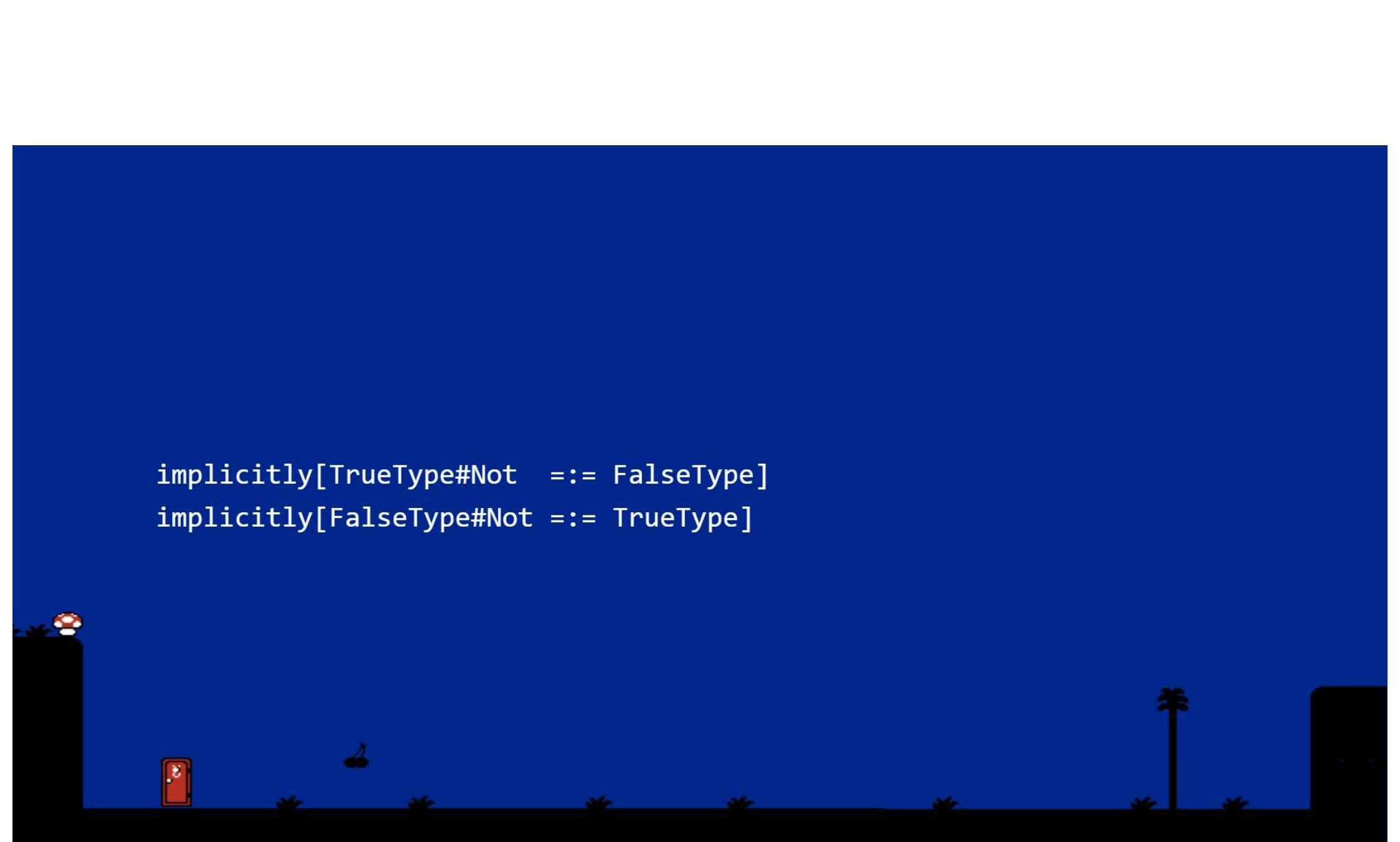
implicitly[TrueType#Not ==:= FalseType]
implicitly[FalseType#Not ==:= TrueType]
```

```
implicitly[TrueType#Or[TrueType] ==:= TrueType]
implicitly[TrueType#Or[FalseType] ==:= TrueType]
implicitly[FalseType#Or[TrueType] ==:= TrueType]
implicitly[FalseType#Or[FalseType] ==:= FalseType]
```



```
// Compile to test
object BoolTypeSpecs {
    implicitly[TrueType  =:= TrueType]
    implicitly[FalseType =:= FalseType]
}
```





```
implicitly[TrueType#Not  =:= FalseType]
implicitly[FalseType#Not =:= TrueType]
```

```
implicitly[TrueType#Or[TrueType] =:= TrueType]
implicitly[TrueType#Or[FalseType] =:= TrueType]
implicitly[FalseType#Or[TrueType] =:= TrueType]
implicitly[FalseType#Or[FalseType] =:= FalseType]
```



```
implicitly[
```

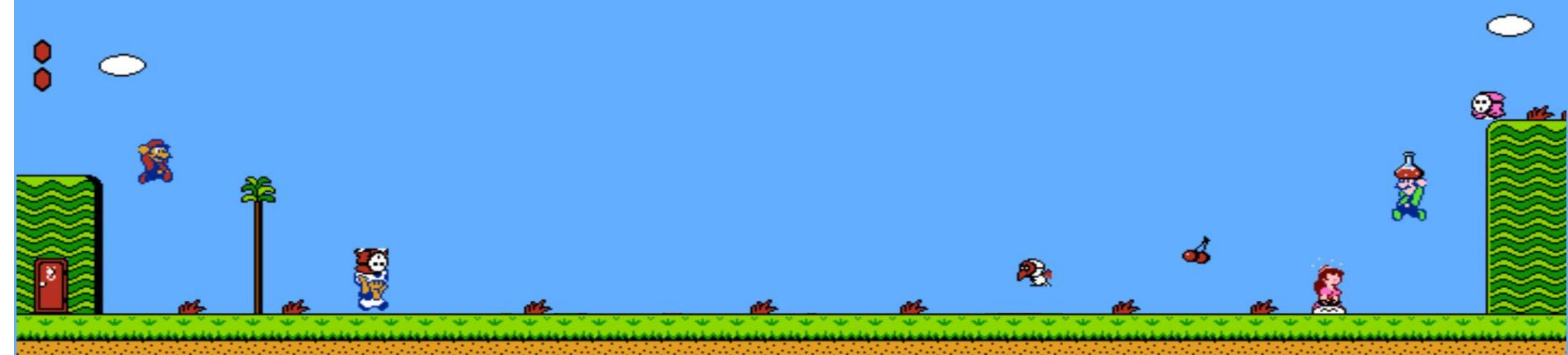
```
}
```

```
implicitly[
```

```
implicitly[
```

```
implicitly[
```

Ok, but what about negative test cases??



```
import shapeless.test.illTyped
// Compiles only if string DOESN'T compile
illTyped("implicitly[TrueType  =:= FalseType]")
illTyped("implicitly[FalseType =:= TrueType]")
```



```
illTyped("implicitly[TrueType#Not  =:= TrueType]")
illTyped("implicitly[FalseType#Not =:= FalseType]")
illTyped("implicitly[TrueType#Or[TrueType] =:= TrueType]")
illTyped("implicitly[TrueType#Or[FalseType] =:= TrueType]")
```

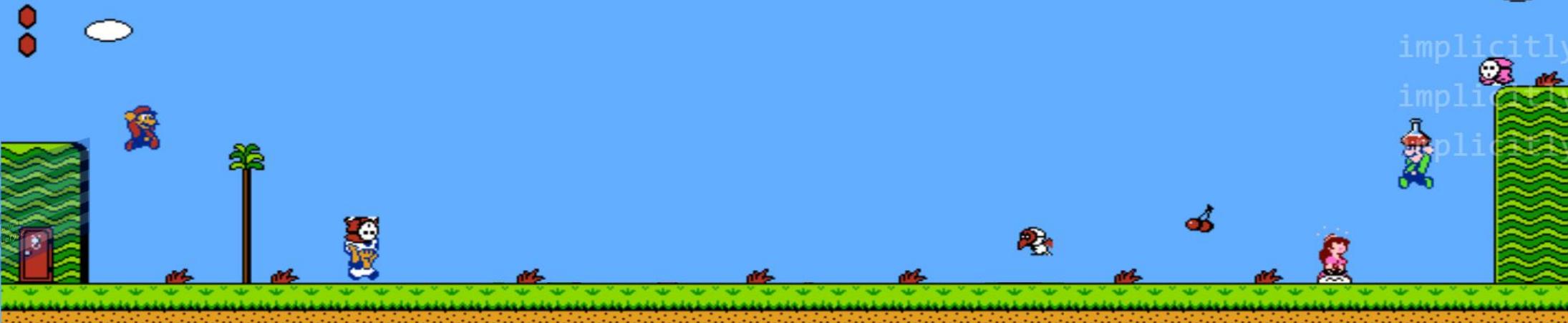


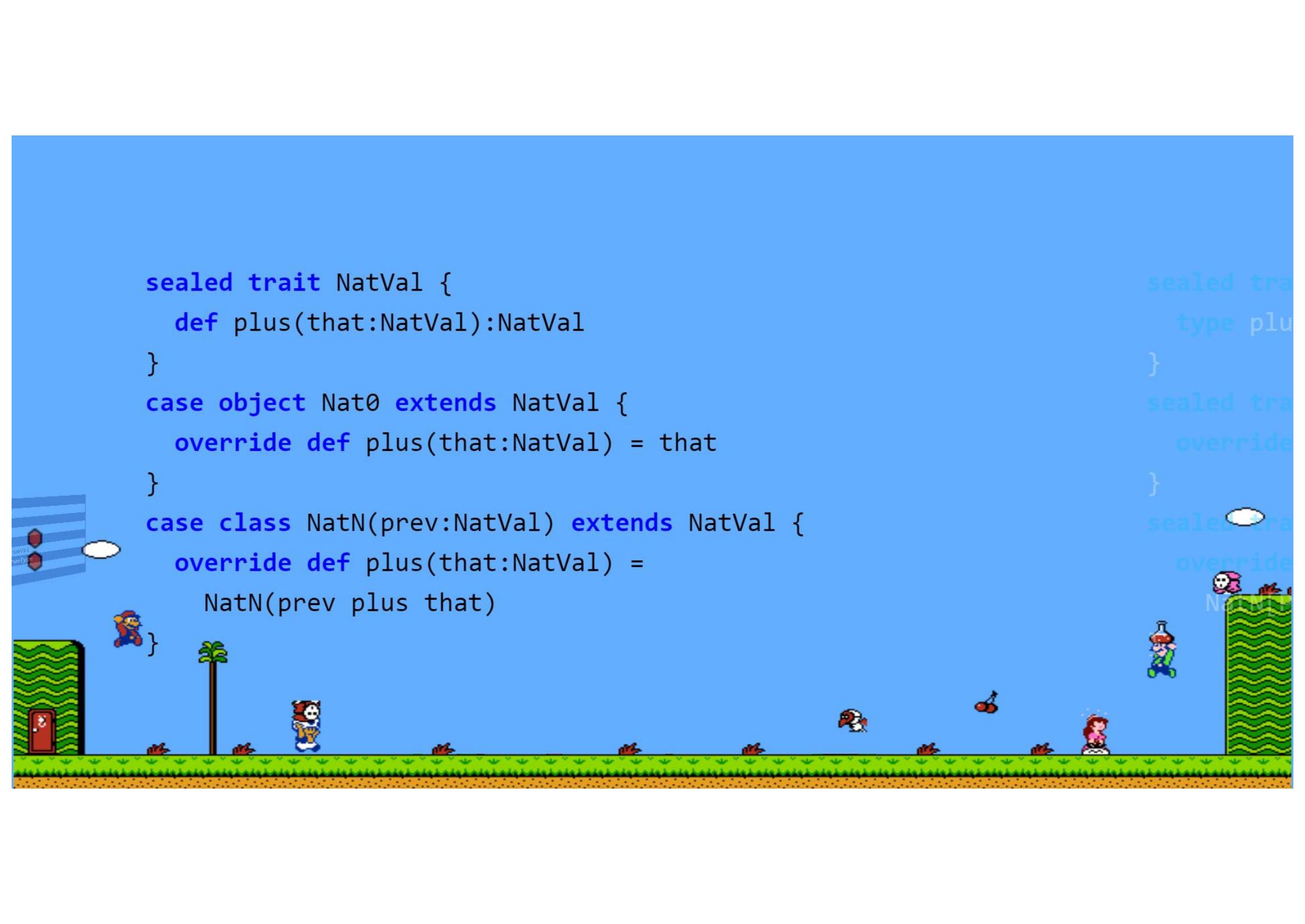


implicitly
illTyped(')

implicitly
impli-
pli-
cally

Well that was easy... It's just two types, really...





```
sealed trait NatVal {  
    def plus(that:NatVal):NatVal  
}  
case object Nat0 extends NatVal {  
    override def plus(that:NatVal) = that  
}  
case class NatN(prev:NatVal) extends NatVal {  
    override def plus(that:NatVal) =  
        NatN(prev plus that)  
}
```

```
sealed tra  
type plu  
}  
sealed tra  
override  
}  
sealed tra  
override  
}  
sealed tra  
override  
} NatN
```

```
val nat1 = NatN(Nat0)  
val nat2 = NatN(nat1)  
val nat3 = NatN(nat2)
```

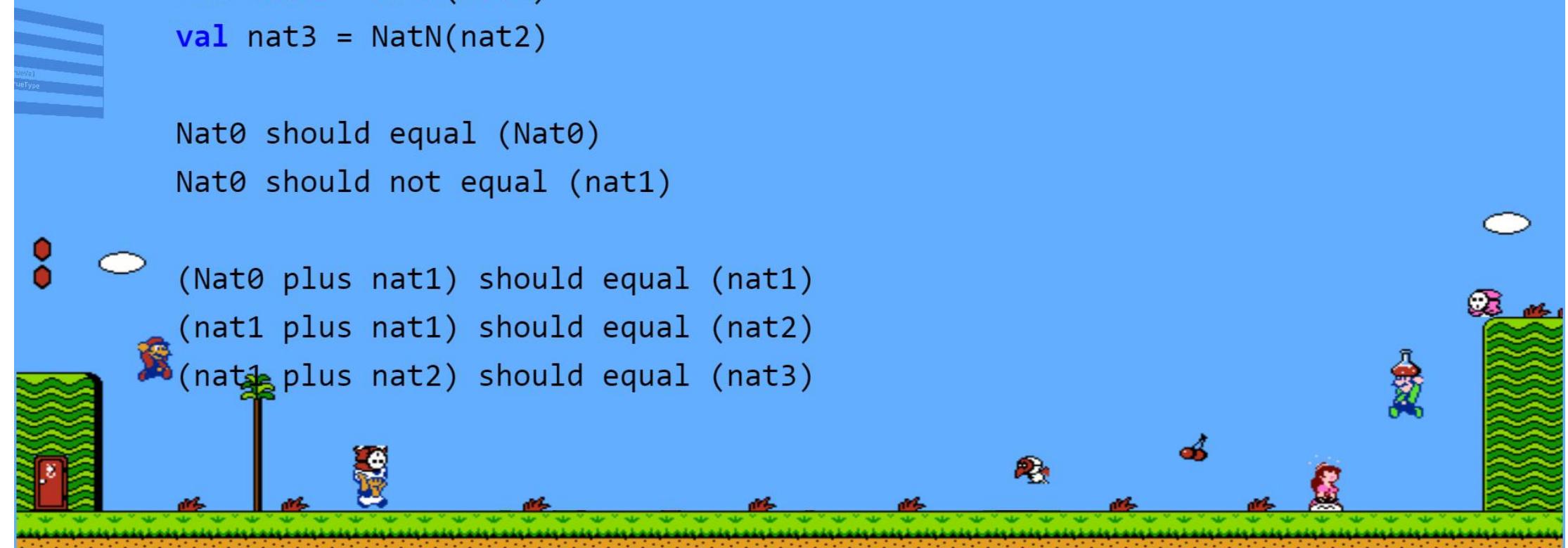
Nat0 should equal (Nat0)

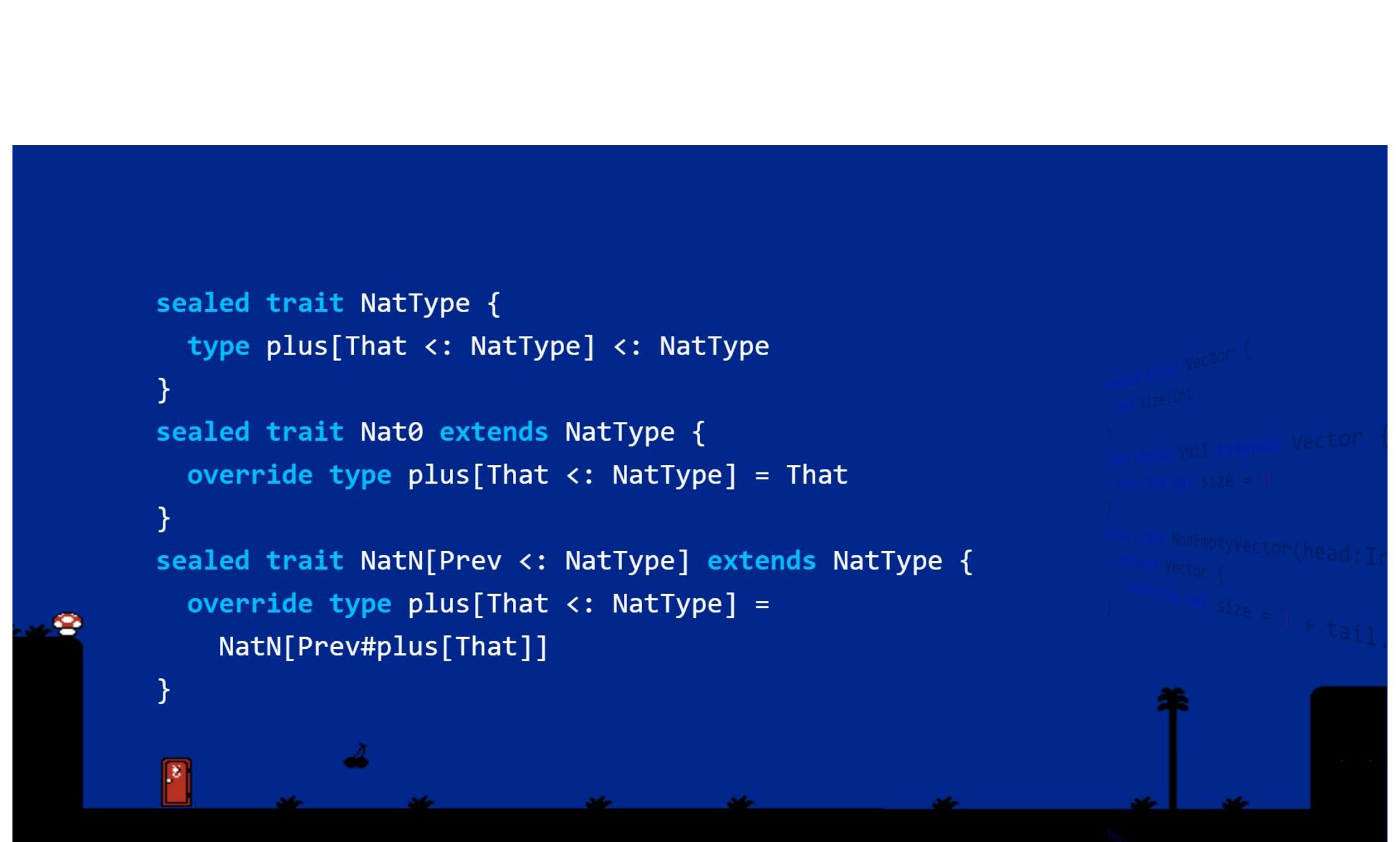
Nat0 should not equal (nat1)

(Nat0 plus nat1) should equal (nat1)

(nat1 plus nat1) should equal (nat2)

(nat1 plus nat2) should equal (nat3)





```
sealed trait NatType {
  type plus[That <: NatType] <: NatType
}
sealed trait Nat0 extends NatType {
  override type plus[That <: NatType] = That
}
sealed trait NatN[Prev <: NatType] extends NatType {
  override type plus[That <: NatType] =
    NatN[Prev#plus[That]]
}
```

```
sealed trait Vector {
  def size:Int
}
case object VNil extends Vector {
  override val size = 0
}
case class NonEmptyVector(head:Int, tail:Vector) {
  override val size = 1 + tail.size
}
```



```
type Nat1 = NatN[Nat0]
type Nat2 = NatN[Nat1]
type Nat3 = NatN[Nat2]

implicitly[Nat0 ==:= Nat0]
illTyped("implicitly[Nat0 ==:= Nat1]")

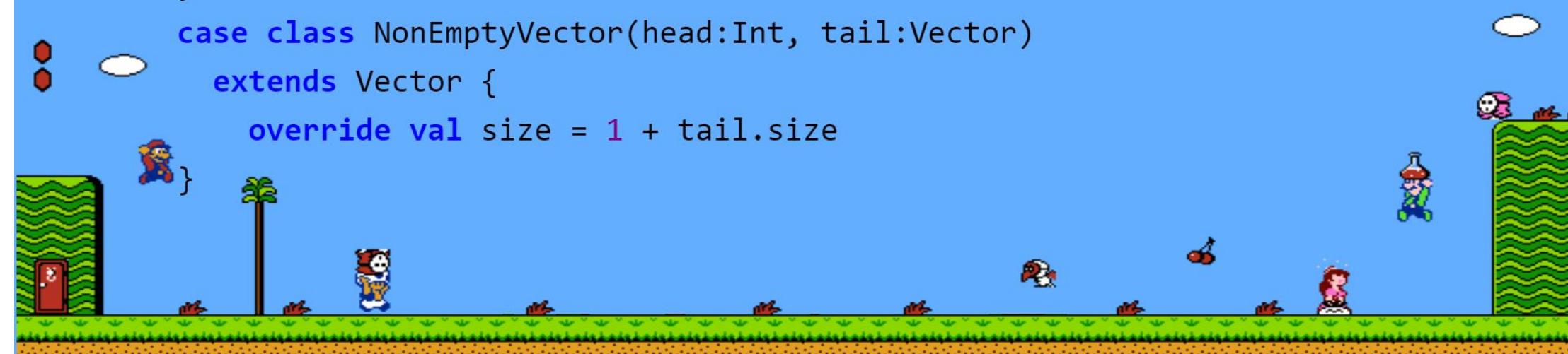
implicitly[Nat0#plus[Nat1] ==:= Nat1]
implicitly[Nat1#plus[Nat1] ==:= Nat2]
implicitly[Nat1#plus[Nat2] ==:= Nat3]
```



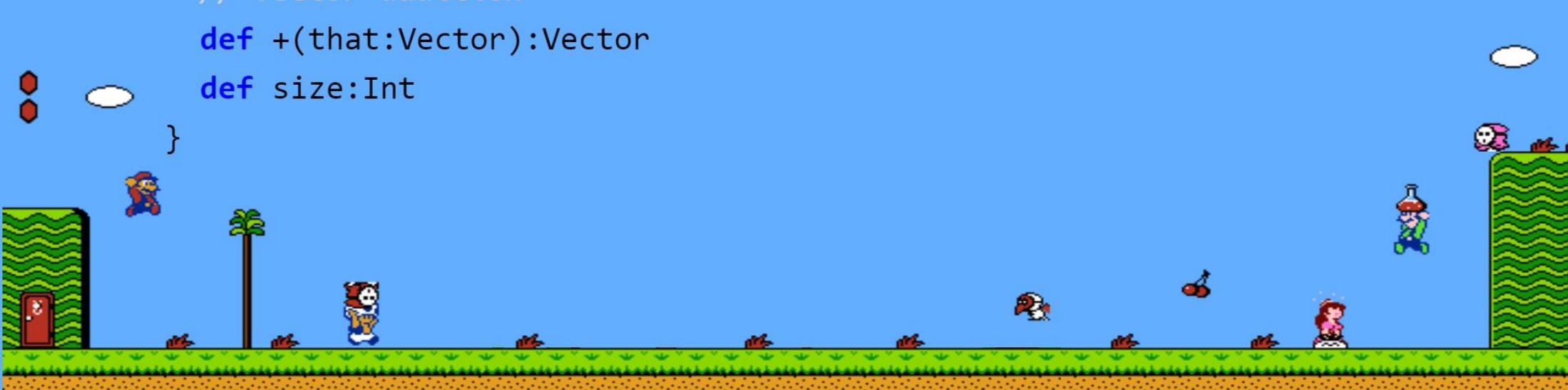
Types, types, and more types, blah, blah, blah. What good is it??

```
sealed trait Vector {  
    def size:Int  
}  
  
case object VNil extends Vector {  
    override val size = 0  
}  
  
case class NonEmptyVector(head:Int, tail:Vector)  
extends Vector {  
    override val size = 1 + tail.size  
}
```

We can validate our length

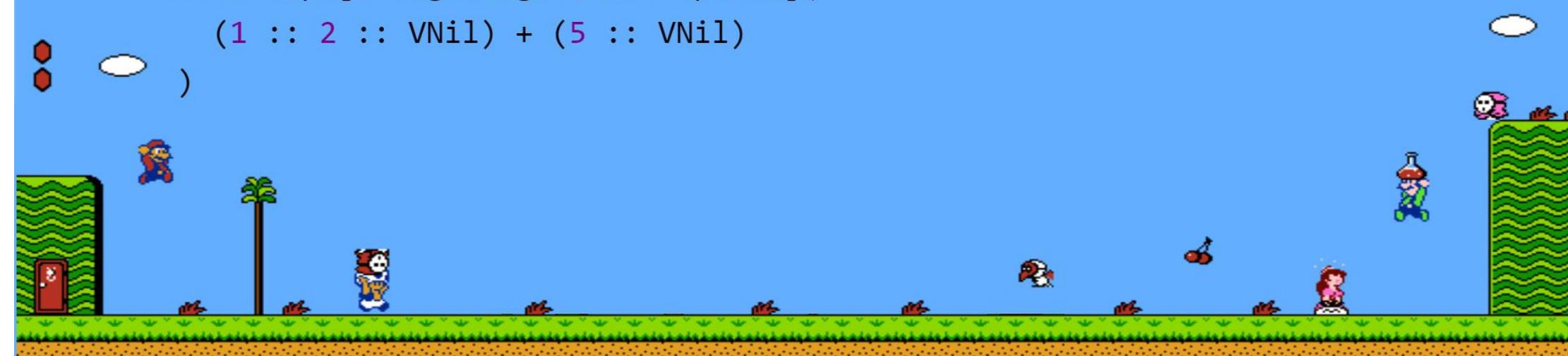


```
sealed trait Vector {  
    // Convenience vector constructor  
    def ::(head:Int):Vector = NonEmptyVector(head, this)  
    // Vector addition  
    def +(that:Vector):Vector  
    def size:Int  
}
```

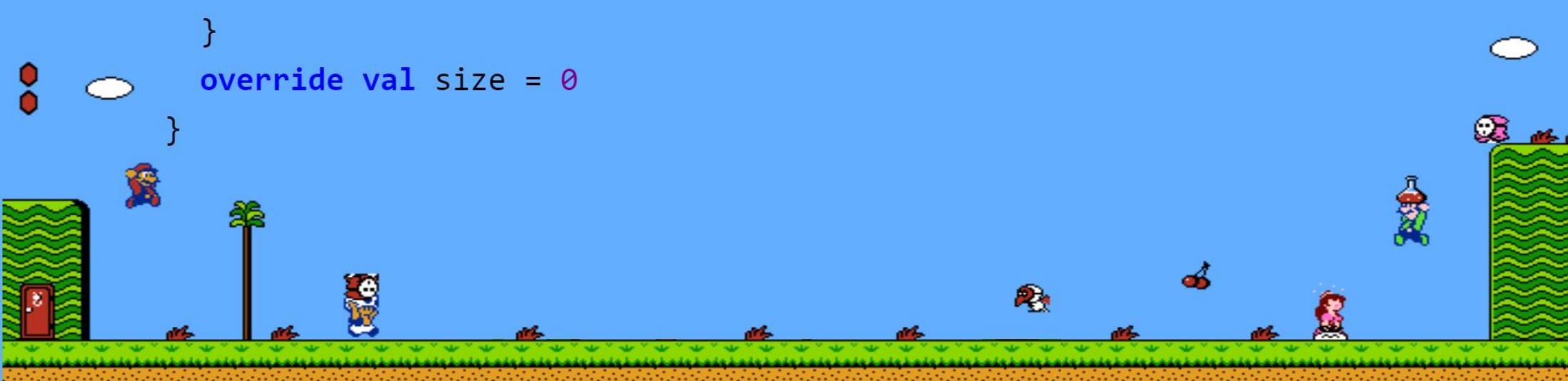


```
val sum = (1 :: 2 :: VNil) + (3 :: 4 :: VNil)  
sum should equal (4 :: 6 :: VNil)
```

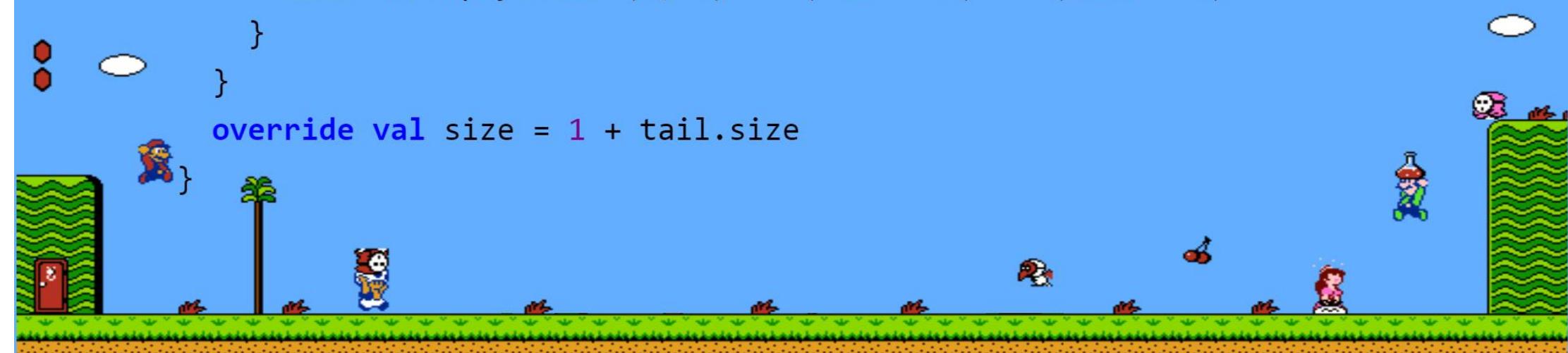
```
intercept[IllegalArgumentException]({  
    (1 :: 2 :: VNil) + (5 :: VNil)  
})
```



```
case object VNil extends Vector {  
    override def +(that:Vector) = {  
        require(that == VNil)  
        this  
    }  
    override val size = 0  
}
```

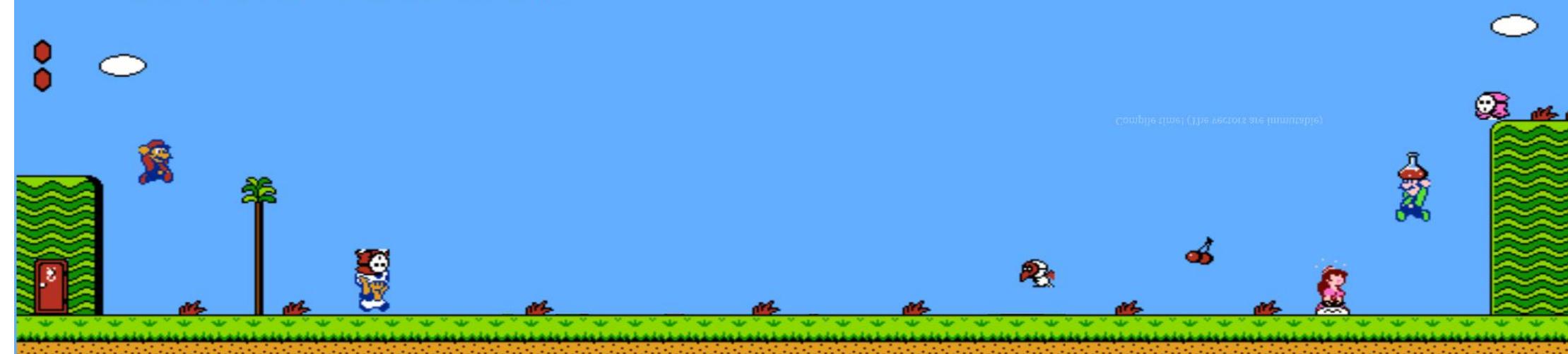


```
case class NonEmptyVector(head:Int, tail:Vector)
  extends Vector {
  override def +(that:Vector) = {
    require(that.size == size)
    that match {
      case NonEmptyVector(h, t) => (head + h) :: (tail + t)
    }
  }
  override val size = 1 + tail.size
}
```



```
        }  
    override val size = 1 + tail.size  
}
```

This implementation validates size at runtime.
But *when* do we know the size?



Compile time! (The vectors are immutable)



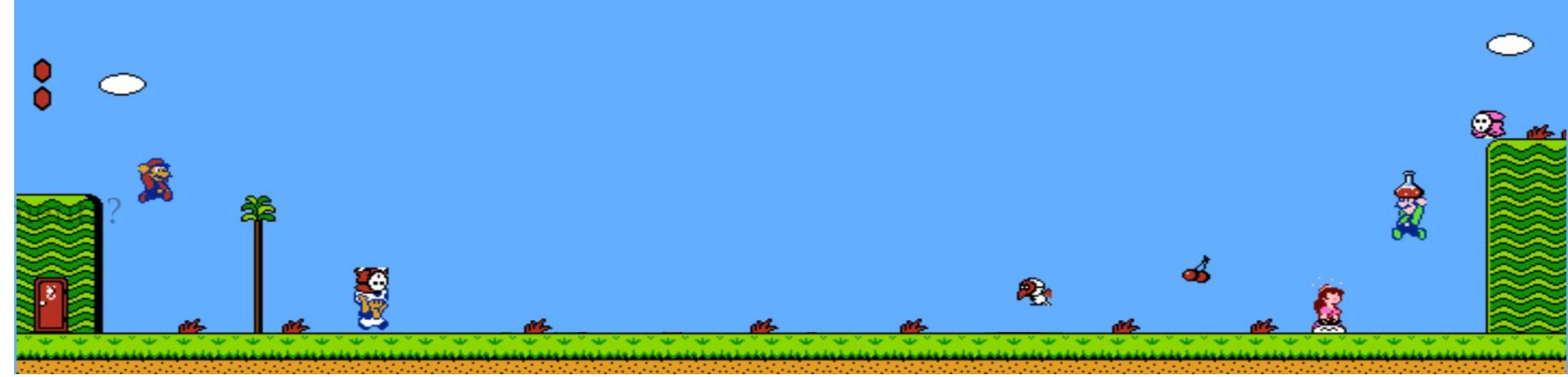


We can validate our lengths without a runtime `IllegalArgumentException`!

Stay tuned for my *Type-Programming in Scala 101 Workshop* to learn how!



Questions?



erns?

Questions?

Comments?



Concerns?

Questions?

Comments?

Download slides

Questions?

Comments?

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[Presentation Source](#)

```
let rec f (l : list) = match l with
| [] :: l' -> f l'
| _ :: l' -> f l' + (1 :: f l')
| _ :: _ :: l' -> f l' + (2 :: f l')
| _ :: _ :: _ :: l' -> f l' + (3 :: f l')
| _ :: _ :: _ :: _ :: l' -> f l' + (4 :: f l')
| _ :: _ :: _ :: _ :: _ :: l' -> f l' + (5 :: f l')
| _ :: _ :: _ :: _ :: _ :: _ :: l' -> f l' + (6 :: f l')
```

