Question 1. A vessel is filled completely with liquid water and sealed at 15.0° C and a pressure of 1.00 bar. What is the pressure if the temperature of the system is raised to 75.5° C? Under these conditions,  $\alpha_{water} = 2.04 \times 10^{-4} \ 1/K$ ,  $\alpha_{vessel} = 1.42 \times 10^{-4} \ 1/K$ , and  $\kappa_T = 4.59 \times 10^{-5} \ 1/bar$ .

Question 2. Let  $f(x,y) = xy \sin 5x + x^2 \sqrt{y} \ln y + 3e^{-2x^2} \cos y$ . Determine

(a)  $\frac{\partial f}{\partial x}$ 

 $(c) \frac{\partial^2 f}{\partial x^2}$ 

(e)  $\frac{\partial^2 f}{\partial y \partial x}$ 

(b)  $\frac{\partial f}{\partial u}$ 

 $(d) \frac{\partial^2 f}{\partial u^2}$ 

 $(f) \frac{\partial^2 f}{\partial x \partial y}$ 

Obtain an expression for the exact differential df.

Question 3. A mass of 25.0 g of  $H_2O_{(s)}$  at 273 K is dropped into 130 g of  $H_2O_{(\ell)}$  at 298 K in an insulated container at 1 bar of pressure. Calculate the temperature of the system once equilibrium has been reached. Assume that  $C_{P,m}$  for  $H_2O$  is constant at its values for 298 K throughout the temperature range of interest.

Question 4. A 62.5-g piece of gold at 650 K is dropped into 165 g of  $H_2O_{(\ell)}$  in an insulated container at 1 bar pressure. Calculate the temperature of the system once equilibrium has been reached. Assume that  $C_{P,m}$  for Au and  $H_2O$  are constant at their values for 298 K throughout the temperature range of interest.

**Question 5.** Calculate W, q,  $\Delta H$  and  $\Delta U$  for the process in which 2.50 mol of water undergoes the transition

$$H_2O_{(\ell,373\ K)} \to H_2O_{(g,610\ K)}$$

at 1 bar of pressure. The volume of the liquid water at 373 K is  $1.89 \times 10^{-5}$  m<sup>3</sup>/mol and the volume of steam is 373 K and 610 K is 3.03 and  $5.06 \times 10^{-2}$  m<sup>3</sup>/mol, respectively. For steam,  $C_{P,m}$  can be considered constant over temperature interval of interest at 33.58 J/mol K.

**Question 6.** The molar heat capacity  $C_{P,m}$  of  $SO_{2(g)}$  is described by the following equation over the range 300 K < T < 1700 K:

$$\frac{C_{P,m}}{R} = 3.093 + 6.967 \times 10^{-3} \frac{T}{K} - 45.81 \times 10^{-7} \frac{T^2}{K^2} + 1.035 \times 10^{-9} \frac{T^3}{K^3}$$

In this equation, T is the absolute temperature in Kelvin. The ratios  $T^n/K^n$  ensure that  $C_{P,m}$  has the correct dimension. Assuming ideal gas behavior, calculate q, W,  $\Delta U$  and  $\Delta H$  if 2.25 mol of  $SO_{2(g)}$  are heated from 10.0° C to 1250° C at a constant pressure of 1 bar. Explain the sign of W.

**Question 7.** For a gas that obeys the equation of state

$$V_m = \frac{RT}{P} + B(T)$$

derive the result

$$\frac{\partial H}{\partial P} = B(T) - T\frac{dB}{dT}$$