

Double Integrals

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Vertical Slices

- We have a function measuring something, bounded by two equations of the form $y=T(x)$, $y=B(x)$
 - ▶ $\int_a^b dx \int_{B(x)}^{T(x)} dy f(x, y)$

Horizontal Slices

- We have a function measuring something, bounded by two equations of the form $x=L(y)$, $x=R(y)$
 - ▶ $\int_c^d dy \int_{L(y)}^{R(y)} dx f(x, y)$

Arithmetic of Integration

- $\iint (f(x, y) + g(x, y)) dx dy = \iint f(x, y) dx dy + \iint g(x, y) dx dy$
- $\iint (f(x, y) - g(x, y)) dx dy = \iint f(x, y) dx dy - \iint g(x, y) dx dy$
- $\iint C f(x, y) dx dy = C \iint f(x, y) dx dy$
- $\iint_R f(x, y) dx dy = \iint_{R_1} f(x, y) dx dy + \iint_{R_2} f(x, y) dx dy$