

## MATH 3503 - Assignment 4

Due: March 14 2025

- 1 Suppose there are three carts of equal mass  $m$  and connected by two springs of constant  $k$  (and no connections to walls). Setup the system and find its general solution.
- 2 Let  $A = \begin{bmatrix} 5 & -4 & 4 \\ 0 & 3 & 0 \\ -2 & 4 & -1 \end{bmatrix}$ . a) What are the eigenvalues? b) Find the general solution of  $\vec{x}' = A\vec{x}$ .
- 3 Compute  $e^{tA}$  for the matrix  $A = \begin{bmatrix} 2 & 3 \\ 0 & 2 \end{bmatrix}$ .
- 4 Let  $A = \begin{bmatrix} -1 & -1 \\ 1 & -3 \end{bmatrix}$ . a) Find  $e^{tA}$ . b) Solve  $\vec{x}' = A\vec{x}, \vec{x}(0) = \begin{bmatrix} 1 \\ -2 \end{bmatrix}$