

February 18, 2025

1. When you have a repeated value of  $r$  when solving the characteristic equation of a second order ODE, why do you have to multiply the first solution by a power of  $x$  in order to get the second solution? What are you trying to ensure? (3 Marks)
2. Why do you check if an equation is exact by checking if  $\frac{\partial M}{\partial y}$  is equal to  $\frac{\partial N}{\partial x}$ ? Think about where  $M$  and  $N$  come from. (3 Marks)

3. Find the fundamental matrix for the system of equations  $Y' = AY$ , where A is given by  $\begin{bmatrix} 1 & 1 \\ -1 & 0 \end{bmatrix}$ . You will need to solve this system first. (4 Marks)