MATH 3503 - Assignment 1

Due: January 17 2025

1 Classify the following equations. Is the equation an ODE or a PDE? What order is the DE? Is it homogeneous?

a)
$$sin(t)\frac{d^2x}{dt^2} + xcos(t) = t^2$$

b)
$$\frac{\partial u}{\partial x} + 3\frac{\partial u}{\partial y} = xy$$

c)
$$\frac{\partial^2 u}{\partial x^2} + u \frac{\partial^2 u}{\partial y^2} = 0$$

d)
$$x'' + tx^2 = t$$

e)
$$\frac{d^3 f}{dx^3} = 12f$$

2 Solve the following differential equations by using one of the following techniques: variable-separable or linear (with an integration factor). Please state the technique used. If initial conditions are given, provide the particular solution.

a)
$$\frac{dy}{dx} = \frac{x}{y}; y(0) = 1$$

b)
$$y' + y = 42$$

c)
$$\frac{dy}{dx} = 12x; y(1) = 2$$

d)
$$\frac{df}{dy} = y$$

e)
$$y' + 12y = e^x$$