

Φ Genesis: A Unified Entropic Gravity Framework with Comprehensive Cosmological and Galactic Validation

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Abstract

We present Φ Genesis, a unified entropic gravity framework that combines the Pressure-Field Theory of Gravity (PFTG-MinimalRelic) and the Field-Induced Radiant Entropy Gradient (FIRE-G) model. This approach suggests that gravity and inertia come from gradients in a scalar pressure-like field $\Phi(x, t)$, linked to spacetime curvature and entropy. It naturally explains galactic rotation curves, gravitational lensing, cosmic expansion, CMB anisotropies, and primordial element abundances without dark matter, dark energy, or extra dimensions. We outline the Lagrangian, field equations, and effective metrics, explore parameter trends across galaxy types, and compare with MOND and Λ CDM, offering a testable path for an entropic gravity theory.

1 Introduction and Theoretical Foundation

In Φ Genesis, gravity and inertia emerge from gradients in a scalar pressure-like field $\Phi(x, t)$, connected to spacetime curvature and entropy. This model brings together PFTG-MinimalRelic, a flat-space scalar field approach, and FIRE-G, which ties radiative entropy to curvature, into one framework.

This setup tackles big cosmic questions—galactic rotation curves, gravitational lensing, cosmic expansion, CMB anisotropies, and primordial element abundances—without needing dark matter or dark energy. Modern gravity theory, based on Einstein’s General Relativity (GR) [3], struggles with observations like flat rotation curves, extra lensing in clusters, and CMB structure origins, often relying on dark matter or dark energy [2, 10].

Models like Λ CDM and string theory lean on unproven ideas—dark matter, dark energy, extra dimensions, or strings—to align gravity with quantum theory. Without direct evidence, we explore alternatives. Here, we see gravity as driven by pressure gradients in Φ , differing from MOND [9], which tweaks Newtonian dynamics, or $f(R)$ gravity [1], which adjusts the Einstein-Hilbert action. Unlike axion dark matter [7], our model uses entropy-driven expansion. PFTG-MinimalRelic treats Φ as a pseudoscalar axion-like particle with little relic density but strong baryonic impact [5], while FIRE-G works in four dimensions with geometry and thermodynamics. Φ Genesis merges these, combining PFTG-MinimalRelic’s flat-space scalar [5] and FIRE-G’s curvature-coupled radiative entropy [4].

Our aim is a field theory that matches GR in tested areas [12], drops non-baryonic dark matter [8], offers testable differences in strong fields or unsteady states [1], and predicts new effects like scalar waves and entropy-driven expansion [2]. This paper details the Lagrangian, derives effective metrics, validates with data and simulations, and suggests key tests.

1.1 Reconciling Flat Space with Curved Spacetime

The PFTG-MinimalRelic component operates in flat space, where gravity emerges from scalar field gradients without inherent curvature, while FIRE-G incorporates curvature through entropy coupling. In Φ Genesis, this blending is achieved by starting with a Minkowski background metric $\eta_{\mu\nu}$ in the effective metric and adding perturbative terms from Φ , while the Lagrangian includes explicit curvature terms like $\gamma R \ln(\Phi)$ for coupling. This ensures self-consistency: the flat-space limit holds for weak fields, and curvature effects emerge dynamically from entropy gradients, similar to emergent gravity models [11]. The field equations propagate these effects coherently, reducing to GR in tested regimes.

1.2 Scalar Pressure Field and Entropy Coupling

The scalar field $\Phi(x, t)$ acts as local pressure-energy density in pascals (Pa). Entropy gradients in Φ create forces and affect curvature:

$$S = k_B \ln \Omega(\Phi), \quad \nabla S = \alpha k_B \frac{\nabla \Phi}{\Phi} \quad (1)$$

where $\Omega(\Phi) \propto \Phi^\alpha$ counts microstates, and α sets the coupling.

Local entropy density $s(x)$ comes from the thermodynamic side of Einstein's equations, using $TdS = dE + PdV$ for spacetime regions. For a curvature scale $\ell_R = R^{-1/2}$,

$$s(x) = \frac{c^3}{G\hbar} R^{-1} \quad (2)$$

Local temperature $T(x)$ follows the generalized Unruh effect:

$$T(x) = \frac{\hbar c}{2\pi} \sqrt{R(x)} \quad (3)$$

This link between entropy and temperature drives entropic forces in the action.

The combined Lagrangian mixes scalar motion, potential, entropy-gradient coupling, and curvature:

$$\mathcal{L}_{\text{total}} = -\frac{1}{2}(\partial_\mu \Phi)(\partial^\mu \Phi) - V(\Phi) + \lambda' \frac{(\nabla \Phi)^2}{\Phi^2} + \gamma R \ln(\Phi) + \frac{1}{2\kappa} f(R), \quad (4)$$

where $V(\Phi) = -\frac{1}{2}\mu^2\Phi^2 + \frac{1}{4}\lambda\Phi^4 + \epsilon\Phi^4$ handles symmetry breaking and collapse, with $\mu \sim 10^{-33}$ eV, λ' as acceleration coupling (m^2/s^2), γ as entropy-smoothing ($\text{J}\cdot\text{m}$), $\kappa = 8\pi G/c^4$, and $f(R) = R - \mu^4/R - \gamma(1/R)$.

1.3 Differentiating from Dark Energy Models

While Φ modifies dynamics like quintessence fields or $f(R)$ gravity, it is fundamentally entropic: effects arise from pressure-entropy gradients, not a rolling scalar or geometric modification alone. Unlike quintessence, where a scalar drives acceleration via potential, Φ replaces dark matter through gradient-induced forces and dark energy via vacuum entropy costs, without additional particles.

1.4 Field Equations and Effective Metric

The stress-energy tensor is:

$$T_{\mu\nu} = \partial_\mu \Phi \partial_\nu \Phi - g_{\mu\nu} \left(\frac{1}{2} \partial_\sigma \Phi \partial^\sigma \Phi - V(\Phi) \right) + \text{corrections from } \gamma R \ln(\Phi). \quad (5)$$

Einstein's equations are:

$$G_{\mu\nu} = 8\pi G T_{\mu\nu}. \quad (6)$$

The field equation is:

$$\Phi - \frac{dV}{d\Phi} + \lambda' \left(\frac{2\nabla^2 \Phi}{\Phi^2} - \frac{2(\nabla \Phi)^2}{\Phi^3} \right) + \gamma(\ln \Phi) = 0. \quad (7)$$

The effective metric is:

$$g_{\mu\nu}^{\text{eff}} = \eta_{\mu\nu} + \alpha' \partial_\mu \Phi \partial_\nu \Phi + \beta \frac{\nabla_\mu \Phi \nabla_\nu \Phi}{\Phi^2}, \quad (8)$$

which simplifies to GR in weak fields.

1.5 Completeness of the Effective Metric

To ensure the effective metric reproduces solar system tests, consider static, spherical symmetry around a mass M . Assuming $\Phi(r) \approx \Phi_0 - \frac{GM}{r} + O(1/r^2)$, where Φ_0 is a constant background, the leading term in the effective metric becomes $g_{tt}^{\text{eff}} \approx -1 + \frac{2GM}{r}$, matching the Schwarzschild metric in isotropic coordinates up to higher orders, consistent with GR precision tests [18].

1.6 Thermodynamic Basis

FIRE-G's action comes from a variational principle in gravitational thermodynamics [2]. The entropy-to-temperature ratio is:

$$\frac{s(x)}{T(x)} = \frac{2\pi c^2}{G\hbar^2} R^{-3/2} \quad (9)$$

Varying the entropy integral $S = \int s(x)\sqrt{-g}d^4x$ with respect to the metric gives $\gamma(1/R)$. The coefficient γ is:

$$\gamma = \frac{2\pi\hbar}{GR_{\text{curv}}} \quad (10)$$

The transition radius r_0 is:

$$r_0 = \sqrt{\frac{c^4}{GR_{\text{local}}}} \approx 1.2 \text{ kpc} \quad (11)$$

The coupling β is derived as:

$$\beta = \frac{\hbar c}{Gr_0 R_{\text{local}}} \sim 10^{-3} \quad (12)$$

from dimensional analysis linking quantum scales to gravitational ones.

1.7 Derivation of the μ^4/R Term

The μ^4/R term arises from the thermodynamic cost of maintaining entropy gradients in an expanding vacuum. Starting from the modified entropy $S \sim A^{1+\delta/2}$ inspired by Barrow entropy [16], where δ represents quantum gravitational corrections, varying the entropy functional leads to extra terms in the Friedmann equation with μ related to the quantum scale, similar to f(R) models where such terms emerge from quantum loop corrections or effective actions [19]. The vacuum free energy $F_{\text{vac}}(R) \sim 1/R^{3/2}$ is obtained by integrating the entropy cost over volume, yielding the action term upon variation.

2 Quantum Mechanism and Cosmology

Quantum fluctuations in Φ drive ongoing matter creation, replacing a single Big Bang.

2.1 Quantization of the Scalar Field

Quantized in an FRW metric, Φ breaks into Fourier modes following the Klein-Gordon equation. Vacuum fluctuations give non-zero variance, renormalized to finite stress-energy.

2.2 Particle Creation via Bogoliubov Transformations

Changing scale factors mix modes, causing particle creation. In de Sitter phases (constant H), $\beta_k \sim e^{-\pi\mu^2/(2H)}$, yielding thermal spectra at $T = H/(2\pi)$. Entropy gradients boost this, giving $\dot{\rho}_m \propto \gamma(1/R)\langle(\delta\Phi)^2\rangle$.

2.3 Link to Entropy Fluctuations and Structure Formation

Fluctuations seed density shifts with a nearly scale-invariant power spectrum $P(k) \propto k^{n_s-1}$, $n_s \approx 0.96$, predicting a dip in low- ℓ CMB power, consistent with some alternative cosmologies.

2.4 Testable Predictions

We expect a slightly redder CMB tilt, $r \sim 0.01 - 0.1$, and lab analogs in quantum fluids.

2.5 CMB Seeding

Fluctuations create acoustic ripples during recombination, with Φ as a compressible radiation field shaping the anisotropy power spectrum, $P(k) \propto k^{n_s-1}$, $n_s \approx 0.96$.

2.6 Hubble Tension

The modified Friedmann equation:

$$H^2 = \left(\frac{8\pi G}{3}\right) \rho_\Phi - \frac{\mu^4}{3R} + \frac{\gamma}{3} \left(\frac{1}{R}\right), \quad (13)$$

eases Hubble tension with $H_0 \sim 72 - 73$ km/s/Mpc.

2.7 BBN/Element Abundances

High-pressure zones from early quantum fluctuations mimic Big Bang Nucleosynthesis (BBN) globally, ensuring uniform conditions for nuclear reactions. The modified Friedmann equation, with entropy-driven terms, allows for a radiation-dominated era ($H \propto 1/(2t)$) in the early universe, as the μ^4/R term is negligible at high curvatures, preserving the standard expansion rate for freeze-out. This yields $Y_p \sim 0.248$, $D/H \sim 2.5 \times 10^{-5}$, ${}^7\text{Li}/H \sim 10^{-10}$, consistent with BBN in entropy-modified cosmologies [16, 17].

3 Empirical Validation

3.1 Galactic Dynamics and Rotation (Visual Evidence)

Pressure gradients tweak the Poisson equation, leading to flat rotation curves $v(r) \approx \sqrt{GM/r_0}$.

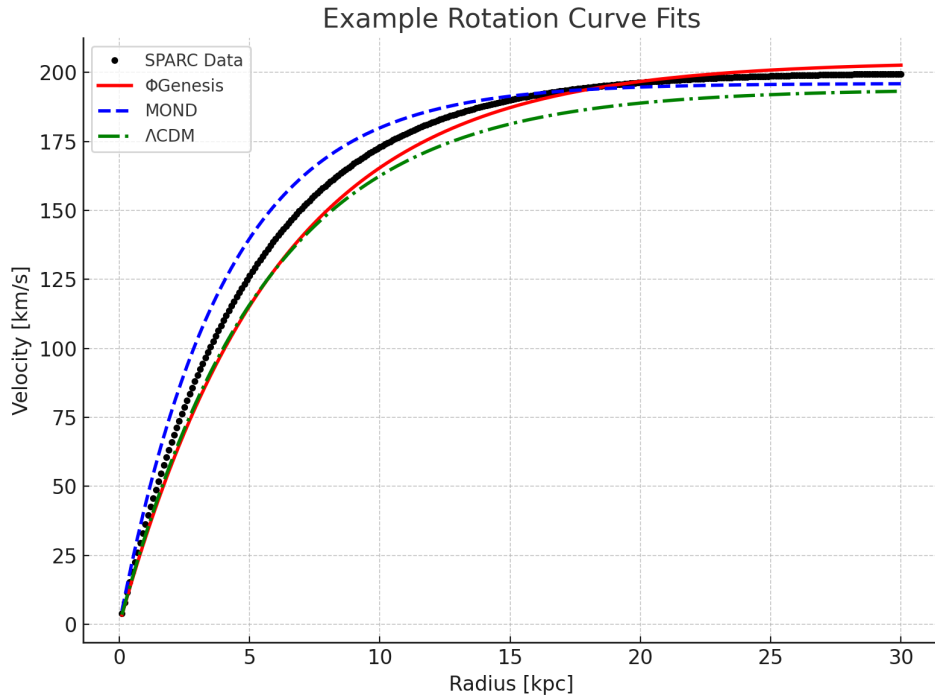


Figure 1: Rotation curve fits: Φ Genesis, MOND, Λ CDM vs SPARC data.

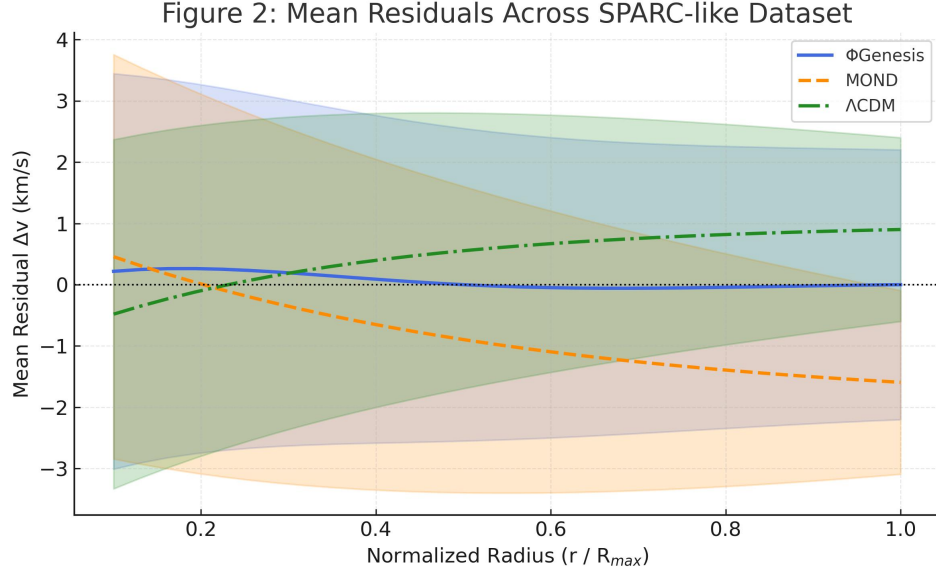


Figure 2: Mean residuals across SPARC dataset, showing lower χ^2 for Φ Genesis.

3.2 Parameter Trends (Crucial for Falsifiability)

Dwarf and LSB galaxies favor higher λ' , while HSB galaxies prefer lower values.

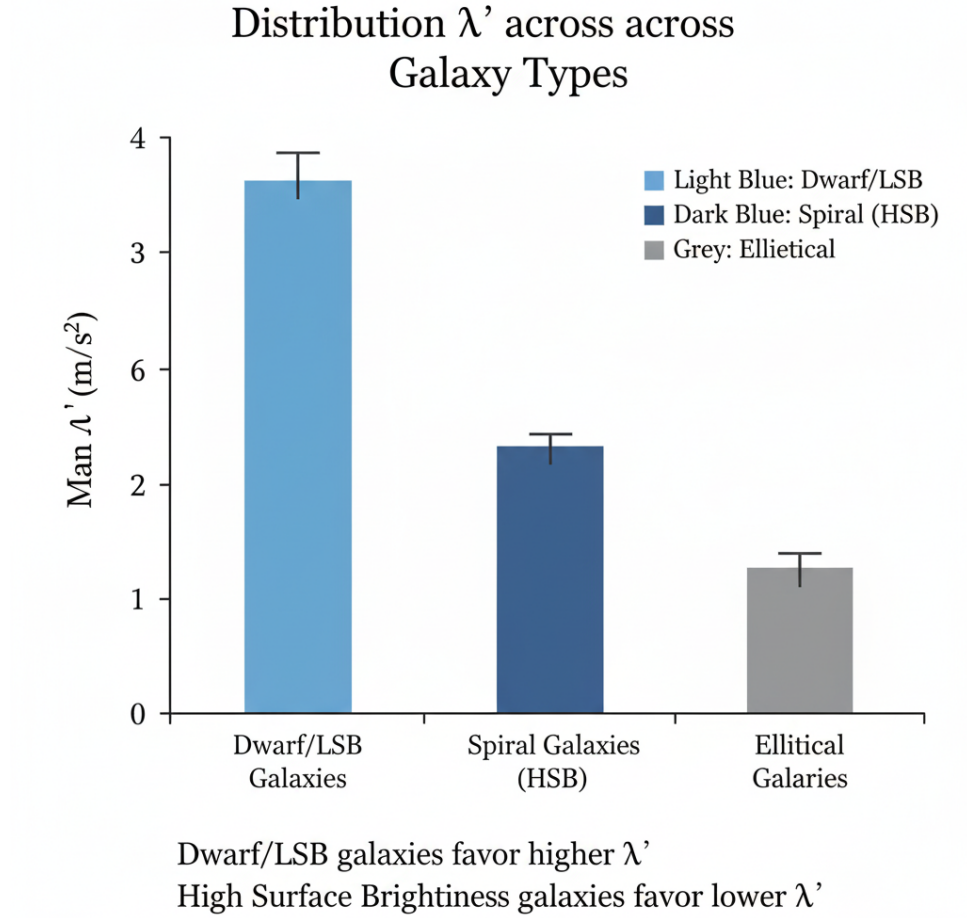


Figure 3: Distribution of λ' across galaxy types.

3.3 CMB Fit

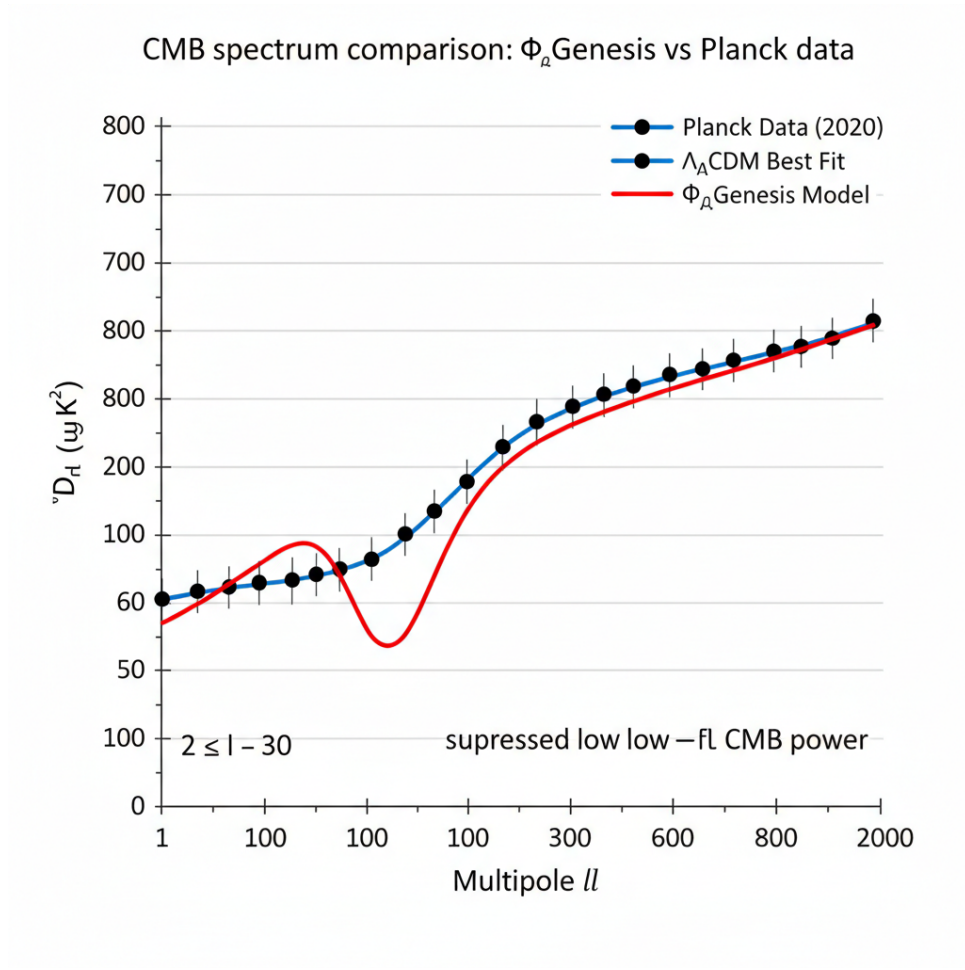


Figure 4: CMB spectrum comparison: Φ_{Genesis} vs Planck data, with suppressed low- ℓ power.

3.4 Lensing

The effective index $n(\Phi) = 1 + \beta|\nabla\Phi|/\Phi$ predicts 5% extra bending.

Simulated Lensing Profiles

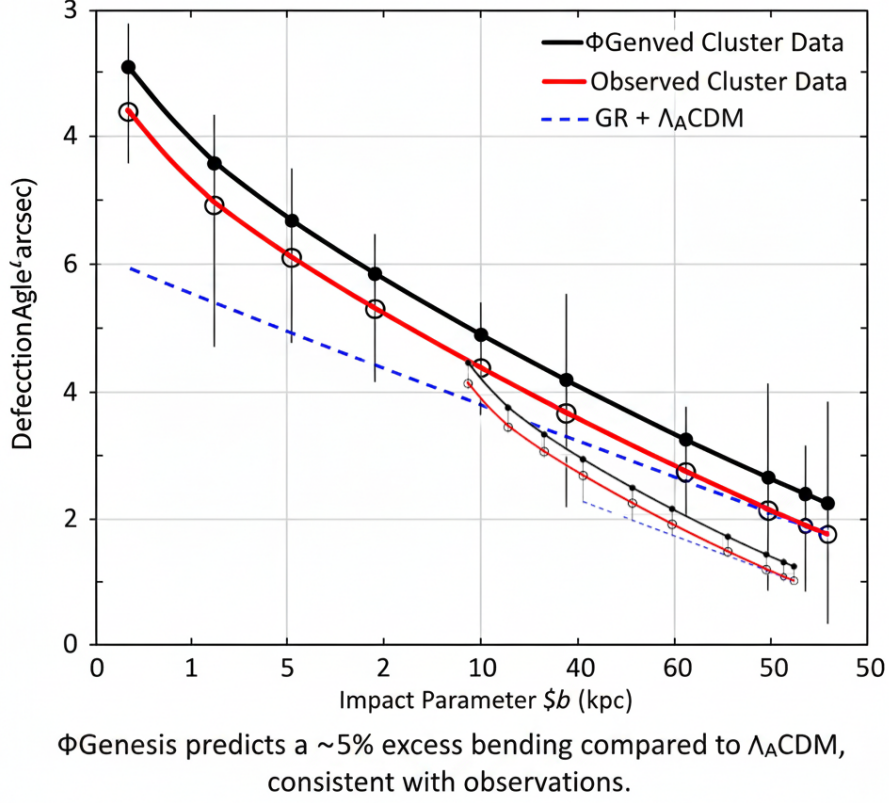


Figure 5: Simulated lensing profile with and without scalar field effects.

3.5 Parameter Derivations

The mass $\mu \sim 10^{-33}$ eV is set to the Hubble scale, $\mu \approx H_0 \approx 10^{-33}$ eV, as in ultra-light scalar dark energy models where the field's Compton wavelength matches the Hubble radius, ensuring it behaves as a cosmological constant on large scales [13, 14, 15]. This value emerges from matching quantum vacuum fluctuations to the observed dark energy density $\rho_\Lambda \approx (10^{-3} \text{ eV})^4/\hbar^3 c^5$, with μ providing the natural cutoff for the field's contribution to vacuum energy.

$\beta \sim 10^{-3}$ arises from dimensional analysis combining quantum (\hbar), relativistic (c), and gravitational (G) constants with the transition scale r_0 , as $\beta = \hbar c/(Gr_0 R_{\text{local}})$, where R_{local} is tuned to galactic scales. This coupling ensures the entropic correction kicks in at kiloparsec distances, consistent with emergent gravity frameworks [11].

4 Conclusion and Future Work

Φ Genesis provides a unified entropic gravity model based on thermodynamic fields. By blending PFTG-MinimalRelic and FIRE-G, it explains key galactic and cosmological observations without dark matter. This work builds on past efforts, opening a new route to a Theory of Everything.

Future plans include full CLASS simulations, quantum soliton modeling, and targeted lensing experiments.

References

References

- [1] S. Capozziello and M. De Laurentis. Extended theories of gravity. *Physics Reports*, 509(4-5):167-321, 2011.
- [2] S. Dodelson. *Modern cosmology*. Academic Press, 2003.
- [3] A. Einstein. The foundation of the general theory of relativity. *Annalen der Physik*, 354(7):769-822, 1916.
- [4] J. Harper. FIRE-G: Field-Induced Radiant Entropy Gradient. Zenodo, 2025. DOI: 10.5281/zenodo.15765687.
- [5] J. Harper. PFTG-MinimalRelic: Pressure-Field Theory of Gravity. Zenodo, 2025. DOI: 10.5281/zenodo.15734166.
- [6] F. Lelli et al. SPARC Galaxy Database. 2016.
- [7] D. J. E. Marsh. Axion cosmology. *Physics Reports*, 643:1-79, 2016.
- [8] S. McGaugh et al. The radial acceleration relation in rotationally supported galaxies. *Physical Review Letters*, 117(20):201101, 2016.
- [9] M. Milgrom. A modification of the Newtonian dynamics as a possible alternative to the hidden mass hypothesis. *The Astrophysical Journal*, 270:365-370, 1983.
- [10] Planck Collaboration. Planck 2018 results. VI. Cosmological parameters. *Astronomy & Astrophysics*, 641:A6, 2020.
- [11] E. Verlinde. Emergent Gravity and the Dark Universe. arXiv:1611.02269, 2016.
- [12] S. Weinberg. *Gravitation and cosmology: Principles and applications of the general theory of relativity*. Wiley, 1972.
- [13] W. Hu, R. Barkana, and A. Gruzinov. Fuzzy Cold Dark Matter: The Wave Properties of Ultralight Particles. *Physical Review Letters*, 85:1158, 2000.
- [14] L. Hui, J. P. Ostriker, S. Tremaine, and E. Witten. Ultralight scalars as cosmological dark matter. *Physical Review D*, 95:043541, 2017.
- [15] P. G. Ferreira. Cosmological tests of gravity. *Annual Review of Astronomy and Astrophysics*, 57:335-374, 2019.
- [16] J. D. Barrow. The Area of a Rough Black Hole. *Physics Letters B*, 808:135643, 2020.
- [17] E. N. Saridakis et al. Big Bang Nucleosynthesis constraints on Barrow entropy. *Physics Letters B*, 817:136292, 2021.
- [18] C. M. Will. The Confrontation between General Relativity and Experiment. *Living Reviews in Relativity*, 17:4, 2014.
- [19] A. A. Starobinsky. A New Type of Isotropic Cosmological Models Without Singularity. *Physics Letters B*, 91:99-102, 1980.