

### Problem Set I: Linear Regression

Suppose you have to quantify the causal effect of the number of children on the wage of married women. To this end, use the data set **mroz.dta** in STATA.

1. Start by estimating the simple linear regression

$$\log(wage) = \beta_0 + \beta_1 kidstotal + u,$$

where *kidstotal* is the total number of (non-adult) kids. Use heteroscedasticity consistent standard errors. (Note: you have to define this variable as the sum of *kidslt6* and *kidsge6*.)

- (a) What is the estimated effect of another child on the wage? Why is it preferable to have  $\log(wage)$  on the LHS instead of *wage*?
  - (b) Is the effect quantitatively relevant and statistically significant?
  - (c) Report a 90% confidence interval for  $\beta_1$ . Interpret.
  - (d) Is *kidstotal* an important driver of the female wage?
  - (e) Which model deficiencies may invalidate the interpretation of  $\beta_1$  as a causal effect?
2. Now augment the regression with the following control variables: *exper*, *exper*<sup>2</sup>, *educ*, and *age*. Re-estimate.
    - (a) Explain for each of the control variables why it makes sense to include it.
    - (b) What is the estimated effect of another child on the wage? What has changed? Why?
    - (c) Is the effect quantitatively relevant and statistically significant?
    - (d) Can you now interpret  $\beta_1$  as a causal effect?
  3. In the next step split *kidstotal* into *kidslt6* and *kidsge6* and estimate

$$\log(wage) = \beta_0 + \beta_1 kidslt6 + \beta_2 kidsge6 + \beta_3 exper + \beta_4 exper^2 + \beta_5 educ + \beta_6 age + u.$$

- (a) Explain why it may make sense to include *kidslt6* and *kidsge6* separately instead of just *kidstotal*.

- (b) What is the estimated effect of another (young or old) child on the wage?
- (c) Are the effects quantitatively relevant and statistically significant?
- (d) Perform an  $F$ -test of the hypothesis of joint significance for kidslt6 and kidsge6.
- (e) Perform an  $LM$ -test of the hypothesis of joint significance for kidslt6 and kidsge6.  
Here (and only here) assume the disturbances are homoscedastic.
- (f) Perform an  $F$ -test of the hypothesis that the age of the kids does not play a role,  
i.e.,  $\beta_1 = \beta_2$ .

4. (*For self study.*) Use the data in CORNWELL.dta (from Cornwell and Trumball, 1994) to estimate a model of county-level crime rates, using the year 1987 only.
  - (a) Using logarithms of all variables, estimate a model relating the crime rate (*crmrte*) to the deterrent variables probability of arrest (*prbarr*), probability of conviction (*prbconv*), probability of prison sentence (*prbpris*), and average sentence (*avgsen*, in days). Interpret the coefficients. Are the effects quantitatively relevant and statistically significant?
  - (b) Add  $\log(\text{crmrte})$  for 1986 as an additional explanatory variable, and comment on how estimates elasticities differ from part a.
  - (c) Add the various wage variables as regressors (in logs). Why could they be relevant? Compute the  $F$  statistic for joint significance of all the wage variables.
  - (d) Redo part c, but make the test robust to heteroscedasticity of unknown form.
5. (*For self study.*) Use the data in NLS80.dta (from Blackburn and Neumark, 1992). Assume the model

$$\begin{aligned}\log(\text{wage}) = & \beta_0 + \beta_1 \text{exper} + \beta_2 \text{tenure} + \beta_3 \text{married} + \beta_4 \text{south} + \dots \\ & \dots + \beta_5 \text{urban} + \beta_6 \text{black} + \beta_7 \text{educ} + \gamma \text{abil} + \nu.\end{aligned}$$

- (a) Use either *kww* or *iq* (two different test scores) as proxies for ability. Compare the estimated returns to education without a proxy for ability, with *kww* as proxy, with *iq* as proxy, and with both proxies. Interpret.
- (b) Include both *kww* and *iq* and test for joint significance.
- (c) Compare the equation without proxy for ability with the equation that includes both *kww* and *iq*. How does the estimated wage differential between nonblacks and blacks change? Try to explain.
- (d) Compute the new variables  $kww0 = kww - \overline{kww}$ , where  $\overline{kww}$  is the average *kww* score in the sample. Include *kww0*, *educ* and the interaction  $\text{educ} \times kww0$  as regressors. Calculate the partial effect of another year in school for people with  $kww = 20, 35, 50$ . Also calculate the partial effect predicted for each individual and display its distribution with the help of a histogram (Stata command `histogram >varname<`). Interpret your results.