

Question 5

a)

COUNT(x.key)

    y = x \\ y points to the tree

    while y is not null

        if y.key == x.key

            break

        else if y.key < x.key

            y = y.right

        else

            y = y.left

    y = y.right

    if y == null

        return

    else

        return y.size

\\ this should be  $O(\log n)$  same time as RB-Traverals

b) you would have to set  $x.size = \text{size.x.right} + \text{size.x.left} + 1$ ,  
after an insertion operation, this operation is  $O(1)$

LEFT-ROTATE(T, x)

    y = x.right

    x.right = y.left

    if y.left is not T.nil

        y.left.p = x

    y.p = x.p

    if x.p == T.nil

        T.root = y

    elseif x == x.p.left

        x.p.left = y

    else x.p.right = y

        y.left = x

        x.p = y

RB-INSERT(T, z.key)

    y = T.nil

    x = T.root

    while x is not T.nil

        y = x

        if z.key < x.key

            x = x.left

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        else
            x = x.right

z.p = y

if y == T.nil
    T.root = z

else
    y.right = z

z.left = T.nil
z.right = T.nil
z.color = RED
z.size += x.right.size + x.left.size + 1

RB-INSERT-FIXUP(T, z)
    while z.p.color == RED
        if z.p == z.p.p.left
            y = z.p.p.right

            if y.color == RED
                z.p.color = BLACK
                y.color = BLACK
                z.p.p.color = RED
                z = z.p.p
            else if z == z.p.p.right
                z = z.p
                LEFT-ROTATE(T, z)
                z.p.color = BLACK
                z.p.p.color = RED
                RIGHT-ROTATE(T, z.p.p)
        else
            z = z.p
            RIGHT-ROTATE(T, z)
            z.p.color = BLACK
            z.p.p.color = RED
            LEFT-ROTATE(T, z.p.p)

z.size += x.right.size + x.left.size + 1

T.root.color = BLACK

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