Homework 2

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October 6, 2021

Question 1

Part A

$$y_i \sim Pois(e^{\beta_{intercept} + \beta_{condition} x_{1i} + \beta_{sex} x_{2i} + \beta_{weight} x_{3i}})$$

$$Var(\mathbf{Y}) = \mu$$

```
# part a (Poisson model)
model1 = glm(c1 ~ cond + factor(sex) + wt1, family = poisson(link = 'log'), data = data)
summary1 = summary(model1)
summary1$coefficients
```

```
##                  Estimate Std. Error   z value     Pr(>|z|)
## (Intercept)     0.9979487  0.1987601  5.020869 5.143815e-07
## cond            0.8645418  0.1349809  6.404921 1.504474e-10
## factor(sex)1   -0.1988221  0.0822303 -2.417869 1.561169e-02
## wt1             0.1973105  0.1323242  1.491114 1.359317e-01
```

Using a poisson regression model, in the presence of sex and weight, the odds of being in the experimental increase 2.374 (1.822, 3.093) times over those with no special treatment.

Part B

$$y_i \sim Pois(e^{\beta_{intercept} + \beta_{condition} x_{1i} + \beta_{sex} x_{2i} + \beta_{weight} x_{3i}})$$

$$Var(\mathbf{Y}) = \phi\mu$$

```
# part b (Quasi-Poisson model)
model2 = glm(c1 ~ cond + factor(sex) + wt1, family=quasipoisson(link='log'), data=data)
summary2 = summary(model2)
summary2$coefficients
```

```
##                  Estimate Std. Error    t value     Pr(>|t|)
## (Intercept)     0.9979487  0.3410728  2.9259112 0.0042961192
## cond            0.8645418  0.2316274  3.7324672 0.0003229435
## factor(sex)1   -0.1988221  0.1411073 -1.4090131 0.1620961288
## wt1             0.1973105  0.2270686  0.8689464 0.3870664892
```

```
se1 = summary1$coefficients[2,2]
se1_by_dispersion = summary2$coefficients[2,2]/sqrt(summary2$dispersion)
```

Using a quasi-likelihood poisson regression model, in the presence of sex and weight, the odds of being in the experimental increase 2.374 (1.508, 3.738) times over those with no special treatment.

Part C

```
# part c (Random Normal Error Poisson model)
model3 = glmer(
  c1 ~ cond + factor(sex) + wt1 + (1 | fam_idno),
  family=poisson(link='log'),
  data=data
)
summary3 = summary(model3)
summary3$coefficients
```

```
##                 Estimate Std. Error    z value     Pr(>|z|)
## (Intercept)    0.8817447  0.3242098  2.7196732 0.0065346455
## cond           0.8551232  0.1970427  4.3397869 0.0000142621
## factor(sex)1 -0.1534800  0.1433302 -1.0708139 0.2842531194
## wt1            0.1637159  0.2361203  0.6933583 0.4880847452
```

$$y_i \sim Pois(e^{\beta_{intercept} + \beta_{condition} x_{1i} + \beta_{sex} x_{2i} + \beta_{weight} x_{3i} + \epsilon_i})$$

$$\epsilon_i \sim \mathcal{N}(0, \sigma^2)$$

Using a poisson regression model with random normal errors, in the presence of sex and weight, the odds of being in the experimental increase 2.374 (1.598, 3.46) times over those with no special treatment.

Part D

$$y_i \sim EF(\mu_i = log(\beta_{intercept} + \beta_{condition} x_{1i} + \beta_{sex} x_{2i} + \beta_{weight} x_{3i}), \phi)$$

```
##                  Estimate Std. Error    z value     Pr(>|z|)
## (Intercept)    1.10550725  0.3228816  3.4238780 6.173434e-04
## cond           0.85734373  0.1954837  4.3857545 1.155844e-05
## factor(sex)1 -0.17108413  0.1436796 -1.1907338 2.337581e-01
## wt1            0.09944037  0.2339898  0.4249773 6.708532e-01
```

Using a negative-binomial regression model, in the presence of sex and weight, the odds of being in the experimental increase 2.357 (1.607, 3.457) times over those with no special treatment.

Question 2

	Poisson Regression	Poisson QL	Poisson + Normal error	NB NLMIXED
Intercept	2.713	2.713	2.415	3.021
Condition	2.374 (1.822, 3.093)	2.374 (1.508, 3.738)	2.352 (1.598, 3.46)	2.357 (1.607, 3.457)
Sex	0.82 (0.698, 0.963)	0.82 (0.622, 1.081)	0.858 (0.648, 1.136)	0.843 (0.636, 1.117)
Weight	1.218 (0.94, 1.579)	1.218 (0.781, 1.901)	1.178 (0.742, 1.871)	1.105 (0.698, 1.747)
Other	NA	2.945	0.543	3.164

Table1. Table of results from the four comparison models, Poisson, Quasi-Poisson, Random Normal Error Poisson, and Negative-Binomial.

According to all our analyses (Poisson Regression, Quasi-Poisson Regression, Poisson Regression with Random Normal Error, and Negative Binomial Regression), the experimental group (cond=1) had much higher consumption. The Poisson and Quasi-Poisson Regression models both estimated that the experimental group was consuming 2.374 times as much cereal. The normal random error model estimated that the experimental group was consuming 2.352 times as much cereal, and the negative binomial model estimated that the experimental group was consuming 2.357 times as much cereal, compared to the control group.