ETH
Eidgenössische Technische Hochschule Zürich
Swiss Federal Institute of Technology Zurich

Lecture with Computer Exercises:
Modelling and Simulating Social Systems with MATLAB

Project Report

Evacuation Bottleneck
Simulating a Panic on a Cruise Ship

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Zurich
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Evacuation Bottleneck — Simulating a Panic on a Cruise Ship

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Contents

1 Abstract

This work takes a look into the evacuation mechanisms of a cruise ship in case of an emergency. A simple model is implemented which is used to simulate the dynamics of such a system. The main emphasis was on the limited capacity of the exits, since that is the key element for a rescue boat.

2 Individual Contributions

The work on this project was split among us to fit our strengths the best way possible. Because of his knowledge in image editing and formats, Johannes Weinbuch focused on the image manipulation for the input and implemented the loading of the image into MATLAB, improving the existing solutions from the previous courses. He further took a large part of the writing for the report and executing the simulations, which were written by Benedek Vartok. He evaluated which code from previous semesters could and should be reused, and implemented the missing parts for our special case. Also, he wrote the output mechanisms for the simulation, so that the data could be used for analysis.

3 Introduction and Motivations

In January 2012, the Costa Concordia hit a rock and ran aground[1]. This event got great media attention for a long time so we decided to take a closer look at the evacuation of a cruise ship. The question is, what is the best strategy to leave the ship? This question should for sure be answered with one of the emergency drills, but it is always good to have some background knowledge.

So, our key questions are: Which is the best strategy for evacuation concerning the choice of the way towards the rescue boats? Should all passengers distribute equally over the entries, or is there a better one? Also, which one takes longer: a high panic level on a nearly empty ship or a low panic level on a very full ship? What happens if a boat is suddenly inoperable? How can the reaction be optimized?

4 Description of the Model

The model is a big simplification of real life, otherwise it would be way too complex to simulate. It assumes that the ship is intact, that there is calm sea and that the passengers are obliged to leave the ship. A possible explanation for this could be a machine defect which leaks explosive gas in a badly ventilated room in the ship.

Further, we assume that the rescue boats are like doors which close after a certain amount of people going through them.

Since we also assume that the other doors, for example between the rooms or floors, are constantly open and working, we only simulate one deck, the one with the exits to the rescue boats. The evacuation of multiple floors in a static building has already been researched in [2].

After these simplifications, the task left to simulate was the evacuation of a single floor with some elements that can change. For this task, we chose a simple agent based modeling solution as described in [3]. A passenger is treated as a particle. It has a mass, and there are physical and social forces, accelerating that mass so that it cannot always follow its desired direction. The desired direction is implemented as the shortest path to the nearest exit. For the exact formulas for the forces see section 5.2.5.

The floor is given by a deck plan for the Costa Voyager [4]. Since these deck plans usually are made for advertisement purposes, it is to be expected that they are not absolutely accurate. So during image processing for simplification of this plan, a few further assumptions were made, mainly about the actual sizes and capacities. We won't list them all here, because they are also in the configuration files.

The last element of additional complexity was added to get an idea of how the closing of an exit works. A switch was added to decide whether every agent should know instantaneously about the closed exit or if the knowledge spreads over time. The technical aspect of this is further explained in section 5.2.6.

5 Implementation

5.1 Input

Since we had some good projects which covered similar problems as ours, we could get some ideas from them, but at the same time improve them. Namely, there are [2] and [5]. As far as the input for the simulation is concerned, we see two approaches in these works for getting the map data into the simulation. In [2], a simple PNG image is used to get a map into the simulation. The problem here is that only a certain RGB color value can be read out of the image. This can lead to problems if the image is processed with automatic or semiautomatic image manipulation programs, since only a minor difference in color can prevent the generation of the desired data. In [5], the image format is even more simple. There is only a bitmap image read into MATLAB. Since the bitmap images can use a color map, MATLAB doesn't use 3 channels but a unique number for each color in an image matrix to give every pixel its color. This has the same problem as the PNG solution regarding how exactly the

colors have to be set, but the different parts of the image can be separated with less code.

We took the best of both solutions. We used the PNG-format with indexed colors. So we have the most flexibility with very little usage of disk space. There is no special "wall color" or anything like that, just a simple rule on how the color map is read: Color 0 of the map specifies walls, color 1 free space. Then, there can be any number of spawn zones. Spawn zones are the areas in the image where new agents can be placed. With different spawn zones, it is possible to account for different situations: A ballroom is different from a staircase. The number of spawn zones is specified in the configuration file. At last, there is an arbitrary number of exits. Again, each exit can have its own parameters or can even be handled specially in the program's code.

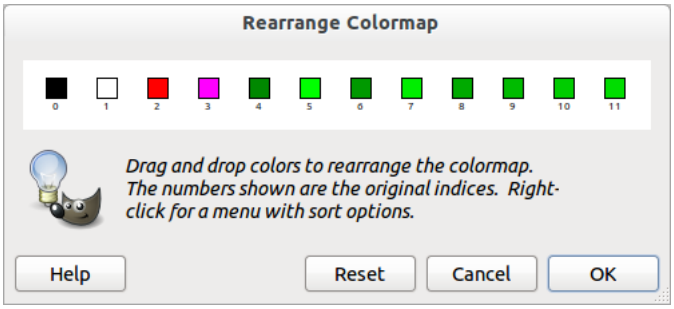

Figure 1: Screenshot of the Rearrange Colormap dialog in Gimp 2.6.11.

To manipulate the color map, any slightly sophisticated image manipulation program should suffice. We used the free software Gimp [6]. It has a very convenient command which allows the user to rearrange the color map. This is shown in figure 1.

5.2 The Simulation Routines

5.2.1 Code Reuse from Multilevel Evacuation

Since this project has very similar foundations as [2] (like the forces used in the model), we were able to use a lot of code and some design decisions from their program. Some of the structure needed to be changed to implement our custom features, but for example the utility functions for the Fast Sweeping algorithm (`fastSweeping.c`), generating gradients (`getNormalizedGradient.c`) and the linear interpolation (`lerp2.c`) which the other group wrote in C were copied without modification into our code-tree.

5.2.2 General Structure

During the entire program run, one single big structure is used to hold and pass around the state of the simulation.

At first, this structure is initialized with the fields that are given in the configuration file by `loadConfig`[1]. Then, `initialize` runs over the struct and calculates some data needed in the simulation, such as the vector fields needed for the wall and exit force fields using the `fastSweeping` method which we got from [2].

5.2.3 Main Loop

`simulate` is the routine we call when we do an entire simulation. It uses the `loadConfig` and `initialize` functions to initialize its runtime data, then it does the loop calculating forces, adding new agents, progressing the agents, updating the exit vector fields, potentially plotting and saving frames and collecting data.

These steps will be explained in detail in the following sections.

5.2.4 Agent Placement

As mentioned in section 5.1, our model of the ship has different spawning zones where new agents can start out at. The way we implemented it, in every step of the simulation loop it is checked whether there are any remaining agents that need to be placed (i.e. agents which are not in the simulation yet). If there are, then for every agent the program chooses a random point in the spawning zones and places him there, unless it detects that the agent would collide either with walls or other agents. In that case, the routine tries the placement for that agent up to five times, each time with a new random position. If the agent couldn't be placed, then he will have a chance to spawn in the next time step.

This method was implemented in `placeAgents`. In the same method, the basic properties of the agent get assigned, like the starting zero velocity and a random radius.

5.2.5 Agent Dynamics

To simulate the movement of the agents in this physical model, different forces need to be calculated in every step on every agent. All of the force formulas have been taken from [3]. These forces have been separated into the following functions which are called by `simulate`:

[1] The MATLAB implementation of our functions is in the `code` directory: `loadConfig` can be found in the file `code/loadConfig.m` etc.

`addDesiredForces` is responsible for making the agents seek the exits of the layout, in our case the rescue boats.

This is accomplished by giving an agent a "desired" velocity vector pointing along the shortest path to the nearest exit. The vector is sampled and interpolated (using `lerp2` from [2]) from a vector field which is calculated at the beginning of the simulation (see 5.2.2) and when the exits change (see 5.2.6).

Using this desired vector $\vec{e}$ we can say what force addition the agent gets:

$$\vec{F}_{\text{desired}} = m\frac{v_0\vec{e} - \vec{v}}{\tau}$$

where m is the agent's mass, v_0 is his target speed, $\vec{v}$ is his current velocity vector and τ is a characteristic time determining how fast the desired velocity should be reached.

`addInterAgentForces` models the repulsive forces between agents: They do not want to get too close together and if they touch, they have to be kept apart physically and some friction appears. The model we use has this formula:

$$\vec{F}_{\text{agents}} = \big(Ae^{(r-d)/B} + k\max\{0, r-d\}\big)\vec{n} + \kappa\max\{0, r-d\}\Delta\vec{v}\cdot\vec{t}$$

where r is the sum of radii of both agents, d is the distance between the center points of the agents, $\vec{n}$ is the normalized vector between the two agents, $\vec{t}$ is the tangential vector and $\Delta\vec{v}$ is the velocity difference vector. A influences the magnitude of the "social" repulsive force, B specifies a factor for the range of influence for this force, k gives the strength of the physical separation force and κ is a friction coefficient.

For finding possible agent pairs to calculate the function on we used the naive approach of checking every possible pairing with two nested loops and then using a cutoff distance to avoid calculating this complicated force expression when it's too small to matter anyways. This method has complexity $O(N^2_{\text{agents}})$ which is far from optimal; we also tested the Range Tree implementation of [2] for our program, however benchmarks didn't show a noticeable gain in efficiency.

`addWallForces` calculates agents avoiding and experiencing resistance from walls. Just like agent-agent repulsion, this force has a "social", a physical and a frictional component:

$$\vec{F}_{\text{walls}} = \big(Ae^{(r-d)/B} + k\max\{0, r-d\}\big)\vec{n} - \kappa\max\{0, r-d\}(\vec{v}\cdot\vec{t})\vec{t}$$

where r is the radius of the agent, d is his distance from the wall, $\vec{n}$ is the wall normal vector, $\vec{t}$ is the wall tangent vector and $\vec{v}$ is the agent's velocity vector. The coefficients are the same as in F_{agents}.

Accessing the wall distances and normals is done similarly to `addDesiredForces`, with precalculated fields using the Fast Sweeping method.

`progressAgents` applies the forces from the above listed functions, using them to update the agents' positions and velocities for the next simulation step.

To accomplish this, the leap-frog integration scheme was used. In every step, the following recalculations of the velocities and positions of the agents take place:

$$\vec{v} = \vec{v} + \Delta t \cdot \frac{\vec{F}}{m}$$
$$\vec{x} = \vec{x} + \Delta t \cdot \vec{v}$$

This method is fairly well suited for physical simulations with forces such as these. However, extra measures were taken to improve the stability of our program: Before doing any further calculations with them, the velocities and forces get clipped to a configurable maximum magnitude to avoid instabilities for too high step-sizes or too strong force parameters.

Without this, the simulation of some agents might get out of control if they get too close to walls or to other agents and behave in unphysical ways.

This function also checks whether some agents have entered a non-full exit zone (a rescue boat) and if the exit got full from them, it closes that one. What exactly happens then is explained in the next section.

5.2.6 Removing Filled Exits

In our model we have several exit zones, each with a maximum capacity (since they are rescue boats with limited size). Because of that the simulation needs to take it into account when one of them gets filled: It needs to remove the exit and update the vector fields for the desired velocities which the agents use to find the nearest exit. For this update we modeled and implemented two different approaches which can be chosen in the configuration file.

The first one simply recalculates the entire vector field when an exit is closed with the Fast Sweeping method, just like in the initialization, but with the full exits removed. The update is instantaneous, so every agent on the entire ship reacts to

it immediately. This can be unrealistic under certain conditions, which is why we came up with the second method.

Instead of updating the entire vector field right away, we can just calculate the updated field and use that to update growing regions. To be exact, when an exit closes, a circle starts growing around at a configurable rate, and in this area the new destination vector field is used. That way, at first only agents close to that exit react to the change, then over time the more distant agents also "notice" the filled exit and go for a different one.

The circle-shaped destination field update is implemented in `progressDestFields`.

5.3 Output and Plotting

Our program has two plotting functions:

`plotFloor` draws the ship's layout and all the agents on it in the current simulation state. It is called from `simulate` in every loop iteration and the resulting picture is saved to `code/frames/`, but only if the option for saving frames has been enabled in the configuration file.

`plotExitedAgents` is called at the end of the simulation and creates time series plots of the rescue boat occupations.

Also the program saves its entire state data object to a file in `code/frames/` at the end, which includes other information as well, such as the time needed for all agents to reach the exits and the time series of the total escaped agents.

6 Simulation Results and Discussion

6.1 Passenger Distribution

If we plot the exited agents over a time axis for each exit, we can see that the boats tend to be filled in a sequential way (see figure 2 and 3). This means that a new boat mostly gets frequented if the old boat is already full. This effect is very strong and good to see if we have only few passengers, but also if there are many, a tendency towards this can be observed. The only thing that interferes with this observation is that at the beginning, two boats are filled at the same time. This is because some agents are placed so that they have a shorter distance to the left.

Although there could be numerous reasons for this to happen, in reality a more distributed and parallel filling of the boats is expected. The simulation is based on a model which takes the distance to the nearest exit as the indicator for the desired direction. In reality, people want to get out of the ship the fastest way possible, especially if there are only limited capacities on the boats. This suggests that the nearest exit is not the best strategy to get out fast. On the specific geometry of

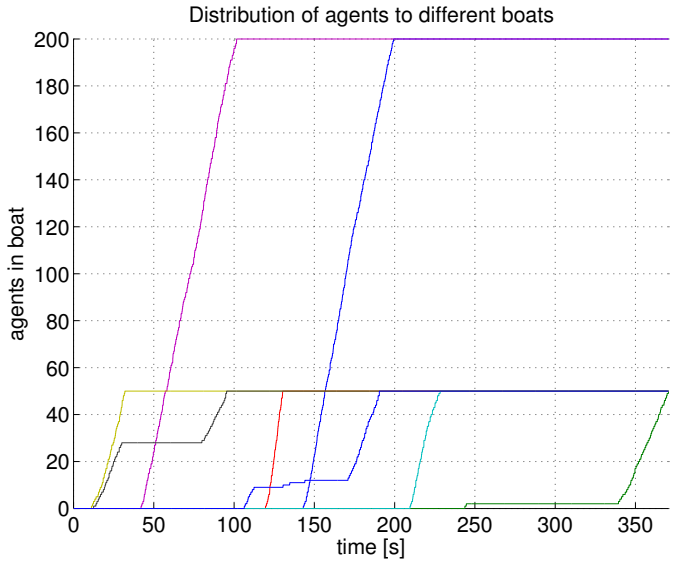

Figure 2: Plot of the filling of the rescue boats on a ship with 700 agents, $v_0 = 1.5\frac{m}{s}$. Each line represents a different rescue boat.

the Costa Concordia, the corridor from bow to stern ends more on the starboard (right) side. The agents follow the shortest path and start to jam up, while on the left there are no obstacles. Without regard to the beginning, two boats get used in parallel only if there are many agents. This can be explained by the jam, so people get pushed back towards the other boat. Also, if a boat is empty, the crowd can separate into two parts: One that is nearer to the next boat on the same side and one which is farther away from the empty boat, which now has the nearest boat on the other side.

The expectation for reality is that people would recognize that the nearest boats take more time to reach than the ones farther away. Thus, they would distribute more equally over the different boats.

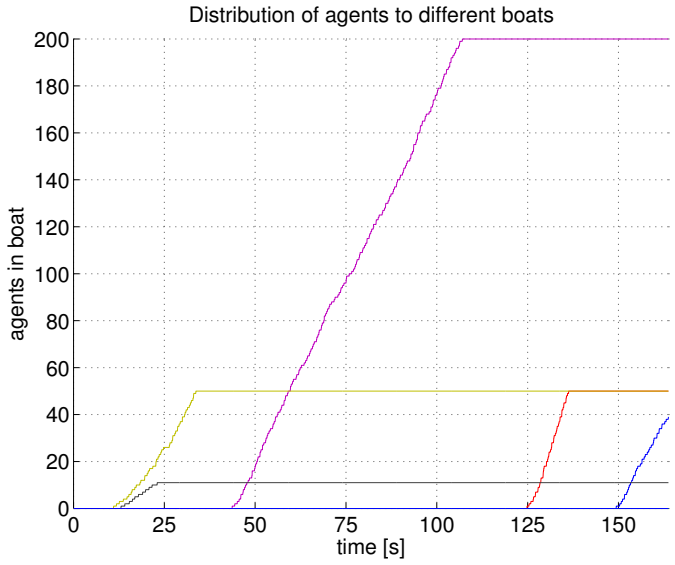

Figure 3: Plot of the filling of the rescue boats on a ship with 350 agents, $v_0 = 1.5\frac{m}{s}$. Each line represents a different rescue boat.

6.2 Panic Level

As described in [3], a greater desired velocity v_0 can lead to longer evacuation times. At a higher panic level, people want to go faster, but it can take longer to get out. When v_0 is below $1.5\frac{m}{s}$, we could reproduce the results of decreasing evacuation times both with many and few agents, as seen in figures 4 and 5.

However, with higher values for v_0, we could not reproduce the results, because agents got pushed into walls and remained stuck there. In figure 4, we had two agents stuck in walls at $v_0 = 1.4\frac{m}{s}$, so we looked at the results and set the finish time to the value when the last agent before them left the ship. This introduces an error which only gets bigger with higher values of v_0.

To circumvent this, a simulation with a smaller time step was run, but even with the timestep being a millisecond, we still got agents stuck in walls. An example is shown in figure 6. This is a part during the simulation with $v_0 = 3.8\frac{m}{s}$ and a timestep of a millisecond.

A timestep of a millisecond means that an agent, moving at five meters per second goes a distance of 5 millimeters per timestep. Since the agents get pushed into walls at these rather precise steps of movement, an even smaller timestep will likely yield similar results.

Because of this, we cannot answer our question whether a high panic level (which

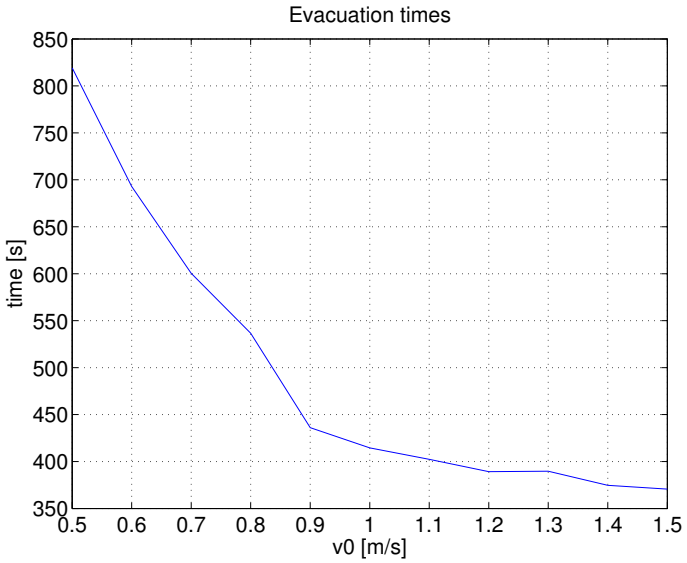

Figure 4: Evacuation times with 700 agents and varying v_0.

means a high value for v_0) with few people or a low panic level with many people is faster, since on high panic levels there are too many agents stuck, as seen in figure 7. Instead, we try to find reasons for this outcome.

A timestep which is too big can be excluded from the reasons, as we have seen before. We chose the parameters to be the same as in [3] on page 488. They have been found suitable to simulate people leaving a room. The difference to our case is that we have more walls nearby and because of that, we get a situation where more pressure is applied from more sides. Since that is a remarkable difference to the situation of a single room with one door, it is plausible that the parameters are not suited for high densities of people in narrow places.

Of course, this could also be interpreted as people being hurt, but since we did not take this into account for our model, no relevant statements can be made. It should be part of a next simulation to account for the sum of physical forces acting upon an agent. If they are too big, the agent gets hurt. In our case, this would be a realistic assumption, since a ship with limited exit possibilities can make the people feel trapped rather fast and is so more likely to trigger panics than other places.

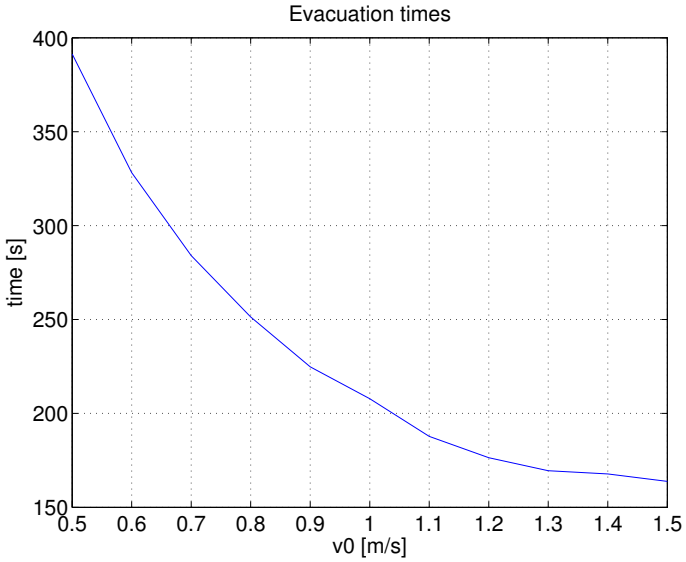

Figure 5: Evacuation times with 350 agents and varying v_0.

Figure 6: Agents stuck in walls due to too high v_0. Image was taken with $v_0 = 3.8\frac{m}{s}$ and a timestep of a millisecond.

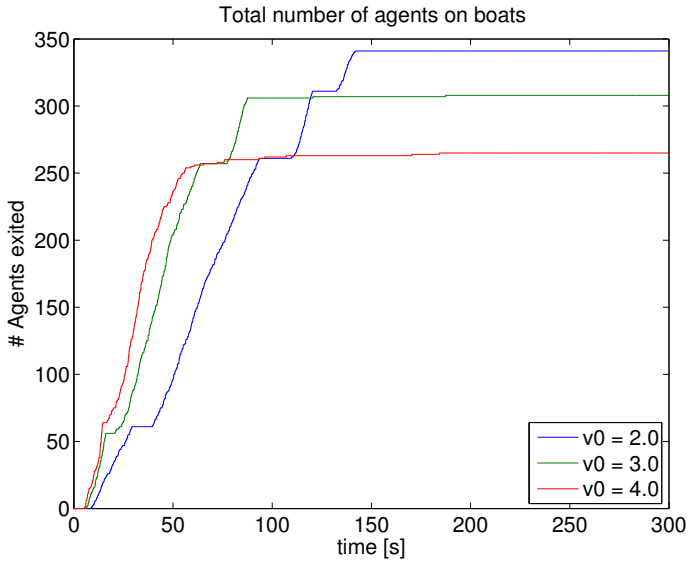

Figure 7: At high values for v_0, not all 350 agents exit. The rest is stuck in walls.

6.3 Closed Exits

In the simulation, two ways were defined to react to a full boat, as described in Section 5.2.6. First, there is an instantaneous update on the whole ship. This is a model for an announcement over speakers over the whole ship. The agents adapt their direction immediately, which can be seen on a video of the simulation. This behavior is realistic in a case when the following conditions are met: There are not too many people and they aren't panicking.

The second way is that the information is spread in a circle around the exit. This is supposed to model simple communication between agents that takes time. With this simple rule of updating the directions, the behavior is much more realistic, even though the rule doesn't account for the number of people nearby. This means that the information spreads even if there is nobody there. However, an interesting phenomenon during the updates can be observed: While the people near the exit try to get to the next one, they get pushed back by the others who don't know of the change yet.

The flaw of this is that a slow expansion rate leads to more pushing, but if it's too slow, even an agent that escaped can be run against the border of the expansion circle. This is then seen as the agent stopping, even if there is nothing blocking his path. That happens because the agent is faster than the expansion rate of the information. From observations in the simulation, we found $0.5\frac{m}{s}$ to look mostly as we expected, even though occasionally there are still some agents slowed down by the expansion rate. On the other hand, if the expansion rate is chosen too high, the pushing effect is too small to meet the expected result of a panicking crowd.

However, the effect of the push-back on the evacuation time is clearly visible in figures 8 and 9. In figure 8, it was again necessary to correct the evacuation times because of agents in walls as described in 6.2. Two agents were stuck at the run $v0 = 1.4\frac{m}{s}$ with radial propagation. In the runs with instantaneous propagation, one agent was stuck for $1.3\frac{m}{s}$, two for $1.4\frac{m}{s}$ and two for $1.5\frac{m}{s}$.

Agents that are informed instantaneously can adapt their way earlier and reduce the overall evacuation time. This expected result can be seen in both figures. The effect is smaller for less people. This fact is also expectable, because the space remains the same. If we have many people on the same amount of space going in different directions, they have to be slower to avoid collisions.

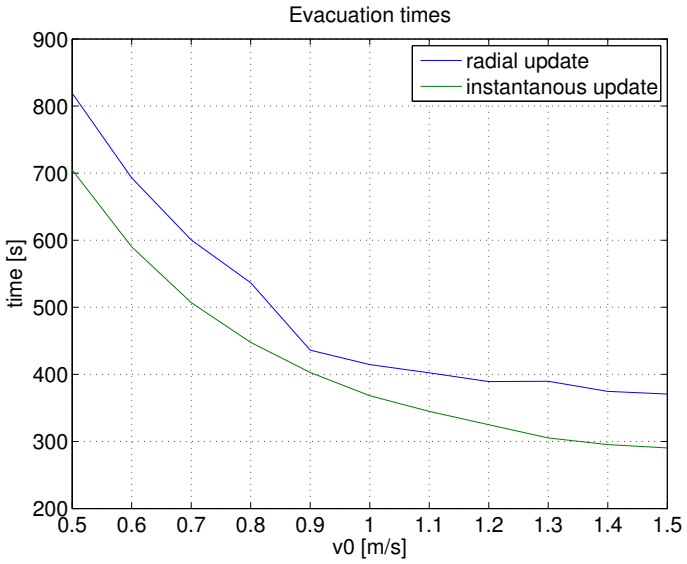

Figure 8: Comparison of evacuation times with 700 agents and varying v_0 with instantaneous or radial update.

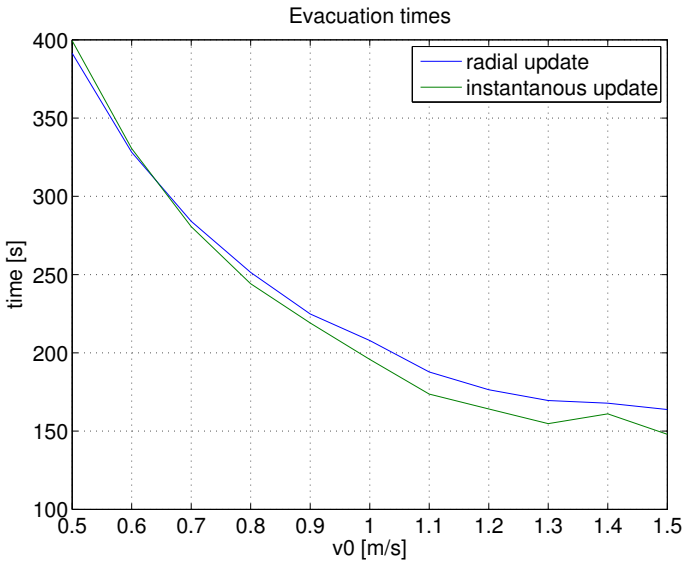

Figure 9: Comparison of evacuation times with 350 agents and varying v_0 with instantaneous or radial update.

7 Summary and Outlook

Even though we could not answer all our questions, we got some new knowledge that is needed to answer them. We found out that the agents should not choose their direction by the shortest way to the next exit but by the fastest expected exit time, which can mean to go a longer distance.

Regarding the panic level, we could not reproduce the "faster-is-slower effect"[2] for higher panic levels. We mentioned possible reasons for this in section 6.2 and mentioned the idea of taking hurt people into account.

When an exit closed, we managed to get a realistic model with a very simple update rule. We also discussed the weaknesses and limitations of this rule.

All in all, we have laid out a base for simulating the evacuation of any place that has exits with limited capacities, as for example a cruise ship. We mentioned some points to take care of, so that people interested in doing simulations like this can avoid some problems. To give a visual impression, we have made a video, which we put in the videos directory or on vimeo [7], where others may follow.

[2] [3], p. 488, caption of figure 1

8 References

[1] http://www.bbc.co.uk/news/world-europe-16563562, 9.12.2012

[2] *Modelling Situations of Evacuation in a Multi-level Building*, Hans Hardmeier, Andrin Jenal, Beat Küng, Felix Thaler, Zurich, April 2012

[3] *Simulating dynamical features of escape panic*, Dirk Helbing, Illés Farkas, Tamás Vicsek, Nature, 28. September 2000

[4] http://www.kreuzfahrtberater.de/deckplan.php?schiff=Costa+Voyager&bf&dpe=2

[5] *Pedestrian Dynamics Airplane Evacuation Simulation*, Philipp Heer, Lukas Bhler, Zurich, May 2011

[6] http://www.gimp.org/, 9.12.2012

[7] https://vimeo.com/55640942, 14.12.2012

9 Appendix

9.1 MATLAB Code

```
function data = addDesiredForces(data)
% Calculates the forces for agents looking for the exits.

for ai = 1:length(data.agents);
    % Use shorter variable names:
    p  = data.agents(ai).p / data.meter_per_pixel;
    v  = data.agents(ai).v;
    v0 = data.agents(ai).v0;

    % Calculate desired vector:
    e = [lerp2(data.floor.dir_y, p(2), p(1)), ...
         lerp2(data.floor.dir_x, p(2), p(1))];

    % Add force:
    data.agents(ai).f = data.agents(ai).f + data.m * (v0 * e - v) /
        data.tau;
end

end
```

Listing 1: addDesiredForces.m

```
function data = addInterAgentForces(data)
% Calculates the repulsive forces between agents.

n = length(data.agents);
if n == 0; return; end

for ai = 1:n  % agent index
    p_i = data.agents(ai).p;
    v_i = data.agents(ai).v;

    % Get indices of all near agents:
    rmax = data.r_influence;
    for aj = ai+1:n  % other agent index
            p_j = data.agents(aj).p;
            v_j = data.agents(aj).v;

            r = data.agents(ai).r + data.agents(aj).r;

            % Calculate different vectors between agent-agent pair:
            dPos = p_i - p_j;
            d = norm(dPos);

            % Distance cutoff:
            if d > rmax; continue; end
```

```
            normal = dPos / d;
            tangent = [-normal(2), normal(1)];

            dVel = dot(v_j - v_i, tangent);

            % Calculate force for one agent-agent pair:
            F = ...
                (data.A * exp((r-d)/data.B) + data.k * max(0, r-d)) *
                    normal + ...
                data.kappa * max(0, r-d) * dVel * tangent;

            data.agents(ai).f = data.agents(ai).f + F;
            data.agents(aj).f = data.agents(aj).f - F;
    end
end
```

Listing 2: addInterAgentForces.m

```
function data = addWallForces(data)
% Calculates the forces of walls acting on the agents.

for ai = 1:length(data.agents)
    % Use shorter variable names:
    p = data.agents(ai).p / data.meter_per_pixel;
    v = data.agents(ai).v;
    r = data.agents(ai).r;

    % Calculate wall normal vector:
    ny = lerp2(data.floor.wall_dist_grad_x, p(2), p(1));
    nx = lerp2(data.floor.wall_dist_grad_y, p(2), p(1));
    normal = [nx ny];

    % Calculate wall tangent vector:
    tangent = [-ny nx];

    % Calculate wall distance:
    d = lerp2(data.floor.wall_dist, p(2), p(1));

    % Add force:
    data.agents(ai).f = data.agents(ai).f + ...
             (data.A * exp((r-d)/data.B) + data.k * max(0, r-d)) * normal
                 - ...
             data.kappa * max(0, r-d) * dot(v, tangent) * tangent;
end

end
```

Listing 3: addWallForces.m

```
function val = checkForIntersection(data, agent_idx)
% Check an agent for an intersection with another agent or a wall.
% the check is kept as simple as possible
%
%  arguments:
%   data            global data structure
%   agent_idx       which agent on that floor
%
%  return:
%   0               for no intersection
%   1               has an intersection with wall
%   2                                  with another agent

val = 0;

p = data.agents(agent_idx).p;
r = data.agents(agent_idx).r;

% Check for agent intersection:
for i = 1:length(data.agents)
    if i ~= agent_idx
        if norm(data.agents(i).p - p) ...
           <= r + data.agents(i).r
            val=2;
            return;
        end
    end
end

% Vheck for wall intersection:
if lerp2(data.floor.wall_dist, p(2), p(1)) < r
    val = 1;
end
```

Listing 4: checkForIntersection.m

```
function data = createExitFields(data)
% Calculates the desired vector fields for the agents to find the exits,
% only including non-full exits.
% Fields are placed in data.floor.dir_new_{x,y}.

boundary_data = zeros(size(data.floor.wall));
boundary_data(data.floor.wall) = 1;

for i = 1:length(data.floor.exits)
    % Check if exit has been filled:
    if data.exit_capacities(i) > 0
        boundary_data(data.floor.exits{i}) = -1;
    end
end
```

```
15
exit_dist = fastSweeping(boundary_data) * data.meter_per_pixel;
17 [data.floor.dir_new_x, data.floor.dir_new_y] = ...
    getNormalizedGradient(boundary_data, -exit_dist);
19
end
```

Listing 5: createExitFields.m

```
function data = initAgents(config, data)
2
% The properties of the agents are stored in a struct.
4 data.agents = [];
```

Listing 6: initAgents.m

```
function data = initialize(config)
2
data = config;
4


6 % Seed random number generator:
rng(data.rseed);
8
% Initialize agents:
10 data = initAgents(config, data);

12 % Calculate wall force fields:
boundary_data = zeros(size(data.floor.wall));
14 boundary_data(data.floor.wall) = -1;
data.floor.wall_dist = fastSweeping(boundary_data) * data.meter_per_pixel;
16 [data.floor.wall_dist_grad_x, data.floor.wall_dist_grad_y] = ...
    getNormalizedGradient(boundary_data, data.floor.wall_dist -
        data.meter_per_pixel);
18
% Calculate exit force fields:
20 data = createExitFields(data);
data.floor.dir_x = data.floor.dir_new_x;
22 data.floor.dir_y = data.floor.dir_new_y;

24 % Calculate middle points of exits in pixels and
% initialize destination field update progresses:
26 for ei = 1:length(data.floor.exits)
    [rs cs] = find(data.floor.exits{ei});
28     n = length(rs);
    data.floor.exit_midpoints{ei} = [sum(rs) sum(cs)] / n;
30
    data.floor.dfieldupdate_cur_radii(ei) = 0;
32 end
data.floor.dfieldupdate_full_exits = [];
```

```
data.floor.dfieldupdate_dir_x = [];
data.floor.dfieldupdate_dir_y = [];

% Maximum distance for influence of agents on each other:
data.r_influence = ...
    fzero(@(r) data.A * exp((2*data.r_max-r)/data.B) - 1e-4, data.r_max);

% Initialize exit statistics:
data.agents_exited = zeros(1, data.num_exits);
data.agents_exited_time_series = [];
```

Listing 7: initialize.m

```
function config = loadConfig(config_file)
% Populate config struct from given config file.
%
% Arguments:
%   config_file     string, path to configuration file to load
%


% Get the path from the config file to read images from same directory:
config_path = fileparts(config_file);
if strcmp(config_path, '') == 1
    config_path = '.';
end

fid = fopen(config_file);
input = textscan(fid, '%s=%s', 'CommentStyle','%');
fclose(fid);

keynames = input{1};
values = input{2};

% Convert numerical values from string to double:
v = str2double(values);
idx = ~isnan(v);
values(idx) = num2cell(v(idx));

config = cell2struct(values, keynames);


% Read the image describing the floor layout:
% Building structure:
file = config.floor_build;
file_name = [config_path '/' file];
img_build = imread(file_name);
    [x,y] = size(img_build); %Get dimensions

config.floor.img_build = img_build;
```

```
39
% Decode images:
41 % Walls, Colormapped to 0
config.floor.wall = img_build==0;
43
%Spawn Zones, Colormapped from 2..num_spawn_zones+1
45 for j=2:config.num_spawn_zones+1
    currentIndex = j-1; %Shift Index to start from 1
47
    config.floor.spawn_zones{currentIndex} = img_build==j;
49
    % Get each spawn count into an array:
51  config.spawn_counts(currentIndex) = config.(sprintf('spawn_count_%d',
        currentIndex));
end
53
% Exits, The remaining part of the colormap
55 for j=config.num_spawn_zones+2:config.num_spawn_zones+2+config.num_exits-1
    currentIndex = j-config.num_spawn_zones-1; % Index Shifting
57
    config.floor.exits{currentIndex} = img_build==j; %Same as above, Not
        sure...
59  config.exit_capacities(currentIndex) =
        config.(sprintf('exit_capacity_%d', currentIndex));
end
```

Listing 8: loadConfig.m

```
function data = placeAgents(data)
2 % Try to place remaining agents in all spawning zones.

4 % Calculate a random agent radius:
function r = getRadius()
6     r = data.r_min + (data.r_max-data.r_min)*rand(1);
end
8

10 % Get number of agents existing so far:
numAgents = length(data.agents);
12
% Iterate through each of the spawn zones:
14 for si = 1:data.num_spawn_zones
    % Get pixel coordinates for spawning spots:
16  [ySpots,xSpots] = find(data.floor.spawn_zones{si}==1);
    % Convert to meters:
18  xSpots = xSpots * data.meter_per_pixel;
    ySpots = ySpots * data.meter_per_pixel;
20
    % Try to place remaining number of agents for this spawn zone:
```

```
22      curSpawnCount = data.spawn_counts(si);
        for j = 1:curSpawnCount
24          ai = numAgents + 1;  % new agent index

26          data.agents(ai).r = getRadius();
            data.agents(ai).v0 = data.v0;
28          data.agents(ai).v = [0 0];  % velocity
            data.agents(ai).f = [0 0];  % force
30
            % Try to find an empty spot:
32          tries = 5;
            while tries > 0
34              % Randomly pick a spot and check if it's free:
                idx = randi(length(xSpots));
36              data.agents(ai).p = [xSpots(idx), ySpots(idx)];

38              % Check for agent intersections:
            if checkForIntersection(data, ai) == 0
40            tries = -1;  % leave the loop
                end
42
                % Agent was intersecting; try again or give up.
44              tries = tries - 1;
            end
46
            if tries > -1
48              % If placement failed, remove the new agent
                data.agents = data.agents(1:end-1);
50          else
                numAgents = numAgents + 1;
52              % Decrease spawn count for this zone:
                data.spawn_counts(si) = data.spawn_counts(si) - 1;
54          end
        end
56  end

58  end
```

Listing 9: placeAgents.m

```
    function data = plotExitedAgents(config, data)
2   % Plots the time series of the exit occupations.

4   % Plot separate exits:
    for i = 1 : data.num_exits
6   %     subplot(data.num_exits, 1, i);
        figure;
8       axis([0 data.finish_time 0 config.exit_capacities(i)]);
        plot(data.agents_exited_time_series(:,1), ...
10           data.agents_exited_time_series(:,1+i));
```

```
    xlabel('time [s]');
    ylabel('# agents');
    title(sprintf('Agents on boat %i', i));
    print('-depsc2', sprintf('frames/%s_exit_occupation_%d.eps', ...
                              data.frame_basename, i));
end

% Plot totals:
figure;
axis([0 data.finish_time 0 config.exit_capacities(i)]);
plot(data.agents_exited_time_series(:,1), ...
     sum(data.agents_exited_time_series(:,2:data.num_exits+1), 2));
xlabel('time [s]');
ylabel('# agents');
title('Total number of agents on boats');
print('-depsc2', sprintf('frames/%s_exit_occupation_total.eps', ...
                          data.frame_basename));


end
```

Listing 10: plotExitedAgents.m

```
function plotFloor(data)
% Draws the floor layout with the agents.

hold off;
imagesc(data.floor.wall);
colormap([1 1 1; 0 0 0]);
axis equal;
axis off;
hold on;

% Prepare circle data for drawing:
t = linspace(0, 2*pi, 16);
x = cos(t);
y = sin(t);

for ai = 1:length(data.agents)
    % Draw an agent as a circle with his middle point and radius:
    x0 = data.agents(ai).p(1);
    y0 = data.agents(ai).p(2);
    r  = data.agents(ai).r;
    line((r * x + x0) / data.meter_per_pixel, ...
         (r * y + y0) / data.meter_per_pixel);
end

drawnow;

end
```

Listing 11: plotFloor.m

```
function data = progressAgents(data)
% Move agents by applying the forces calculated so far and check for
% exiting agents.

% Shorter constant name for convenience:
mpp = data.meter_per_pixel;

% Store which agents have reached which exit (index of array is agent
% index, value is exit index):
exited = false(length(data.agents), 1);

% Store floor size:
floorW = size(data.floor.img_build, 2) * mpp;
floorH = size(data.floor.img_build, 1) * mpp;

% Progress agents with Leap-Frog integration:
for ai = 1:length(data.agents)
    % Clip force:
    afn = norm(data.agents(ai).f);
    if(afn > data.f_max)
        data.agents(ai).f = data.f_max * data.agents(ai).f / afn;
    end

    % Calculate new velocity:
    newvel = data.agents(ai).v + data.dt * data.agents(ai).f / ...
                                 data.m;

    % Clip velocity:
    avn = norm(newvel);
    if(avn > data.v_max)
        newvel = data.v_max * newvel / avn;
    end

    % Calculate new position:
    oldpos = data.agents(ai).p;
    newpos = oldpos + data.dt * newvel;
    % Restrict position to floor:
    if any(isnan(newpos)); newpos    = [0,0];  end
    if newpos(1) < mpp;    newpos(1) = mpp;    end
    if newpos(2) < mpp;    newpos(2) = mpp;    end
    if newpos(1) > floorW; newpos(1) = floorW; end
    if newpos(2) > floorH; newpos(2) = floorH; end

    % Apply new state:
    data.agents(ai).v = newvel;
    data.agents(ai).p = newpos;
```

```
    % Reset force:
    data.agents(ai).f = [0 0];

    % Check for exiting:
    for ei = 1:length(data.floor.exits)
        if data.exit_capacities(ei) > 0 && ...
           data.floor.exits{ei}(round(newpos(2) / mpp), ...
                                round(newpos(1) / mpp))
            exited(ai) = true;
            data.exit_capacities(ei) = data.exit_capacities(ei) - 1;
            data.agents_exited(ei) = data.agents_exited(ei) + 1;

            % Update exits and desired vector fields:
            if data.exit_capacities(ei) == 0
                data = createExitFields(data);

                if data.dfieldupdate_enable
                    % Add current exit to list of filled ones:
                    numFull = length(data.floor.dfieldupdate_full_exits) +
                        1;
                    data.floor.dfieldupdate_full_exits(numFull) = ei;
                    data.floor.dfieldupdate_dir_x{numFull} = ...
                         data.floor.dir_new_x;
                    data.floor.dfieldupdate_dir_y{numFull} = ...
                         data.floor.dir_new_y;
                else
                    % If fancy circular updating is disabled, update the
                    % entire field immediately:
                    data.floor.dir_x = data.floor.dir_new_x;
                    data.floor.dir_y = data.floor.dir_new_y;
                end
            end
            break;
        end
    end
end

% Remove exited agents:
data.agents = data.agents(~exited);

end
```

Listing 12: progressAgents.m

```
function data = progressDestFields(data)
% Updates the destination vector fields in radially growing shapes from
% closed exits (only when data.dfieldupdate_enable is set).

if ~data.dfieldupdate_enable; return; end
```

```
% Get size of layout in pixels:
floorSize = size(data.floor.img_build);

for fei = 1:length(data.floor.dfieldupdate_full_exits)
    ei = data.floor.dfieldupdate_full_exits(fei);
    curRadius = data.floor.dfieldupdate_cur_radii(ei);
    if data.exit_capacities(ei) == 0 && curRadius < max(floorSize)
        % Grow circle (all units in pixels):
        newRadius = curRadius + ...
            data.dt * data.dfieldupdate_speed / data.meter_per_pixel;

        data.floor.dfieldupdate_cur_radii(ei) = newRadius;

        % Generate a corresponding circular mask:
        [rs cs] = meshgrid(1:floorSize(1), 1:floorSize(2));
        r0 = data.floor.exit_midpoints{ei}(1);
        c0 = data.floor.exit_midpoints{ei}(2);
        circleMask = ((rs - r0).^2 + (cs - c0).^2 <= newRadius^2)';

        % Update fields:
        data.floor.dir_x(circleMask) =
            data.floor.dfieldupdate_dir_x{fei}(circleMask);
        data.floor.dir_y(circleMask) =
            data.floor.dfieldupdate_dir_y{fei}(circleMask);
    end
end

end
```

Listing 13: progressDestFields.m

```
function simulate(configFile)

% Initialize the environment from config file:
if nargin == 1
    config = loadConfig(configFile);
else
    config = loadConfig('../data/democonfig.conf');
end
data = initialize(config);

% Simulation loop:
time = 0;
it = 0;
% Termination criteria:  The program stops if there are no more agents or
% exits left, but it runs for at least two seconds in any case.
while (length(data.agents) > 0 && sum(data.exit_capacities) > 0 &&
    time<data.duration) || time < 2
    % Possibly spawn new agents:
    data = placeAgents(data);
```

```
19
    % Update desired vector fields:
21  data = progressDestFields(data);

23  % Calculate forces:
    data = addDesiredForces(data);
25  data = addInterAgentForces(data);
    data = addWallForces(data);
27
    % Progress agents:
29  data = progressAgents(data);

31  % Draw floor and agents:
    if data.save_frames
33      plotFloor(data);
        print('-dpng', sprintf('frames/%s_%05i.png', ...
35          data.frame_basename, it));
    end
37
    % Collect statistics:
39  data.agents_exited_time_series = ...
        [data.agents_exited_time_series; time, data.agents_exited];
41
  time = time + data.dt;
43  it = it + 1;
end
45
data.finish_time = time;
47
% Plot exit occupations:
49 %plotExitedAgents(config, data);

51 % Store time needed to evacuate:
%timeFileID = fopen(sprintf('frames/%s_finish_time.txt',
    data.frame_basename), 'w');
53 %fprintf(timeFileID, '%.1f\n', data.finish_time);
%fclose(timeFileID);
55
% Save the simulation data:
57 saveFile = sprintf('frames/%s_config_data.mat', data.frame_basename), 'w';
save(saveFile, 'config', 'data');
```

Listing 14: simulate.m

9.2 C Code (from [2])

```
1 #include "mex.h"

3 #include <math.h>
```

```
#if defined __GNUC__ && defined __FAST_MATH__ && !defined __STRICT_ANSI__
#define MIN(i, j) fmin(i, j)
#define MAX(i, j) fmax(i, j)
#define ABS(i)    fabs(i)
#else
#define MIN(i, j) ((i) < (j) ? (i) : (j))
#define MAX(i, j) ((i) > (j) ? (i) : (j))
#define ABS(i)    ((i) < 0.0 ? -(i) : (i))
#endif


#define SOLVE_AND_UPDATE    udiff = uxmin - uymin; \
                            if (ABS(udiff) >= 1.0) \
                            { \
                                up = MIN(uxmin, uymin) + 1.0; \
                            } \
                            else \
                            { \
                                up = (uxmin + uymin + sqrt(2.0 - udiff *
                                    udiff)) / 2.0; \
                                up = MIN(uij, up); \
                            } \
                            err_loc = MAX(ABS(uij - up), err_loc); \
                            u[ij] = up;

#define I_STEP(_uxmin, _uymin, _st) if (boundary[ij] == 0.0) \
                                    { \
                                        uij = un; \
                                        un = u[ij + _st]; \
                                        uxmin = _uxmin; \
                                        uymin = _uymin; \
                                        SOLVE_AND_UPDATE \
                                        ij += _st; \
                                    } \
                                    else \
                                    { \
                                        up = un; \
                                        un = u[ij + _st]; \
                                        ij += _st; \
                                    }



#define I_STEP_UP(_uxmin, _uymin)   I_STEP(_uxmin, _uymin, 1)
#define I_STEP_DOWN(_uxmin, _uymin) I_STEP(_uxmin, _uymin,-1)

#define UX_NEXT un
#define UX_PREV up
```

```
#define UX_BOTH MIN(UX_PREV, UX_NEXT)

#define UY_RIGHT u[ij + m]
#define UY_LEFT  u[ij - m]
#define UY_BOTH  MIN(UY_LEFT, UY_RIGHT)



static void iteration(double *u, double *boundary, int m, int n, double
    *err)
{
    int i, j, ij;
    int m2, n2;
    double up, un, uij, uxmin, uymin, udiff, err_loc;

    m2 = m - 2;
    n2 = n - 2;

    *err = 0.0;
    err_loc = 0.0;

    /* first sweep */
    /* i = 0, j = 0 */
    ij = 0;
    un = u[ij];
    I_STEP_UP(UX_NEXT, UY_RIGHT)

    /* i = 1->m2, j = 0 */
    for (i = 1; i <= m2; ++i)
        I_STEP_UP(UX_BOTH, UY_RIGHT)

    /* i = m-1, j = 0 */
    I_STEP_UP(UX_PREV, UY_RIGHT)

    /* i = 0->m-1, j = 1->n2 */
    for (j = 1; j <= n2; ++j)
    {
        I_STEP_UP(UX_NEXT, UY_BOTH)

        for (i = 1; i <= m2; ++i)
            I_STEP_UP(UX_BOTH, UY_BOTH)

        I_STEP_UP(UX_PREV, UY_BOTH)
    }

    /* i = 0, j = n-1 */
    I_STEP_UP(UX_NEXT, UY_LEFT)

    /* i = 1->m2, j = n-1 */
    for (i = 1; i <= m2; ++i)
```

```
        I_STEP_UP(UX_BOTH, UY_LEFT)

    /* i = m-1, j = n-1 */
    I_STEP_UP(UX_PREV, UY_LEFT)


    /* sweep 2 */
    /* i = 0, j = n-1 */
    ij = (n-1)*m;
    un = u[ij];
    I_STEP_UP(UX_NEXT, UY_LEFT)

    /* i = 1->m2, j = n-1 */
    for (i = 1; i <= m2; ++i)
        I_STEP_UP(UX_BOTH, UY_LEFT)

    /* i = m-1, j = n-1 */
    I_STEP_UP(UX_PREV, UY_LEFT)

    /* i = 0->m-1, j = n2->1 */
    for (j = n2; j >= 1; --j)
    {
        ij = j*m;
        un = u[ij];
        I_STEP_UP(UX_NEXT, UY_BOTH)

        for (i = 1; i <= m2; ++i)
            I_STEP_UP(UX_BOTH, UY_BOTH)

        I_STEP_UP(UX_PREV, UY_BOTH)
    }

    /* i = 0, j = 0 */
    ij = 0;
    un = u[ij];
    I_STEP_UP(UX_NEXT, UY_RIGHT)

    /* i = 1->m2, j = 0 */
    for (i = 1; i <= m2; ++i)
        I_STEP_UP(UX_BOTH, UY_RIGHT)

    /* i = m-1, j = 0 */
    I_STEP_UP(UX_PREV, UY_RIGHT)

    /* sweep 3 */
    /* i = m-1, j = n-1 */
    ij = m*n - 1;
    un = u[ij];
    I_STEP_DOWN(UX_NEXT, UY_LEFT)

```

```
    /* i = m2->1, j = n-1 */
    for (i = m2; i >= 1; --i)
        I_STEP_DOWN(UX_BOTH, UY_LEFT)

    /* i = 0, j = n-1 */
    I_STEP_DOWN(UX_PREV, UY_LEFT)

    /* i = m-1->0, j = n2->1 */
    for (j = n2; j >= 1; --j)
    {
        I_STEP_DOWN(UX_NEXT, UY_BOTH)

        for (i = m2; i >= 1; --i)
            I_STEP_DOWN(UX_BOTH, UY_BOTH)

        I_STEP_DOWN(UX_PREV, UY_BOTH)
    }

    /* i = m-1, j = 0 */
    I_STEP_DOWN(UX_NEXT, UY_RIGHT)

    /* i = m2->1, j = 0 */
    for (i = m2; i >= 1; --i)
        I_STEP_DOWN(UX_BOTH, UY_RIGHT)

    /* i = 0, j = 0 */
    I_STEP_DOWN(UX_PREV, UY_RIGHT)

    /* sweep 4 */
    /* i = m-1, j = 0 */
    ij = m - 1;
    un = u[ij];
    I_STEP_DOWN(UX_NEXT, UY_RIGHT)

    /* i = m2->1, j = 0 */
    for (i = m2; i >= 1; --i)
        I_STEP_DOWN(UX_BOTH, UY_RIGHT)

    /* i = 0, j = 0 */
    I_STEP_DOWN(UX_PREV, UY_RIGHT)

    /* i = m-1->0, j = 1->n2 */
    for (j = 1; j <= n2; ++j)
    {
        ij = m - 1 + j*m;
        un = u[ij];
        I_STEP_DOWN(UX_NEXT, UY_BOTH)

        for (i = m2; i >= 1; --i)
            I_STEP_DOWN(UX_BOTH, UY_BOTH)
```

```
203         I_STEP_DOWN(UX_PREV, UY_BOTH)
    }
205
    /* i = m-1, j = n-1 */
207 ij = m*n - 1;
    un = u[ij];
209 I_STEP_DOWN(UX_NEXT, UY_LEFT)

211 /* i = m2->1, j = n-1 */
    for (i = m2; i >= 1; --i)
213     I_STEP_DOWN(UX_BOTH, UY_LEFT)

215 /* i = 0, j = n-1 */
    I_STEP_DOWN(UX_PREV, UY_LEFT)
217
    *err = MAX(*err, err_loc);
219 }

221 void mexFunction(int nlhs, mxArray *plhs[], int nrhs, const mxArray
    *prhs[])
{
223 double *u, *boundary;
    double tol, err;
225 int m, n, entries, max_iter, i;

227 /* Check number of outputs */
    if (nlhs < 1)
229     return;
    else if (nlhs > 1)
231     mexErrMsgTxt("At most 1 output argument needed.");

233 /* Get inputs */
    if (nrhs < 1)
235     mexErrMsgTxt("At least 1 input argument needed.");
    else if (nrhs > 3)
237     mexErrMsgTxt("At most 3 input arguments used.");


239


241 /* Get boundary */
    if (!mxIsDouble(prhs[0]) || mxIsClass(prhs[0], "sparse"))
243     mexErrMsgTxt("Boundary field needs to be a full double precision
            matrix.");

245 boundary = mxGetPr(prhs[0]);
    m = mxGetM(prhs[0]);
247 n = mxGetN(prhs[0]);
    entries = m * n;
249
```

```
    /* Get max iterations  */
    if (nrhs >= 2)
    {
        if (!mxIsDouble(prhs[1]) || mxGetM(prhs[1]) != 1 ||
            mxGetN(prhs[1]) != 1)
            mexErrMsgTxt("Maximum iteration needs to be positive
                integer.");
        max_iter = (int) *mxGetPr(prhs[1]);
        if (max_iter <= 0)
            mexErrMsgTxt("Maximum iteration needs to be positive
                integer.");
    }
    else
        max_iter = 20;

    /* Get tolerance */
    if (nrhs >= 3)
    {
        if (!mxIsDouble(prhs[2]) || mxGetM(prhs[2]) != 1 ||
            mxGetN(prhs[2]) != 1)
            mexErrMsgTxt("Tolerance needs to be a positive real number.");
        tol = *mxGetPr(prhs[2]);
        if (tol < 0)
            mexErrMsgTxt("Tolerance needs to be a positive real number.");
    }
    else
        tol = 1e-12;


    /* create and init output (distance) matrix */
    plhs[0] = mxCreateDoubleMatrix(m, n, mxREAL);
    u = mxGetPr(plhs[0]);

    for (i = 0; i < entries; ++i)
        u[i] = boundary[i] < 0.0 ? 0.0 : 1.0e10;

    err = 0.0;
    i = 0;
    do
    {
        iteration(u, boundary, m, n, &err);
        ++i;
    } while (err > tol && i < max_iter);
}
```

Listing 15: fastSweeping.c

```
#include "mex.h"

#include <math.h>
```

```
#define INTERIOR(i, j)  (boundary[(i) + m*(j)] == 0)

#define DIST(i, j)  dist[(i) + m*(j)]
#define XGRAD(i, j) xgrad[(i) + m*(j)]
#define YGRAD(i, j) ygrad[(i) + m*(j)]

void mexFunction(int nlhs, mxArray *plhs[], int nrhs, const mxArray
    *prhs[])
{
    double *xgrad, *ygrad, *boundary, *dist;
    double dxp, dxm, dyp, dym, xns, yns, nrm;
    int m, n, i, j, nn;

    /* Check number of outputs */
    if (nlhs < 2)
        mexErrMsgTxt("At least 2 output argument needed.");
    else if (nlhs > 2)
        mexErrMsgTxt("At most 2 output argument needed.");

    /* Get inputs */
    if (nrhs < 2)
        mexErrMsgTxt("At least 2 input argument needed.");
    else if (nrhs > 2)
        mexErrMsgTxt("At most 2 input argument used.");


    /* Get boundary */
    if (!mxIsDouble(prhs[0]) || mxIsClass(prhs[0], "sparse"))
        mexErrMsgTxt("Boundary field needs to be a full double precision
            matrix.");

    boundary = mxGetPr(prhs[0]);
    m = mxGetM(prhs[0]);
    n = mxGetN(prhs[0]);

    /* Get distance field */
    if (!mxIsDouble(prhs[1]) || mxIsClass(prhs[1], "sparse") ||
        mxGetM(prhs[1]) != m || mxGetN(prhs[1]) != n)
        mexErrMsgTxt("Distance field needs to be a full double precision
            matrix with same dimension as the boundary.");

    dist = mxGetPr(prhs[1]);
    m = mxGetM(prhs[1]);
    n = mxGetN(prhs[1]);

    /* create and init output (gradient) matrices */
    plhs[0] = mxCreateDoubleMatrix(m, n, mxREAL);
    plhs[1] = mxCreateDoubleMatrix(m, n, mxREAL);
```

```
    xgrad = mxGetPr(plhs[0]);
    ygrad = mxGetPr(plhs[1]);



    for (j = 0; j < n; ++j)
        for (i = 0; i < m; ++i)
            if (INTERIOR(i,j))
            {
                if (i > 0)
                    dxm = INTERIOR(i-1,j) ? DIST(i-1,j) : DIST(i,j);
                else
                    dxm = DIST(i,j);

                if (i < m-1)
                    dxp = INTERIOR(i+1,j) ? DIST(i+1,j) : DIST(i,j);
                else
                    dxp = DIST(i,j);

                if (j > 0)
                    dym = INTERIOR(i,j-1) ? DIST(i,j-1) : DIST(i,j);
                else
                    dym = DIST(i,j);

                if (j < n-1)
                    dyp = INTERIOR(i,j+1) ? DIST(i,j+1) : DIST(i,j);
                else
                    dyp = DIST(i,j);

                XGRAD(i, j) = (dxp - dxm) / 2.0;
                YGRAD(i, j) = (dyp - dym) / 2.0;
                nrm = sqrt(XGRAD(i, j)*XGRAD(i, j) + YGRAD(i, j)*YGRAD(i,
                    j));
                if (nrm > 1e-12)
                {
                    XGRAD(i, j) /= nrm;
                    YGRAD(i, j) /= nrm;
                }
            }
            else
            {
                XGRAD(i, j) = 0.0;
                YGRAD(i, j) = 0.0;
            }

    for (j = 0; j < n; ++j)
        for (i = 0; i < m; ++i)
            if (!INTERIOR(i, j))
            {
                xns = 0.0;
```

```
                yns = 0.0;
                nn = 0;
                if (i > 0 && INTERIOR(i-1,j))
                {
                    xns += XGRAD(i-1,j);
                    yns += YGRAD(i-1,j);
                    ++nn;
                }
                if (i < m-1 && INTERIOR(i+1,j))
                {
                    xns += XGRAD(i+1,j);
                    yns += YGRAD(i+1,j);
                    ++nn;
                }
                if (j > 0 && INTERIOR(i,j-1))
                {
                    xns += XGRAD(i,j-1);
                    yns += YGRAD(i,j-1);
                    ++nn;
                }
                if (j < n-1 && INTERIOR(i,j+1))
                {
                    xns += XGRAD(i,j+1);
                    yns += YGRAD(i,j+1);
                    ++nn;
                }

                if (nn > 0)
                {
                    XGRAD(i, j) = xns / nn;
                    YGRAD(i, j) = yns / nn;
                }
            }
}
```

Listing 16: getNormalizedGradient.c

```
#include <mex.h>

void mexFunction(int nlhs, mxArray *plhs[], int nrhs, const mxArray
    *prhs[])
{
    size_t m, n, i0, i1, j0, j1, idx00;
    double *data, *out, x, y, wx0, wy0, wx1, wy1;
    double d00, d01, d10, d11;

    if (nlhs < 1)
        return;
    else if (nlhs > 1)
        mexErrMsgTxt("Exactly one output argument needed.");
```

```
    if (nrhs != 3)
        mexErrMsgTxt("Exactly three input arguments needed.");

    m = mxGetM(prhs[0]);
    n = mxGetN(prhs[0]);
    data = mxGetPr(prhs[0]);
    x = *mxGetPr(prhs[1]) - 1;
    y = *mxGetPr(prhs[2]) - 1;

    plhs[0] = mxCreateDoubleMatrix(1, 1, mxREAL);
    out = mxGetPr(plhs[0]);

    x = x < 0 ? 0 : x > m - 1 ? m - 1 : x;
    y = y < 0 ? 0 : y > n - 1 ? n - 1 : y;
    i0 = (size_t) x;
    j0 = (size_t) y;
    i1 = i0 + 1;
    i1 = i1 > m - 1 ? m - 1 : i1;
    j1 = j0 + 1;
    j1 = j1 > n - 1 ? n - 1 : j1;

    idx00 = i0 + m * j0;
    d00 = data[idx00];
    d01 = data[idx00 + m];
    d10 = data[idx00 + 1];
    d11 = data[idx00 + m + 1];

    wx1 = x - i0;
    wy1 = y - j0;
    wx0 = 1.0 - wx1;
    wy0 = 1.0 - wy1;

    *out = wx0 * (wy0 * d00 + wy1 * d01) + wx1 * (wy0 * d10 + wy1 * d11);
}
```

Listing 17: lerp2.c