

RADIX TREE

EDAA 23/24

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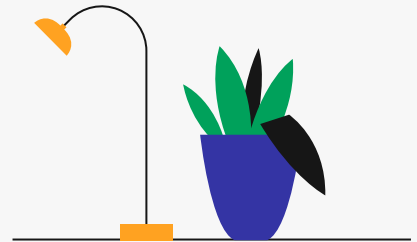
Addressed Problem

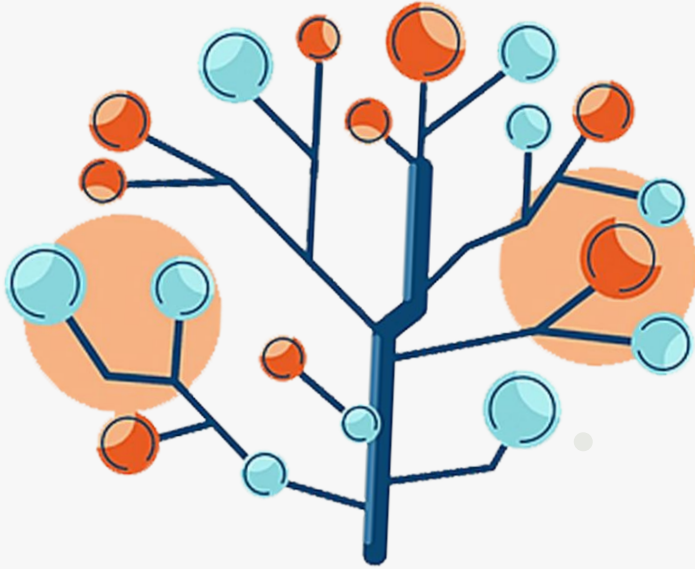
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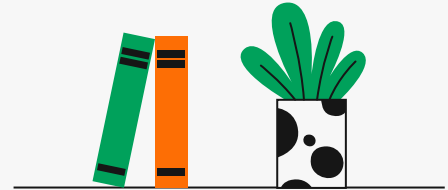
References





01

What is a Radix Tree?



Data Structure



Trie Tree

A Radix Tree is a compressed Trie (Prefix Tree)



Radix

Number of children of every internal node is $\leq R$ (Power of 2)



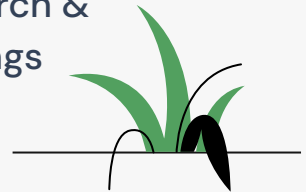
Leaves

The path from the root node to any leaf corresponds to a string



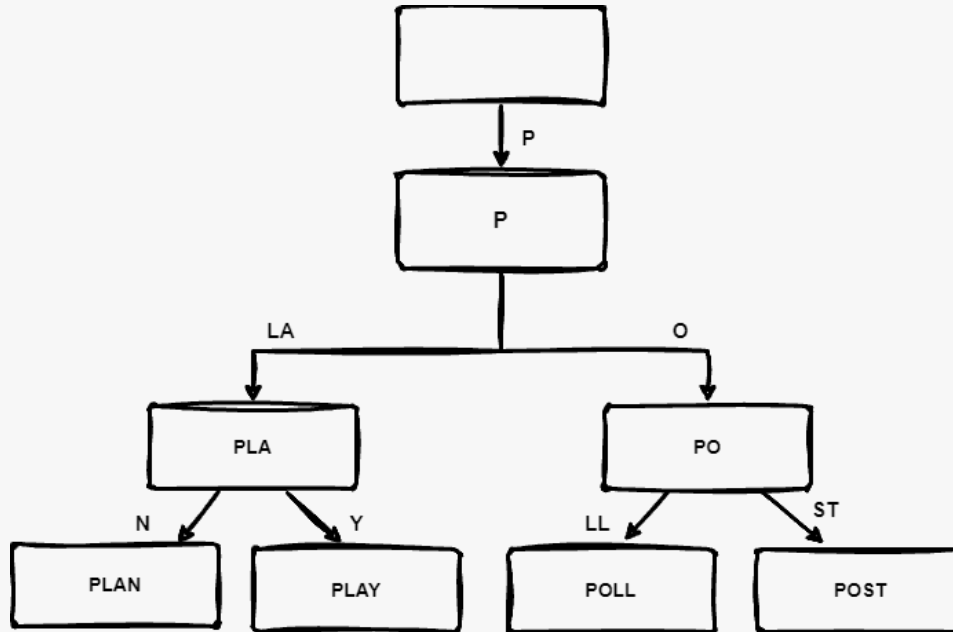
Operations

Insertion, Deletion, Search & Common Prefix Strings



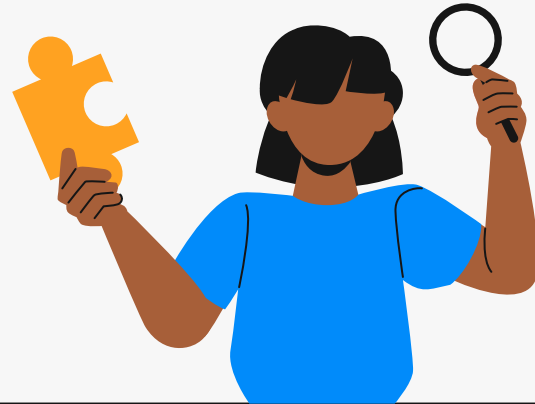
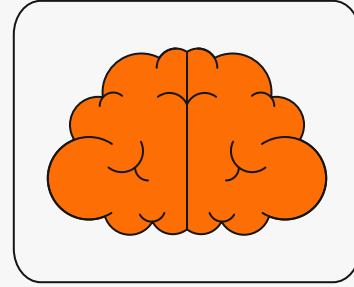
Radix Tree Example

PLAN
PLAY
POLL
POST



02

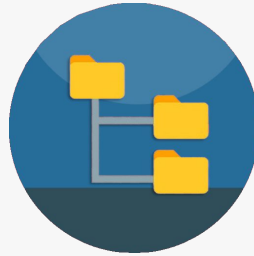
Basic Applications



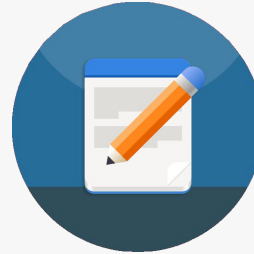
Where & how is it being used



Store IP Routing
Tables



Represent &
Search File Paths



Spell-Checking &
Autocomplete



Inverted Indexes

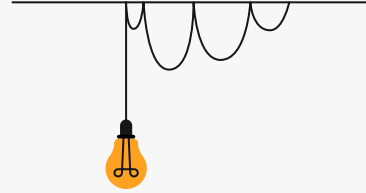
03

Data Structure Operations

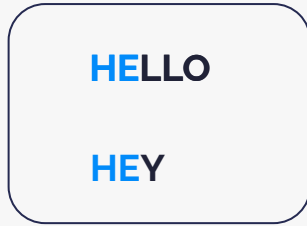


Insertion ⊕

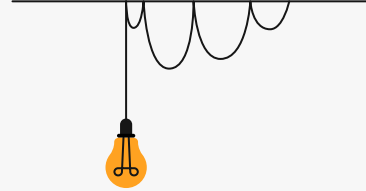
Insert “Hello”



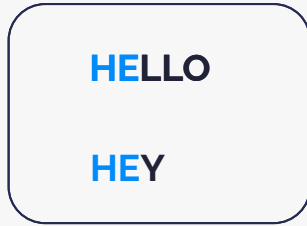
Insert “Hey”



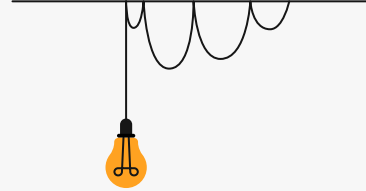
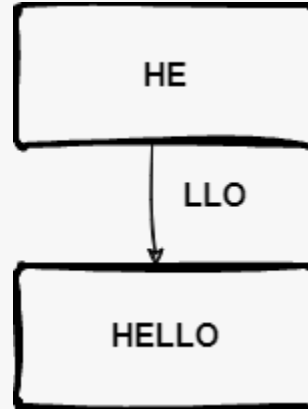
Comparing next letter in
insert term to next letter
in prefix of current node



Insert “Hey”



Connect new node to the
old, and reset prefix
stored at the previous
node

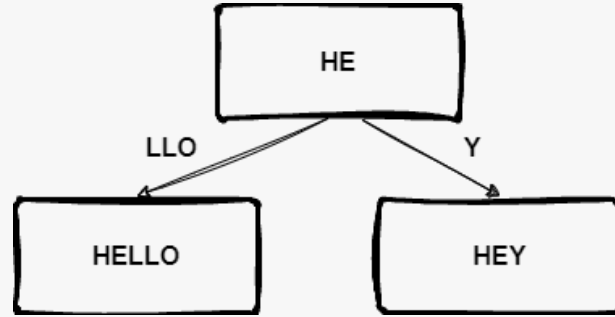


Insert "Hey"

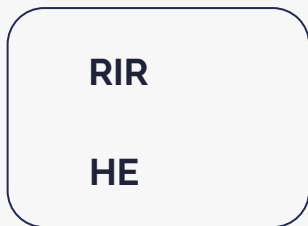
HELLO

HEY

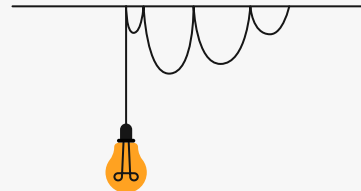
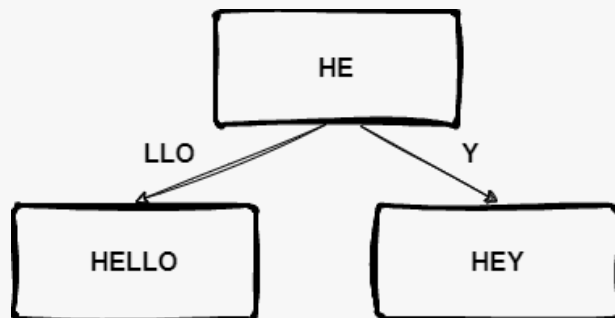
Inserting "Y"



Insert "Rir"



Comparing next letter in
insert term to next letter
in prefix of current node

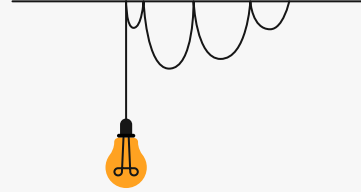
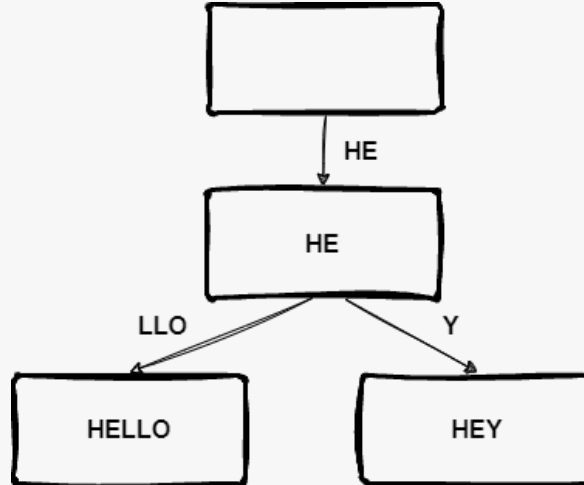


Insert “Rir”

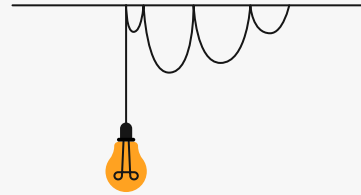


Prefix mismatch

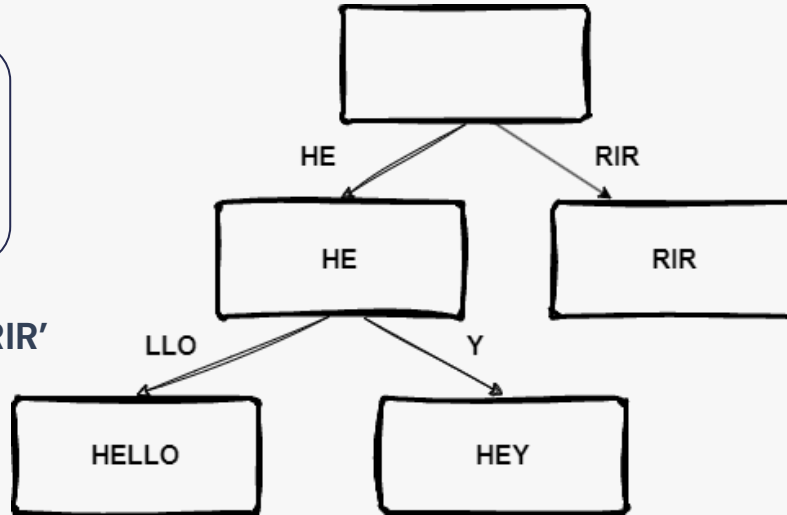
Create new root node



Insert "Rir"

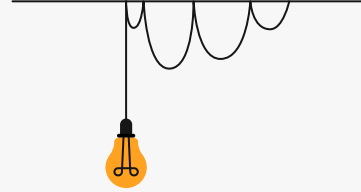
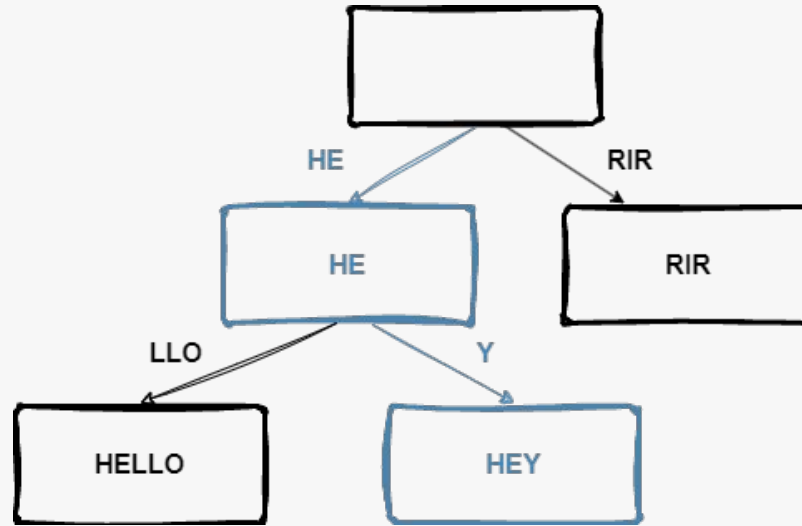


Insert new node 'RIR'



Search

Search “Hey”



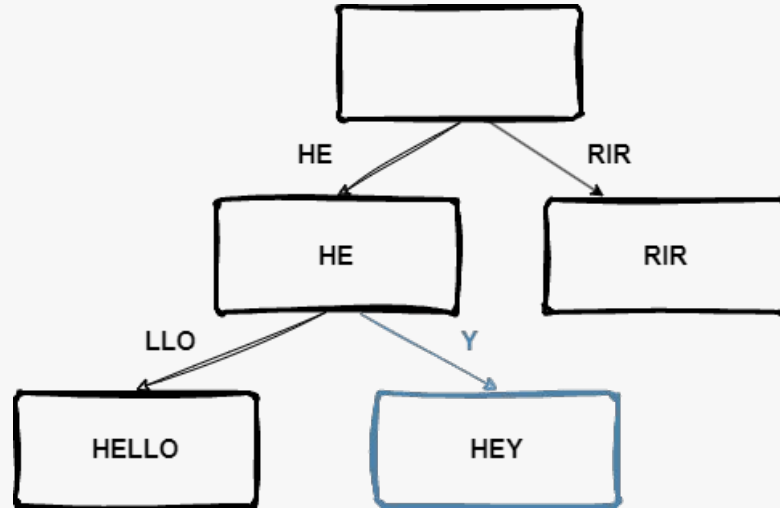
Delete



Delete “Hey”

Search for “Hey”

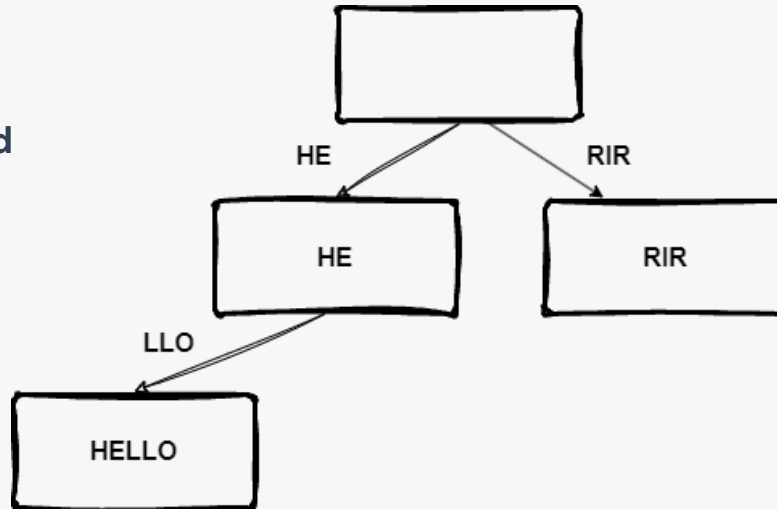
Delete leaf node



Delete “Hey”

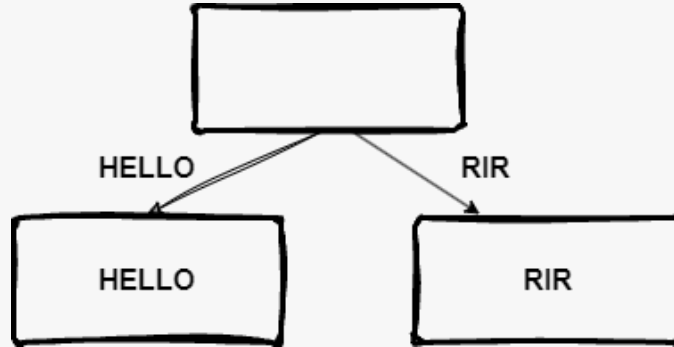
Deleted node

Node left with 1 child



Delete “Hey”

Merged with parent node





04



Addressed Problem



Problems...



**Memory
Inefficiency**

**Search
Inefficiency**



**Pattern
Matching**

**Lack of
Scalability**



05

Competing Data Structures

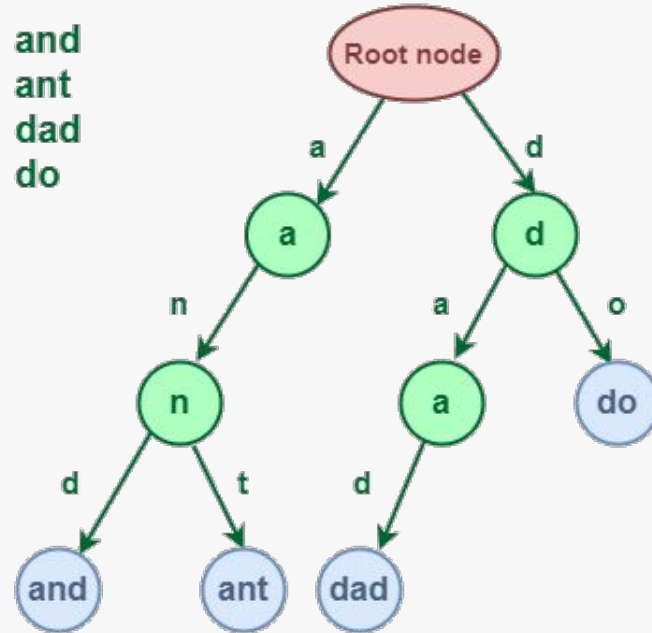


What are the other options?

Trie Tree

Same logic of the radix tree,
however each edge is a single
character

- and
- ant
- dad
- do

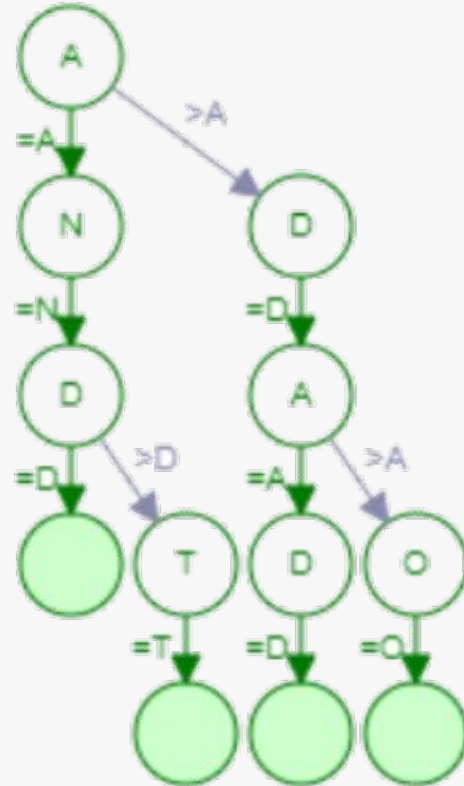


What are the other options?

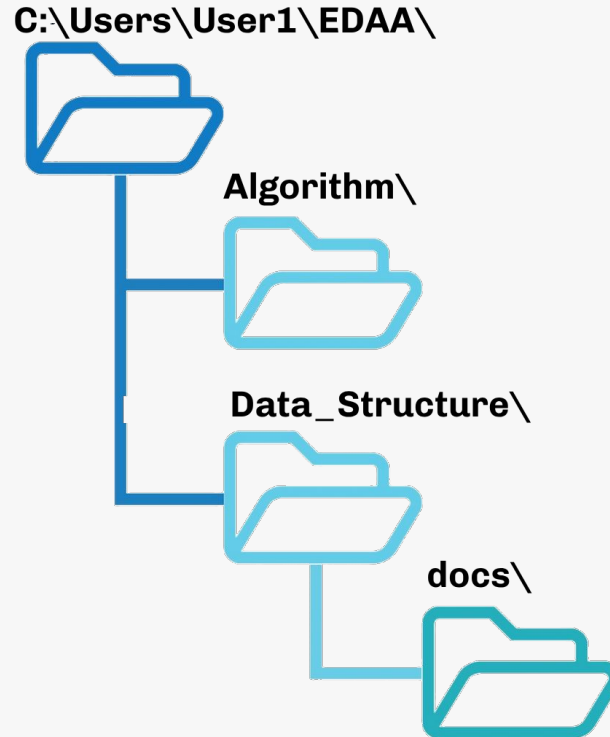
Ternary Search Tree

Each node stores a single character
and may have 3 children (<, =, >)

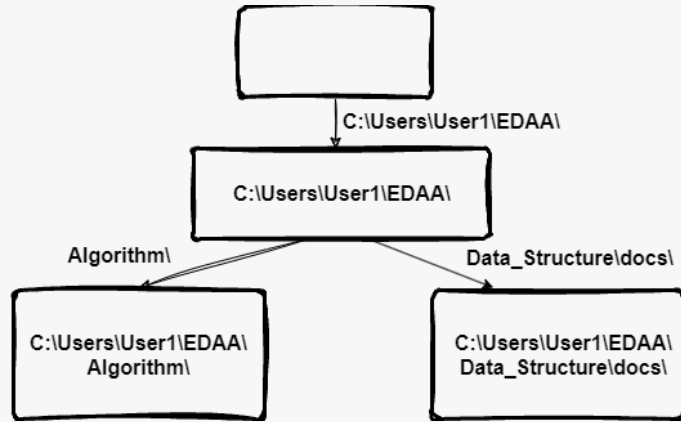
- and
- ant
- dad
- do



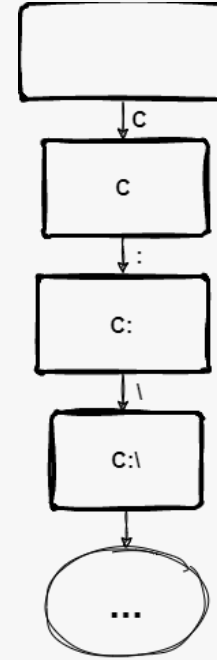
Directory Example...



Directory Example...



Radix Tree



Trie & Ternary Search Tree

Time Complexity

Operation	Radix	Trie	Ternary
Search	$O(N)$	$O(N)$	$O(\log N)$
Insertion	$O(N)$	$O(N)$	$O(\log N)$
Deletion	$O(N)$	$O(N)$	$O(\log N)$

~ Where N is the length of the input string

Conclusions



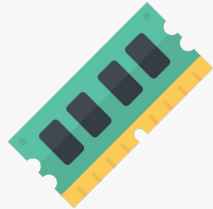
No Rebalancing

ABC...

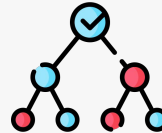
Lexicographical
Order



Complexity
depends on Key
Length



Space Efficiency



Better for
non-sparse datasets



06

References



References

Radix Tree

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Trie Tree

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<https://www.geeksforgeeks.org/ternary-search-tree/>

<https://www.youtube.com/watch?v=CI GyewO7868>