ExerciseRound09

November 7, 2024

```
[1]: # This cell is used for creating a button that hides/unhides code cells to ...
      ⇔quickly look only the results.
     # Works only with Jupyter Notebooks.
     from IPython.display import HTML
     HTML('''<script>
     code_show=true;
     function code_toggle() {
     if (code show){
     $('div.input').hide();
     } else {
     $('div.input').show();
     code_show = !code_show
     $( document ).ready(code_toggle);
     </script>
     <form action="javascript:code_toggle()"><input type="submit" value="Click here_</pre>
      →to toggle on/off the raw code."></form>''')
```

[1]: <IPython.core.display.HTML object>

```
[2]: # Description:
    # Exercise09 notebook.
#

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#

# This software is distributed under the GNU General Public
# Licence (version 2 or later); please refer to the file
# Licence.txt, included with the software, for details.

# Preparations
import os
import numpy as np
import matplotlib.pyplot as plt
```

```
from utils import from data file, theta_to_model, model_to_theta,_
 ⇔initial_model, logistic, \
   log_sum_exp_over_rows, classification_performance
# Select data directory
if os.path.isdir('/coursedata'):
    # JupyterHub
    course_data_dir = '/coursedata'
elif os.path.isdir('../../coursedata'):
    # Local installation
    course_data_dir = '../../coursedata'
else:
    # Docker
    course_data_dir = '/home/jovyan/work/coursedata/'
print('The data directory is %s' % course_data_dir)
data_dir = os.path.join(course_data_dir, 'exercise-09-data')
print('Data stored in %s' % data_dir)
```

The data directory is /coursedata

Data stored in /coursedata/exercise-09-data

1 CS-E4850 Computer Vision Exercise Round 9

The problems should be solved before the exercise session and solutions returned via MyCourses. Upload the files: (1) a pdf file containing your written answers to Exercise 1, and (2) both the pdf and .ipynb versions of the notebook containing your answers to Exercises 2 and 3. Scanned, **neatly** handwritten, solutions are ok for problem 1. If possible, combine your pdf solution of Exercise 1 with the notebook pdf into a single pdf and return that with the notebook .ipynb file.

Notice also that the last two problems can be done without solving Exercise 1 since the solutions are already written out in the subtasks of Exercise 1 (i.e. only the derivations are missing and asked in Exercise 1).

If you have not studied basics of neural networks in previous courses and the problem context of these exercises is not clear, it may be helpful to check the slides of the first four lectures of prof. Hinton's course "Introduction to neural networks and machine learning":

http://www.cs.toronto.edu/~hinton/coursera_slides.html http://www.cs.toronto.edu/~hinton/coursera_lectures.html (lecture videos).

1.1 Exercise 1 - Neural networks and backpropagation

This is a pen-&-paper problem. See Exercise09penandpaper.pdf for the questions.

1.2 Exercise 2 - Image classification using a neural network

The first exercise problem above gives the solution to Part 2 of the second programming assignment of professor Hinton's course "Introduction to neural net-

works and machine learning". The assignment and related material are available at https://www.cs.toronto.edu/~tijmen/csc321/assignments/a2/.

Check out the contents of the above web page and complete the programming task of Part 2 according to the instructions given there. The code template for the python version is below. The solution for the pen and paper part of the task is already given above in **Exercise 1**. Hence, the programming part is a relatively straightforward implementation and can be done without carrying out the derivations since the results of the derivations are already given in **Exercise 1** above.

```
[3]: def test gradient(model, data, wd coefficient):
         import sys
         base_theta = model_to_theta(model)
         h = 1e-2
         correctness threshold = 1e-5
         analytic_gradient_struct = d_loss_by_d_model(model, data, wd_coefficient)
         analytic_gradient = model_to_theta(analytic_gradient_struct);
         if True in np.isnan(analytic_gradient) or True in np.
      ⇔isinf(analytic_gradient):
             sys.exit('Your gradient computation produced a NaN or infinity. That is _{\sqcup}
      →an error.')
         # We want to test the gradient not for every element of theta, because,
      \hookrightarrow that's a
         # lot of work. Instead, we test for only a few elements. If there's anu
      ⇔error, this
         # is probably enough to find that error.
         # We want to first test the hid\_to\_class gradient, because that's most_{\sqcup}
      ⇔likely
         # to be correct (it's the easier one).
         # Let's build a list of theta indices to check. We'll check 20 elements of
         # hid_to_class, and 80 elements of input_to_hid (it's bigger than_
      ⇔hid to class).
         input_to_hid_theta_size = model['input_to_hid'].size
         hid_to_class_theta_size = model['hid_to_class'].size
         big_prime = 1299721; # 1299721 is prime and thus ensures a somewhatu
      →random-like selection of indices.
         hid to class indices to check = np.mod(big prime * np.arange(20),
      ⇔hid_to_class_theta_size) \
                                              + input_to_hid_theta_size
         input_to_hid_indices_to_check = np.mod(big_prime * np.arange(80),__
      →input_to_hid_theta_size)
         a = hid_to_class_indices_to_check[np.newaxis,:]
         b = input_to_hid_indices_to_check[np.newaxis,:]
         indices_to_check = np.ravel(np.hstack((a,b)))
         for i in range(100):
             test index = indices to check[i]
```

```
analytic_here = analytic_gradient[test_index]
        theta step = base theta * 0
        theta_step[test_index] = h
        contribution_distances = np.array([-4., -3., -2., -1., 1., 2., ]
 4.]) →3.,
        contribution weights = np.array([1/280., -4/105., 1/5., -4/5., 4/5., -1/
 →5., 4/105., -1/280.])
        temp = 0;
        for contribution_index in range(8):
            temp = temp + loss(theta_to_model(base_theta + theta_step * \
 →contribution_distances[contribution_index]), data, wd_coefficient) * \
 →contribution_weights[contribution_index]
        fd_here = temp / h
        diff = np.abs(analytic_here - fd_here)
        if True in (diff > correctness threshold) and \
            True in (diff / (np.abs(analytic_here) + np.abs(fd_here)) >__
 ⇔correctness threshold):
            part_names = ['input_to_hid', 'hid_to_class']
            sys.exit('Theta element #{} (part of {}), with value {}, has finite_\( \)
 ⊸difference gradient {} but analytic gradient {}. That looks like an error.

¬\n'.format(test_index, part_names[(i<20)], base_theta[test_index], fd_here,
</pre>
 →analytic_here))
        if i==19:
            print('Gradient test passed for hid_to_class. ')
        if i==99:
            print('Gradient test passed for input_to_hid. ')
    print('Gradient test passed. That means that the gradient that your code_{\sqcup}
 ⇔computed is within 0.001%% of the gradient that the finite difference ⊔
 \hookrightarrowapproximation computed, so the gradient calculation procedure is probably.

¬correct (not certainly, but probably).\n')

def forward_pass(model, data):
    # This function does the forward pass through the network: calculating the
 ⇔states of all units, and some related data.
    # This function is used in functions loss() and d loss by d model().
    # model.input_to_hid is a matrix of size <number of hidden units> by_
 → <number of inputs i.e. 256>. It contains the weights from the input units to ⊔
 → the hidden units.
    # model.hid_to_class is a matrix of size <number of classes i.e. 10> by_
 → <number of hidden units>. It contains the weights from the hidden units to | |
 → the softmax units.
```

```
# data.inputs is a matrix of size <number of inputs i.e. 256> by <number of \Box
 ⇔data cases>. Each column describes a different data case.
    # data.targets is a matrix of size <number of classes i.e. 10> by <number_
 of data cases. Each column describes a different data case. It contains all
 →one-of-N encoding of the class, i.e. one element in every column is 1 and
 \hookrightarrow the others are 0.
    hid_input = np.dot(model['input_to_hid'], data['inputs']) # input to the_
 \hookrightarrowhidden units, i.e. before the logistic. size: <number of hidden units> by_{\sqcup}
 ⇔ < number of data cases>
    hid_output = logistic(hid_input) # output of the hidden units, i.e. after_
 →the logistic. size: <number of hidden units> by <number of data cases>
    class_input = np.dot(model['hid_to_class'], hid_output) # input to the_
 →components of the softmax. size: <number of classes, i.e. 10> by <number of L
 ⇔data cases>
    # The following three lines of code implement the softmax.
    # However, it's written differently from what the lectures say.
    # In the lectures, a softmax is described using an exponential divided by a_{\sqcup}
 ⇔sum of exponentials.
    # What we do here is exactly equivalent (you can check the math or just \Box
 scheck it in practice), but this is more numerically stable.
    # "Numerically stable" means that this way, there will never be really big_{\sqcup}
 →numbers involved.
    # The exponential in the lectures can lead to really big numbers, which are
 \rightarrow fine in mathematical equations, but can lead to all sorts of problems in
 \rightarrow Matlab
    # Matlab isn't well prepared to deal with really large numbers, like the \Box
 →number 10 to the power 1000. Computations with such numbers get unstable, soll
 ⇔we avoid them.
    class_normalizer = log_sum_exp_over_rows(class_input) # log(sum(exp_of_u)
 sclass input)) is what we subtract to get properly normalized log class,
 ⇔probabilities. size: <1> by <number of data cases>
    log_class_prob = class_input - np.tile(class_normalizer, (class_input.
 →shape[0], 1)) # log of probability of each class. size: <number of classes, ⊔
 \hookrightarrow i.e. 10> by <number of data cases>
    class_prob = np.exp(log_class_prob) # probability of each class. Each_
 →column (i.e. each case) sums to 1. size: <number of classes, i.e. 10> by
 → <number of data cases>
    return hid_input, hid_output, class_input, log_class_prob, class_prob
def loss(model, data, wd_coefficient):
    hid_input, hid_output, class_input, log_class_prob, class_prob =__
 →forward_pass(model, data);
```

```
classification_loss = -np.mean(np.sum(np.multiply(log_class_prob,_
      odata['target']), 0)) # select the right log class probability using that sum;
      → then take the mean over all data cases.
         wd_loss = (np.sum(np.ravel(model['input_to_hid']) ** 2 ) + np.sum(np.
      ravel(model['hid_to_class']) ** 2 )) / 2. * wd_coefficient; # weight decay_
      \hookrightarrow loss. very straightforward: E = 1/2 * wd_coeffecient * parameters^2
         ret = classification_loss + wd_loss
         return ret
[4]: def d loss by d model(model, data, wd coefficient):
         # model.input_to_hid is a matrix of size <number of hidden units> by_
      → <number of inputs i.e. 256>
         # model.hid_to_class is a matrix of size <number of classes i.e. 10> by_{\sqcup}
      ⇔ < number of hidden units>
         # data.inputs is a matrix of size <number of inputs i.e. 256> by <number of
      →data cases>
         # data.targets is a matrix of size <number of classes i.e. 10> by <number_u
      ⇔of data cases>
         # The returned object <ret> is supposed to be exactly like parameter_
      → <model>, i.e. it has fields ret.input_to_hid and ret.hid_to_class, and those_
      →are of the same shape as they are in <model>.
         # However, in \langle ret \rangle, the contents of those matrices are gradients (d loss \Box
      \hookrightarrowby d weight), instead of weights.
         ret = dict()
         # This is the only function that you're expected to change. Right now, it \Box
      ight returns a lot of zeros, which is obviously not the correct output. Young
      \rightarrow job is to change that.
         #--your-code-starts-here--#
         W_input_to_hid = model['input_to_hid']
         W_hid_to_class = model['hid_to_class']
         inputs = data['inputs']
         targets = data['target']
         # Forward pass
         hidden = np.dot(W_input_to_hid, inputs) # <number of hidden units> by_
      → < number of data cases>
         hidden = 1 / (1 + np.exp(-hidden))
         output = np.dot(W_hid_to_class, hidden) # <number of classes> by <number_
      ⇔of data cases>
         # Compute the softmax output and loss (assuming cross-entropy loss)
         exp_output = np.exp(output - np.max(output, axis=0)) # Stable softmax
         softmax_output = exp_output / np.sum(exp_output, axis=0)
```

```
# Calculate the gradient of the loss with respect to output
         error = softmax_output - targets # <number of classes> by <number of data_
      ⇔cases>
         # Gradients
         d loss hid to class = np.dot(error, hidden.T) / inputs.shape[1] # <number_1
      ⇔of classes> by <number of hidden units>
         d_loss_hidden = np.dot(W_hid_to_class.T, error) * hidden * (1 - hidden) #__
      → < number of hidden units > by < number of data cases >
         d loss input to hid = np.dot(d loss hidden, inputs.T) / inputs.shape[1] #__
      → <number of hidden units> by <number of inputs>
         # Weight decay
         d_loss_input_to_hid += wd_coefficient * W_input_to_hid
         d_loss_hid_to_class += wd_coefficient * W_hid_to_class
         ret['input_to_hid'] = d_loss_input_to_hid
         ret['hid_to_class'] = d_loss_hid_to_class
         #--your-code-ends-here--#
         return ret
[5]: def a2(wd_coefficient, n_hid, n_iters, learning_rate, momentum_multiplier, __
      →do_early_stopping, mini_batch_size):
         model = initial model(n hid)
         datas = from_data_file(data_dir)
         n_training_cases = datas['train']['inputs'].shape[1]
         if n iters != 0:
             print("Now testing the gradient on the whole training set...")
             test_gradient(model, datas['train'], wd_coefficient)
         # optimization
         training_batch = dict()
         best_so_far = dict()
         theta = model_to_theta(model)
         momentum\_speed = theta * 0.
         training data losses = []
         validation_data_losses = []
         if do early stopping:
             best_so_far['theta'] = -1 # this will be overwritten soon
             best so far['validation loss'] = np.Inf
             best_so_far['after_n_iters'] = -1
         for optimization_iteration_i in range(1, n_iters+1):
             model = theta_to_model(theta)
             training_batch_start = np.mod((optimization_iteration_i-1) *_
```

mini_batch_size, n_training_cases);

```
training_batch['inputs'] = datas['train']['inputs'][:,__
straining_batch_start : training_batch_start + mini_batch_size]
      training_batch['target'] = datas['train']['target'][:,__
otraining_batch_start : training_batch_start + mini_batch_size]
      gradient = model_to_theta(d_loss_by_d_model(model, training_batch,__
→wd_coefficient))
      momentum_speed = np.multiply(momentum_speed, momentum_multiplier) -
⇒gradient;
      theta = theta + momentum_speed * learning_rate;
      model = theta_to_model(theta);
      training data losses.append(loss(model, datas['train'], wd coefficient))
      validation_data_losses.append(loss(model, datas['val'], wd_coefficient))
      if do_early_stopping and validation_data_losses[-1] <__
⇔best_so_far['validation_loss']:
          best_so_far['theta'] = theta; # this will be overwritten soon
          best_so_far['validation_loss'] = validation_data_losses[-1]
          best_so_far['after_n_iters'] = optimization_iteration_i
      if np.mod(optimization_iteration_i, np.round(n_iters / 10.)) == 0:
          print('After {} optimization iterations, training data loss is {},⊔
wand validation data loss is {}\n'.format(optimization_iteration_i,
→training_data_losses[-1], validation_data_losses[-1]))
      if optimization_iteration_i == n_iters: # check gradient again, this_
stime with more typical parameters and with a different data size
          print('Now testing the gradient on just a mini-batch instead of the ⊔
⇔whole training set... ')
          test_gradient(model, training_batch, wd_coefficient)
  if do_early_stopping:
      print('Early stopping: validation loss was lowest after {} iterations...
\hookrightarrow We chose the model that we had then.\n'.format(best_so_far['after_n_iters']))
      theta = best_so_far['theta']
  # the optimization is finished. Now do some reporting.
  model = theta_to_model(theta)
  if n iters != 0:
      ax = plt.figure(1, figsize=(15,10))
      plt.plot(training_data_losses, 'b')
      plt.plot(validation_data_losses, 'r')
      plt.tick params(labelsize=25)
      ax.legend(('training', 'validation'), fontsize=25)
      plt.ylabel('loss', fontsize=25);
      plt.xlabel('iteration number', fontsize=25);
      plt.show()
```

```
datas2 = [datas['train'], datas['val'], datas['test']]
data_names = ['training', 'validation', 'test'];
for data_i in range(3):
    data = datas2[data_i]
    data_name = data_names[data_i]
    print('\nThe total loss on the {} data is {}\n'.format(data_name, \u)

$\text{loss(model, data, wd_coefficient))})
    print('The classification loss (i.e. without weight decay) on the {}\u]

$\text{data is {}\n'.format(data_name, loss(model, data, 0)));}
    print('The classification error rate on the {} data is {}\n'.

$\text{format(data_name, classification_performance(model, data)))}
```

```
[6]: # Start training the neural network a2(0, 10, 70, 20.0, 0, False, 4)
```

Now testing the gradient on the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001%% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).

After 7 optimization iterations, training data loss is 2.302585091837178, and validation data loss is 2.3025850910767875

After 14 optimization iterations, training data loss is 2.302585091837178, and validation data loss is 2.3025850910767875

After 21 optimization iterations, training data loss is 2.302585091837178, and validation data loss is 2.3025850910767875

After 28 optimization iterations, training data loss is 2.302585091837178, and validation data loss is 2.3025850910767875

After 35 optimization iterations, training data loss is 2.302585091837178, and validation data loss is 2.3025850910767875

After 42 optimization iterations, training data loss is 2.302585091837178, and validation data loss is 2.3025850910767875

After 49 optimization iterations, training data loss is 2.302585091837178, and validation data loss is 2.3025850910767875

After 56 optimization iterations, training data loss is 2.3025850918371775, and validation data loss is 2.302585091076785

After 63 optimization iterations, training data loss is 2.3025850918371775, and validation data loss is 2.302585091076785

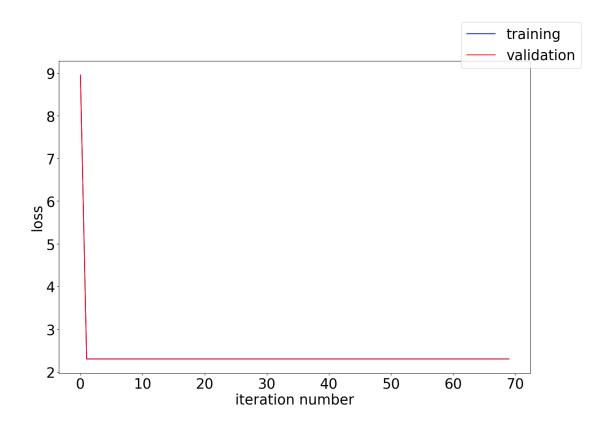
After 70 optimization iterations, training data loss is 2.3025850918371775, and validation data loss is 2.302585091076785

Now testing the gradient on just a mini-batch instead of the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).



The total loss on the training data is 2.3025850918371775

The classification loss (i.e. without weight decay) on the training data is

2.3025850918371775

The classification error rate on the training data is 0.9

The total loss on the validation data is 2.302585091076785

The classification loss (i.e. without weight decay) on the validation data is 2.302585091076785

The classification error rate on the validation data is 0.9

The total loss on the test data is 2.3025850220361597

The classification loss (i.e. without weight decay) on the test data is 2.3025850220361597

The classification error rate on the test data is 0.9

When you have completed the programming part, run a2(0, 10, 30, 0.01, 0, False, 10) and report the resulting training data classification loss here:

Training data classification loss:

1.3 Exercise 3 - Optimisation using backpropagation

Do Part 3 of the assignment as described at http://www.cs.toronto.edu/~tijmen/csc321/assignments/a2/

The task is to experiment with the example code given above and report your findings. There is no need to program anything in this part but completing it requires that Part 2 is successfully solved.

```
[7]: #def a2(wd_coefficient, n_hid, n_iters, learning_rate, momentum_multiplier, odo_early_stopping, mini_batch_size):

a2(0, 10, 70, 0.005, 0, False, 4)
a2(0, 10, 70, 0.5, 0, False, 4)
```

Now testing the gradient on the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input to hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001%% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).

After 7 optimization iterations, training data loss is 2.302547565972378, and validation data loss is 2.3024807897490174

After 14 optimization iterations, training data loss is 2.302468383398046, and validation data loss is 2.3024018553608787

After 21 optimization iterations, training data loss is 2.3023760042763626, and validation data loss is 2.302306202285404

After 28 optimization iterations, training data loss is 2.3022977185605495, and validation data loss is 2.3022274695639147

After 35 optimization iterations, training data loss is 2.3022163995581155, and validation data loss is 2.302146693739379

After 42 optimization iterations, training data loss is 2.302112210841646, and validation data loss is 2.3020412870764924

After 49 optimization iterations, training data loss is 2.3020270021112794, and validation data loss is 2.301960350592735

After 56 optimization iterations, training data loss is 2.30192702343772, and validation data loss is 2.3018599090410063

After 63 optimization iterations, training data loss is 2.301837755621561, and validation data loss is 2.3017682368142576

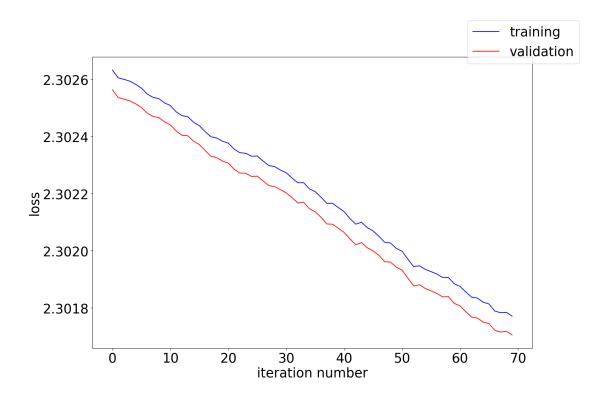
After 70 optimization iterations, training data loss is 2.30177112183998, and validation data loss is 2.3017055742751227

Now testing the gradient on just a mini-batch instead of the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).



The total loss on the training data is 2.30177112183998

The classification loss (i.e. without weight decay) on the training data is 2.30177112183998

The classification error rate on the training data is 0.888

The total loss on the validation data is 2.3017055742751227

The classification loss (i.e. without weight decay) on the validation data is 2.3017055742751227

The classification error rate on the validation data is 0.893

The total loss on the test data is 2.3017283379819546

The classification loss (i.e. without weight decay) on the test data is 2.3017283379819546

The classification error rate on the test data is 0.88666666666666667

Now testing the gradient on the whole training set ...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001%% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).

After 7 optimization iterations, training data loss is 2.2959955408041206, and validation data loss is 2.2962197987885515

After 14 optimization iterations, training data loss is 2.2858275283763096, and validation data loss is 2.286007399240133

After 21 optimization iterations, training data loss is 2.27068240854692, and validation data loss is 2.270843067579077

After 28 optimization iterations, training data loss is 2.2496666773527596, and validation data loss is 2.2501560769818156

After 35 optimization iterations, training data loss is 2.2184063268798844, and validation data loss is 2.219121556789807

After 42 optimization iterations, training data loss is 2.162092267121496, and validation data loss is 2.1630387462718423

After 49 optimization iterations, training data loss is 2.092659142301978, and validation data loss is 2.094904112660853

After 56 optimization iterations, training data loss is 2.0107205696180137, and validation data loss is 2.0142516172002045

After 63 optimization iterations, training data loss is 1.9502024647122225, and validation data loss is 1.953984301481608

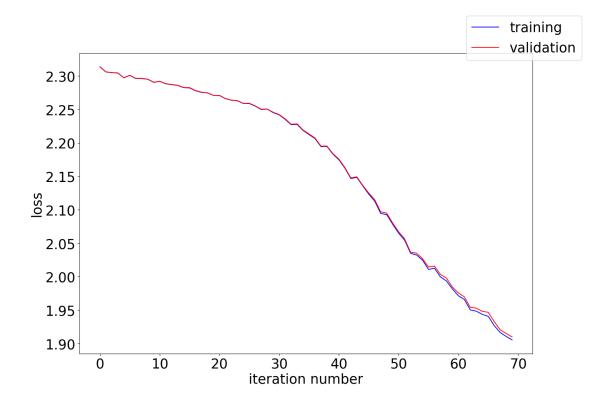
After 70 optimization iterations, training data loss is 1.905314662909433, and validation data loss is 1.9097706461624864

Now testing the gradient on just a mini-batch instead of the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001%% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).



The total loss on the training data is 1.905314662909433

The classification loss (i.e. without weight decay) on the training data is 1.905314662909433

The classification error rate on the training data is 0.792

The total loss on the validation data is 1.9097706461624864

The classification loss (i.e. without weight decay) on the validation data is 1.9097706461624864

The classification error rate on the validation data is 0.791

The total loss on the test data is 1.9005034615639416

The classification loss (i.e. without weight decay) on the test data is 1.9005034615639416

[8]: #try with learning_rate = 0.002, 0.01, 0.05, 0.2, 1.0, 5.0, and 20.0, and without momentum
a2(0, 10, 70, 0.002, 0, False, 4)

Now testing the gradient on the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).

After 7 optimization iterations, training data loss is 2.3026037735735647, and validation data loss is 2.302535720632007

After 14 optimization iterations, training data loss is 2.3025720131272993, and validation data loss is 2.30250405879389

After 21 optimization iterations, training data loss is 2.302535038202373, and validation data loss is 2.3024657731529024

After 28 optimization iterations, training data loss is 2.3025037337757612, and validation data loss is 2.302434289157999

After 35 optimization iterations, training data loss is 2.302471417748011, and validation data loss is 2.3024021893657527

After 42 optimization iterations, training data loss is 2.302429461368185, and validation data loss is 2.3023597450783813

After 49 optimization iterations, training data loss is 2.302395320339885, and validation data loss is 2.3023273136661047

After 56 optimization iterations, training data loss is 2.302355289106732, and validation data loss is 2.302287095990645

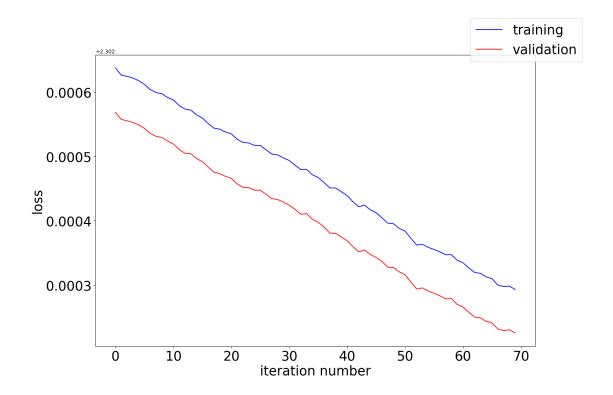
After 63 optimization iterations, training data loss is 2.3023194864578405, and validation data loss is 2.302250331078315

After 70 optimization iterations, training data loss is 2.3022931081482074, and validation data loss is 2.3022255410002384

Now testing the gradient on just a mini-batch instead of the whole training set...

Gradient test passed for hid_to_class. Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).



The total loss on the training data is 2.3022931081482074

The classification loss (i.e. without weight decay) on the training data is 2.3022931081482074

The classification error rate on the training data is 0.897

The total loss on the validation data is 2.3022255410002384

The classification loss (i.e. without weight decay) on the validation data is 2.3022255410002384

The classification error rate on the validation data is 0.898

The total loss on the test data is 2.3022526843851967

The classification loss (i.e. without weight decay) on the test data is 2.3022526843851967

The classification error rate on the test data is 0.895

[9]: a2(0, 10, 70, 0.01, 0, False, 4)

Now testing the gradient on the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001%% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).

After 7 optimization iterations, training data loss is 2.3024552683451076, and validation data loss is 2.3023906286460742

After 14 optimization iterations, training data loss is 2.302297582234424, and validation data loss is 2.302233443721875

After 21 optimization iterations, training data loss is 2.3021129528245314, and validation data loss is 2.302042276395394

After 28 optimization iterations, training data loss is 2.30195621918477, and validation data loss is 2.3018846557884483

After 35 optimization iterations, training data loss is 2.301791772390124, and validation data loss is 2.301721302195465

After 42 optimization iterations, training data loss is 2.3015853406613815, and validation data loss is 2.3015124422278097

After 49 optimization iterations, training data loss is 2.3014150373714997, and validation data loss is 2.301350680390506

After 56 optimization iterations, training data loss is 2.3012148850962446, and validation data loss is 2.301149618073701

After 63 optimization iterations, training data loss is 2.3010365412147777, and validation data loss is 2.3009664718489464

After 70 optimization iterations, training data loss is 2.3009006724646897, and validation data loss is 2.3008385536916567

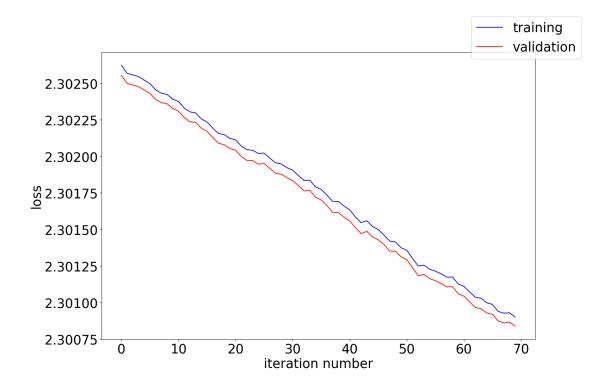
Now testing the gradient on just a mini-batch instead of the whole training

set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001%% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).



The total loss on the training data is 2.3009006724646897

The classification loss (i.e. without weight decay) on the training data is 2.3009006724646897

The classification error rate on the training data is 0.886

The total loss on the validation data is 2.3008385536916567

The classification loss (i.e. without weight decay) on the validation data is 2.3008385536916567

The classification error rate on the validation data is 0.887

The total loss on the test data is 2.300854001904353

The classification loss (i.e. without weight decay) on the test data is 2.300854001904353

The classification error rate on the test data is 0.88166666666666667

[10]: a2(0, 10, 70, 0.05, 0, False, 4)

Now testing the gradient on the whole training set ...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).

After 7 optimization iterations, training data loss is 2.3017738673111223, and validation data loss is 2.3017267523295453

After 14 optimization iterations, training data loss is 2.301002353575769, and validation data loss is 2.300957756628203

After 21 optimization iterations, training data loss is 2.3000716047410164, and validation data loss is 2.299994828079743

After 28 optimization iterations, training data loss is 2.299265340148979, and validation data loss is 2.299184558841718

After 35 optimization iterations, training data loss is 2.298360684957857, and validation data loss is 2.2982852385950183

After 42 optimization iterations, training data loss is 2.2973286018142134, and validation data loss is 2.2972416728022447

After 49 optimization iterations, training data loss is 2.296406009560148, and validation data loss is 2.296362261705057

After 56 optimization iterations, training data loss is 2.2952863962740557, and validation data loss is 2.2952398915093526

After 63 optimization iterations, training data loss is 2.2942723433523486, and validation data loss is 2.29420266941243

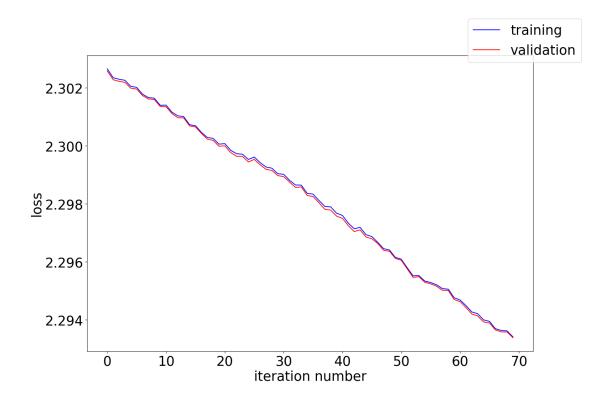
After 70 optimization iterations, training data loss is 2.2934118640834638, and validation data loss is 2.2933835722400375

Now testing the gradient on just a mini-batch instead of the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001%% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).



The total loss on the training data is 2.2934118640834638

The classification loss (i.e. without weight decay) on the training data is 2.2934118640834638

The classification error rate on the training data is 0.765

The total loss on the validation data is 2.2933835722400375

The classification loss (i.e. without weight decay) on the validation data is 2.2933835722400375

The classification error rate on the validation data is 0.766

The total loss on the test data is 2.2933294102198447

The classification loss (i.e. without weight decay) on the test data is 2.2933294102198447

The classification error rate on the test data is 0.7576666666666667

[11]: a2(0, 10, 70, 0.2, 0, False, 4)

Now testing the gradient on the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001%% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).

After 7 optimization iterations, training data loss is 2.2998186272412102, and validation data loss is 2.299845785723998

After 14 optimization iterations, training data loss is 2.296523212630369, and validation data loss is 2.296548875548235

After 21 optimization iterations, training data loss is 2.292173208378639, and validation data loss is 2.2920876391449765

After 28 optimization iterations, training data loss is 2.287752802332703, and validation data loss is 2.2876742660413685

After 35 optimization iterations, training data loss is 2.2820078100912022, and validation data loss is 2.2819382701810915

After 42 optimization iterations, training data loss is 2.2743706863363853, and validation data loss is 2.2742967218075636

After 49 optimization iterations, training data loss is 2.265194570580782, and validation data loss is 2.2653619324217233

After 56 optimization iterations, training data loss is 2.2518845971525456, and validation data loss is 2.2521737288357193

After 63 optimization iterations, training data loss is 2.236970156868212, and validation data loss is 2.237258560331139

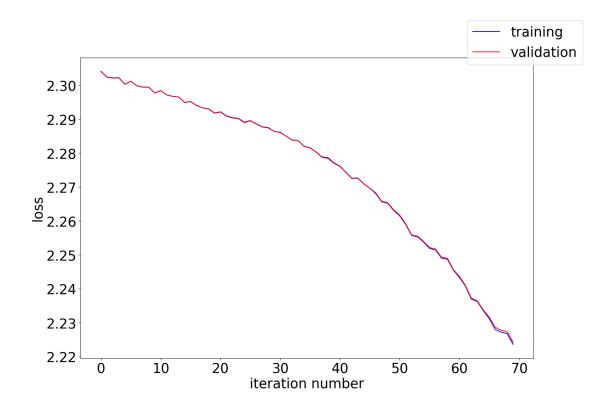
After 70 optimization iterations, training data loss is 2.2235813589660016, and validation data loss is 2.224201123725473

Now testing the gradient on just a mini-batch instead of the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001%% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).



The total loss on the training data is 2.2235813589660016

The classification loss (i.e. without weight decay) on the training data is 2.2235813589660016

The classification error rate on the training data is 0.801

The total loss on the validation data is 2.224201123725473

The classification loss (i.e. without weight decay) on the validation data is 2.224201123725473

The classification error rate on the validation data is 0.797

The total loss on the test data is 2.222849187609189

The classification loss (i.e. without weight decay) on the test data is 2.222849187609189

The classification error rate on the test data is 0.79566666666666666

[12]: a2(0, 10, 70, 1.0, 0, False, 4)

Now testing the gradient on the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001%% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).

After 7 optimization iterations, training data loss is 2.288632771565589, and validation data loss is 2.2894001227767964

After 14 optimization iterations, training data loss is 2.2740065933806797, and validation data loss is 2.2749978891062344

After 21 optimization iterations, training data loss is 2.239245624394231, and validation data loss is 2.2406088548601995

After 28 optimization iterations, training data loss is 2.167752965975292, and validation data loss is 2.1703832013196314

After 35 optimization iterations, training data loss is 2.064690677036345, and validation data loss is 2.0683542079341324

After 42 optimization iterations, training data loss is 1.9548602774911705, and validation data loss is 1.9591103260327536

After 49 optimization iterations, training data loss is 1.8497568912452225, and validation data loss is 1.858573464810318

After 56 optimization iterations, training data loss is 1.7703130911939102, and validation data loss is 1.7833624668563843

After 63 optimization iterations, training data loss is 1.706710503793043, and validation data loss is 1.7180966243310214

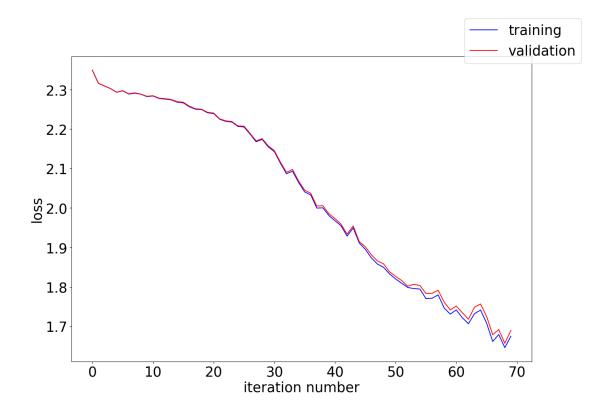
After 70 optimization iterations, training data loss is 1.674933214461265, and validation data loss is 1.6900252783448697

Now testing the gradient on just a mini-batch instead of the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).



The total loss on the training data is 1.674933214461265

The classification loss (i.e. without weight decay) on the training data is 1.674933214461265

The classification error rate on the training data is 0.697

The total loss on the validation data is 1.6900252783448697

The classification loss (i.e. without weight decay) on the validation data is 1.6900252783448697

The classification error rate on the validation data is 0.714

The total loss on the test data is 1.676162605073363

The classification loss (i.e. without weight decay) on the test data is 1.676162605073363

The classification error rate on the test data is 0.703222222222222

[13]: a2(0, 10, 70, 5.0, 0, False, 4)

Now testing the gradient on the whole training set ...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).

After 7 optimization iterations, training data loss is 2.302067196784302, and validation data loss is 2.302340910584947

After 14 optimization iterations, training data loss is 2.3020191850189793, and validation data loss is 2.3023001127502645

After 21 optimization iterations, training data loss is 2.302014482280857, and validation data loss is 2.302296675017002

After 28 optimization iterations, training data loss is 2.3019893530648567, and validation data loss is 2.3022820933145955

After 35 optimization iterations, training data loss is 2.301980512310046, and validation data loss is 2.302281410337269

After 42 optimization iterations, training data loss is 2.301902179137929, and validation data loss is 2.302240807694258

After 49 optimization iterations, training data loss is 2.3018942353043887, and

validation data loss is 2.3022192579508376

After 56 optimization iterations, training data loss is 2.301630568304788, and validation data loss is 2.302088602304471

After 63 optimization iterations, training data loss is 2.3016214258765095, and validation data loss is 2.3020443490933222

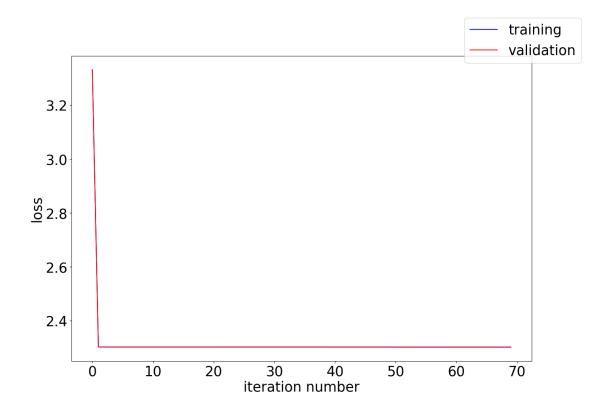
After 70 optimization iterations, training data loss is 2.3016188038504537, and validation data loss is 2.3020434221578814

Now testing the gradient on just a mini-batch instead of the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).



The total loss on the training data is 2.3016188038504537

The classification loss (i.e. without weight decay) on the training data is 2.3016188038504537

The classification error rate on the training data is 0.899

The total loss on the validation data is 2.3020434221578814

The classification loss (i.e. without weight decay) on the validation data is 2.3020434221578814

The classification error rate on the validation data is 0.9

The total loss on the test data is 2.302442636292494

The classification loss (i.e. without weight decay) on the test data is 2.302442636292494

[14]: a2(0, 10, 70, 20.0, 0, False, 4)

Now testing the gradient on the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input to hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001%% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).

After 7 optimization iterations, training data loss is 2.302585091837178, and validation data loss is 2.3025850910767875

After 14 optimization iterations, training data loss is 2.302585091837178, and validation data loss is 2.3025850910767875

After 21 optimization iterations, training data loss is 2.302585091837178, and validation data loss is 2.3025850910767875

After 28 optimization iterations, training data loss is 2.302585091837178, and validation data loss is 2.3025850910767875

After 35 optimization iterations, training data loss is 2.302585091837178, and validation data loss is 2.3025850910767875

After 42 optimization iterations, training data loss is 2.302585091837178, and validation data loss is 2.3025850910767875

After 49 optimization iterations, training data loss is 2.302585091837178, and validation data loss is 2.3025850910767875

After 56 optimization iterations, training data loss is 2.3025850918371775, and validation data loss is 2.302585091076785

After 63 optimization iterations, training data loss is 2.3025850918371775, and validation data loss is 2.302585091076785

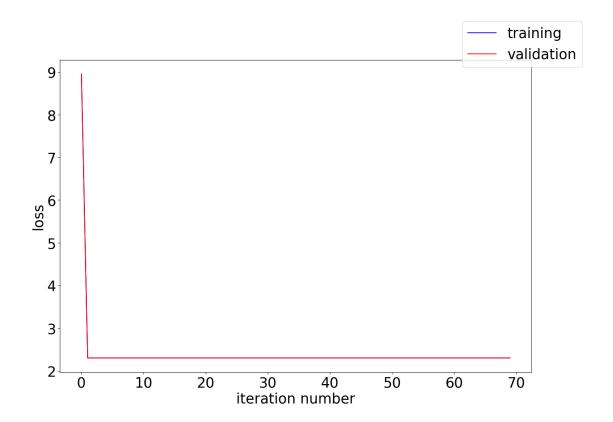
After 70 optimization iterations, training data loss is 2.3025850918371775, and validation data loss is 2.302585091076785

Now testing the gradient on just a mini-batch instead of the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001%% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).



The total loss on the training data is 2.3025850918371775

The classification loss (i.e. without weight decay) on the training data is 2.3025850918371775

The classification error rate on the training data is 0.9

The total loss on the validation data is 2.302585091076785

The classification loss (i.e. without weight decay) on the validation data is 2.302585091076785

The classification error rate on the validation data is 0.9

The total loss on the test data is 2.3025850220361597

The classification loss (i.e. without weight decay) on the test data is 2.3025850220361597

The classification error rate on the test data is 0.9

```
[15]: #try with momentum = 0.9
a2(0, 10, 70, 0.002, 0.9, False, 4)
```

Now testing the gradient on the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001%% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).

After 7 optimization iterations, training data loss is 2.3025220073253787, and validation data loss is 2.3024543319222457

After 14 optimization iterations, training data loss is 2.3022850269062314, and validation data loss is 2.3022204310423118

After 21 optimization iterations, training data loss is 2.301973937768185, and validation data loss is 2.301908906063454

After 28 optimization iterations, training data loss is 2.3016673234667206, and validation data loss is 2.3015975800942

After 35 optimization iterations, training data loss is 2.301362642120604, and validation data loss is 2.301292370391952

After 42 optimization iterations, training data loss is 2.301016759188716, and validation data loss is 2.300941506610587

After 49 optimization iterations, training data loss is 2.300650985578013, and validation data loss is 2.3005793371911767

After 56 optimization iterations, training data loss is 2.3002596286331856, and validation data loss is 2.3001943676292913

After 63 optimization iterations, training data loss is 2.2999095721273934, and validation data loss is 2.299843602349599

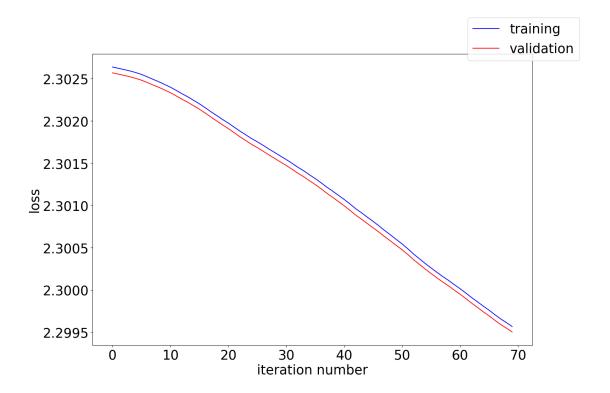
After 70 optimization iterations, training data loss is 2.2995666217165343, and validation data loss is 2.299502143963026

Now testing the gradient on just a mini-batch instead of the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001%% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).



The total loss on the training data is 2.2995666217165343

The classification loss (i.e. without weight decay) on the training data is 2.2995666217165343

The classification error rate on the training data is 0.848

The total loss on the validation data is 2.299502143963026

The classification loss (i.e. without weight decay) on the validation data is 2.299502143963026

The classification error rate on the validation data is 0.839

The total loss on the test data is 2.29951033761895

The classification loss (i.e. without weight decay) on the test data is 2.29951033761895

The classification error rate on the test data is 0.850777777777777

[16]: a2(0, 10, 70, 0.01, 0.9, False, 4)

Now testing the gradient on the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).

After 7 optimization iterations, training data loss is 2.3020813945993357, and validation data loss is 2.3020187410306927

After 14 optimization iterations, training data loss is 2.3009380114989297, and validation data loss is 2.3008911765811164

After 21 optimization iterations, training data loss is 2.2993772208619867, and validation data loss is 2.2993287631006223

After 28 optimization iterations, training data loss is 2.2978194866837964, and validation data loss is 2.2977479808271046

After 35 optimization iterations, training data loss is 2.2962135486738213, and validation data loss is 2.296139801365338

After 42 optimization iterations, training data loss is 2.294351957179535, and validation data loss is 2.294253983382684

After 49 optimization iterations, training data loss is 2.292273720128319, and validation data loss is 2.292195676733541

After 56 optimization iterations, training data loss is 2.2898782825276793, and validation data loss is 2.2898348258583265

After 63 optimization iterations, training data loss is 2.287560557562744, and validation data loss is 2.287517928063843

After 70 optimization iterations, training data loss is 2.285062439744801, and validation data loss is 2.285036193485089

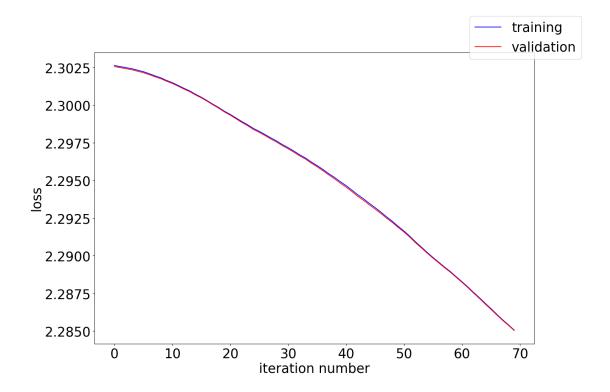
Now testing the gradient on just a mini-batch instead of the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001%% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not

certainly, but probably).



The total loss on the training data is 2.285062439744801

The classification loss (i.e. without weight decay) on the training data is 2.285062439744801

The classification error rate on the training data is 0.751

The total loss on the validation data is 2.285036193485089

The classification loss (i.e. without weight decay) on the validation data is 2.285036193485089

The classification error rate on the validation data is 0.756

The total loss on the test data is 2.284912589785349

The classification loss (i.e. without weight decay) on the test data is 2.284912589785349

The classification error rate on the test data is 0.76166666666666667

[17]: a2(0, 10, 70, 0.05, 0.9, False, 4)

Now testing the gradient on the whole training set ...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001%% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).

After 7 optimization iterations, training data loss is 2.3005679758421396, and validation data loss is 2.3005343196843526

After 14 optimization iterations, training data loss is 2.294690290846375, and validation data loss is 2.294746863670597

After 21 optimization iterations, training data loss is 2.2848258595613196, and validation data loss is 2.284874532284197

After 28 optimization iterations, training data loss is 2.2727373216064093, and validation data loss is 2.2726641075461638

After 35 optimization iterations, training data loss is 2.25555407462529, and validation data loss is 2.2554664120483583

After 42 optimization iterations, training data loss is 2.2274351873988976, and validation data loss is 2.2273050892212876

After 49 optimization iterations, training data loss is 2.183651335804252, and validation data loss is 2.1839613369615654

After 56 optimization iterations, training data loss is 2.123048056013555, and validation data loss is 2.1239245408160095

After 63 optimization iterations, training data loss is 2.0584067828771593, and validation data loss is 2.059957243385048

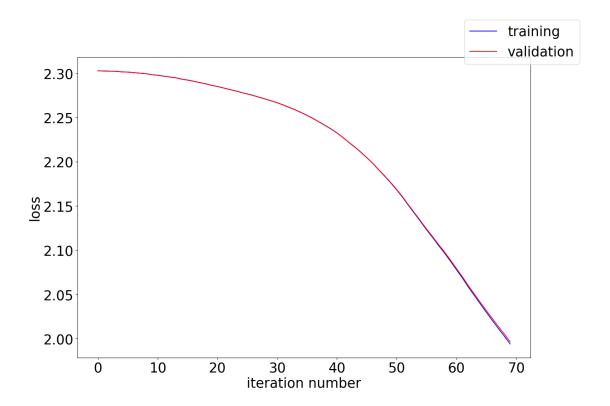
After 70 optimization iterations, training data loss is 1.9940517127340163, and validation data loss is 1.9965592899672242

Now testing the gradient on just a mini-batch instead of the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).



The total loss on the training data is 1.9940517127340163

The classification loss (i.e. without weight decay) on the training data is 1.9940517127340163

The classification error rate on the training data is 0.708

The total loss on the validation data is 1.9965592899672242

The classification loss (i.e. without weight decay) on the validation data is 1.9965592899672242

The classification error rate on the validation data is 0.7

The total loss on the test data is 1.9891214271086306

The classification loss (i.e. without weight decay) on the test data is 1.9891214271086306

[18]: a2(0, 10, 70, 0.2, 0.9, False, 4)

Now testing the gradient on the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001%% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).

After 7 optimization iterations, training data loss is 2.2962604475303907, and validation data loss is 2.296427744922369

After 14 optimization iterations, training data loss is 2.2579364788991034, and validation data loss is 2.2586294562618083

After 21 optimization iterations, training data loss is 2.160121574696398, and validation data loss is 2.1604465477872683

After 28 optimization iterations, training data loss is 1.9896511913758645, and validation data loss is 1.9915902358021196

After 35 optimization iterations, training data loss is 1.8196056237510982, and validation data loss is 1.8235035235068375

After 42 optimization iterations, training data loss is 1.6998341654758864, and validation data loss is 1.7113373685413482

After 49 optimization iterations, training data loss is 1.5557933603105996, and validation data loss is 1.5751828655649056

After 56 optimization iterations, training data loss is 1.457982907852304, and validation data loss is 1.485891949135234

After 63 optimization iterations, training data loss is 1.3872728587256975, and validation data loss is 1.4365642633107423

After 70 optimization iterations, training data loss is 1.2924955789540329, and validation data loss is 1.3372647971195855

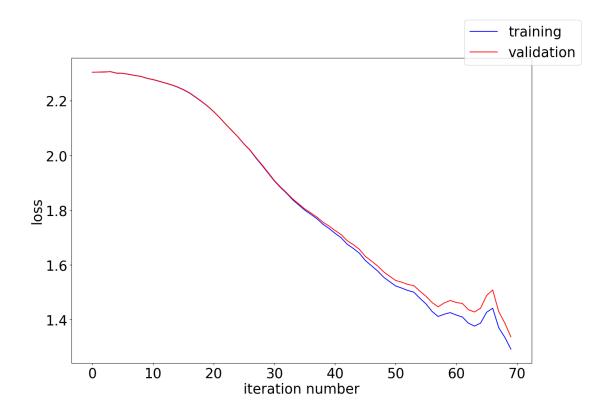
Now testing the gradient on just a mini-batch instead of the whole training

set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001%% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).



The total loss on the training data is 1.2924955789540329

The classification loss (i.e. without weight decay) on the training data is 1.2924955789540329

The classification error rate on the training data is 0.409

The total loss on the validation data is 1.3372647971195855

The classification loss (i.e. without weight decay) on the validation data is 1.3372647971195855

The classification error rate on the validation data is 0.423

The total loss on the test data is 1.301506175378702

The classification loss (i.e. without weight decay) on the test data is 1.301506175378702

The classification error rate on the test data is 0.407

[19]: a2(0, 10, 70, 1.0, 0.9, False, 4)

Now testing the gradient on the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).

After 7 optimization iterations, training data loss is 2.2888414340263377, and validation data loss is 2.2899073907965075

After 14 optimization iterations, training data loss is 2.223790743518183, and validation data loss is 2.229455494094939

After 21 optimization iterations, training data loss is 2.155925194578511, and validation data loss is 2.164376997320488

After 28 optimization iterations, training data loss is 2.2765877201020124, and validation data loss is 2.2793687668534575

After 35 optimization iterations, training data loss is 2.2184360338093594, and validation data loss is 2.226489978348415

After 42 optimization iterations, training data loss is 2.0235643717010214, and validation data loss is 2.040535030890207

After 49 optimization iterations, training data loss is 1.925252962587876, and validation data loss is 1.928535766294873

After 56 optimization iterations, training data loss is 1.950692631253381, and validation data loss is 1.9650248878282532

After 63 optimization iterations, training data loss is 1.930966104869863, and validation data loss is 1.978541742080101

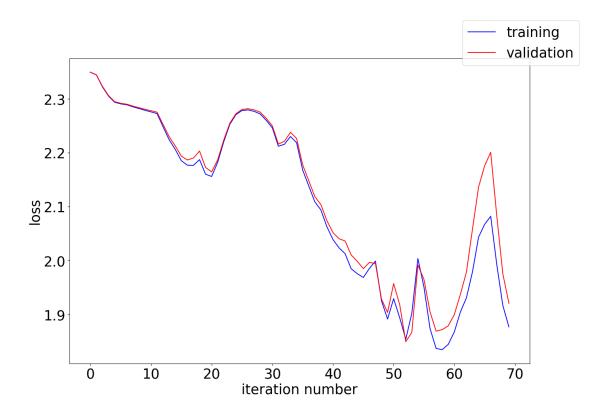
After 70 optimization iterations, training data loss is 1.8770514360277157, and validation data loss is 1.9209129479143945

Now testing the gradient on just a mini-batch instead of the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).



The total loss on the training data is 1.8770514360277157

The classification loss (i.e. without weight decay) on the training data is 1.8770514360277157

The classification error rate on the training data is 0.721

The total loss on the validation data is 1.9209129479143945

The classification loss (i.e. without weight decay) on the validation data is 1.9209129479143945

The classification error rate on the validation data is 0.737

The total loss on the test data is 1.8974511412914217

The classification loss (i.e. without weight decay) on the test data is 1.8974511412914217

The classification error rate on the test data is 0.7242222222222222

[20]: a2(0, 10, 70, 5.0, 0.9, False, 4)

Now testing the gradient on the whole training set ...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001%% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).

After 7 optimization iterations, training data loss is 2.3025850783281085, and validation data loss is 2.302585023871894

After 14 optimization iterations, training data loss is 2.302585092986651, and validation data loss is 2.3025850929239517

After 21 optimization iterations, training data loss is 2.3025850929938483, and validation data loss is 2.3025850929915532

After 28 optimization iterations, training data loss is 2.302585092994011, and validation data loss is 2.302585092993543

After 35 optimization iterations, training data loss is 2.302585092994031, and validation data loss is 2.3025850929938123

After 42 optimization iterations, training data loss is 2.302585092994036, and validation data loss is 2.302585092993884

After 49 optimization iterations, training data loss is 2.3025850929940375, and validation data loss is 2.30258509299391

After 56 optimization iterations, training data loss is 2.302585092994038, and validation data loss is 2.3025850929939207

After 63 optimization iterations, training data loss is 2.302585092994039, and validation data loss is 2.302585092993926

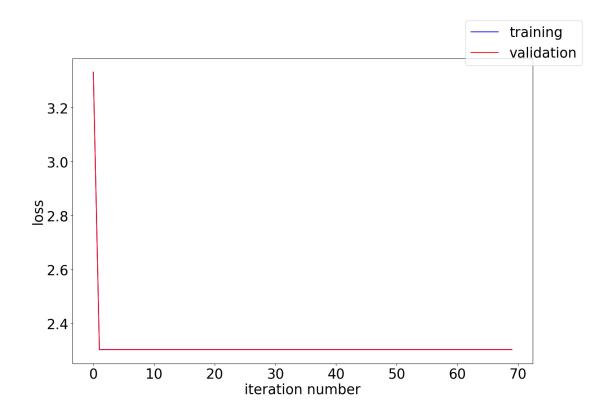
After 70 optimization iterations, training data loss is 2.302585092994039, and validation data loss is 2.3025850929939278

Now testing the gradient on just a mini-batch instead of the whole training set...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).



The total loss on the training data is 2.302585092994039

The classification loss (i.e. without weight decay) on the training data is 2.302585092994039

The classification error rate on the training data is 0.886

The total loss on the validation data is 2.3025850929939278

The classification loss (i.e. without weight decay) on the validation data is 2.3025850929939278

The classification error rate on the validation data is 0.897

The total loss on the test data is 2.3025850919707307

The classification loss (i.e. without weight decay) on the test data is 2.3025850919707307

The classification error rate on the test data is 0.887777777777778

[21]: a2(0, 10, 70, 20.0, 0.9, False, 4)

Now testing the gradient on the whole training set ...

Gradient test passed for hid_to_class.

Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).

After 7 optimization iterations, training data loss is 2.3025850929940463, and validation data loss is 2.3025850929940463

After 14 optimization iterations, training data loss is 2.3025850929940463, and validation data loss is 2.3025850929940463

After 21 optimization iterations, training data loss is 2.3025850929940463, and validation data loss is 2.3025850929940463

After 28 optimization iterations, training data loss is 2.3025850929940463, and validation data loss is 2.3025850929940463

After 35 optimization iterations, training data loss is 2.3025850929940463, and validation data loss is 2.3025850929940463

After 42 optimization iterations, training data loss is 2.3025850929940463, and validation data loss is 2.3025850929940463

After 49 optimization iterations, training data loss is 2.3025850929940463, and

validation data loss is 2.3025850929940463

After 56 optimization iterations, training data loss is 2.3025850929940463, and validation data loss is 2.3025850929940463

After 63 optimization iterations, training data loss is 2.3025850929940463, and validation data loss is 2.3025850929940463

After 70 optimization iterations, training data loss is 2.3025850929940463, and validation data loss is 2.3025850929940463

Now testing the gradient on just a mini-batch instead of the whole training set...

Gradient test passed for hid_to_class.

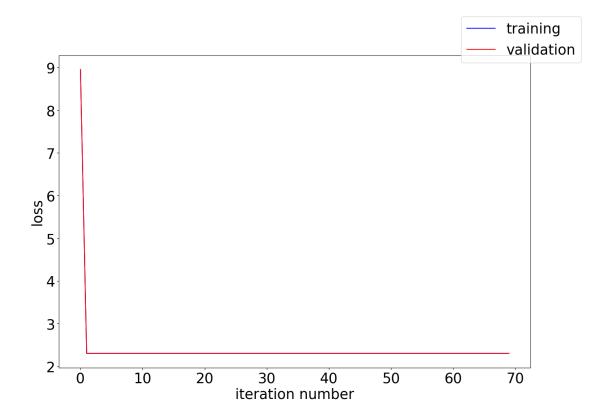
Gradient test passed for input_to_hid.

Gradient test passed. That means that the gradient that your code computed is within 0.001% of the gradient that the finite difference approximation computed, so the gradient calculation procedure is probably correct (not certainly, but probably).

/notebooks/compvis2024/exercise-09/utils.py:50: RuntimeWarning: overflow encountered in exp

ret = 1 / (1 + np.exp(-input))

/tmp/ipykernel_567/1086520247.py:20: RuntimeWarning: overflow encountered in exp
hidden = 1 / (1 + np.exp(-hidden))



The total loss on the training data is 2.3025850929940463

The classification loss (i.e. without weight decay) on the training data is 2.3025850929940463

The classification error rate on the training data is 0.874

The total loss on the validation data is 2.3025850929940463

The classification loss (i.e. without weight decay) on the validation data is 2.3025850929940463

The classification error rate on the validation data is 0.882

The total loss on the test data is 2.302585092994046

The classification loss (i.e. without weight decay) on the test data is 2.302585092994046

2 Optimization Experiment: Learning Rate and Momentum

2.0.1 Initial Experiment: No Momentum

We started with a learning rate of 0.005 and no momentum. After running the optimization for 70 iterations, the training loss converged to approximately 2.301771. While this loss steadily decreased, the rate of improvement was slow, indicating that the learning rate may not have been optimal.

Next, we tried increasing the learning rate to 0.5, which significantly improved performance. The loss decreased faster, showing that a higher learning rate can accelerate convergence. However, when we pushed the learning rate to 1.0 or higher, we noticed instability in the training process, with erratic fluctuations in the loss, suggesting that excessively large learning rates may cause the optimization to overshoot the optimal solution.

2.0.2 Introducing Momentum

Momentum was then introduced to smooth the optimization process. With momentum set to 0.9, we observed a more stable and efficient convergence. In particular, a learning rate of 0.2 performed the best. This suggests that momentum helps reduce oscillations, as the curves were more smooth. A learning rate of 1.0 with momentum, although effective, was not as efficient as 0.2, showing that momentum helps to optimize the learning rate by moderating larger updates.

2.0.3 Observations and Conclusion

The experiments revealed that learning rates above 1.0 were too large and led to erratic behavior, while smaller learning rates below 0.2 resulted in slow progress or no change in the loss. With momentum, the learning rate of 0.2 was the most effective in terms of smooth and rapid convergence.

These findings emphasize the importance of choosing an appropriate learning rate and incorporating momentum into the optimization process. Fine-tuning the learning rate around 0.2 to 1.0, combined with momentum, appears to yield the best results for optimizing training loss in this setup.