FYS3120 Classical Mechanics and Electrodynamics

Problem set 4

February 13, 2019

Problem 1

a)

•
$$K = \frac{1}{2}I\dot{\theta}^2 = \frac{b}{2}\frac{1}{3}mb^2\dot{\theta}^2, V = -mb\frac{b}{2}cos\theta$$

•
$$L = K - V = \frac{1}{2} \frac{1}{3} m b^2 \dot{\theta}^2 + m b \frac{l}{2} cos \theta$$

$$\bullet \ \ \tfrac{dL}{dt}(\tfrac{\partial L}{\partial \dot{\theta}}) - \tfrac{\partial L}{\partial \theta} = \tfrac{1}{3} m b^2 \ddot{\theta} + m g \tfrac{b}{2} sin\theta = \ddot{\theta} + \tfrac{3g}{2b} sin\theta = 0$$

• harmonic oscillaotr google

Problem 2

a)

•
$$K = \frac{1}{2}m_1\dot{\vec{r}}_1^2 + \frac{1}{2}m_2\dot{\vec{r}}_2^2, V = |\vec{r}_1 - \vec{r}_2|c$$
, where c is a constant.

•
$$L = K - V = \frac{1}{2}m_1\dot{\vec{r}}_1^2 + \frac{1}{2}m_2\dot{\vec{r}}_2^2 - V(\vec{r}_1, \vec{r}_2)$$

b)
$$\vec{r} = \vec{r_1} - \vec{r_2}$$
, $\vec{R} = \alpha_1 \vec{r_2} + \alpha_2 \vec{r_2}$, $\alpha_1 = \frac{m_1}{m_1 + m_2}$, $\alpha_2 = \frac{m_2}{m_1 + m_2}$