



1404.5951

The background of the slide features two Feynman diagrams illustrating WW scattering on the Higgs pole. The top diagram shows an incoming photon (p) interacting with a W or Z boson (q1) at a vertex, which then splits into a neutrino (ν) and a lepton (l+). The bottom diagram shows an incoming photon (p) interacting with a W or Z boson (q2) at a vertex, which then splits into a lepton (l-) and an anti-neutrino (ν-bar). The central text box is overlaid on these diagrams.

Polarized WW Scattering on the Higgs Pole

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Tilman Plehn


Electroweak symmetry breaking (EWSB)

- EWSB reconciles the W^\pm , Z masses with gauge invariance
- General description:

$$\left. \begin{array}{l} SU(2)_L \times U(1)_Y \text{ gauge symmetry} \\ \text{Gauge bosons } W_\mu^i, B_\mu \\ \text{Some object } \Sigma \end{array} \right\} \xRightarrow{\Sigma \text{ acquires vev}} \left\{ \begin{array}{l} U(1)_Q \\ \text{Massive } W_\mu^\pm, Z_\mu \end{array} \right.$$


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- Alternatives to a fundamental Higgs:
 - No Higgs (Technicolor, ...)
 - Composite Higgs (Little Higgs, Holographic Higgs, ...)

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- Alternatives after the Higgs discovery:
 - ~~No Higgs~~ (Technicolor, ...)
 - Composite Higgs (Little Higgs, Holographic Higgs, ...)

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Gauge boson polarisations

- Counting degrees of freedom:

$$\begin{array}{ccccc} & \text{Massive } W^\pm & & & \text{Gauge boson} \\ & & & & \\ 2 & + & 1 & \stackrel{?!}{=} & 2 \\ \text{transverse} & & \text{longitudinal} & & \text{transverse} \end{array}$$

Gauge boson polarisations

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$$\begin{array}{ccccccc} & \text{Massive } W^\pm & & & \text{Gauge boson} & & \text{Goldstone } w_\pm \\ & & & & & & \\ 2 & + & 1 & = & 2 & + & 1 \\ \text{transverse} & & \text{longitudinal} & & \text{transverse} & & \text{scalar} \end{array}$$

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- Equivalence theorem:

$$\begin{array}{c} w_L^\pm \end{array} \text{ (wavy blue line)} \rightarrow \text{blob} = \begin{array}{c} w_\pm \end{array} \text{ (dashed green line)} \rightarrow \text{blob} + \mathcal{O}\left(\frac{m_W}{E}\right)$$

[Cornwall et al., 1974; Lee et al., 1977]

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$$\begin{array}{c} w_L^\pm \end{array} \text{ (blue wavy line) } \rightarrow \text{ (shaded circle) } = \begin{array}{c} w_\pm \end{array} \text{ (green dashed line) } \rightarrow \text{ (shaded circle) } + \mathcal{O}\left(\frac{m_W}{E}\right)$$

[Cornwall et al., 1974; Lee et al., 1977]

- Longitudinal modes dominate for high energies:

$$p^\mu = (E, 0, 0, p_3)^\mu \quad \varepsilon_T^\mu = \frac{1}{\sqrt{2}}(0, 1, \pm i, 0)^\mu \quad \varepsilon_L^\mu = \frac{1}{m_W}(p_3, 0, 0, E)^\mu$$

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- New Physics can affect W_L , W_T differently

A simple model

- Idea: measure coupling of H to longitudinal and transverse W separately
- SM:

$$\mathcal{L}_{\text{SM}} \supset g_{\text{SM}} HW_{L\mu}^+ W_L^{-\mu} + g_{\text{SM}} HW_{T\mu}^+ W_T^{-\mu}$$

- Our model:

$$\mathcal{L}_{\text{pol}} \supset a_L g_{\text{SM}} HW_{L\mu}^+ W_L^{-\mu} + a_T g_{\text{SM}} HW_{T\mu}^+ W_T^{-\mu}$$

with parameters $a_L, a_T \in \mathbb{R}$

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WW scattering and unitarity

- $W_L^+ W_L^- \rightarrow W_L^+ W_L^-$ scattering in the SM in the limit $s \gg m_H^2$:

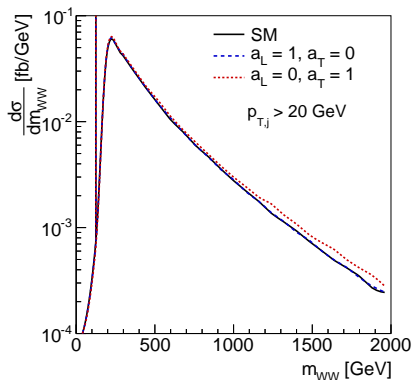
$$\begin{array}{c} \text{t-channel } W \\ \text{u-channel } W \end{array} + \begin{array}{c} \text{s-channel } \gamma, Z \\ \text{t-channel } \gamma, Z \end{array} + \begin{array}{c} \text{s-channel } \gamma, Z \\ \text{u-channel } \gamma, Z \end{array} = i \frac{s+t}{v^2} + \dots$$

$$\begin{array}{c} \text{s-channel } H \\ \text{t-channel } H \end{array} + \begin{array}{c} \text{s-channel } H \\ \text{u-channel } H \end{array} = -i \frac{s+t}{v^2} + \dots$$

- Models with $HW_L W_L$ coupling different from the SM: unitarity violation at $\sqrt{s} \gtrsim 1 \text{ TeV}$

Classical approach: WW scattering at large energies

[Bagger et al., 94–95; Butterworth et al., 02; Ballestrero et al., 09–12; ...]



- Theoretically well motivated
 - W_L equivalent to Goldstones
- Measurement prospects dim
 - Low rates
 - Large scale uncertainties

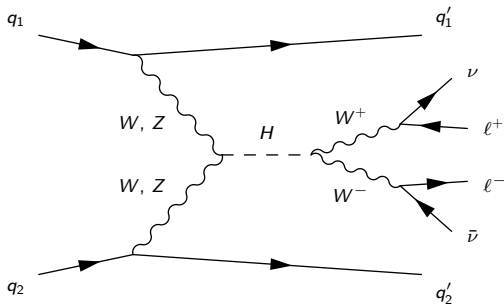
[Han et al., 09]

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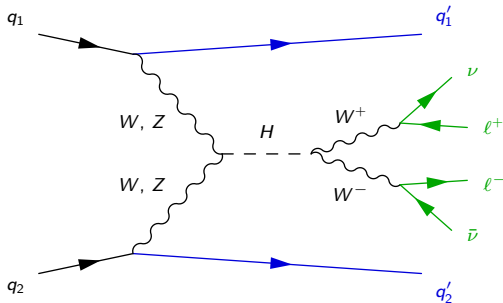
Our approach: WW scattering on the Higgs pole

- Higgs production in weak boson fusion, $H \rightarrow W^+ W^- \rightarrow \ell^+ \nu \ell^- \bar{\nu}$



Our approach: WW scattering on the Higgs pole

- Higgs production in weak boson fusion, $H \rightarrow W^+W^- \rightarrow \ell^+\nu \ell^-\bar{\nu}$



- Choice of observables:

- Leptons, E_T^{miss} sensitive to final polarisations. . . works and has been done

[Han et al., 09]

- Tagging jets sensitive to initial polarisations (our focus)

Motivation: the effective W approximation (EWA)

$$\begin{aligned}
 & \approx \underbrace{q \rightarrow q' + W}_{\text{Emission}} \otimes W \rightarrow Y \\
 & \sim \frac{p_T^3}{(m_W^2 + p_T^2)^2} \text{ for transverse } W, \\
 & \sim \frac{p_T m_W^2}{(m_W^2 + p_T^2)^2} \text{ for longitudinal } W
 \end{aligned}$$

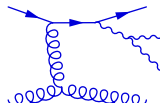
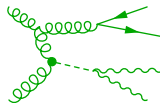
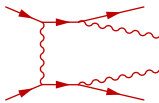
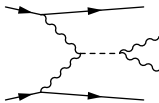
[Kane et al., 84; Dawson, 85]

■ Implication for WBF:

- Hard tagging jets \leftrightarrow transverse initial W
- Soft tagging jets \leftrightarrow longitudinal initial W

Simulation details

- LHC at $\sqrt{s} = 13$ TeV
- Processes (parton level):
 - WBF $H \rightarrow W^+ W^- + 2$ jets at $\mathcal{O}(\alpha^4)$
 - Continuum $W^+ W^- + 2$ jets at $\mathcal{O}(\alpha^4)$
 - GF $H \rightarrow W^+ W^- + 2$ jets at $\mathcal{O}(\alpha_{ggH} \alpha_s^2 \alpha)$
 - Continuum $W^+ W^- + 2$ jets at $\mathcal{O}(\alpha_s^2 \alpha^2)$



- Acceptance cuts:

Leptons	Tagging jets
$ \eta(\ell) < 2.5$	$ \eta(j) < 5.0$
$p_T(\ell) > 10$ GeV	$p_T(j) > 25$ GeV
$p_T(\ell_1) > 20$ GeV	$m_{jj} > 500$ GeV
	$\eta(j_1) \cdot \eta(j_2) < 0$
$p_T^{\text{miss}} > 20$ GeV	$\Delta\eta_{jj} > 4.2$

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Higgs-resonance selection

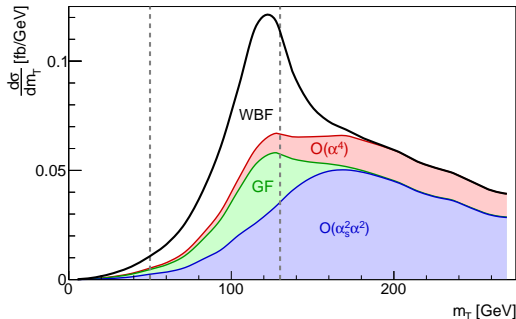
- Transverse mass m_T :

$$m_T^2 = (E_{T,\ell\ell} + E_{T,\nu\nu})^2 - (\mathbf{p}_{T,\ell\ell} + \mathbf{p}_T^{\text{miss}})^2$$

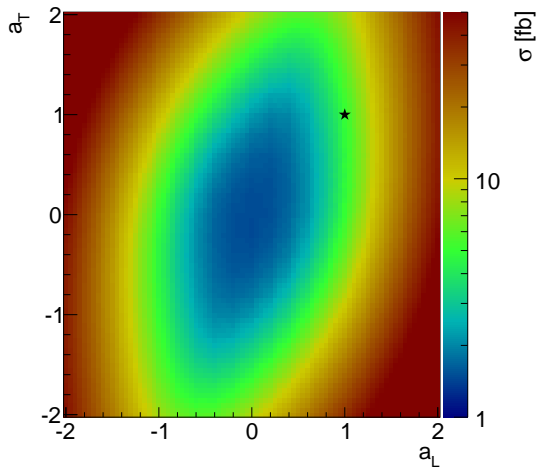
$$E_{T,\ell\ell} = \sqrt{\mathbf{p}_{T,\ell\ell}^2 + m_{\ell\ell}^2}$$

$$E_{T,\nu\nu} = \sqrt{\mathbf{p}_T^{\text{miss}2} + m_{\ell\ell}^2}$$

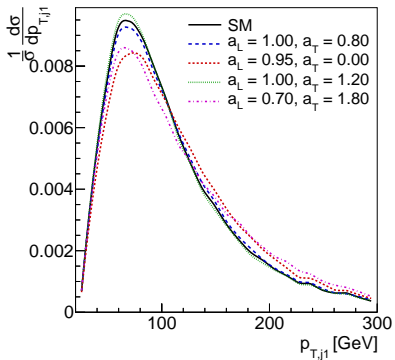
- Higgs-resonance cut: $50 \text{ GeV} < m_T < 130 \text{ GeV}$



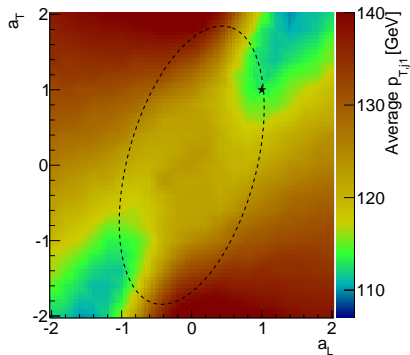
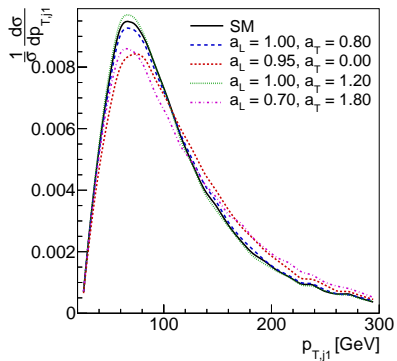
Resonance rate



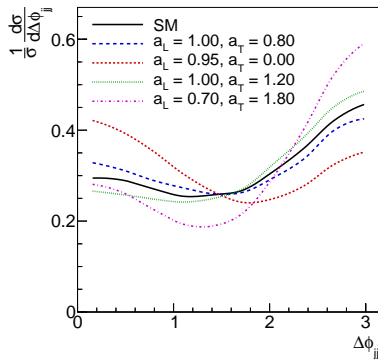
Leading jet p_T



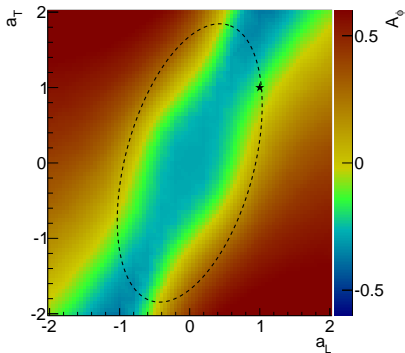
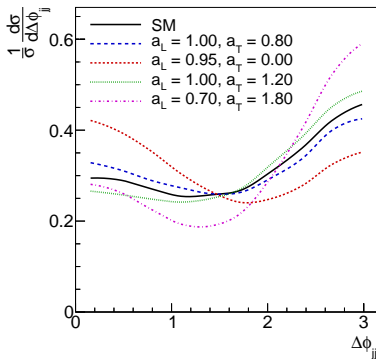
Leading jet p_T



Angular correlation between jets



Angular correlation between jets

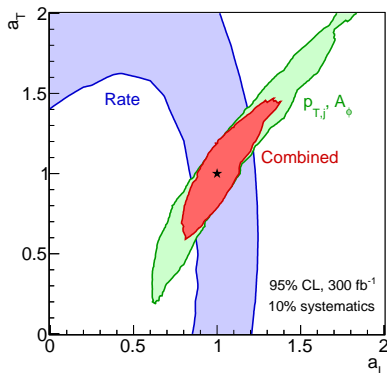
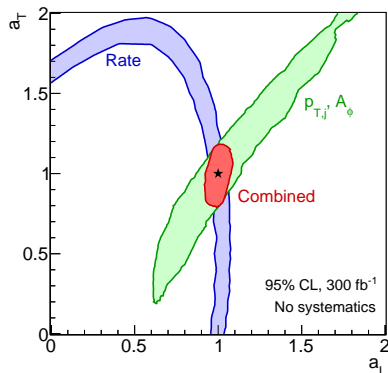


$$A_\phi = \frac{\sigma(\Delta\phi_{jj} < \frac{\pi}{2}) - \sigma(\Delta\phi_{jj} > \frac{\pi}{2})}{\sigma(\Delta\phi_{jj} < \frac{\pi}{2}) + \sigma(\Delta\phi_{jj} > \frac{\pi}{2})}$$

[Eboli et al., 00; Plehn et al., 02, ...]

Significance at LHC Run II

Expected exclusion regions after 300 fb^{-1} , assuming no signal:



Conclusions

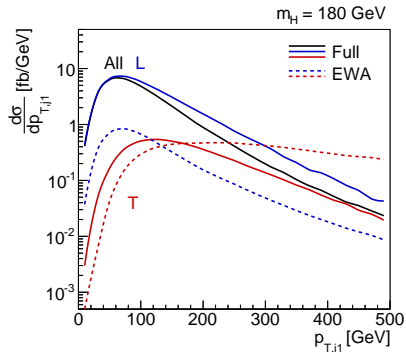
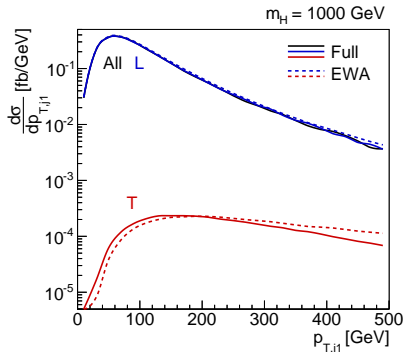
- W polarisations linked to structure of symmetry breaking
- WW scattering at Higgs resonance:
tagging jets probe polarisations of initial WW pair
 - Jet p_T
 - $\Delta\phi$ between jets
- Longitudinal and transverse Higgs–gauge couplings can be probed at $\mathcal{O}(20\%)$ after 300 fb^{-1} of data at 13 TeV

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Bonus material

Validity of the EWA



- $m_H < 2m_W$: on-shell assumption not valid anymore
⇒ cannot use EWA at Higgs resonance

Effective field theory

- New physics at large energies \rightarrow effective operators at low energies
- Models with composite Higgs can e.g. generate

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \frac{c_W}{\Lambda^2} (D_\mu \phi)^\dagger \hat{W}^{\mu\nu} (D_\nu \phi)$$

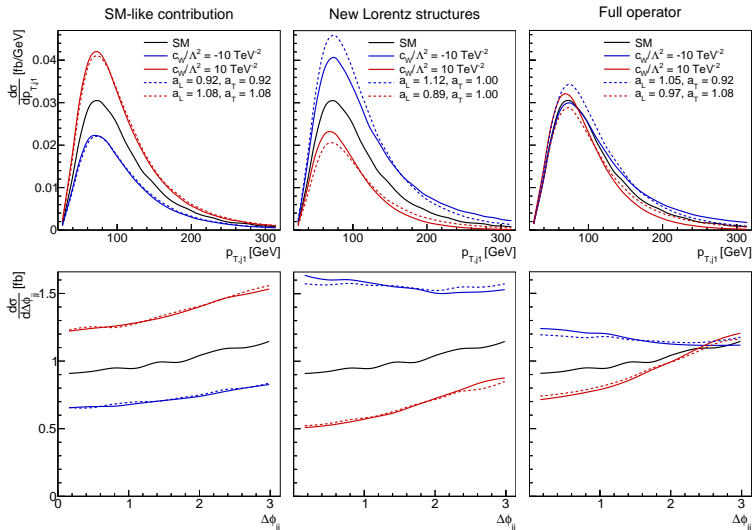
[Giudice et al., 07]

- Modification of HWW vertex:

$$H \text{ --- } \begin{array}{c} W_\mu^+ \\ \text{---} \\ W_\nu^- \end{array} = igm_W \left[\left(1 + \frac{c_W}{2\Lambda^2} m_H^2 \right) \eta_{\mu\nu} + \frac{c_W}{2\Lambda^2} (p_\mu^H p_\nu^+ + p_\mu^- p_\nu^H) \right]$$

- **First term** scales SM vertex $\longleftrightarrow a_L = a_T = 1 + \frac{c_W}{2\Lambda^2} m_H^2$
- **Second term** only affects longitudinal W $\longleftrightarrow a_L$ is momentum-dependent, $a_T = 0$

Dimension-6 operator vs simple model



Polarisations and reference frames

