

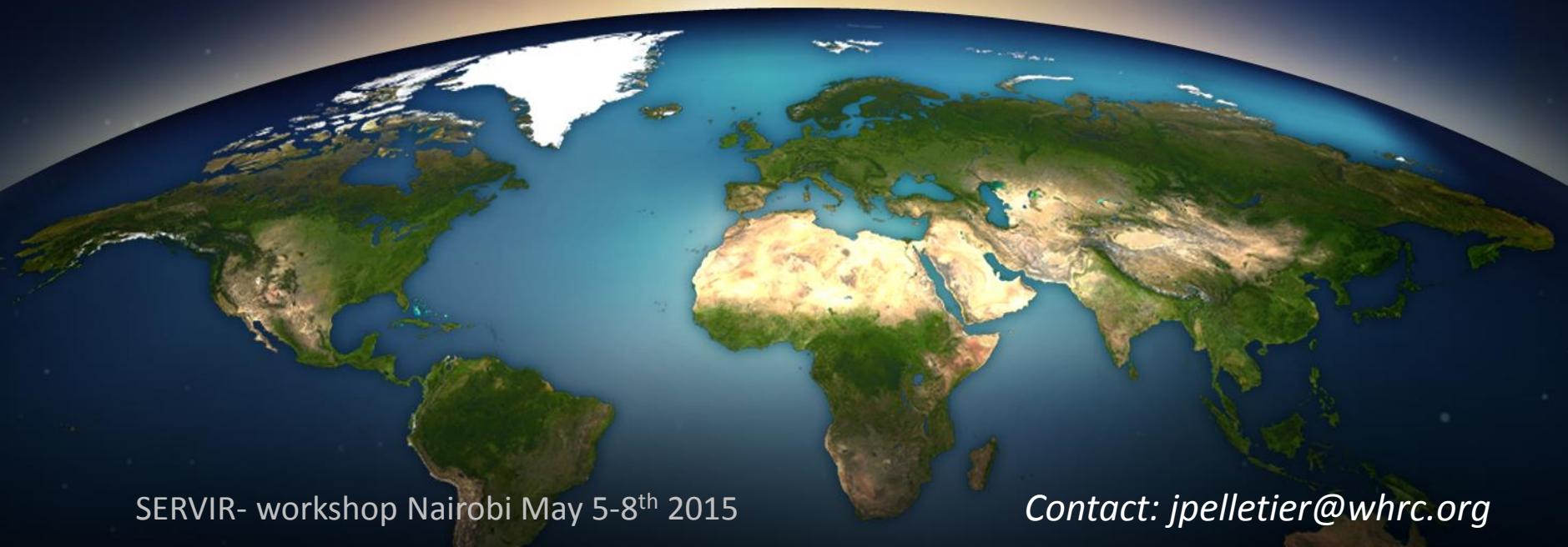
# Forest carbon assessment for REDD+ in the East & South Africa SERVIR region

*“Filling the gap between Carbon Science and policy”*

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SERVIR- workshop Nairobi May 5-8<sup>th</sup> 2015

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**SERVIR** GLOBAL





# Forest Carbon Assessment for REDD+ in the East & South Africa SERVIR Region



## Objectives

Our Project demonstrates how NASA Earth science products and derived models can assist East African countries, including the DR Congo, with their terrestrial carbon assessment and forest conservation strategy. The main focus of the project is:

- **Establishing forest carbon stock baselines and trends**, assessing historical and current carbon emissions from deforestation and degradation (Gov/NGOs/Universities)
- **Identifying corridors of high forest carbon stock** to be preserved and potential areas to be replanted in order to connect parks and protected areas and sustain biological diversity. (*Science WHRC-Implementation GOV/NGOs*)
- **Training and building capacity** in the use of maps, tools and models to be developed as part of this project ( *SERVIR Hub, AMNH, JGI partners*)



Our project is assisting countries with developing strategies for reducing emissions from deforestation and forest degradation (REDD) to effectively decrease forest-based emissions.



# Introduction to GHG and uncertainty estimation



## WORK PLAN:

1. Uncertainty in GHG estimation and in the REDD+ context:
  - Sources of uncertainty
  - IPCC principles
  - MRV in the REDD+ context
2. Components of uncertainty in GHG from land-use/cover change:
  - Land-cover change data (Activity data)
  - Biomass estimation (Emission Factors)
  - Accounting (or modelling) approach
3. Estimating uncertainty (IPCC approach)
  - Tier 1: Error propagation
  - Tier 2: Monte Carlo Method
4. Exercise in R



# Uncertainty in GHG estimation and in the REDD+ context



United Nations  
Framework Convention on  
Climate Change



PARIS2015  
UN CLIMATE CHANGE CONFERENCE  
COP21·CMP11

- First objective “*to stabilize GHG concentrations in the atmosphere at a level that would prevent dangerous anthropogenic interference with the climate system*”



**Uncertainty in GHG estimates can hinder the fulfillment of this objective**

- Are we on the global target 2 C degrees?
- Are countries meeting their pledged emission reduction targets?
- Are carbon trading systems working as well as they should for the climate?

# Sources of emissions & uncertainty

6-17% of global emissions

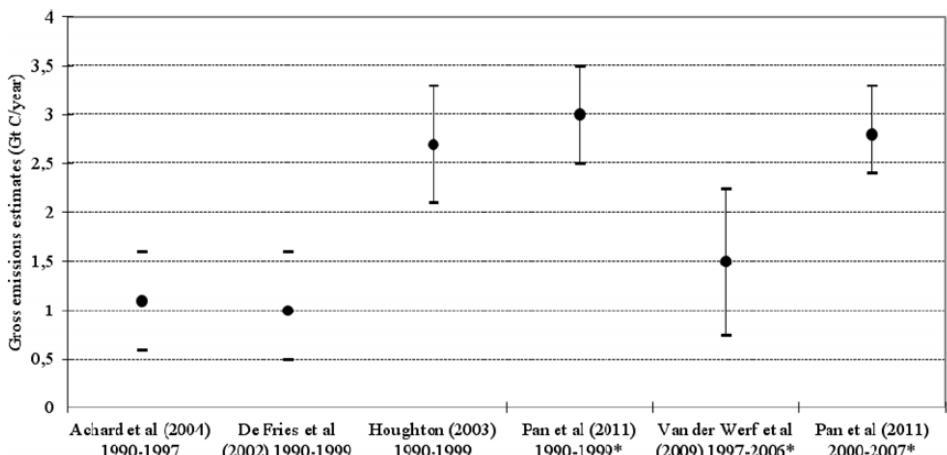
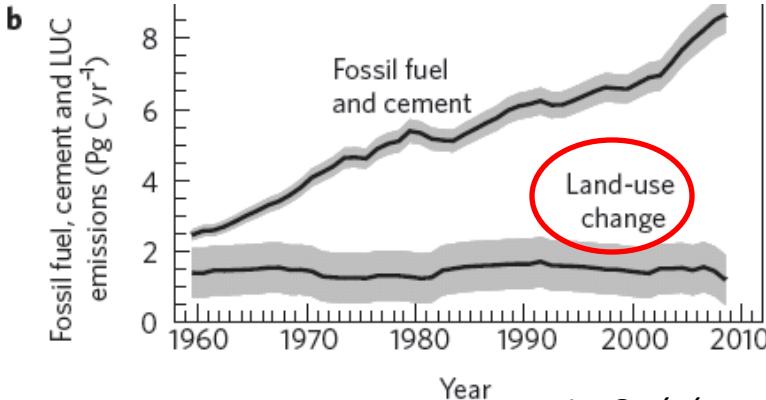
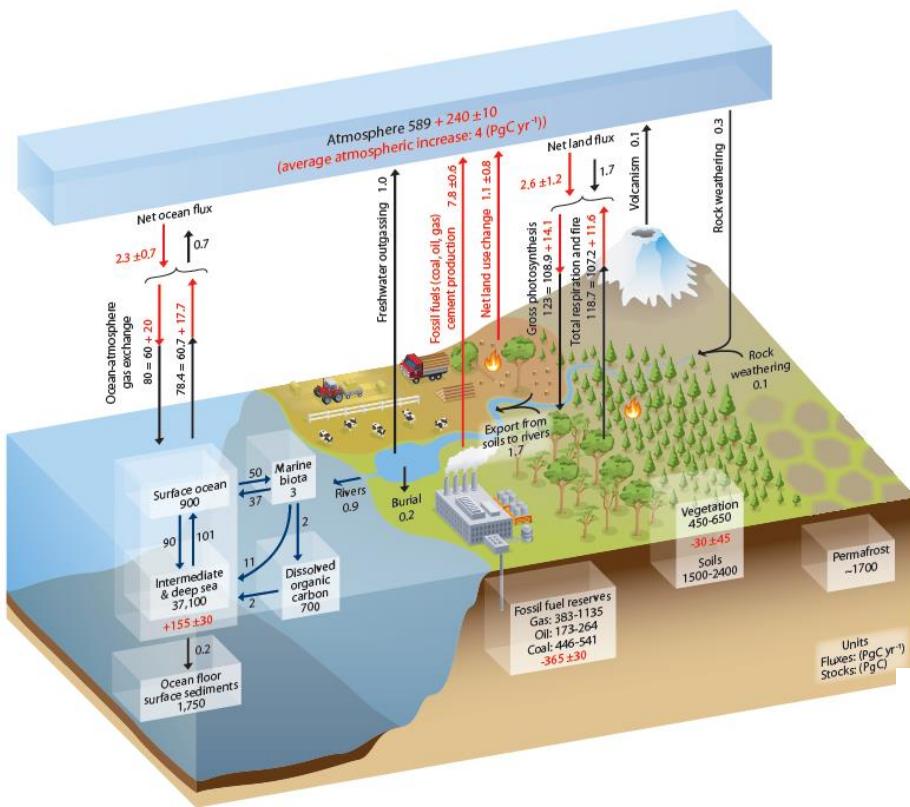
IPCC AR5

Fossil fuel:

$7.8 \pm 0.6 \text{ Pg/yr}$

Land Use Change:

$1.1 \pm 0.8 \text{ Pg/yr}$



Bucki et al. Environmental Research Letters, 2012



# Uncertainty in GHG estimation and in the REDD+ context



## Policy requirements

**UNFCCC**: parties are encouraged, but not obliged, to report on uncertainty in their national GHG inventory

**Kyoto Protocol**: GHG inventory uncertainty is monitored, but it is not regulated, which means that there are no rules to limit or discount for uncertainty when evaluating compliance.

\*\*\*

## Market requirements

**Carbon trading**: UNFCCC does not provide compulsory instructions on how uncertainty must be addressed, and uncertainty is generally ignored (Marland et al. 2009).

BUT NOT FOR LONG

# Five estimating and reporting principles:

**Transparency:** All the assumptions and the methodologies clearly explained time



**Consistency:** The same methodologies and consistent data sets are used along time

**Comparability:** Estimates of emissions and removals should be comparable among parties

**Completeness:** Estimates should include—for all the relevant geographical coverage—all the agreed categories, gases and pools

**Accuracy:** Estimates should be systematically neither over nor under the true value, so far as can be judged, and that uncertainties are reduced so far as is practicable

# Calculating carbon emissions

The general approach for calculating carbon emissions:

$$\text{Emissions} = \text{Activity data (AD)} \times \text{Emission Factor (EF)}$$

**Activity data** refers to the area of forest change (in hectare), e.g., forest converted to grassland or forest converted to cropland,

**Emission factor** relates to the carbon stock change estimations per unit of activity (in carbon per hectare).



# For Emission Factors

**Gain-Loss Method** based on estimates of annual change in biomass from estimates of biomass gain and loss

Where:

- $\Delta CB$  = annual change in carbon stocks in biomass
- $\Delta CG$  = annual increase in carbon stocks due to biomass growth
- $\Delta CL$  = annual decrease in carbon stocks due to biomass loss

\*\*\*

**Stock-Difference Method** which estimates the difference in total biomass carbon stock at time  $t_2$  and time  $t_1$

- Where:
  - $\Delta C$  = annual carbon stock change in the pool, tC/yr
  - $C_{t_1}$  = carbon stock in the pool at time  $t_1$ , tonnes C
  - $C_{t_2}$  = carbon stock in the pool at time  $t_2$ , tonnes C





# Tier approach for emission factor

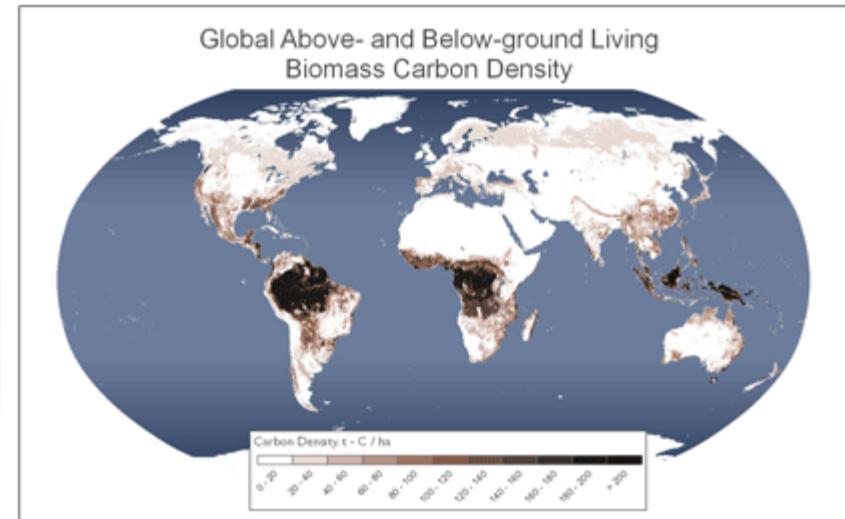


## Level of methodological complexity:

**Tier 1:** Uses IPCC default parameters

**Tier 2:** Requires some country-specific carbon data

**Tier 3:** Uses highly disaggregated national data of carbon pools and assesses any change in pools through repeated measurements and/or modeling.





# Approaches for activity data



## Approach for activity data: Area change

1. total area for each land use category, but no information on conversions (only net changes)
2. tracking of conversions between land-use categories (only between 2 points in time)
3. spatially explicit tracking of land-use conversions over time

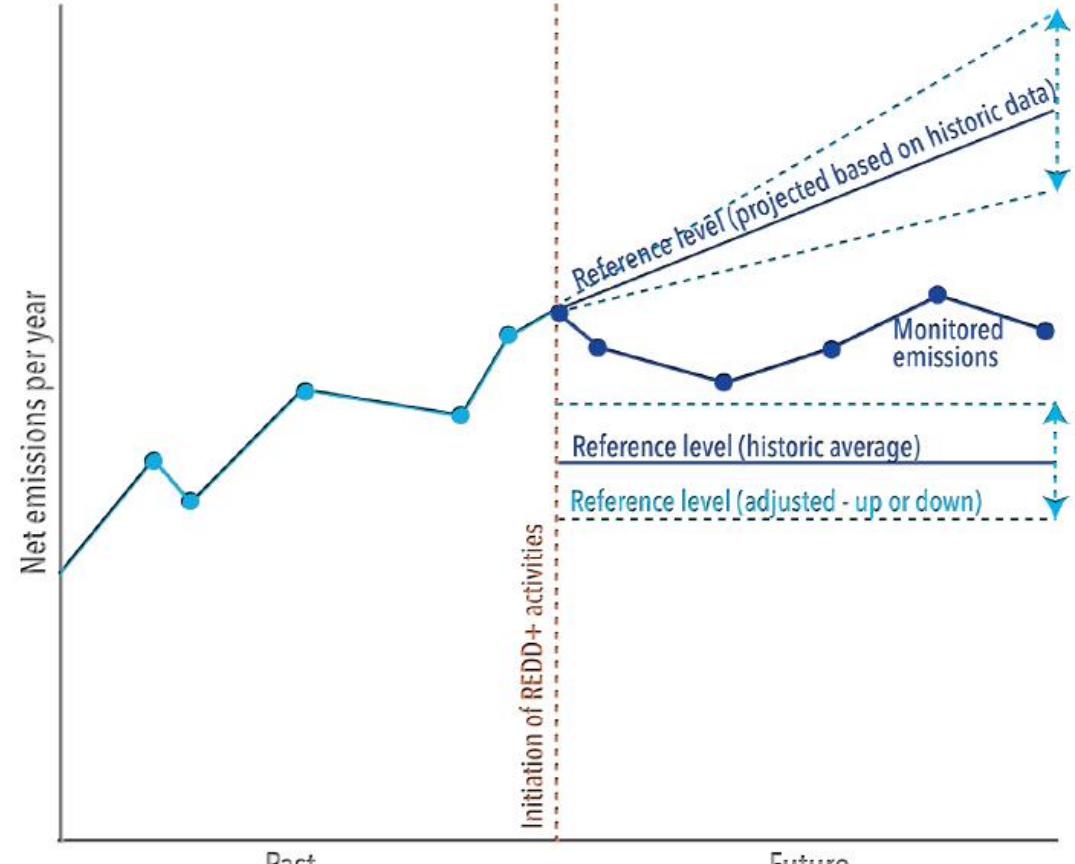
GOFC-GOLD, 2012

**Approach 2 and 3 are likely to be required for REDD+ for traceability**

## Forest Reference Emission Levels or Reference Levels

### Basic criteria:

- Benchmarks, expressed in tonnes of carbon dioxide equivalent per year, for assessing each country's performance in implementing REDD+ activities;
- Must be consistent with GHG national reporting for LULUCF;
- Take into account historic data and adjust to national circumstances (are flexible);
- Develop in a step-wise approach;
- Will be technically assessed and countries need to submit details about the procedure taken on a voluntary basis.



Chagas et al. Climate focus, 2013

## COP 15 -Copenhagen

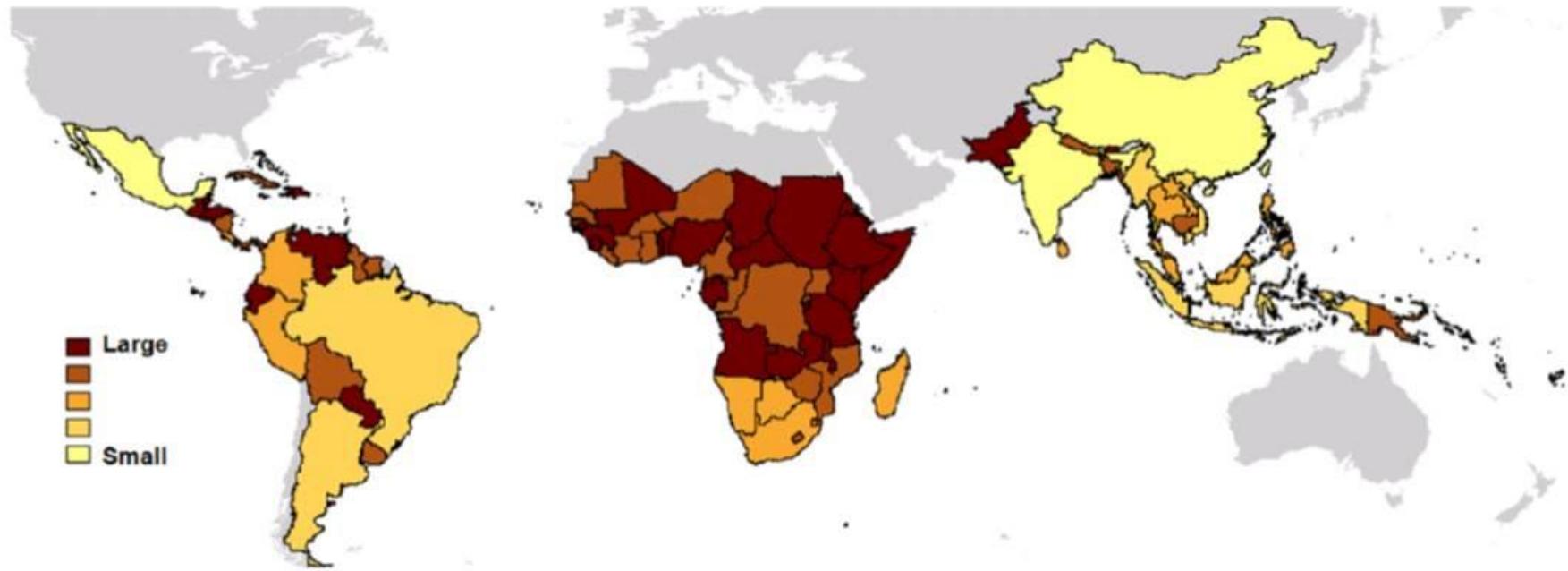
*SBSTA Decision CP.15 1.d) (ii)* Provide estimates that are transparent, consistent, as far as possible accurate, and that reduce uncertainties, taking into account national capabilities and capacities

## COP 19 - Warsaw

Annex to **Decision 13/CP.19** (Warsaw Framework)

(c) The extent to which the information provided was transparent, complete, consistent and accurate, including methodological information, description of data sets, approaches, methods, models, if applicable, and assumptions used

# Inception of REDD+

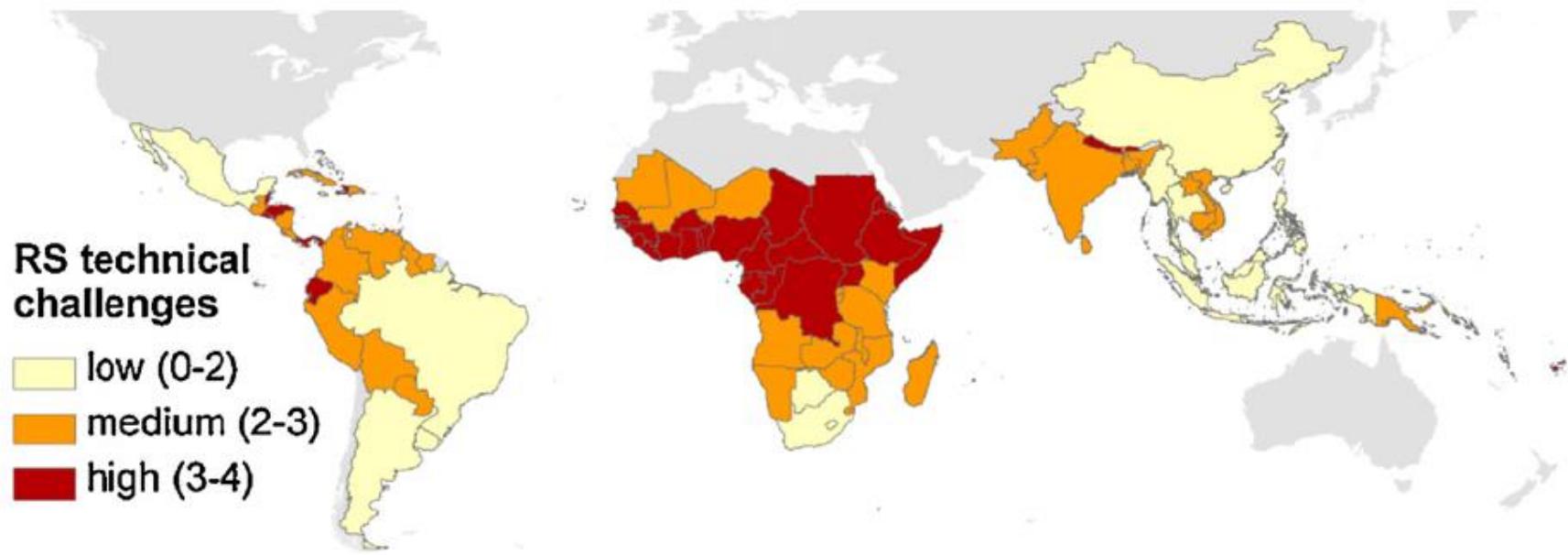


*Figure: Spatial distribution of the capacity gap for different countries analyzed.*

Herold, M. GOFC-GOLD project and University of Jena, 2009)

- “*the majority of non-Annex I countries have limited capacity in providing complete and accurate estimates of GHG emissions and removals from forests*” (UNFCCC, 2009)

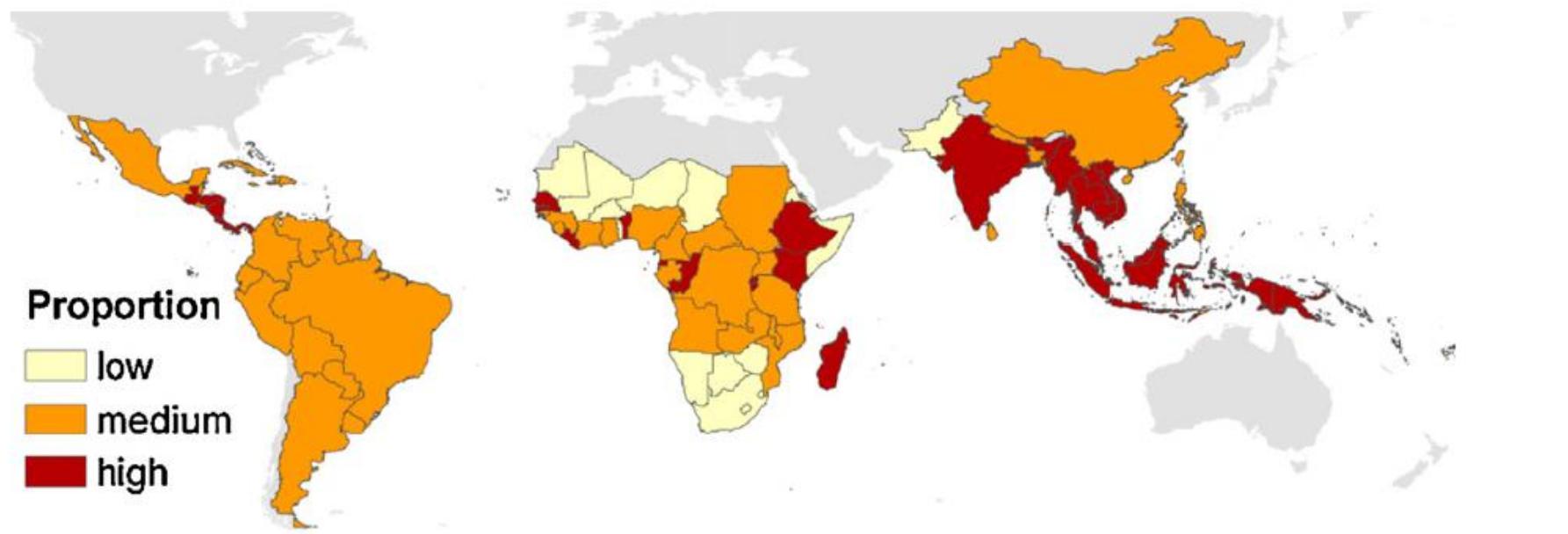
# Challenges with Activity data



Forest area change monitoring capacity



# Challenges with Emission Factors



Proportion of forest (tree cover >40%) with high soil carbon content (>15 kg/m<sup>2</sup>/m) present a challenge due to lack data

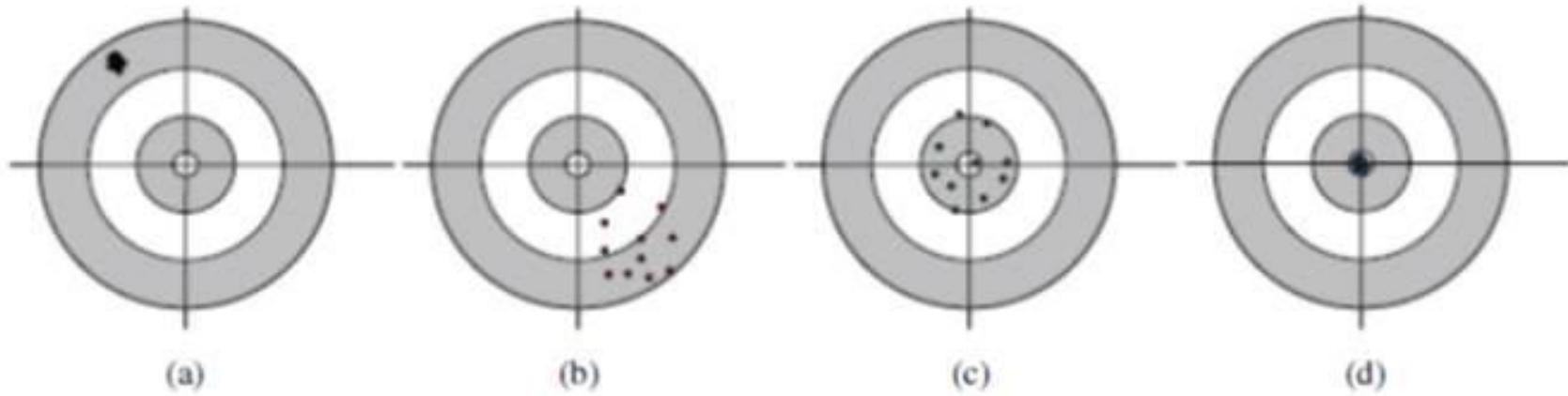


# Causes of uncertainty



- Lack of completeness
- Model:
  - Simplification of the ‘real world’
  - Interpolation
  - Extrapolation
  - Alternatives formulation of the model
  - Model inputs
- Lack of data
- Lack of representativeness of data
- Statistical random sampling error
- Measurement error
- Misreporting or misclassification
- Missing data

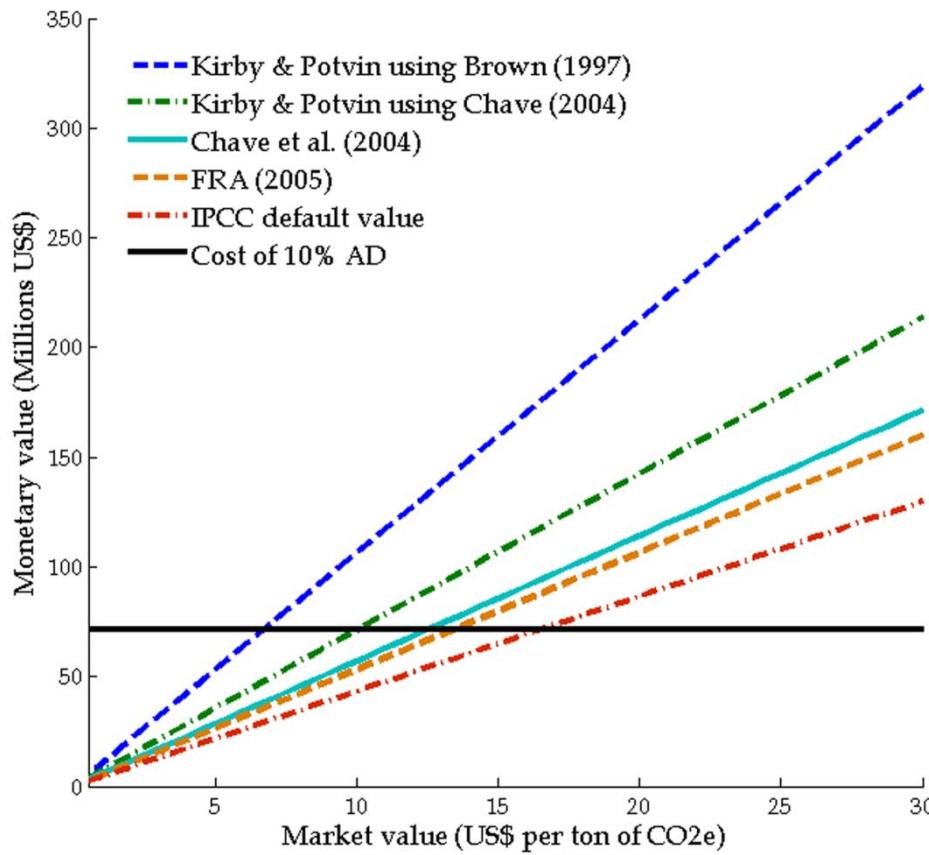
# Illustration of accuracy and precision



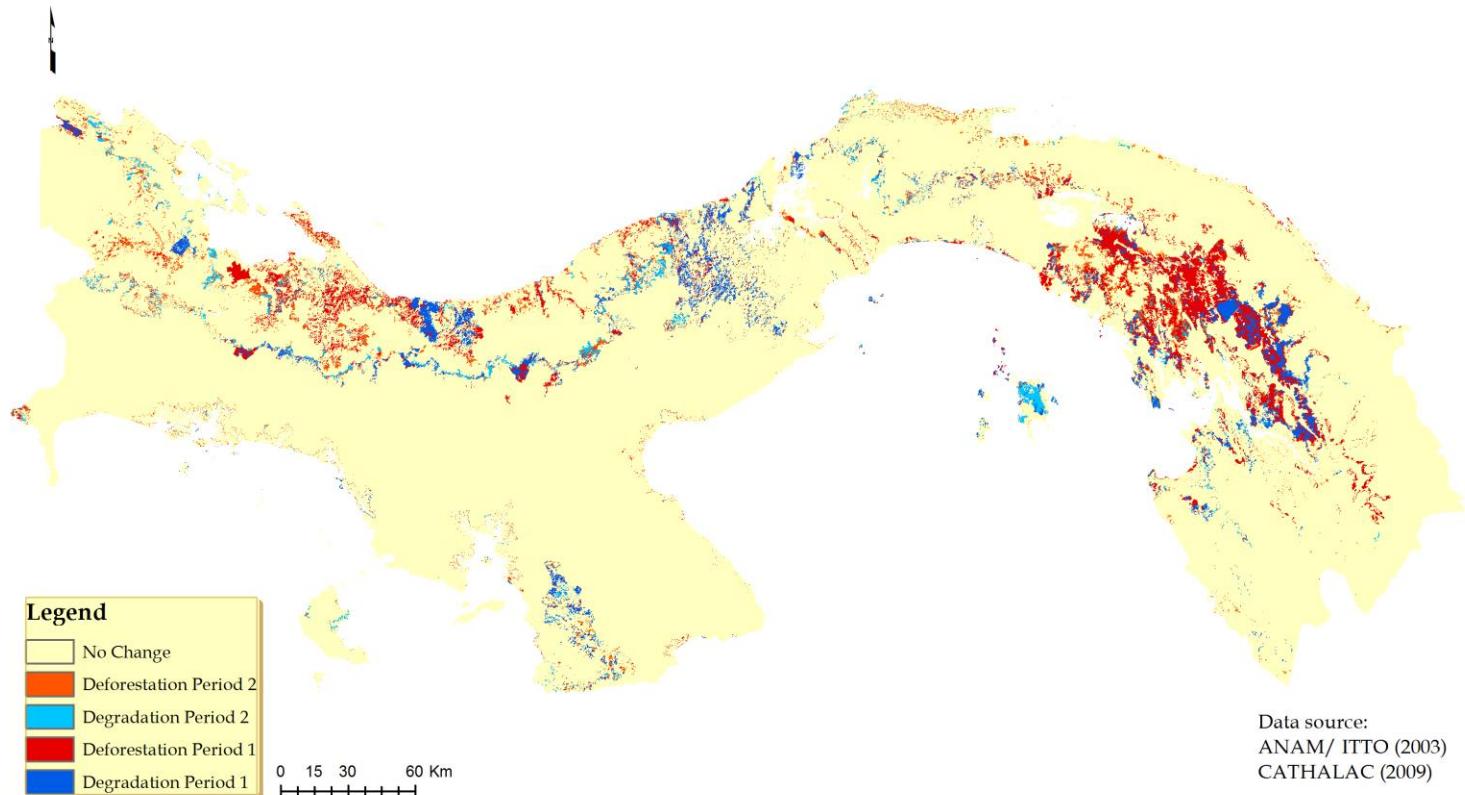
- (a) inaccurate but precise;
- (b) inaccurate and imprecise;
- (c) accurate but imprecise;
- (d) precise and accurate.

# Why does uncertainty matter?

Large uncertainties surround estimates of C stocks and emissions. They have financial implications.



## Credible emission reductions from REDD+



# Dealing with uncertainty upstream or downstream?

## Upstream: *Before emission reduction accounting*

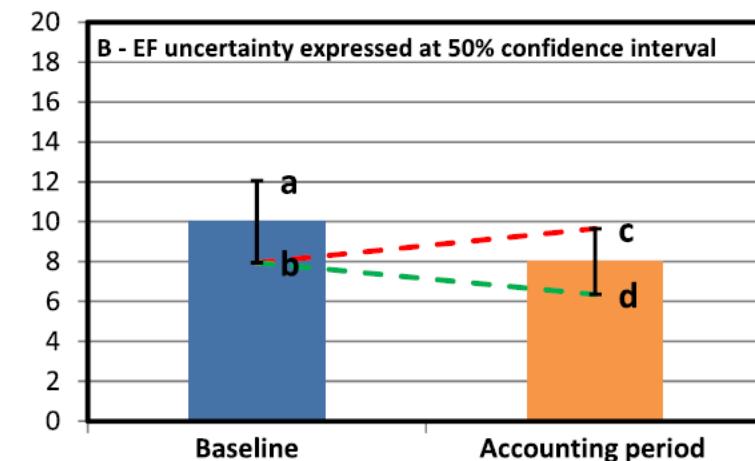
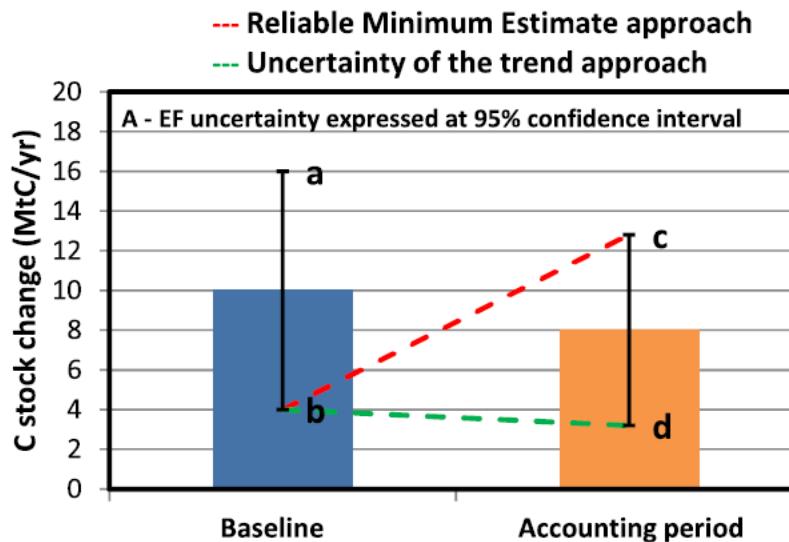


One approach to reduce uncertainties prior to carbon accounting, through 'upstream' investments in improved forest monitoring technologies and techniques.

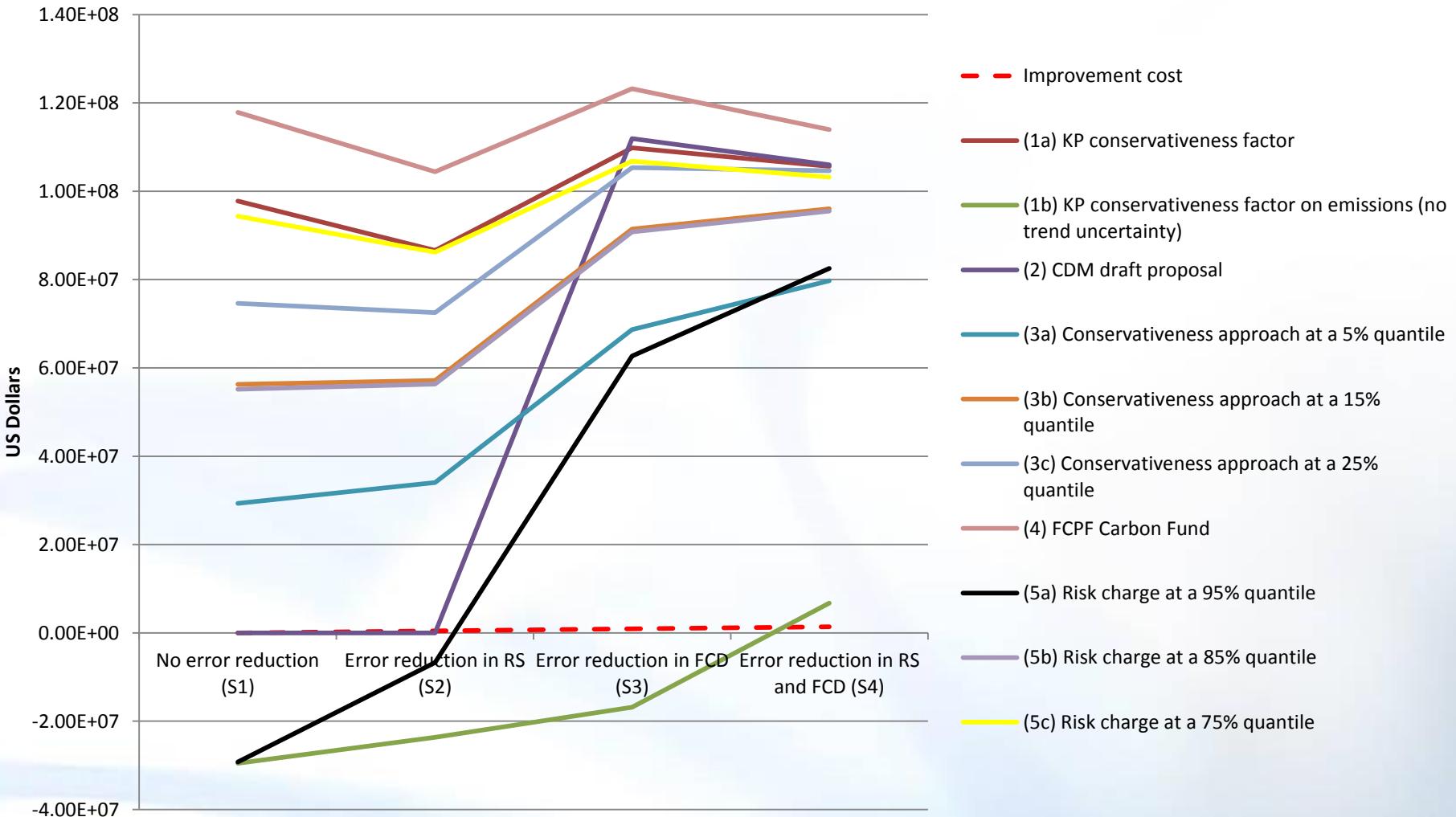
# Dealing with uncertainty Upstream or downstream?

## Downstream: *After emission reduction accounting*

- Discounting approaches under funds or market: the use of an adjustment or crediting rules used *a posteriori* of the carbon accounting that would reduce the risk of overestimating emission reductions or removals.



# Dealing with uncertainty Upstream or downstream?



Forest monitoring improvement costs represents less than 2% of potential carbon credits



# Elements of discussion:



- What are the main sources of error or uncertainty on emission and removals estimation that you can identify through your work?

Group discussion (15 min.)/ report in plenary (15 min.)



# COMPONENTS OF UNCERTAINTY



1. Land-Cover Change and Land-use dynamics
2. Carbon stock and change (from forests to other land uses)
3. Accounting of emissions and removals (modelling approach)

# DIAGNOSIS OF UNCERTAINTIES

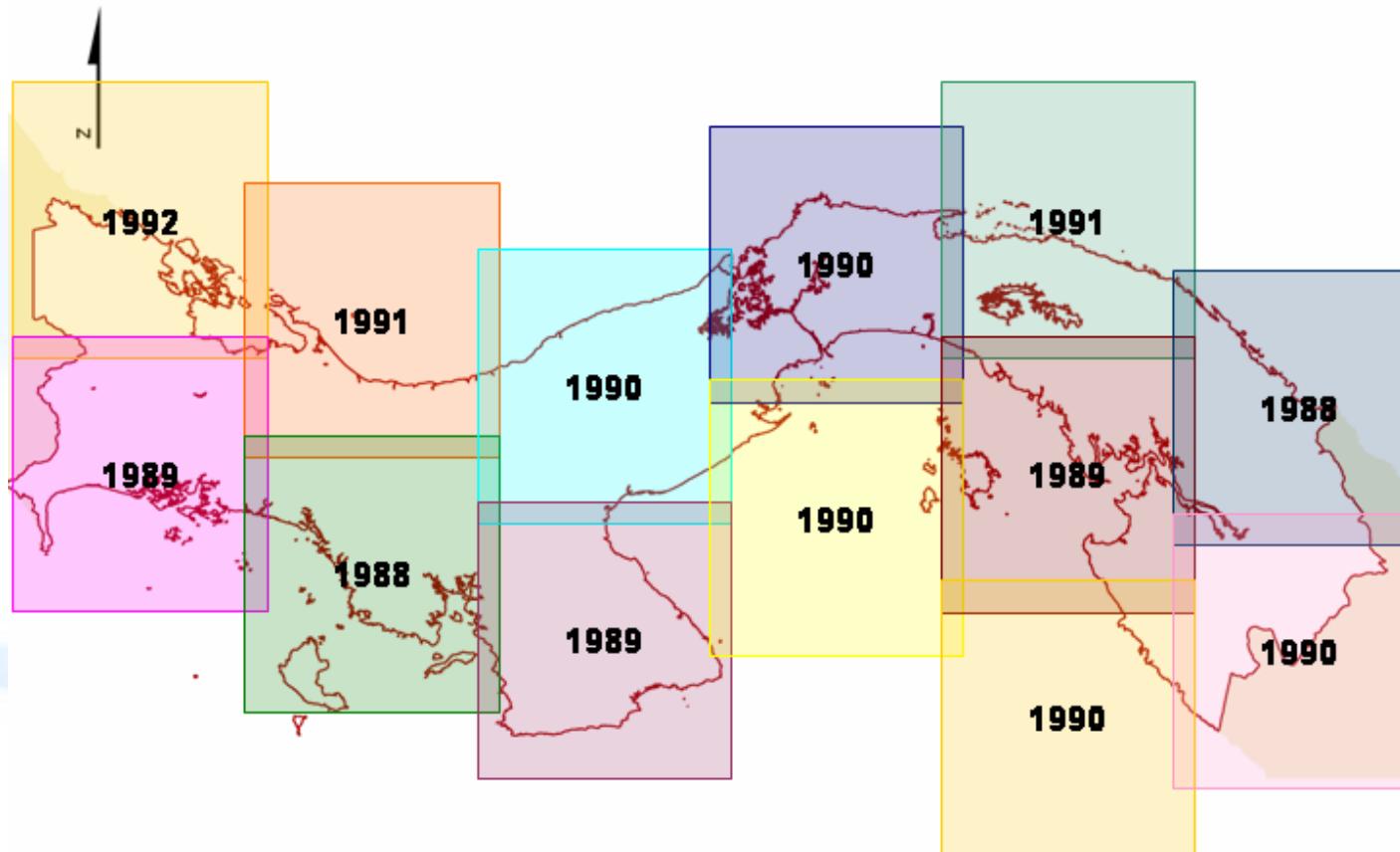
Example from Panama:

	Uncertainty
<b>Mature forest C density</b>	<b>54.5%</b>
Fallow C density	22.4%
Deforested area classification	2.2-19.1%
Snapshot effect	19.3%
Quality of land cover map	15.6-35.2%

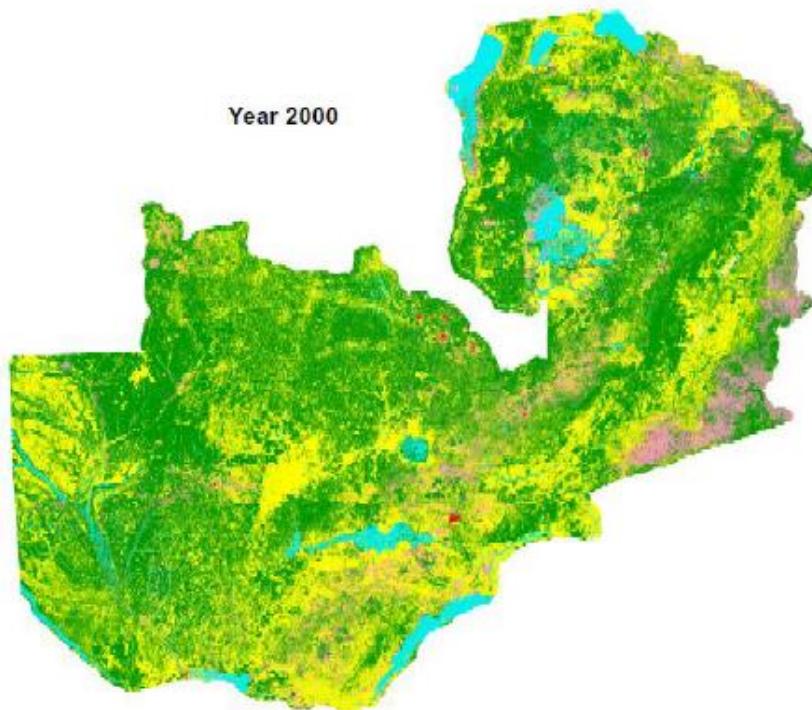
# LAND-COVER MAP QUALITY

**15.6 to 35.2 %**

Map based on a mosaic of multi-year satellite images / Low availability of usable satellite imagery



Year 2000



Land Cover Categories

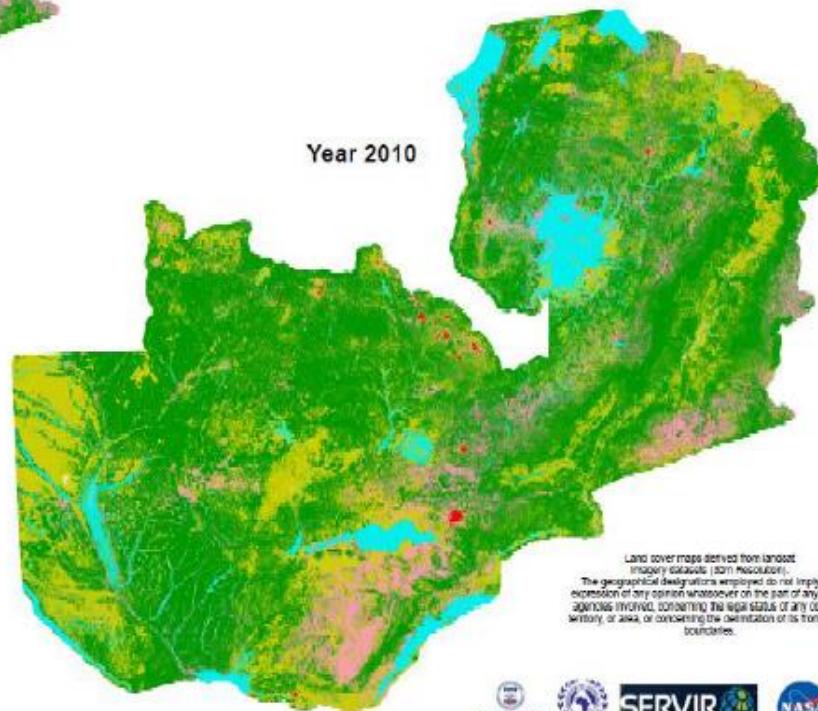
	Forestland		Otherland
	Cropland		Settlement
	Grassland		No Data
	Wetland		

0      250      500      1,000  
Kilometers

Zambia Land Cover Maps for  
GHG Inventory Development



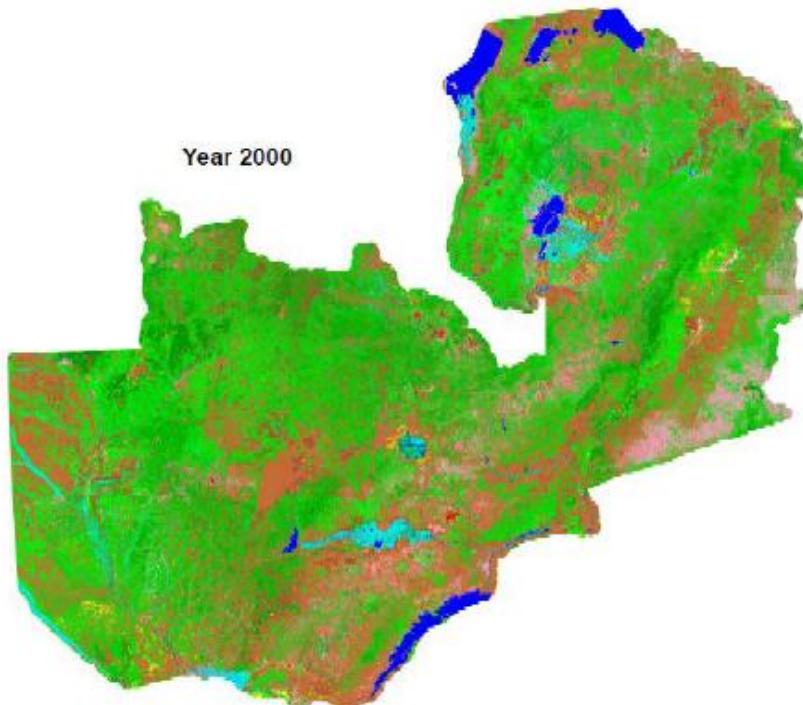
Year 2010



Land cover maps derived from Landsat  
remote sensing imagery (30 m resolution).  
The geographical information contained does not imply the  
expression of any opinion whatever on the part of any of the  
agencies involved, concerning the legal status of any country,  
territory, or area, or concerning the delimitation of its frontiers or  
boundaries.



Year 2000



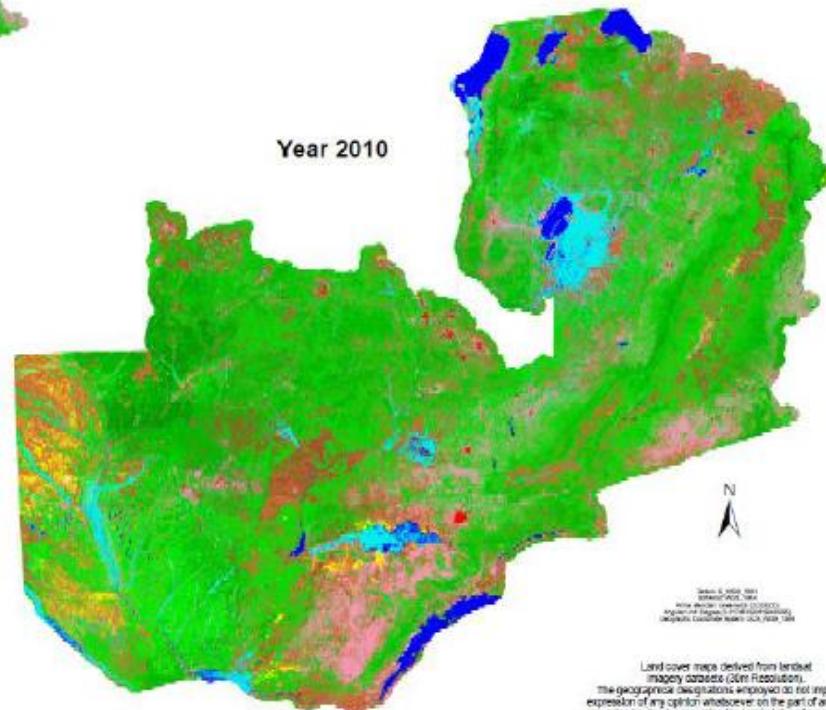
#### Land Cover Categories

Very Dense Forest	Closed Grasslands
High Dense Forest	Open Grasslands
Moderate Forest	Closed Shrublands
Sparse Moderate Forest	Open Shrublands
Sparse Forest	Perennial Cropland
Open Sparse Forest	Annual Cropland
Planted Forest	Wetlands
Woodlands	Water Bodies

0      245      490      980  
Kilometers

## Zambia Land Cover Maps for GHG Inventory Development

Year 2010



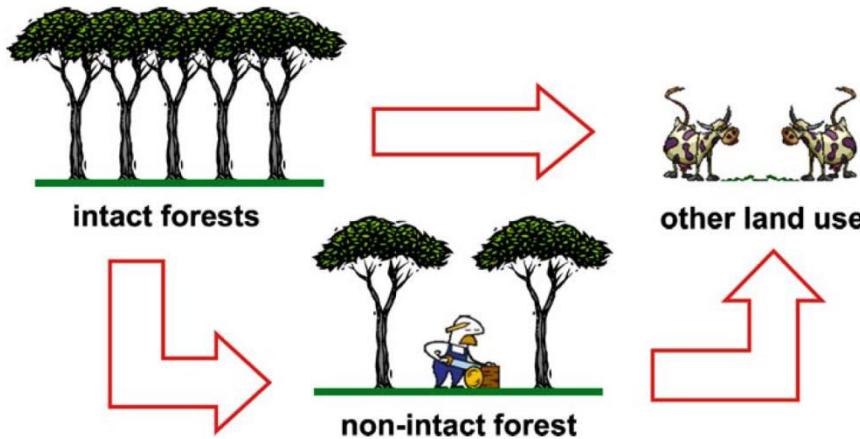
© 2010, NASA  
LANDSAT 7, 2000  
http://www.usgs.gov/landsat  
http://www.usgs.gov/landsat/landsat7.html  
Geographic Coordinate System: UTM Zone 35N

Land cover maps derived from Landsat  
Imagery (30m Resolution).  
The geographical designations employed do not imply the  
expression of any opinion whatsoever on the part of any of the  
agencies involved, concerning the legal status of any country,  
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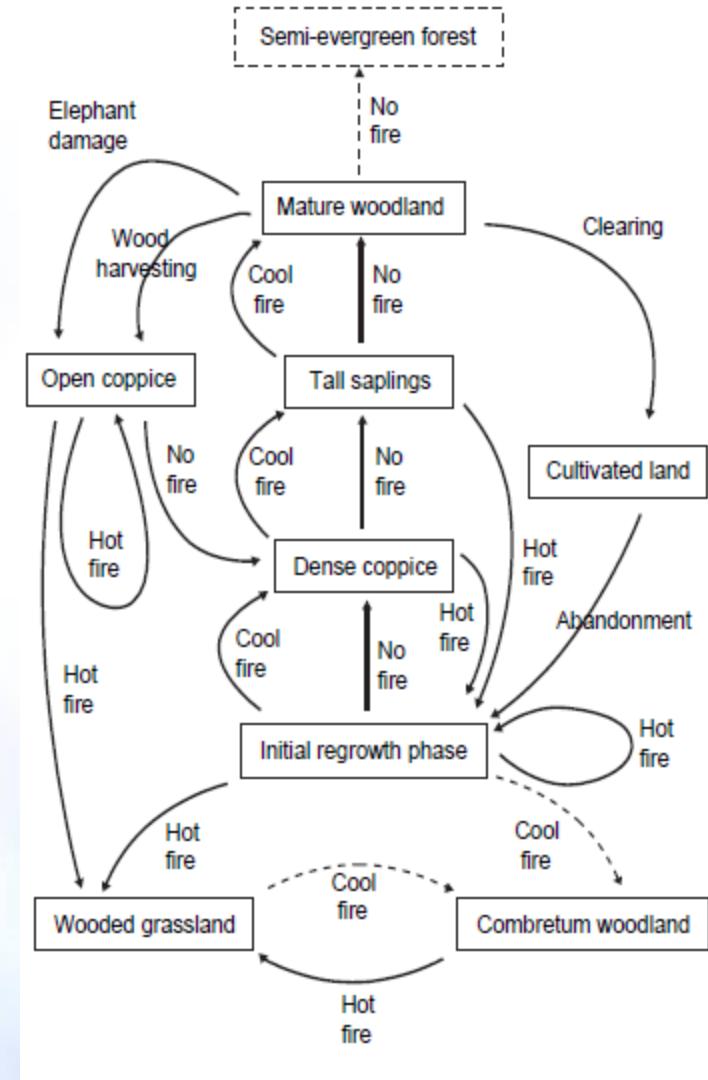
Zambia Scheme 2, Land Cover maps

# Land-use dynamics

- More complex dynamics in the Miombo woodlands



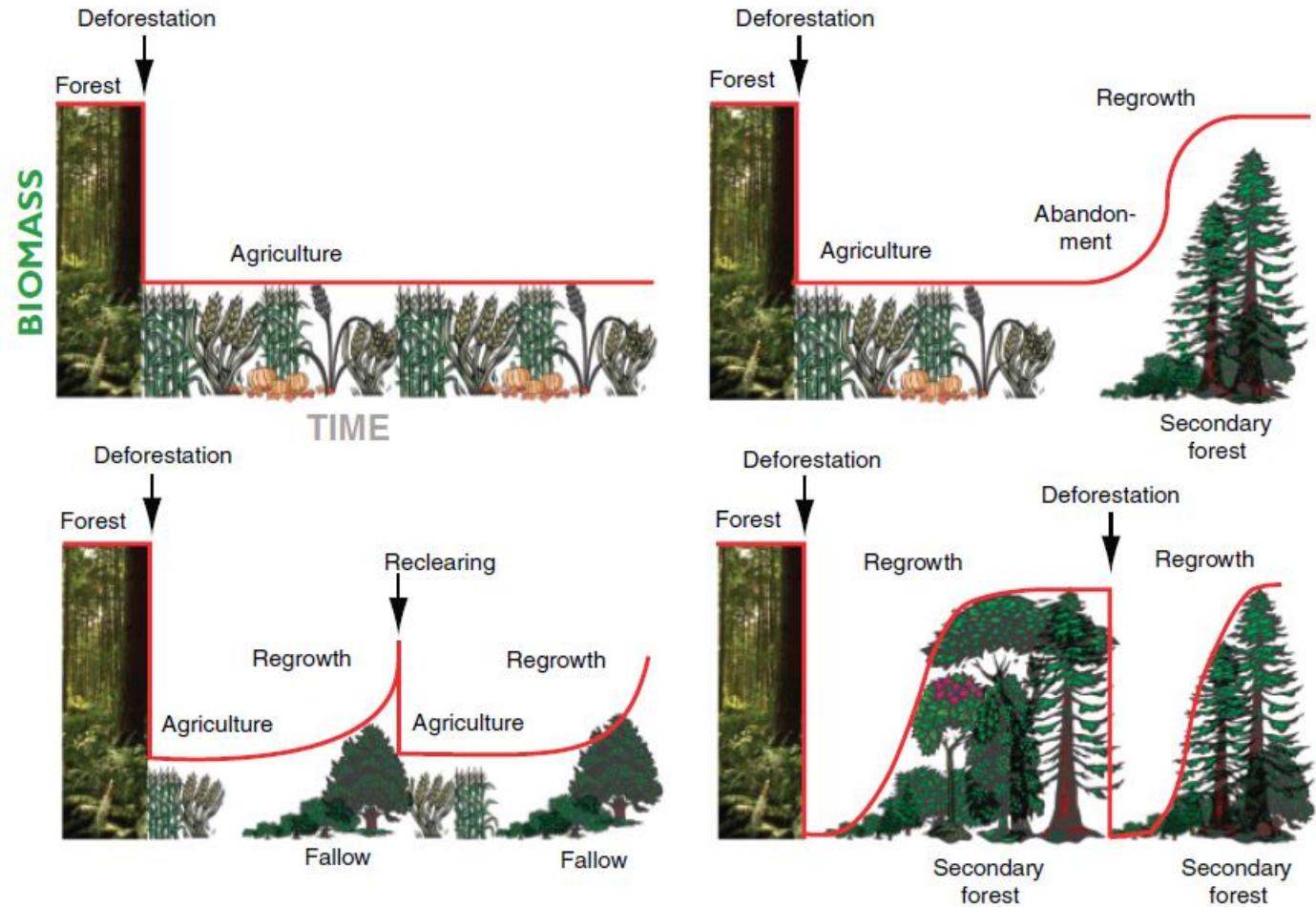
Mollicone et al., *Climatic Change* (2007)



Frost, in Campbell, *Miombo in Transition* (1996)

# Land-use dynamics

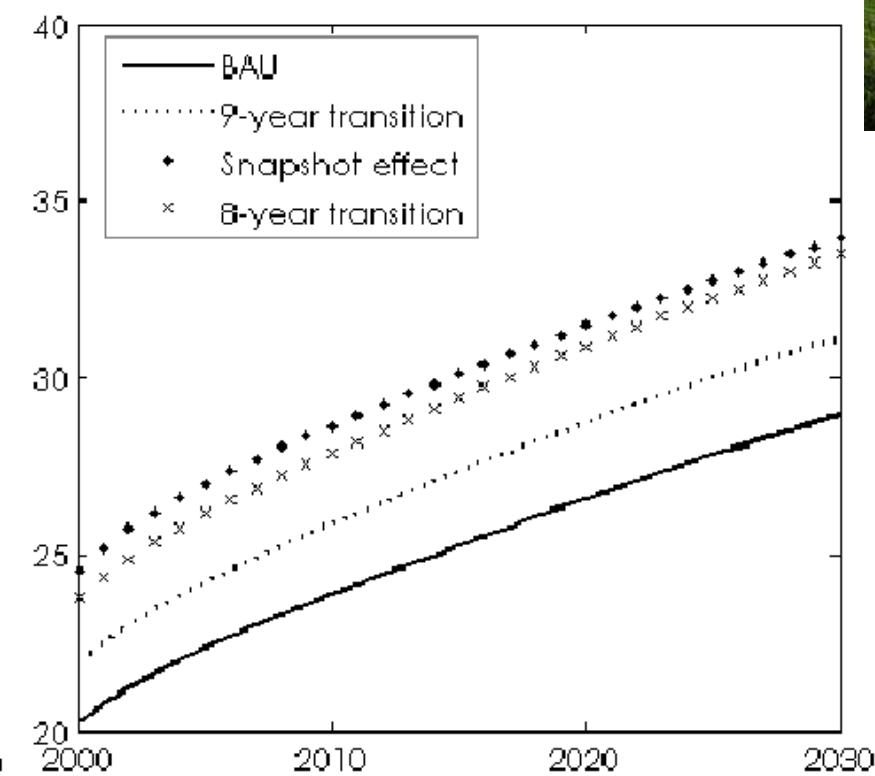
Different pathways of carbon dynamics following deforestation



Ramankutty et al. *Global Change Biology* (2007)

# Land cover change: SNAPSHOT EFFECT

Long time interval between  
two maps/Lack of  
knowledge on land-cover  
dynamics

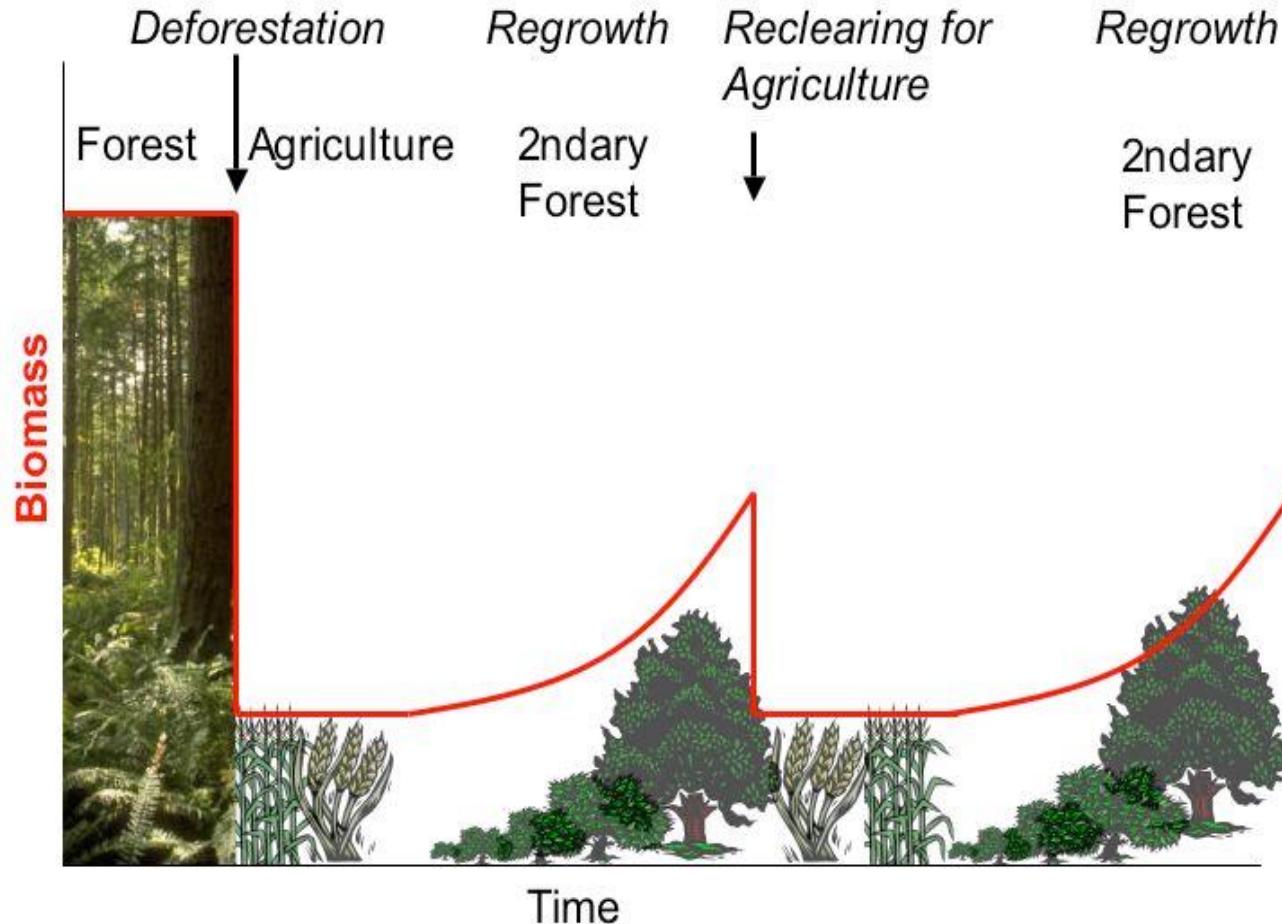


← 19.3 %

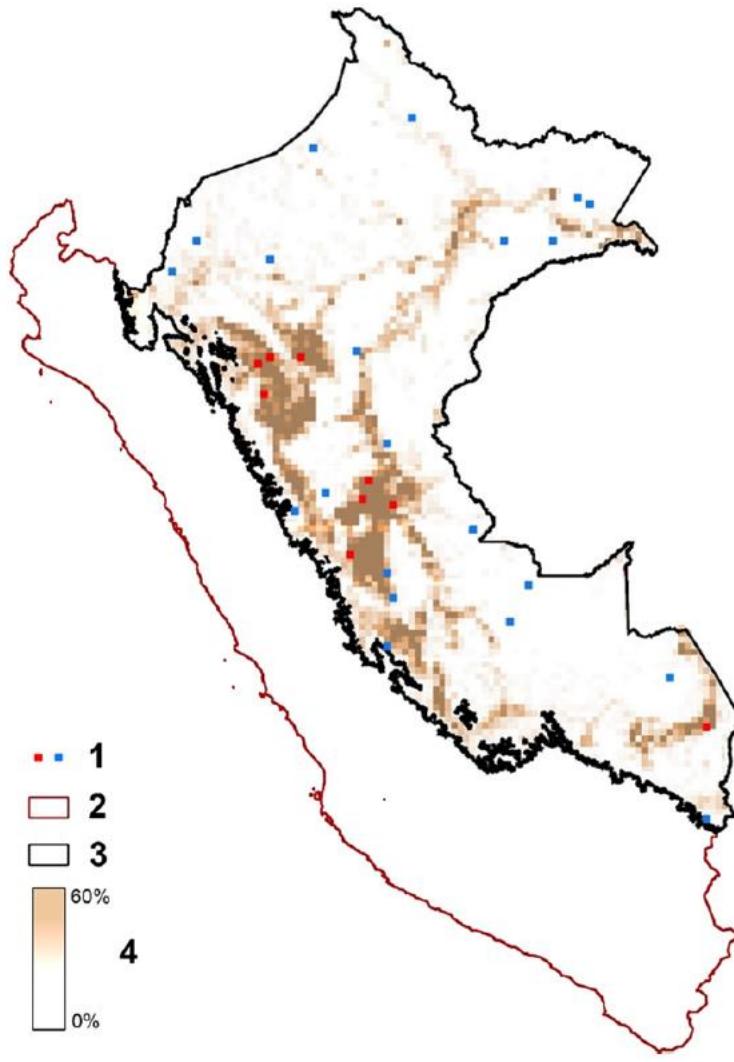
# PROBLEMS MONITORING SHIFTING CULTIVATION

## Overestimating:

- Emissions of new deforestation
- Removals from forest regrowth

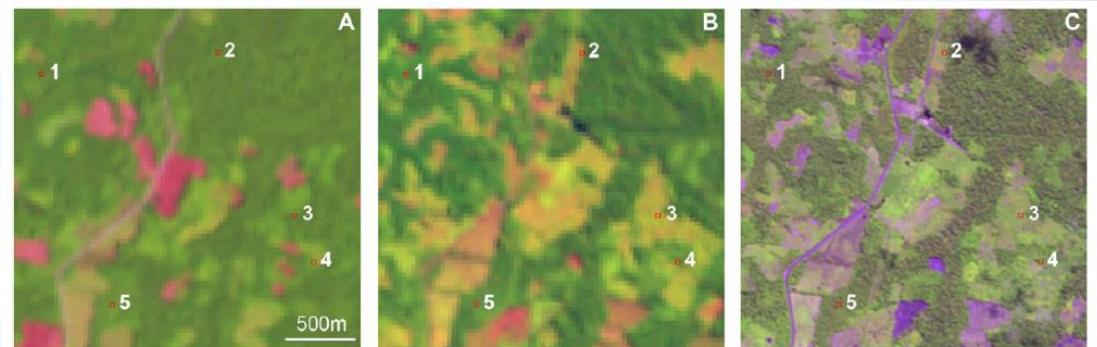


# Assessing accuracy of land change



Stratified sampling design

- Sampling design:
  - Strata
  - Cluster sampling
  - Systematic vs random selection
- Response design
- Analysis:
  - Estimating accuracy, area and uncertainty



Point-based validation

# Assessing accuracy of land change

**Table 3**

Error matrix of sample counts ( $n_{ij}$ ) constructed from the accuracy assessment sample of a change map by Jeon et al. (in press). Class 1 is deforestation, and classes 2 and 3 are no change classes of forest (class 2) and non-forest (class 3). Map categories are the rows while the reference categories are the columns.

Class	1	2	3	Total	Map area [ha]	$W_i$
1	97	0	3	100	22,353	0.013
2	3	279	18	300	1,122,543	0.640
3	2	1	97	100	610,228	0.348
Total	102	280	118	500	1,755,123	1

Olofsson et al.  
Remote Sensing of  
Environment, 2013

Calculating standard error:

$$S(\hat{p}_{.1}) = \sqrt{\sum_{i=1}^3 W_i^2 \frac{\frac{n_{ij}}{n_i} \left(1 - \frac{n_{ij}}{n_i}\right)}{n_i - 1}} = \left( (0.013^2 \frac{97}{100} \frac{(1 - \frac{97}{100})}{99} + 0.64^2 \frac{3}{300} \frac{(1 - \frac{3}{300})}{299} + 0.35^2 \frac{2}{100} \frac{(1 - \frac{2}{100})}{99}) \right)^{\frac{1}{2}} = 0.00613.$$

Standard error of the  
adjusted area estimate:

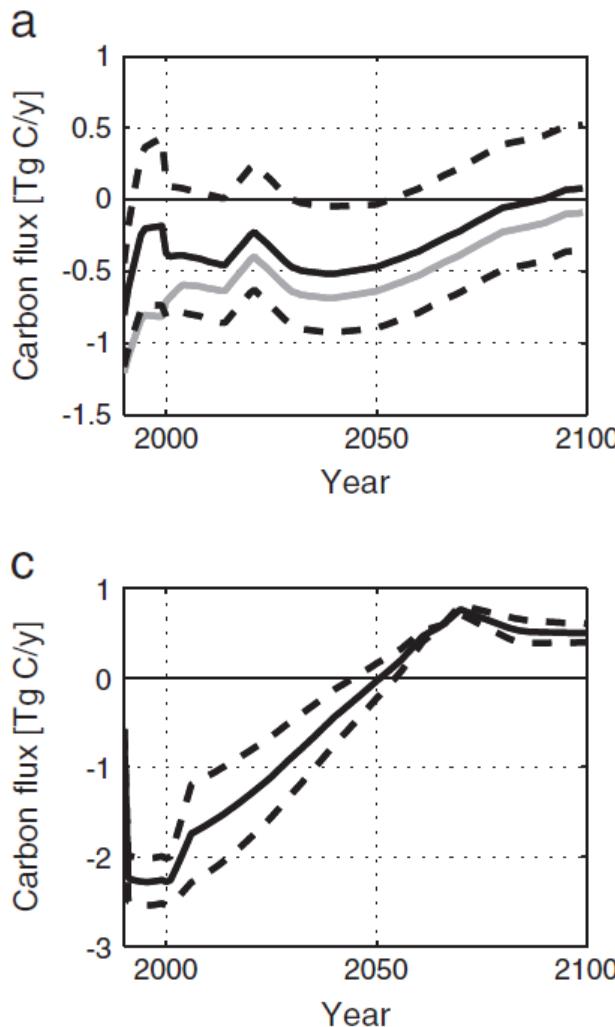
$$S(\hat{A}_1) = A_{tot} \times S(\hat{p}_{.1}) = 1,755,123 \times 0.00613 = 10,751 \text{ ha}$$

A final land change area estimate with  
margin of error (at 95% CI):

$$\hat{A}_1 \pm 2 \times S(\hat{A}_1) = 45,651 \pm 21,502 \text{ ha.}$$

The confidence interval quantifies the uncertainty associated with the sample-based estimate of the area of deforestation.

# Assessing accuracy of land change

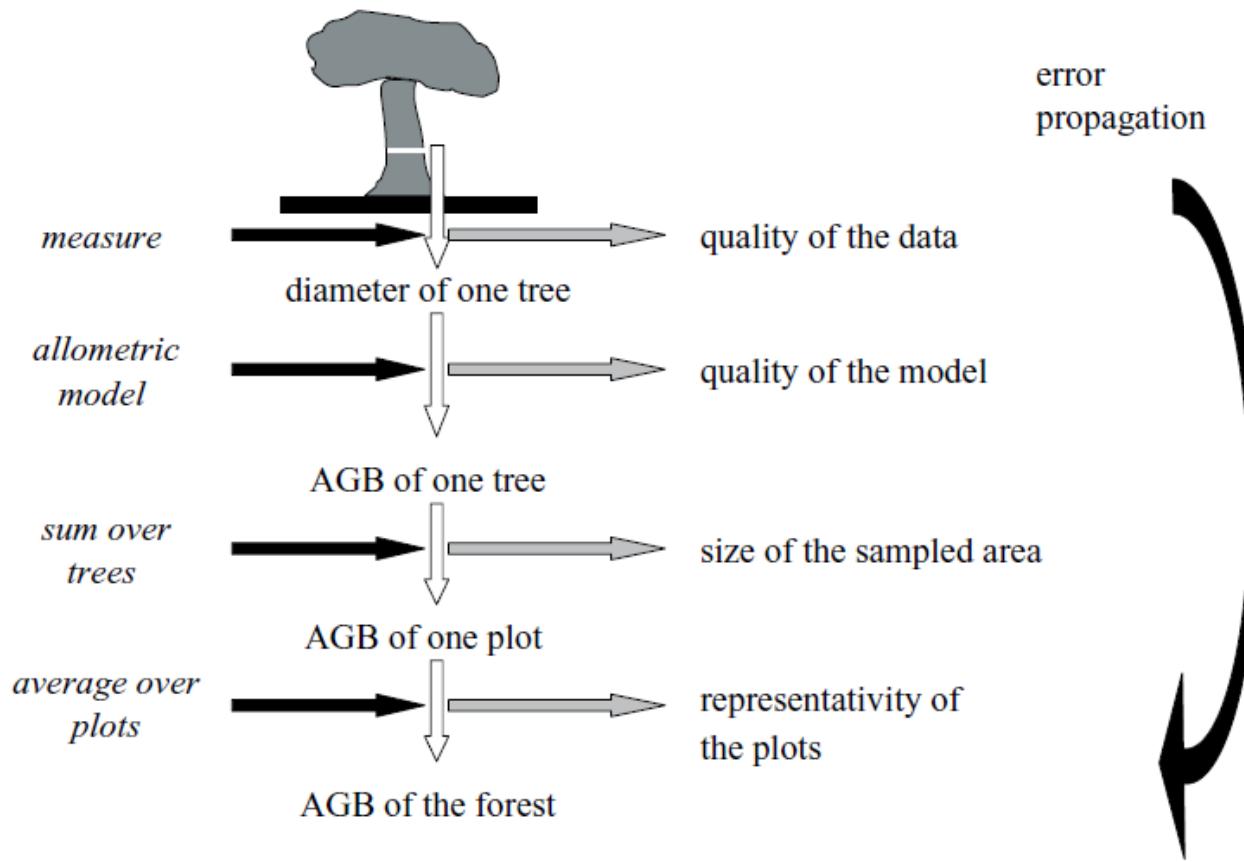


- Adjusted Area
- Mapped Area
- - - 95% CI

The true area of deforestation could be as low as 241,149 ha or as high as 67,153 ha at 95% level of confidence.

Large impact on emission estimates but rarely available.

# Biomass estimation: error propagation



# Biomass estimation: error in measurements

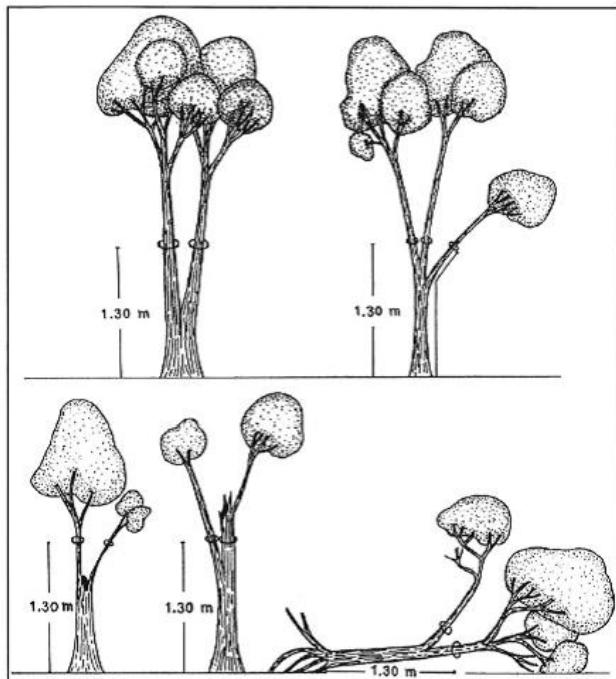
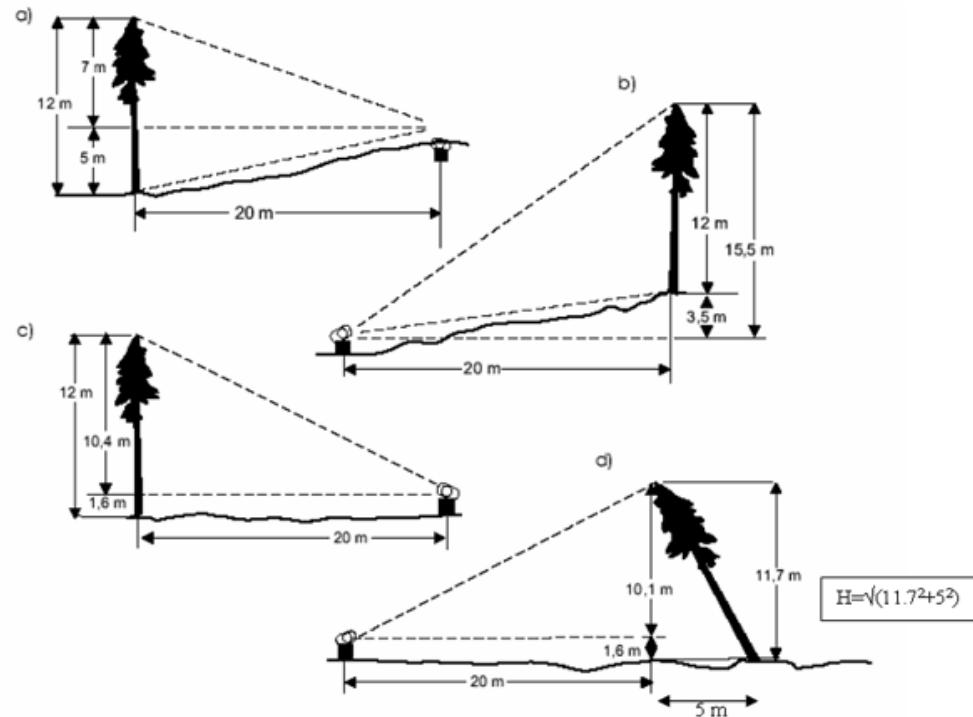


Fig. 2.2.6. Measurement of multiple stems. Any fork between the base and 1.3 m counts as a second stem, and must be measured 1.3 m from the base of the tree.



## WOOD DENSITY

to parameterize allometric models vary with the age of the tree, growth conditions, intraspecific but mostly interspecific

- Can be downloaded from repository:
  1. <http://datadryad.org/resource/doi:10.5061/dryad.234>
  2. <http://db.worldagroforestry.org/wd/>
- The variability in wood density can be included in uncertainty analysis



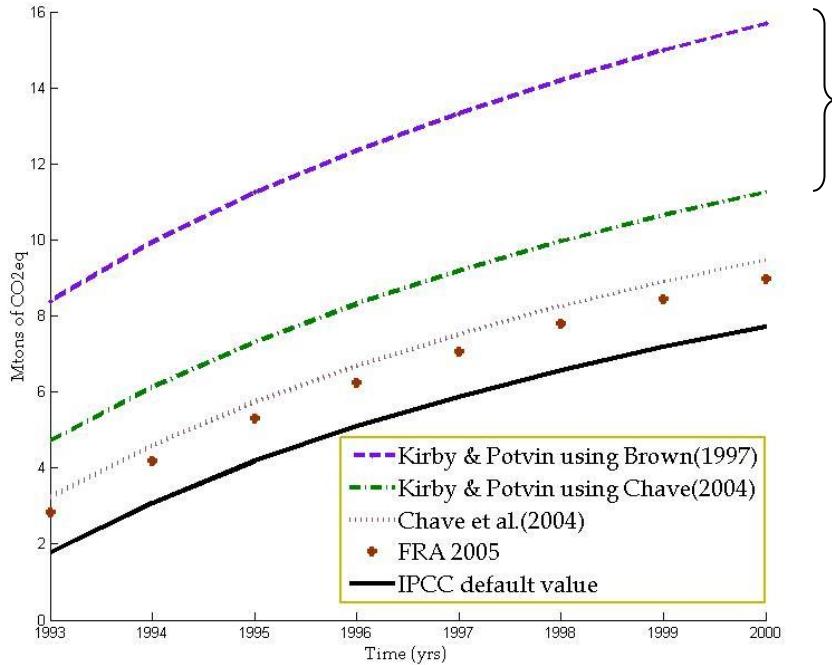
# Biomass estimation: allometric models

- Improved allometric models



Tissue type	Number of samples per tree
Trunk	15
Branches	10
Twigs	10
Flowers	10
Leaves	Small
	10
	Medium
	10
	Large
	10
Coarse Roots	10
Fine Roots	10
<b>Total:</b>	<b>95</b>

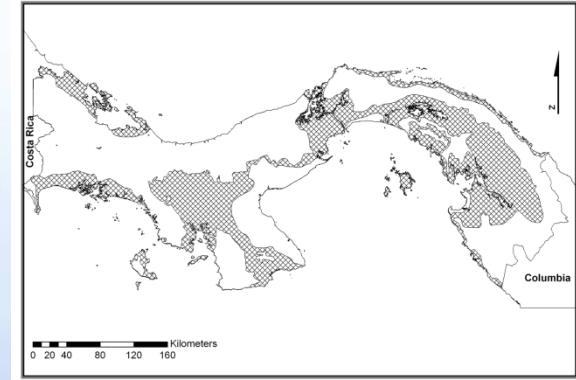
# Biomass estimation: allometric models



Different allometric  
equations,  
Same inventory data

## MATURE FOREST C DENSITY

No standardized  
methodology and error-  
prone allometric equations

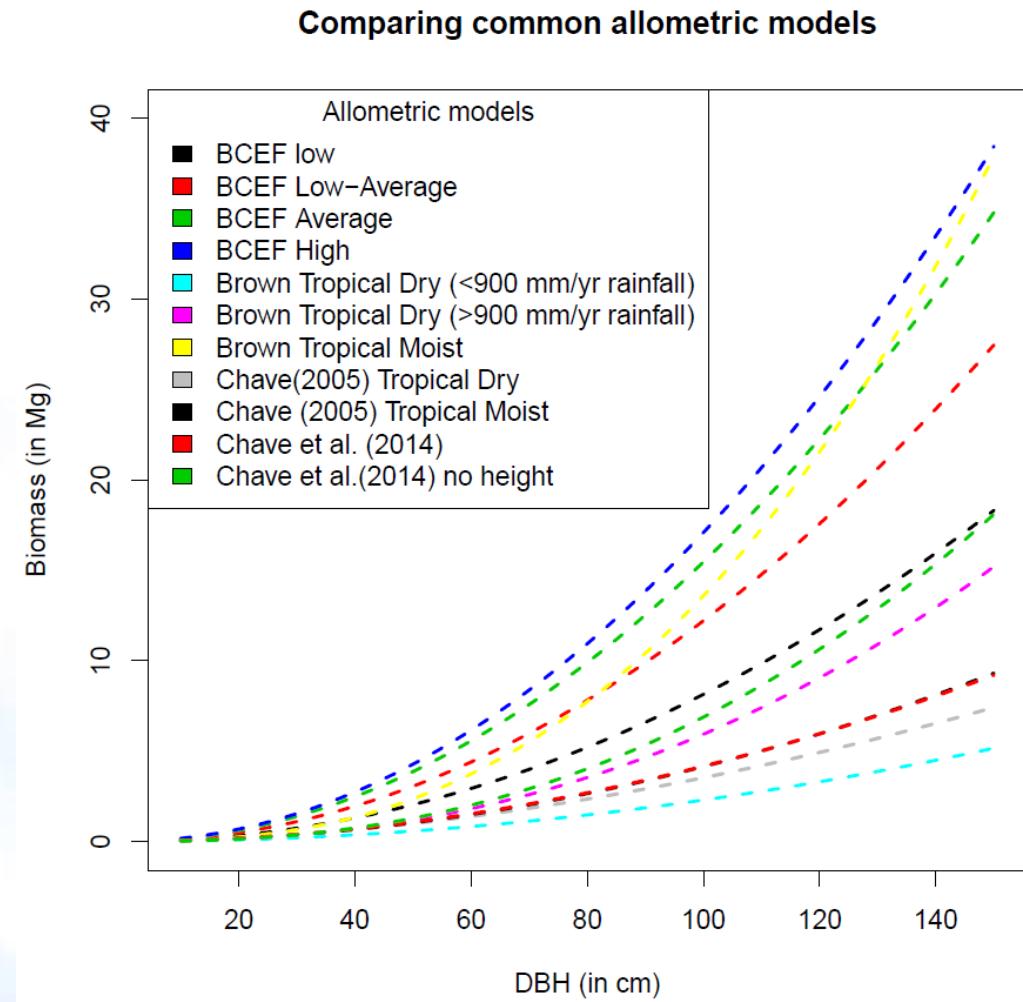
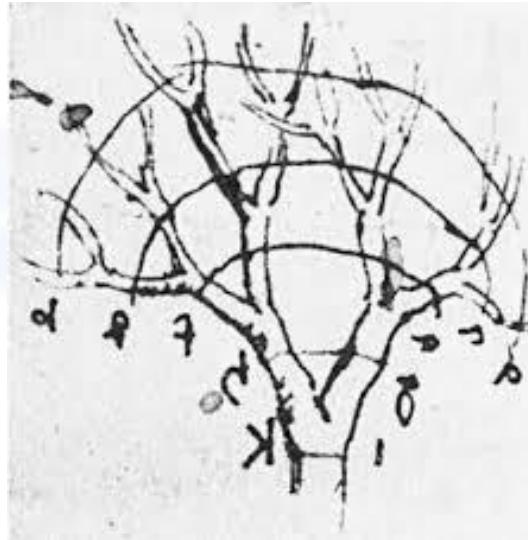


Moist tropical forest

# Biomass estimation: allometric models

## Example for Zambia

Using pan-tropical generalized  
allometric models

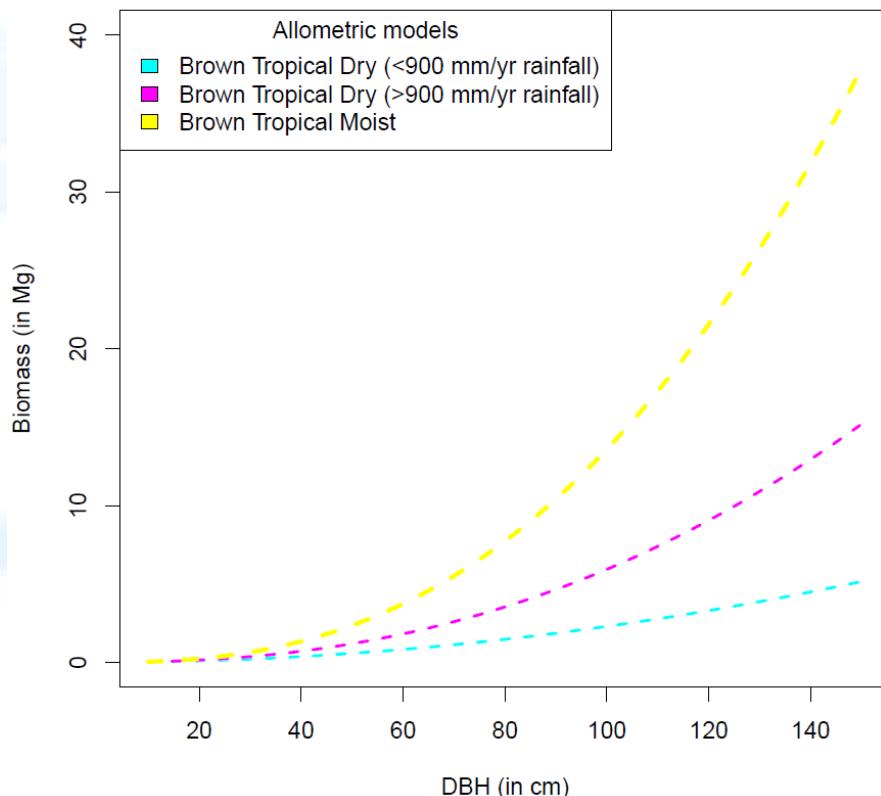


# Biomass estimation: allometric models

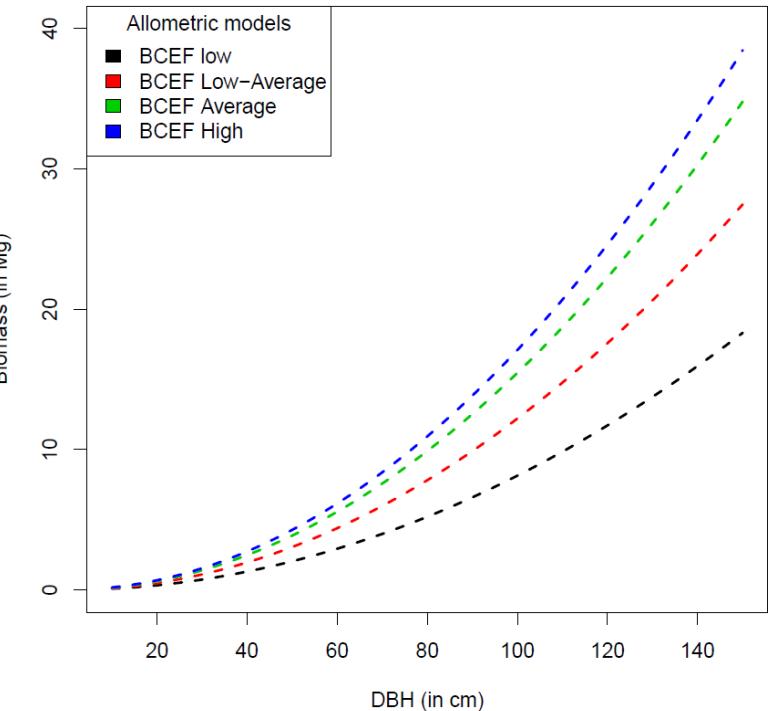
## Example for Zambia

### BIOMASS EXPANSION AND CONVERSION FACTORS

Comparing Brown (1997) allometric models



Comparing Biomass Conversion and Expansion Factor (BCEF) model



### BROWN (1997) ALLOMETRIC EQUATIONS:

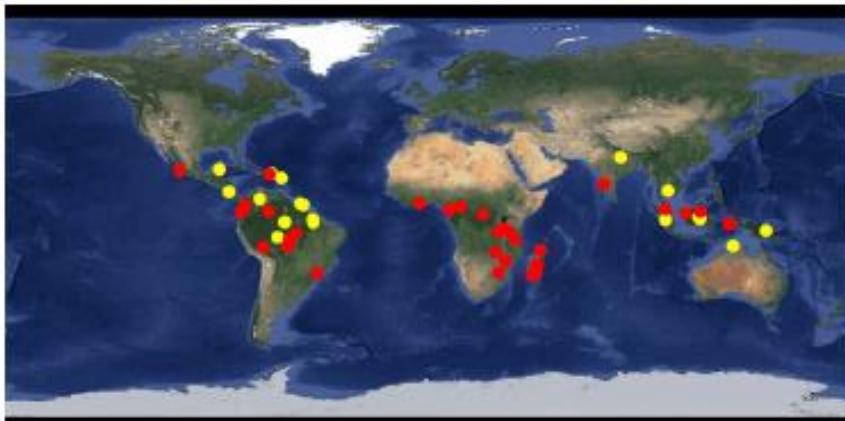
- Based on a limited sample size
- Applicable to different forest types
- No height measurement

# Biomass estimation: allometric models

## Example for Zambia

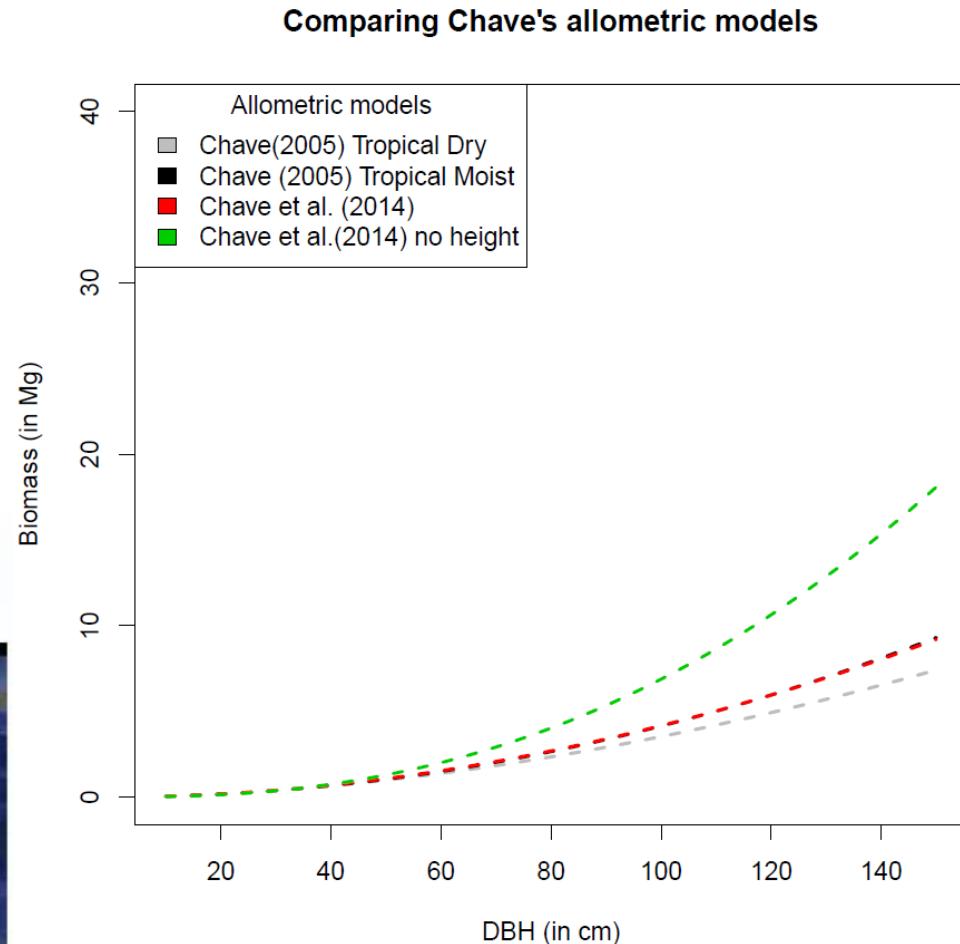
### BEST PAN-TROPICAL ALLOMETRIC MODELS

- With height measurements
- Without height measurements
- Based on the destructive sampling of 4004 trees  $\geq 5$  cm DBH, spanning a range of climatic conditions and vegetation types



Yellow circles: 20 sites included in 2005 eq.

Red circles: 38 new sites included in 2014 eq.



### CHAVE et al. 2005 & 2014 ALLOMETRIC EQUATIONS

Database of harvested trees is available at: [http://chave.ups-tlse.fr/pantropical\\_allometry.htm](http://chave.ups-tlse.fr/pantropical_allometry.htm)



# Global database on tree allometry



- GlobAllomeTree database: *For Assessing volume, biomass and carbon stocks of trees and forests.*

## GlobAllomeTree

Assessing volume, biomass and carbon stocks of trees and forests.



Home About Data Software Documents Contributors Jopei ▾

### Equations

Your current search

Export Results

Equations found: 59

Keyword Kenya clear

Keyword Identification Taxonomy Location Components Input/Output Allometry Reference

Search allometric equations by keyword. This searches across several text fields.  
Example searches: Acacia, Zambia, Beliefontaine, Glutinosum, rainforest

Keyword Kenya

Search

ID	Equation	Genus	Species	Country	Components	Output	Biome (FAO)	Author
1136	-1.0899+2.4937*log(H)	Rhizophora	mucronata	Kenya	L	Biomass	Tropical moist deciduous forest	Kalr
1143	-1.4295+0.9154*log(DBH^H)	Rhizophora	mucronata	Kenya	Rb	Biomass	Tropical moist deciduous forest	Kalr
1314	0.134*DBH+0.0579*DBH^2+0.317*H	Tarchonanthus	camphoratus	Kenya	Bd Bg Bt T	Biomass	Tropical mountain system	Kiru
1319	1.8069*DBH^2.5628	Rhizophora	mucronata	Kenya	L	Biomass	Tropical moist deciduous forest	Kiru
1119	-1.301+2.4044*log(DBH)	Rhizophora	mucronata	Kenya	Rb	Biomass	Tropical moist deciduous forest	Kalr
1121	0.3703+0.2708*log(DBH)	Avicennia	marina	Kenya	Bd Bg Bt	Biomass	Tropical moist deciduous forest	Kalr
1126	0.1862-0.3740*log(DBH)	Ceriops	tagal	Kenya	L	Biomass	Tropical moist deciduous forest	Kalr
1133	-0.9905+2.3918*log(H)	Rhizophora	mucronata	Kenya	Rb	Biomass	Tropical moist deciduous forest	Kalr
1138	-1.4413+1.4267*log(DBH^H)	Rhizophora	mucronata	Kenya	Rb	Biomass	Tropical moist deciduous forest	Kalr
1140	-0.6275+0.8088*log(DBH^H)	Rhizophora	mucronata	Kenya	B T	Biomass	Tropical moist deciduous forest	Kalr
1145	-0.5761+0.4968*log(DBH^H)	Rhizophora	mucronata	Kenya	B T	Biomass	Tropical moist deciduous forest	Kalr

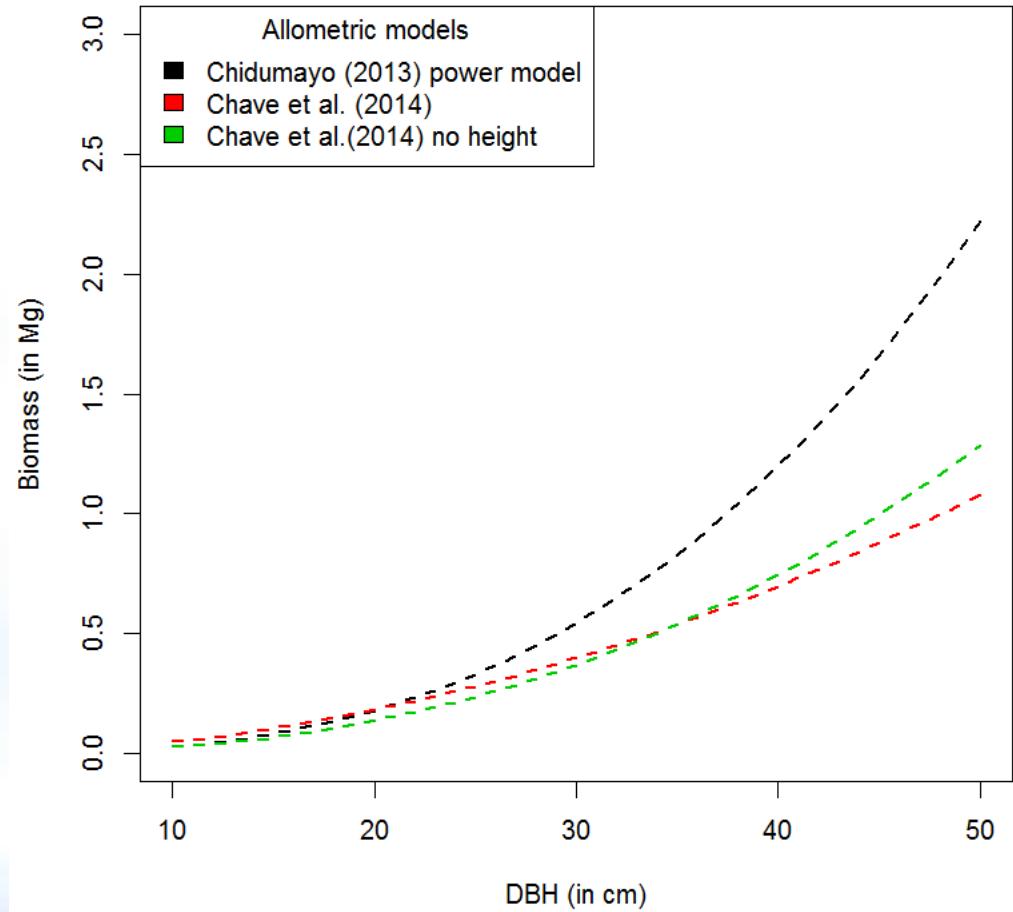
# Biomass estimation: allometric models

## Example for Zambia

- Chidumayo (2013)
- Destructive sampling of 113 trees between 2-39 cm dbh.
- Miombo woodland

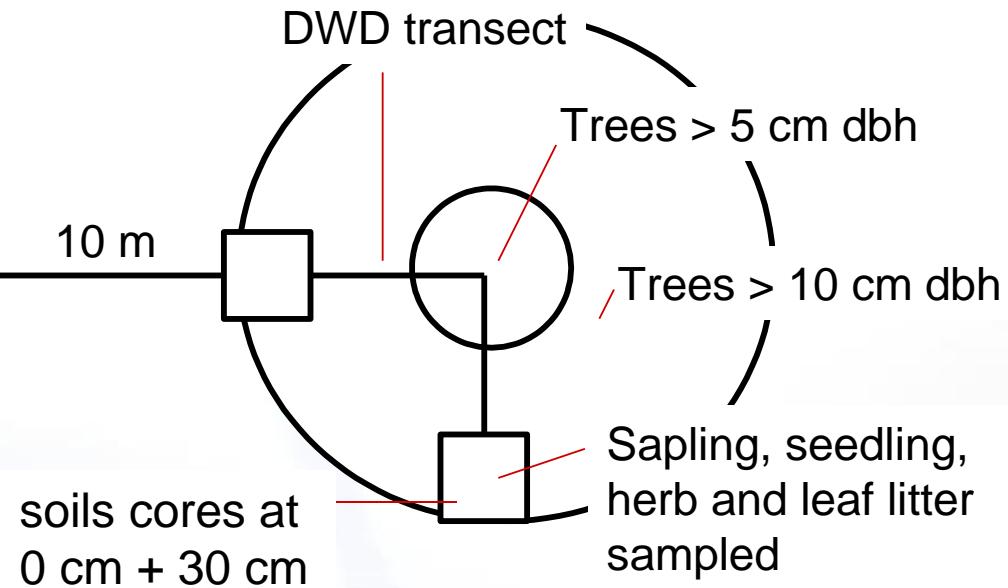
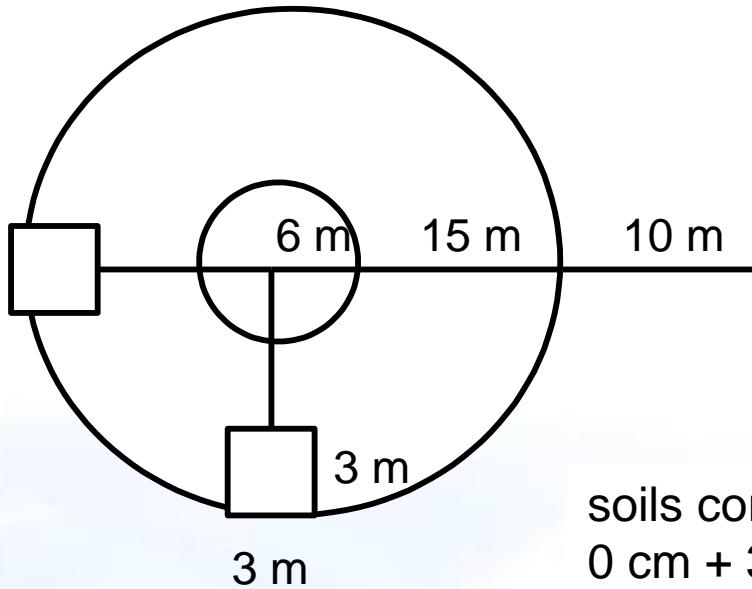


Local allometric models compared to Chave (2014)



# Biomass estimation: sampling design

Area of each sub-plot: 707 m<sup>2</sup>



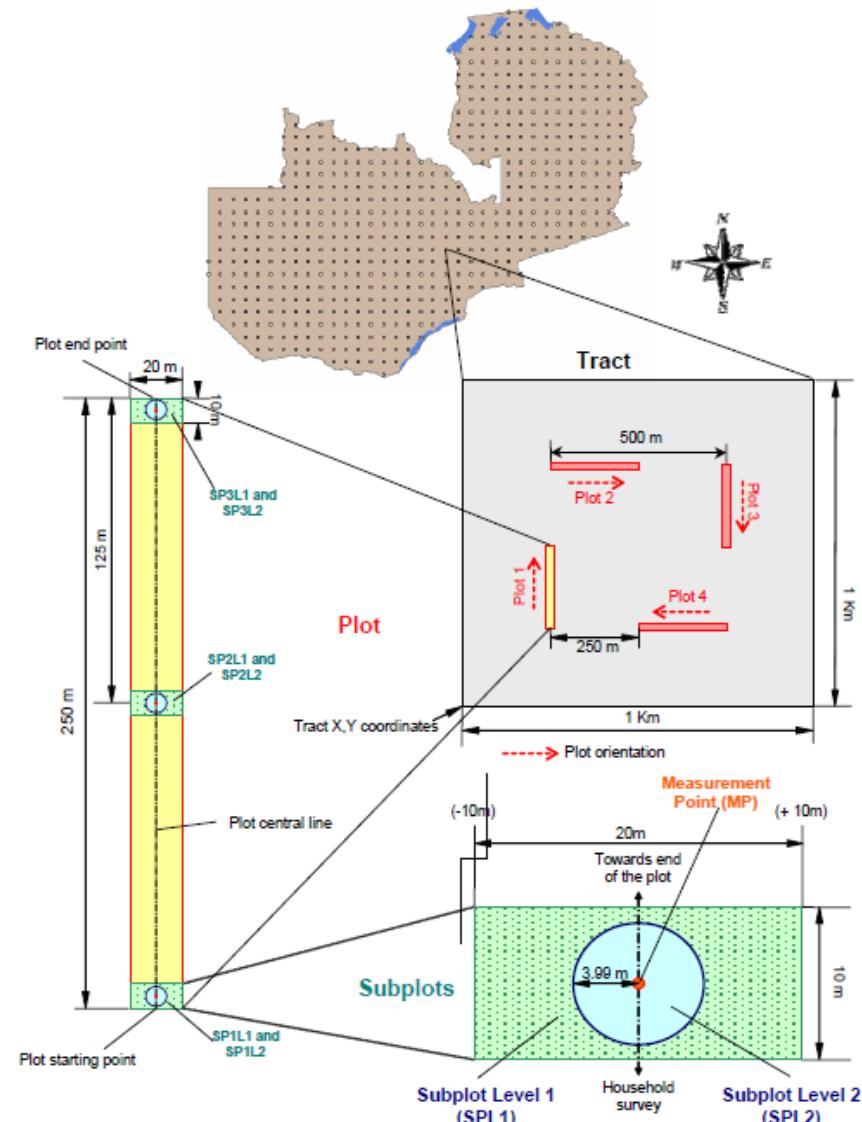
# Biomass estimation: sampling design

- Size of the plots
- Systematic or stratified random design

Plot size (Chave et al., 2004):

sub-plot size (m)	number of plots	s.d.	skewness	kurtosis
10 × 10	5000	385.08	5.42	47.05
20 × 20	1250	187.64	2.57	10.62
25 × 25	800	149.44	1.88	5.34
20 × 50	500	119.52	1.54	3.47
50 × 50	200	77.55	0.57*	-0.24**
100 × 100	50	42.01	-0.06**	-0.12**

With plots of 50X50m and greater, a normal distribution is obtained  
The standard deviation is reduced.

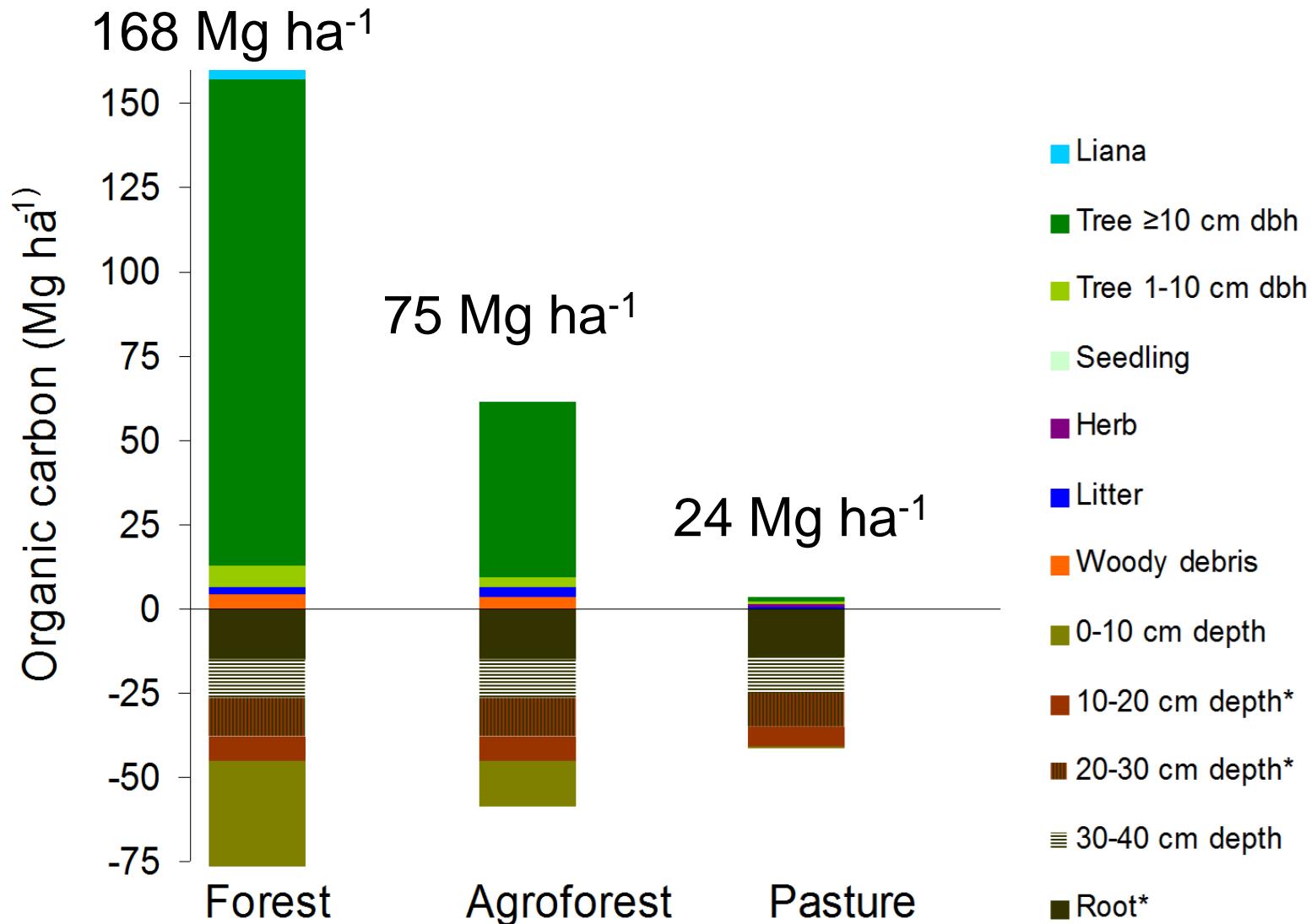


# Biomass estimation: the effect of each component

## Summary of the sources of error in the AGB estimation of a tropical forest

error type		s.e.m. (percentage of the mean)	type of data
1. tree level error	trees > 10 cm diameter	48	BCI plot—pan-tropical allometric model
	trees < 10 cm diameter	78	
2. allometric model	before $\rho$ correction	22	BCI plot—eight allometric models
	after $\rho$ correction	13	
3. within-plot uncertainty	after large tree correction	11	BCI plot—pan-tropical allometric model
	0.1 ha plot	16	
	0.25 ha plot	10	
4. among-plot uncertainty	1 ha plot	5	Marena plots—pan-tropical allometric model
		11	
total	50 1 ha plots, after $\rho$ and large tree corrections	24	—

# Five carbon pools





# Error in the modelling approach



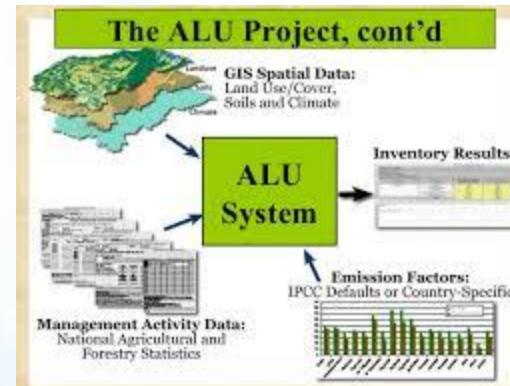
Difference approaches exist to estimate:



- » Carbon Budget Model of the Canadian Forest Sector (CBM-CFS3) ;  
<https://www.nrcan.gc.ca/forests/climate-change/13107>



- » ALU software: Agriculture and Land Use National Greenhouse Gas Inventory Software;



<http://www.nrel.colostate.edu/projects/ALUsoftware/>



openforis

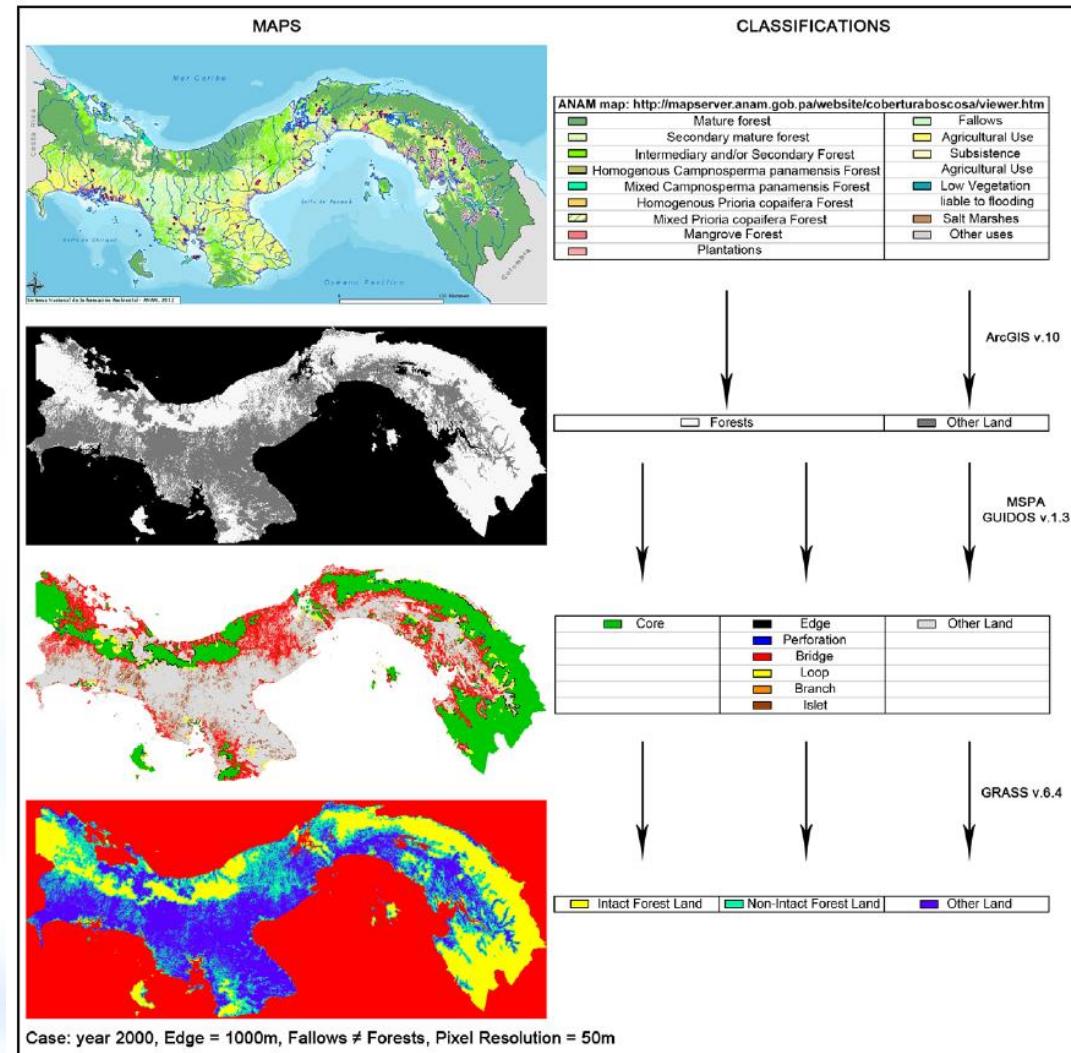
<http://www.openforis.org/>

- » OpenForis, FAO

# Error in the modelling approach

## Testing a proposed accounting approach:

Bucki *et al* (2012)  
 Simplified approach to provide  
**robust performance indicators**  
 for REDD+ using default  
 emission factors  
 with Panama as a case study



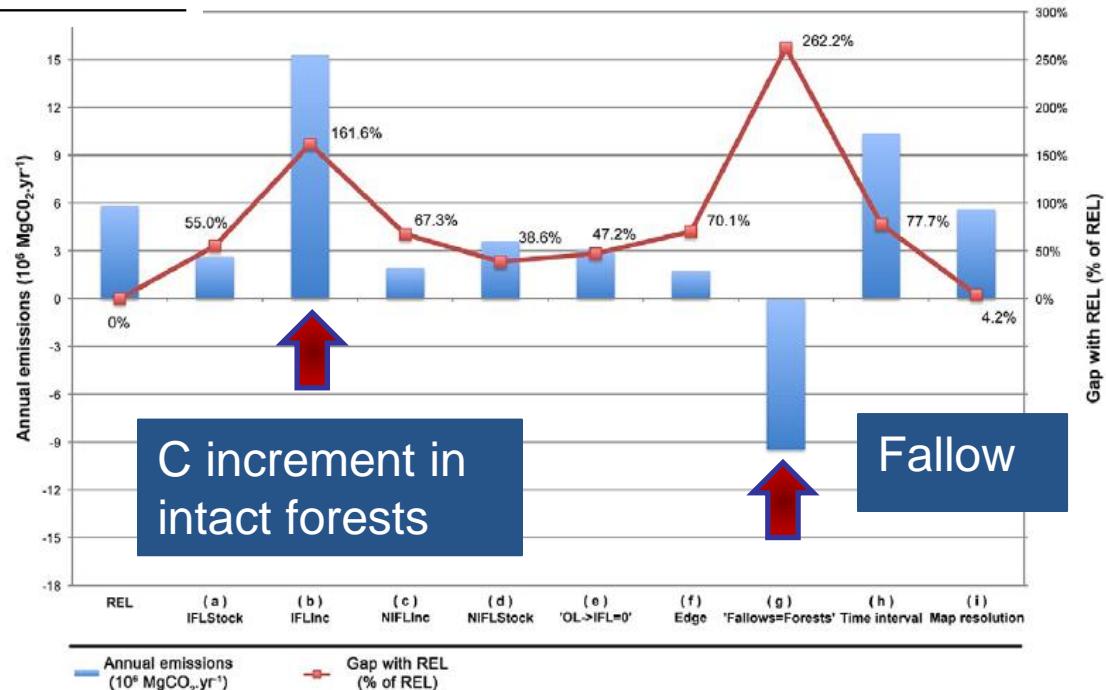
# Error in the modelling approach

	IFL 2000	NIFL 2000	OL 2000
(a)			
IFL 1992	2829 (1374)	311 (207)	239 (173)
NIFL 1992	133 (175)	521 (846)	300 (182)
OL 1992	73 (161)	396 (224)	2596 (1156)
(b)			
IFL 1992	-7.77 (9.43)	11.65 (9.03)	17.49 (7.53)
NIFL 1992	-4.97 (3.85)	-4.53 (3.93)	10.69 (4.62)
OL 1992	0	-16.72 (6.09)	0
(c)			
	Forest conservation	Forest degradation	Deforestation
	Enhancement of carbon stocks	Sustainable management of forests	Deforestation
	Enhancement of carbon stocks	Enhancement of carbon stocks	-

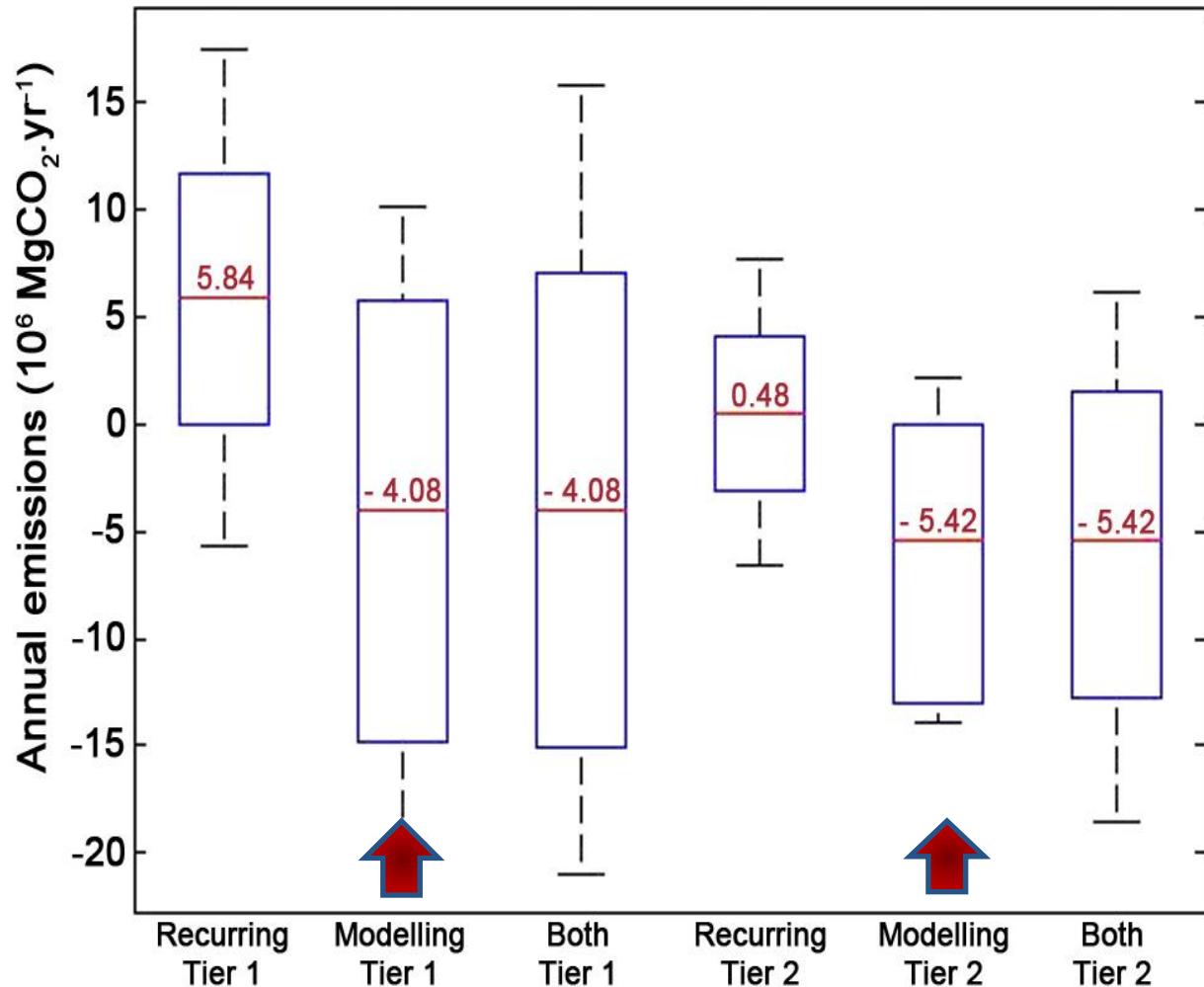
## THE MATRIX APPROACH

Difference between MODELLING and RECURRING (data) sources of error

- Models are based on different sets of assumptions
- Testing the impact of those assumptions is important



# Error in the modelling approach



Major problem for comparability between countries

Modelling error dominates over recurring sources

## Uncertainty analysis:

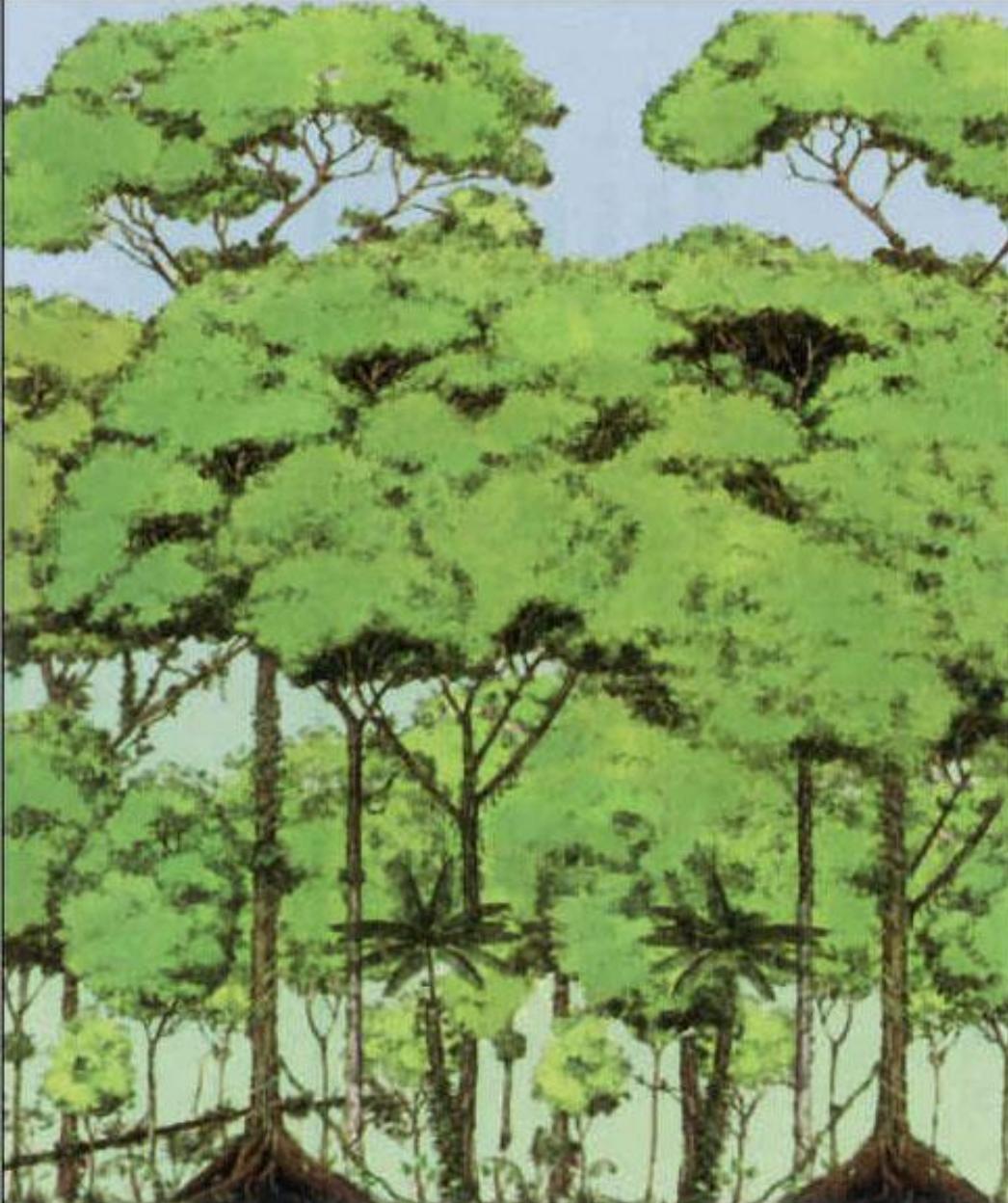
- Determine the uncertainties around the different components in activity data and emission factor (Mean, Standard deviation, Minimum, Maximum value).
- **Combine** uncertainties around different components to provide an overall uncertainty estimates

**2** approaches are proposed by the IPCC:

**TIER 1:** Error propagation

**TIER 2:** Monte Carlo method

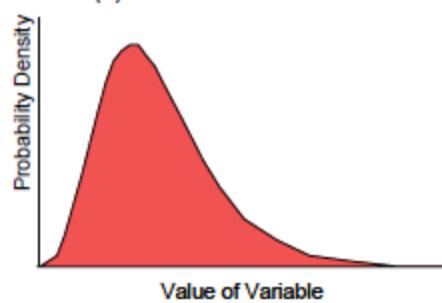
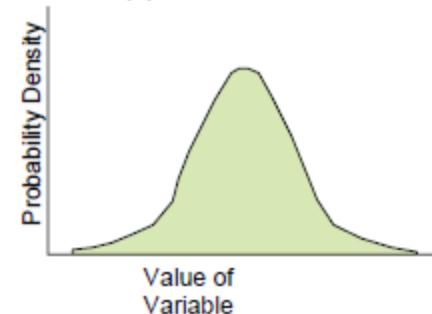
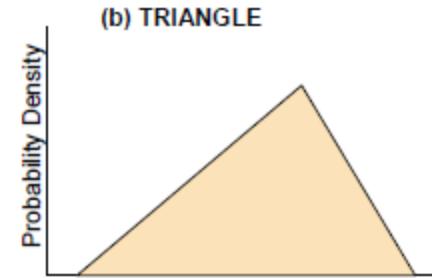
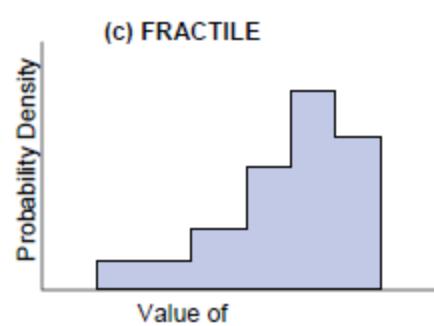
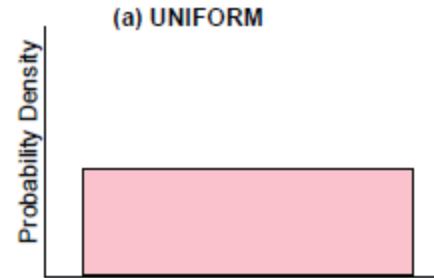
# Benefits of conducting uncertainty analysis



- ❖ Identify key parameters to your estimate
- ❖ Prioritize data collection where most needed
- ❖ Cost-effective investment in forest monitoring

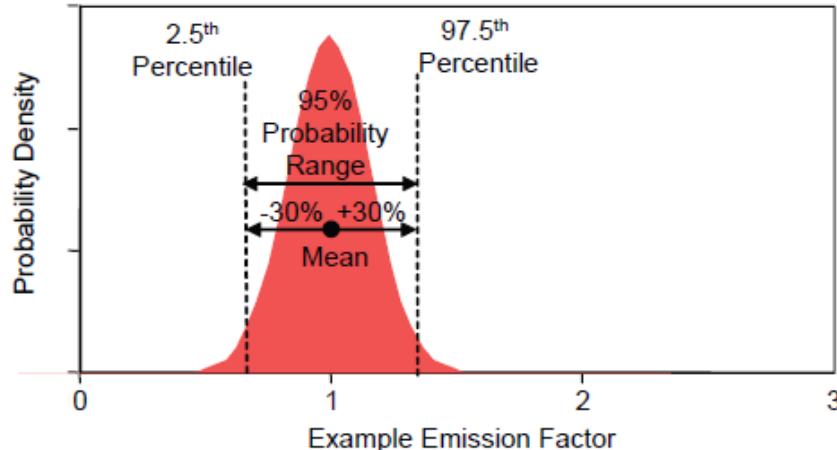
# Representing variables

- Example of commonly used probability density function models

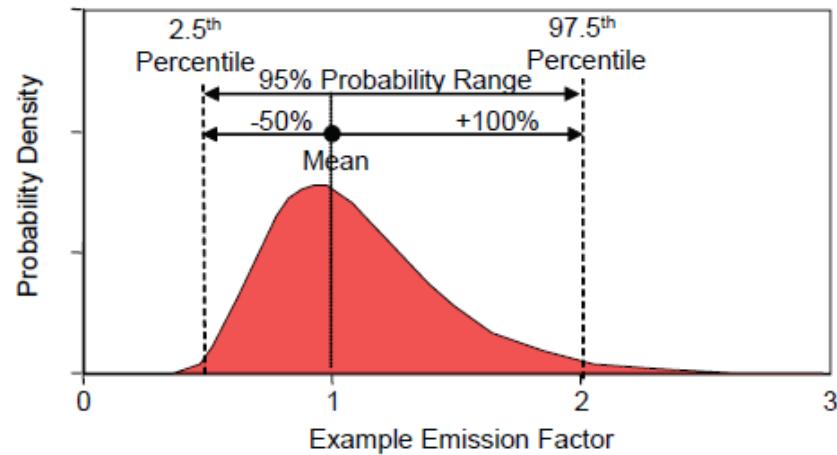


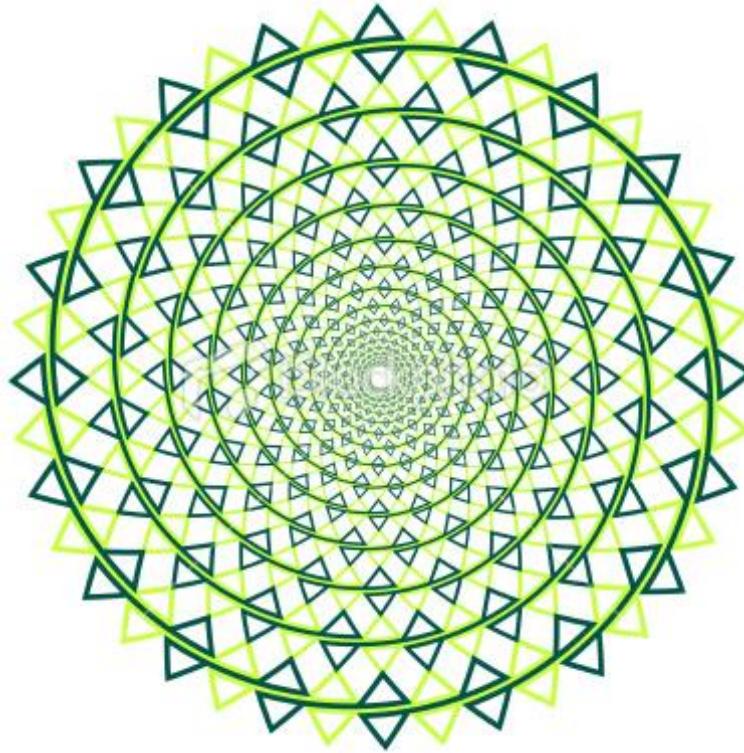
# Symmetric vs Asymmetric distribution

(a) Example of a symmetric uncertainty of  $\pm 30\%$  relative to the mean



(b) Example of an asymmetric uncertainty of -50% to +100% relative to the mean, or a factor of two





## Tier 1: Error propagation

- Simple approach (Spreadsheet)
- Requires the mean and standard deviation of input data
- Assume small error
- Doesn't deal well with large or asymmetric uncertainty
- Doesn't deal well with correlations or covariances

## Tier 1: Error propagation

Type	Example	Standard Deviation ( $\sigma_x$ )
<i>Addition and subtraction</i>	$x = a + b - c$	$\sigma_x = \sqrt{\sigma_a^2 + \sigma_b^2 + \sigma_c^2}$
<i>Multiplication and division</i>	$x = a \times b/c$	$\frac{\sigma_x}{x} = \sqrt{\left(\frac{\sigma_a}{a}\right)^2 + \left(\frac{\sigma_b}{b}\right)^2 + \left(\frac{\sigma_c}{c}\right)^2}$

In practice for multiplication and division, it is usually simplest to convert all of the uncertainties into percentages before applying the formula

These equations assume that the quantities a, b, etc. have errors which are uncorrelated and random

## Tier 2: Monte Carlo analysis

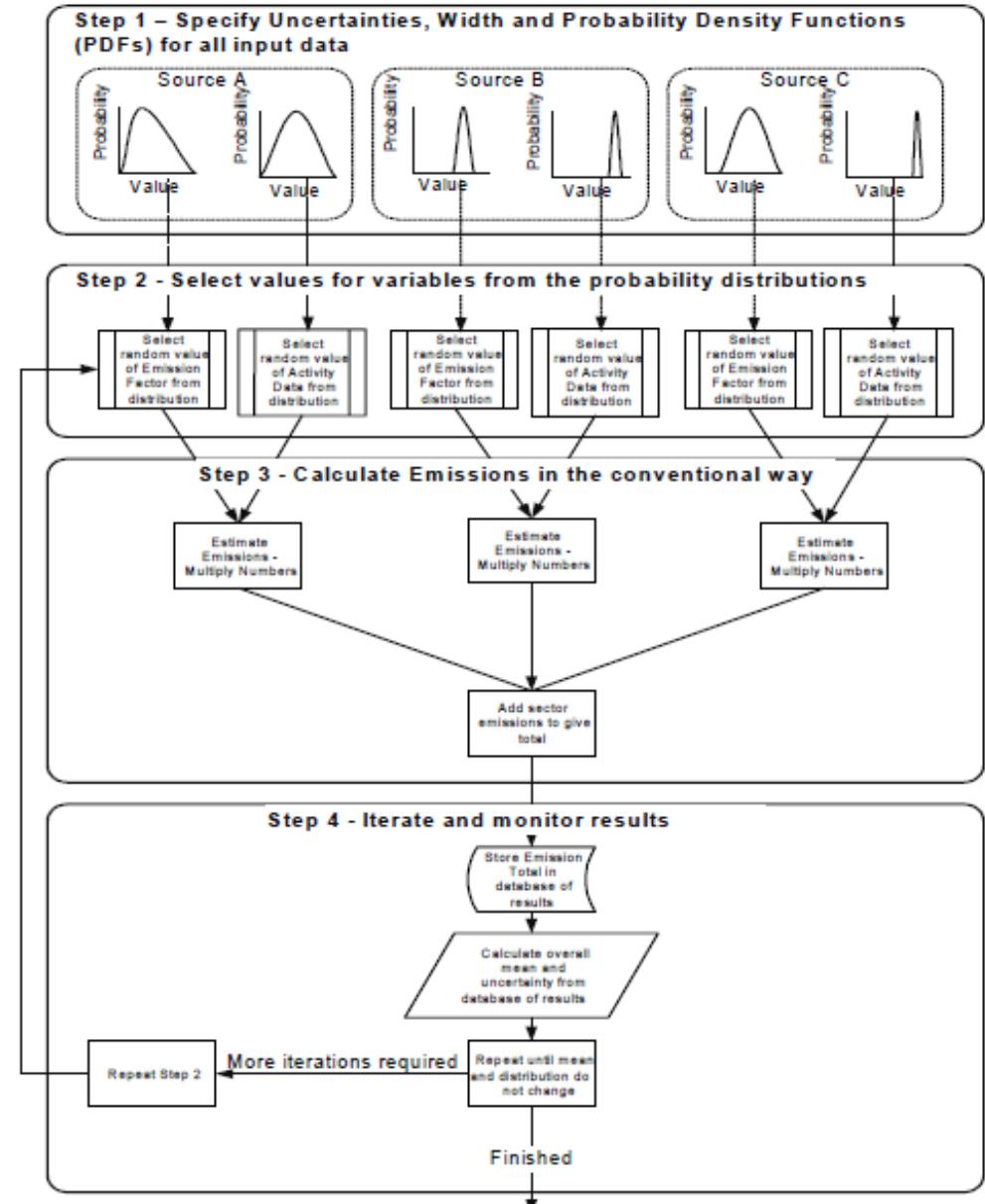
Good for large and asymmetric errors

Take into account correlations easily, e.g. Dependencies of data coming from the same datasets (emission factors)

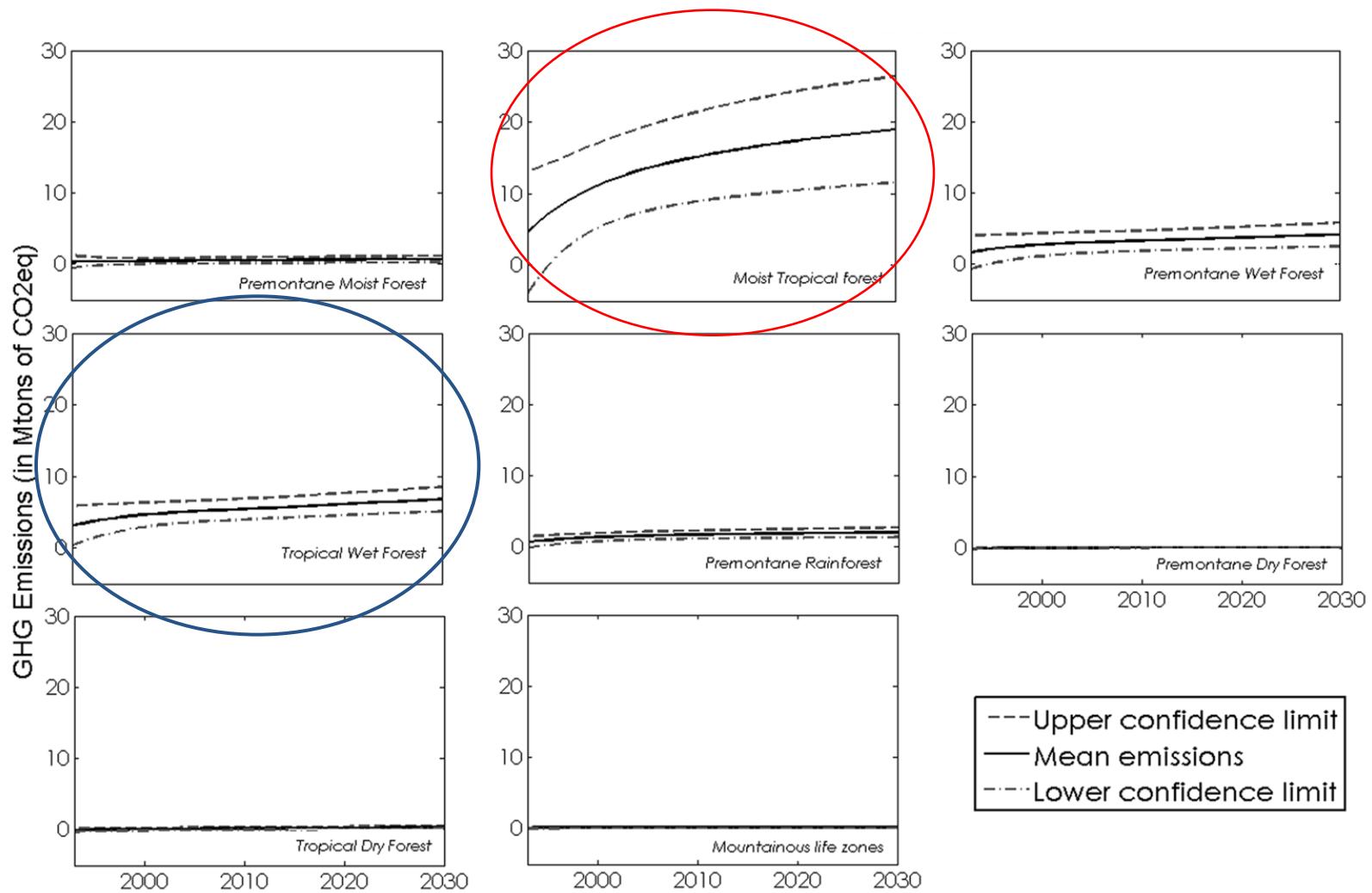


# Illustration of Monte Carlo Method

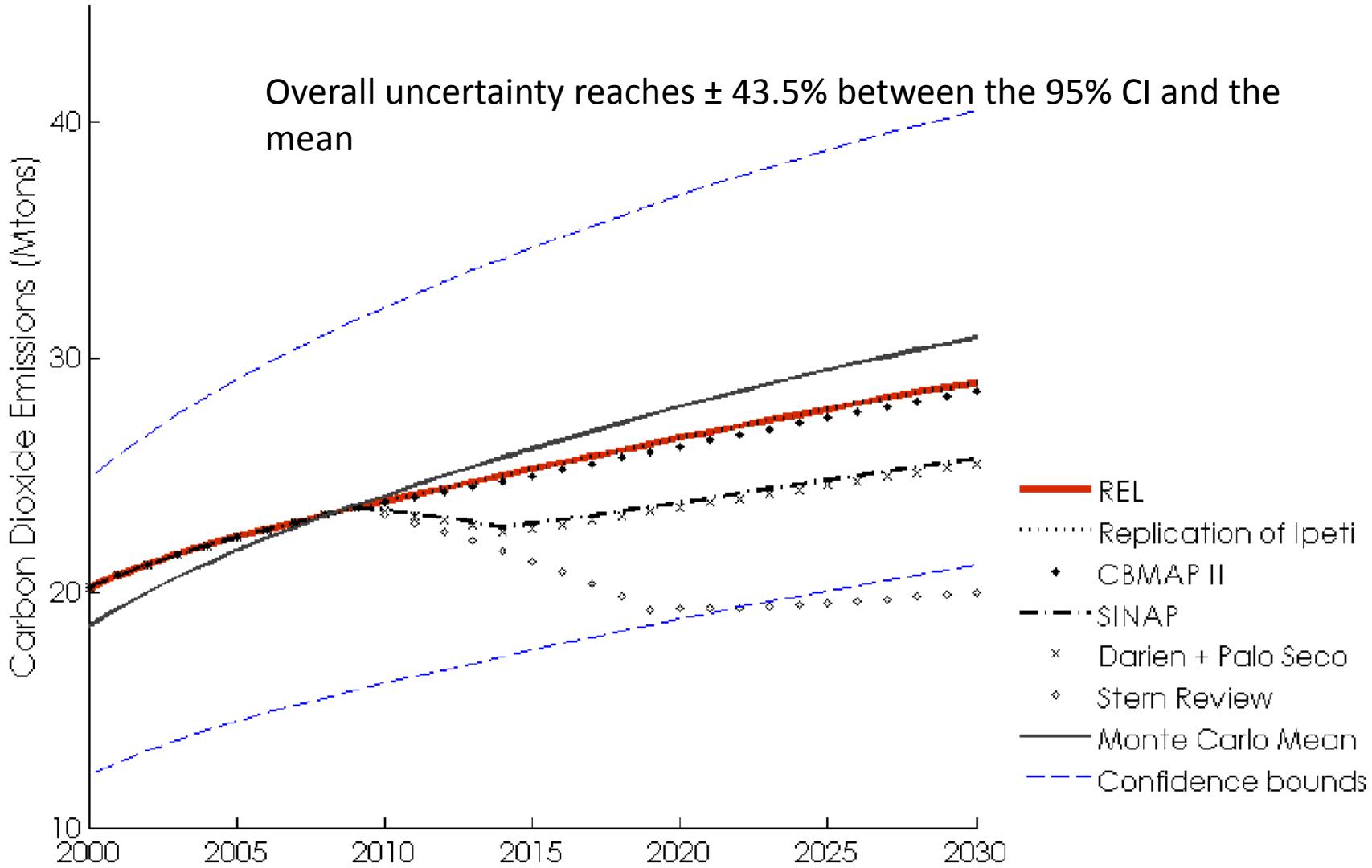
Need to choose a distribution your input variables



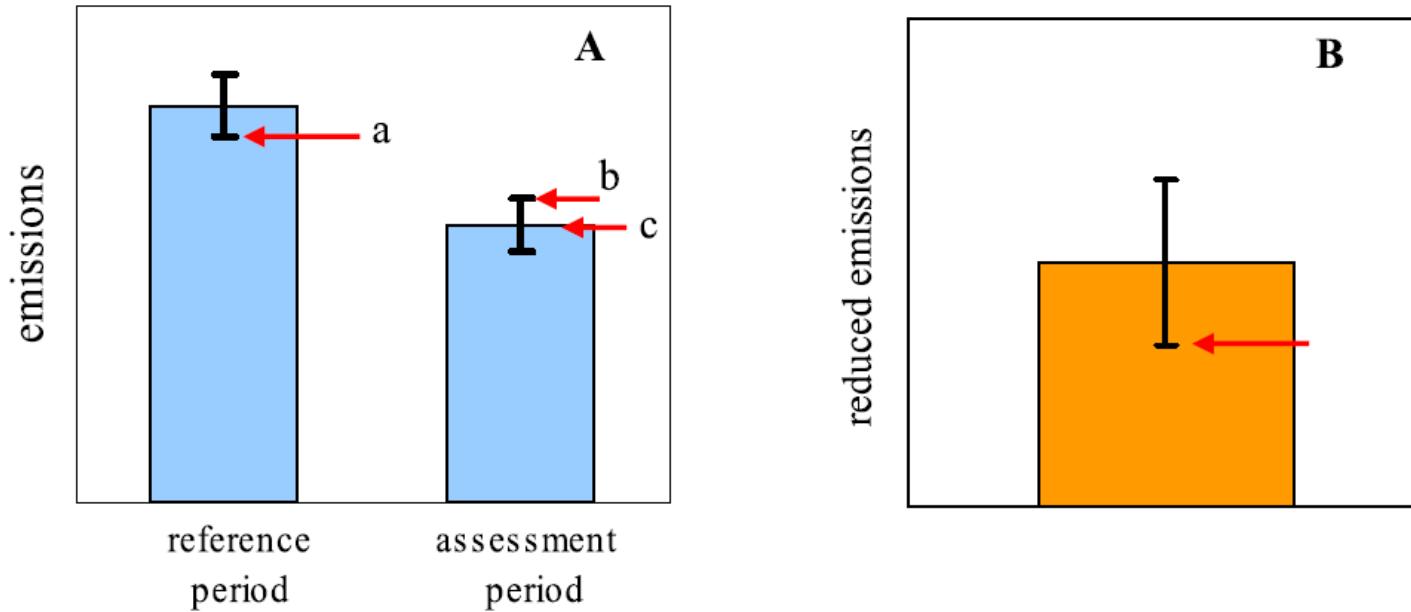
# MONTE CARLO UNCERTAINTY ANALYSIS



# COMPARING SCENARIOS TO THE OVERALL UNCERTAINTY



# Trend Uncertainty

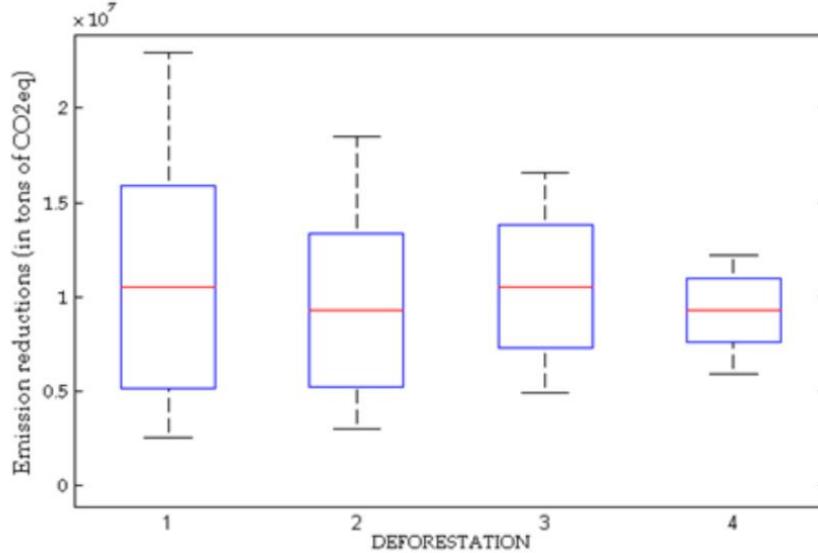


**Approach A:** Evaluate uncertainties of both the reference and the assessment period

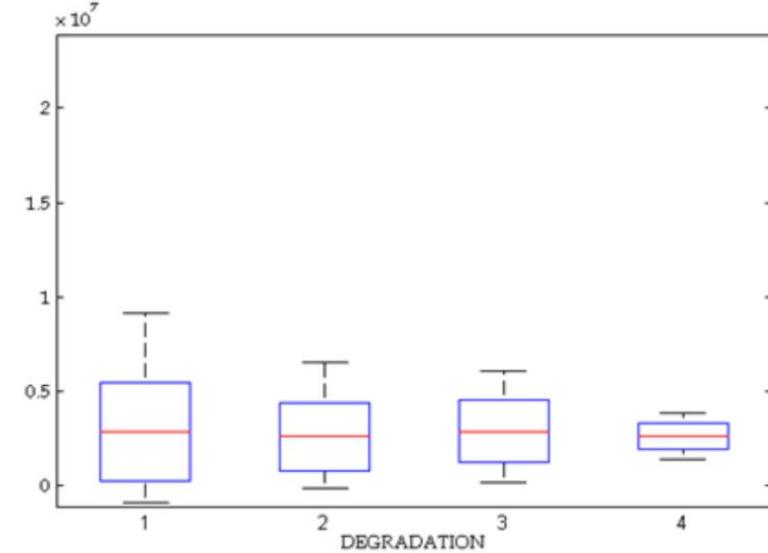
**Approach B:** Uncertainty of the difference of emissions between the reference and the assessment period

# On Emission reductions

## DEFORESTATION



## DEGRADATION



	1= No Error reduction			2=Error reduction in RS			3=Error reduction in FCD			4=Error reduction in RS and FCD		
	Deforestation	Degradation	Overall	Deforestation	Degradation	Overall	Deforestation	Degradation	Overall	Deforestation	Degradation	Overall
50% percentile	2.52	-0.94	2.93	2.99	-0.12	3.40	4.90	0.14	6.87	5.95	1.38	7.97
25% percentile	6.05	0.67	7.46	5.95	1.12	7.25	8.10	1.56	10.54	8.19	2.07	10.46
Mean	10.52	2.87	13.39	9.28	2.59	11.86	10.52	2.87	13.39	9.28	2.59	11.87
75% percentile	13.56	4.28	17.35	11.65	3.64	15.11	12.87	4.03	16.10	10.57	3.09	13.42
95% percentile	22.92	9.14	29.71	18.48	6.53	24.40	16.57	6.07	20.51	12.18	3.87	15.48
CV of SD on emission reductions	63.4%	116.8%	65.6%	53.4%	82.3%	56.9%	32.9%	63.2%	30.4%	19.2%	29.4%	18.4%



# Practicals in R!



## Implementing Monte Carlo approach in R



Asante!

# REDD+ negotiations

