Needs["NonlinearRegression`"]

ConfidenceLevel::shdw:

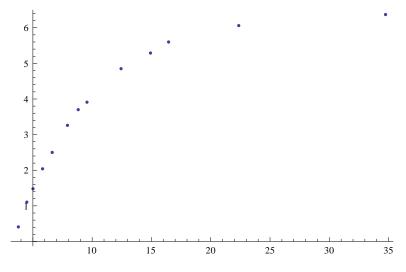
Symbol ConfidenceLevel appears in multiple contexts {HypothesisTesting`, Global`}; definitions in context HypothesisTesting` may shadow or be shadowed by other definitions.

NonlinearRegress::shdw:

Symbol NonlinearRegress appears in multiple contexts {NonlinearRegression`, Global`}; definitions in context NonlinearRegression` may shadow or be shadowed by other definitions.

```
A = Transpose[{{3.775, 5.010, 6.631, 7.917, 8.823,}
    5.816, 9.562, 14.920, 4.488, 12.437, 16.446, 22.362, 34.743},
   \{0.41, 1.48, 2.5, 3.26, 3.70, 2.04, 3.91, 5.29, 1.104, 4.85, 5.6, 6.06, 6.37\}\}
\{\{3.775, 0.41\}, \{5.01, 1.48\}, \{6.631, 2.5\}, \{7.917, 3.26\},
 \{8.823, 3.7\}, \{5.816, 2.04\}, \{9.562, 3.91\}, \{14.92, 5.29\}, \{4.488, 1.104\},
 \{12.437, 4.85\}, \{16.446, 5.6\}, \{22.362, 6.06\}, \{34.743, 6.37\}\}
Export["C:\\IRE02.dat", Transpose[Join[Transpose[A], {Table[0.05, {i, Length[A]}]}]]]
C:\IRE02.dat
Export["C:\\IRE02b.dat", Transpose[
  Join [Transpose [A], {Table [0.05, {i, Length [A]}], Table [0.05, {i, Length [A]}]}]]
C:\IRE02b.dat
"C:\\IRE02b.dat"
```





 $\{ \texttt{BestFitParameters} \rightarrow \{ \texttt{m} \rightarrow 6.10565, \texttt{t} \rightarrow 5.27542 \},$

		Estimate	Asymptotic	SE	CI
$\texttt{ParameterCITable} \rightarrow$	m	6.10565	0.0928267		{5.90134, 6.30996},
	t	5.27542	0.0936383		{5.06933, 5.48152}

EstimatedVariance \rightarrow 0.030266,

FitCurvatureTable
$$\rightarrow$$
 Max Intrinsic 0.00975343 Max Parameter-Effects 0.0306833 95. % Confidence Region 0.50111

(5.901341457941188 + 6.30996163835896) / 2

6.10565

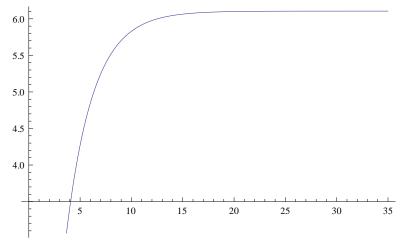
FFA = FindFit[A,
$$\{m (1-2 \exp[-x/t]), \{0 \le m \le 10, 0 \le t \le 50\}\}, \{m, t\}, x]$$

FindFit::eit:

The algorithm does not converge to the tolerance of 4.806217383937354`*^-6 in 500 iterations. The best estimated solution, with feasibility residual, KKT residual or complementary residual of $\left\{0.0000199457, 6.80251 \times 10^{-7}, 5.59289 \times 10^{-6}\right\}$, is returned.

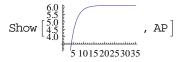
$$\{\text{m} \rightarrow \text{6.10561, t} \rightarrow \text{2.63769}\}$$

$FA = Plot[m (1 - 2 Exp[-x/t]) /. FFA, {x, 0, 35}]$



Show [FA, AP]





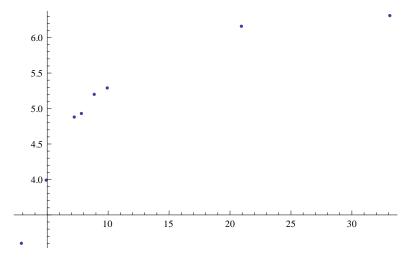
B = Transpose[{{2.8825, 4.921, 7.220, 7.807, 8.86, 9.927, 20.934, 33.112}, {3.10, 3.99, 4.88, 4.93, 5.2, 5.29, 6.16, 6.31}}]

```
\{\{2.8825, 3.1\}, \{4.921, 3.99\}, \{7.22, 4.88\}, \{7.807, 4.93\}, \{8.86, 5.2\}, \{9.927, 5.29\}, \{20.934, 6.16\}, \{33.112, 6.31\}\}
```

Export["C:\\SRE02.dat", Transpose[Append[Transpose[B], Table[0.05, {i, Length[B]}]]]]
C:\SRE02.dat

Export ["C:\\SRE02b.dat", Transpose[
 Join[Transpose[B], {Table[0.05, {i, Length[B]}], Table[0.05, {i, Length[B]}]]]]
C:\\SRE02b.dat

BP = ListPlot[B]



NonlinearRegress[B, m (1 - Exp[-x/t]), $\{m, t\}$, x]

 $\left\{ \texttt{BestFitParameters} \, \rightarrow \, \left\{ \texttt{m} \, \rightarrow \, 6.20275 \, \text{, t} \, \rightarrow \, 4.71361 \right\} \, \text{,} \right.$

		Estimate	Asymptotic	SE	CI	
$\texttt{ParameterCITable} \rightarrow$	m	6.20275	0.100366		{5.95717,	6.44834},
	t	4.71361	0.226975		{4.15822,	5.269}

EstimatedVariance \rightarrow 0.0199299,

		DF	SumOfSq	MeanSq
	Model	2	206.316	103.158
${\tt ANOVATable} \to $	Error	6	0.119579	0.0199299,
	Uncorrected Total	8	206.435	
	Corrected Total	7	7.83275	

 $\mbox{AsymptoticCorrelationMatrix} \rightarrow \left(\begin{array}{cc} \mbox{1.} & \mbox{0.794386} \\ \mbox{0.794386} & \mbox{1.} \end{array} \right) \mbox{,}$

			Curvature
FitCurvatureTable →	Max	Intrinsic	0.0467384
Ficcurvacure able →	Max	Parameter-Effects	0.0393828
	95.	% Confidence Region	0.440942

4.7136 - 4.158221509069886

0.555378

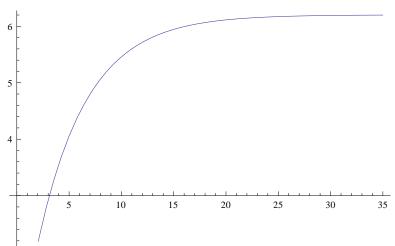
 $FFB = FindFit[B, \{m \ (1 - Exp[-x/t]), \{0 \le m \le 10, 0 \le t \le 50\}\}, \{m, t\}, x]$

FindFit::eit:

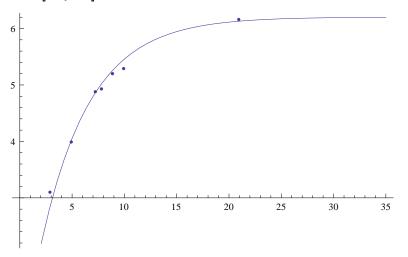
The algorithm does not converge to the tolerance of 4.806217383937354`*^-6 in 500 iterations. The best estimated solution, with feasibility residual, KKT residual or complementary residual of $\{0.0000445421, 3.0439 \times 10^{-6}, 0.0000153363\}$, is returned.

 $\{\text{m} \rightarrow \text{6.20269, t} \rightarrow \text{4.71348}\}$

 $FB = Plot[m (1 - Exp[-x/t]) /. FFB, {x, 0, 35}]$



Show [FB, BP]

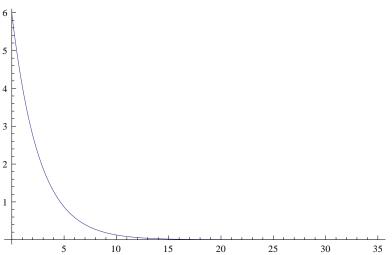


F = Transpose [$\{0.5, \{2.022, 2.84, 4.3, 6.985, 8.713, 12.098\}, \{4.29, 3.11, 2.65, 1.57, 1.15, 0.63\}\}$

 $\{\{1.011, 4.29\}, \{1.42, 3.11\}, \{2.15, 2.65\}, \{3.4925, 1.57\}, \{4.3565, 1.15\}, \{6.049, 0.63\}\}$

Export["C:\\SPE02.dat", Transpose[Append[Transpose[F], Table[0.05, {i, Length[F]}]]]] C:\SPE02.dat

Show [FF, FP]



G = Transpose[{0.5 {5.553, 3.635, 10.686, 14.576, 18.98, 25.62, 37.46, 45.33, 52.4, 60.15}, {3.695, 4.19, 2.893, 2.379, 1.877, 1.327, 0.71, 0.446, 0.299, 0.203}}]

 $\{\{2.7765, 3.695\}, \{1.8175, 4.19\}, \{5.343, 2.893\}, \{7.288, 2.379\}, \{9.49, 1.877\}, \{12.81, 1.327\}, \{18.73, 0.71\}, \{22.665, 0.446\}, \{26.2, 0.299\}, \{30.075, 0.203\}\}$

C:\SPE0x.dat

Export ["C:\\SPE0xb.dat", Transpose[

Join[Transpose[G], {Table[0.05, {i, Length[G]}], Table[0.05, {i, Length[G]}]]]]

C:\SPE0xb.dat

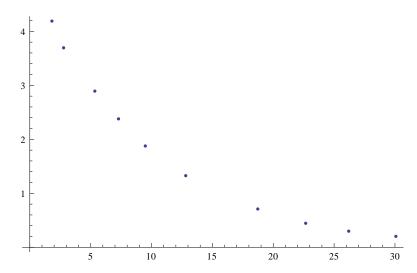
NonlinearRegress [P, m Exp[-2 x /t], $\{m, t\}$, x]

 $\big\{ exttt{BestFitParameters}
ightarrow \{ exttt{m}
ightarrow 2.11027, exttt{t}
ightarrow 226.629 \big\}$,

EstimatedVariance \rightarrow 0.00826723,

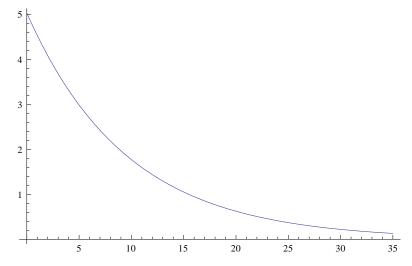
FitCurvatureTable \rightarrow Max Intrinsic 0.0175911 Max Parameter-Effects 0.362073 95. % Confidence Region 0.379478

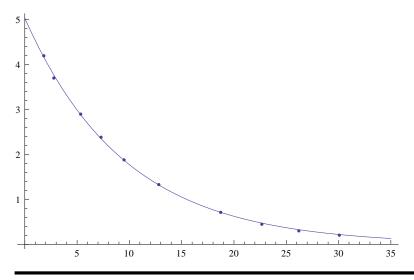
GP = ListPlot[G]



FFG = FindFit[G, {m (Exp[-2 x/t]), {0 \le m <= 10, 0 \le t \le 50}}, {m, t}, x] {m \rightarrow 5.0274, t \rightarrow 19.1526}

Show [GP, Plot[m (Exp[-2x/t]) /. FFG, $\{x, 0, 35\}$]]





```
H = Transpose [
  \{\{2.418, 6.375, 10.092, 13.977, 27.47, 64.65\}, \{2.17, 2.79, 3.19, 3.65, 4.581, 5.74\}\}]
```

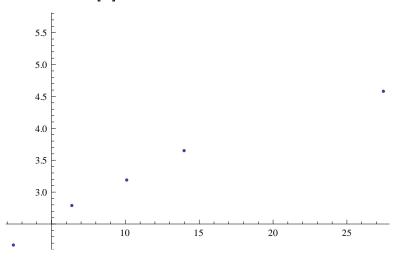
 $\{\{2.418, 2.17\}, \{6.375, 2.79\}, \{10.092, 3.19\}, \{13.977, 3.65\}, \{27.47, 4.581\}, \{64.65, 5.74\}\}$

Export["C:\\SRE0x.dat", Transpose[Append[Transpose[H], Table[0.05, {i, Length[H]}]]]] C:\SRE0x.dat

Export["C:\\SRE0xb.dat", Transpose[Join[Transpose[H], {Table[0.05, {i, Length[H]}], Table[0.05, {i, Length[H]}]]]] C:\SRE0xb.dat

NonlinearRegress [P, m Exp[-2 x/t], $\{m, t\}$, x]

HP = ListPlot[H]



NonlinearRegress[H, m $(1 - Exp[-x/t]), \{m, t\}, x]$

{BestFitParameters \rightarrow {m \rightarrow 5.27226, t \rightarrow 9.63544},

			Asymptotic	SE	CI
$\texttt{ParameterCITable} \rightarrow$	m	5.27226	0.535786		{3.78468, 6.75984},
	t	9.63544	2.65335		{2.26856, 17.0023}

EstimatedVariance \rightarrow 0.408519,

		DF	SumOfSq	MeanSq
	Model	2	88.2907	44.1453
${\tt ANOVATable} \to $	Error	4	1.63408	0.408519,
	Uncorrected Total	6	89.9248	
	Corrected Total	5	8.36832	

 $\mbox{AsymptoticCorrelationMatrix} \rightarrow \begin{pmatrix} \mbox{1.} & 0.742946 \\ 0.742946 & 1. \end{pmatrix} \mbox{,}$

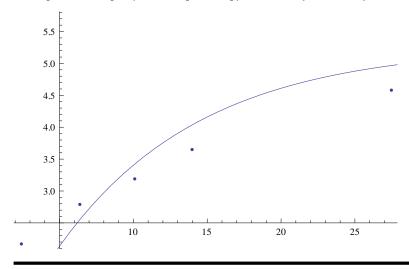
			Curvature
FitCurvatureTable →	Max	Intrinsic	0.26555 _l
Ficcurvacure able →	Max	Parameter-Effects	0.335222
	95.	% Confidence Region	0.379478

9.635440000097441 - 2.2685636900144095

7.36688

FFH = FindFit[H, {m (1 - Exp[-x/t])}, {m,t}, x]
{
$$m \rightarrow 5.27226$$
, t $\rightarrow 9.63544$ }

Show [HP, Plot[m (1 - Exp[-x/t]) /. FFH, $\{x, 0, 35\}$, PlotRange \rightarrow Full]]



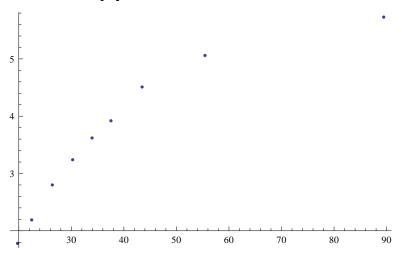
 $J = Transpose[{\{19.762, 26.381, 22.453, 37.537, 33.946, 30.25, 43.47, 55.43, 89.45\},$ {1.78, 2.80, 2.19, 3.92, 3.62, 3.24, 4.51, 5.06, 5.73}}]

```
\{\{19.762,\, 1.78\}\,,\, \{26.381,\, 2.8\}\,,\, \{22.453,\, 2.19\}\,,\, \{37.537,\, 3.92\}\,,
 \{33.946, 3.62\}, \{30.25, 3.24\}, \{43.47, 4.51\}, \{55.43, 5.06\}, \{89.45, 5.73\}\}
```

```
C:\IRE0x.dat
Export["C:\\IRE0xb.dat", Transpose[
                    \label{loss_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuo
```

C:\IRE0xb.dat

JP = ListPlot[J]



 $FFJ = FindFit[J, \{m (1-2 Exp[-x/t]), \{0 \le m \le 10, 0 \le t \le 50\}\}, \{m, t\}, x]$ $\{m \rightarrow 5.70446, t \rightarrow 19.3354\}$

NonlinearRegress [J, m (1-2 Exp[-x/t]), {m,t}, x]

{BestFitParameters \rightarrow {m \rightarrow 5.70454, t \rightarrow 19.3357},

		Estimate	Asymptotic	SE	CI
$\texttt{ParameterCITable} \rightarrow$	m	5.70454	0.092729		{5.48527, 5.92381},
	t	19.3357	0.36729		{18.4672, 20.2042}

EstimatedVariance \rightarrow 0.0136681,

		DF	SumOfSq	MeanSq
	Model	2	133.454	66.7269
${\tt ANOVATable} \to $	Error	7	0.095677	0.0136681,
	Uncorrected Total	9	133.55	
	Corrected Total	8	13.647	

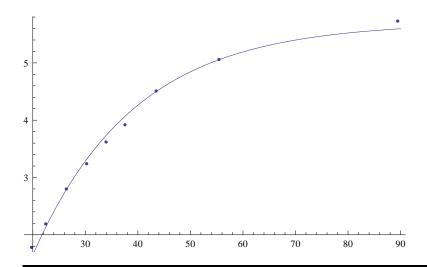
 $\mbox{AsymptoticCorrelationMatrix} \rightarrow \begin{pmatrix} \mbox{1.} & 0.782557 \\ 0.782557 & 1. \end{pmatrix} \mbox{,}$

			Curvature
FitCurvatureTable →	Max	Intrinsic	0.00920316
riccurvacurerable >	Max	Parameter-Effects	0.0508245
	95.	% Confidence Region	0.459441

(19.335671403814917 - 18.467168377086722)

0.868503

Show [JP, Plot[m (1 - 2 Exp[-x/t]) /. FFJ, $\{x, 10, 90\}$, PlotRange \rightarrow Full]]



K = Transpose[{{6.072, 9.047, 7.693, 10.995, 12.988, 14.955, 20.28, 31.318, 66.19},
{0.62, 1.82, 1.22, 2.45, 3.045, 3.44, 4.40, 5.33, 5.91}}]

```
 \{\{6.072,\,0.62\},\,\{9.047,\,1.82\},\,\{7.693,\,1.22\},\,\{10.995,\,2.45\},\\ \{12.988,\,3.045\},\,\{14.955,\,3.44\},\,\{20.28,\,4.4\},\,\{31.318,\,5.33\},\,\{66.19,\,5.91\}\}
```

Export["C:\\IRE01.dat", Transpose[Append[Transpose[K], Table[0.05, {i, Length[K]}]]]]
C:\IRE01.dat

Export ["C:\\IRE01b.dat", Transpose[
 Join[Transpose[K], {Table[0.05, {i, Length[K]}], Table[0.05, {i, Length[K]}]]]]
C:\IRE01b.dat

NonlinearRegress [K, m (1 - 2 Exp[-x/t]), $\{m, t\}$, x, ConfidenceLevel \rightarrow .6827]

 $\left\{ \mathtt{BestFitParameters} \,
ightarrow \left\{ \mathtt{m} \,
ightarrow 5.54784 \,, \, \mathtt{t} \,
ightarrow 8.36
ight\} \,,$

		Estimate	Asymptotic	SE	CI	
$\texttt{ParameterCITable} \rightarrow $	m	5.54784	0.168287		{5.36664,	5.72904},
	t	8.36	0.279064		{8.05952,	8.66048}

EstimatedVariance → 0.0670196,

AsymptoticCorrelationMatrix $\rightarrow \begin{pmatrix} 1. & 0.603315 \\ 0.603315 & 1. \end{pmatrix}$,

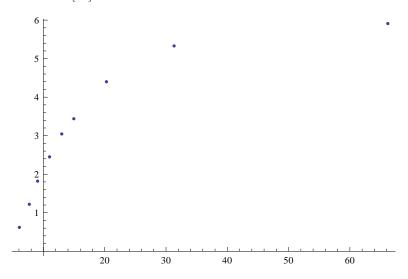
FitCurvatureTable
$$\rightarrow$$
 Max Intrinsic 0.0197504 Max Parameter-Effects 0.0577719 68.27 % Confidence Region 0.857956

(5.729043614424136 - 5.547842876536437)

0.181201

KP = ListPlot[K]

ListPlot[K]

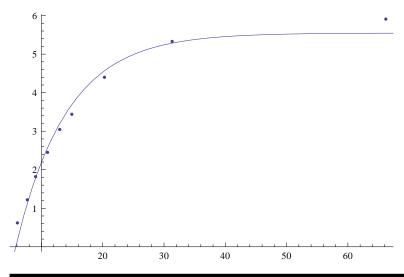


FindFit::eit:

The algorithm does not converge to the tolerance of 4.806217383937354 * ^ -6 in 500 iterations. The best estimated solution, with feasibility residual, KKT residual or complementary residual of $\left\{\,0.0000200426\,,\,6.72046\times10^{-7}\,,\,9.65822\times10^{-6}\,\right\}$, is returned.

 $\{m \rightarrow 5.5478, t \rightarrow 8.35994\}$

Show [KP, FK = Plot[m (1-2 Exp[-x/t]) /. FFK, $\{x, 0, 70\}$, PlotRange \rightarrow Full]]



 $L = Transpose[{\{1.6793, 3.3312, 4.733, 7.663, 11.862, 18.981, 50.17\},}$ {2.56, 2.83, 3.21, 3.83, 4.43, 5.09, 5.87}}]

```
\{\{1.6793, 2.56\}, \{3.3312, 2.83\}, \{4.733, 3.21\},
 \{7.663, 3.83\}, \{11.862, 4.43\}, \{18.981, 5.09\}, \{50.17, 5.87\}\}
```

```
Export["C:\\SRE01.dat", Transpose[Append[Transpose[L], Table[0.05, {i, Length[L]}]]]]
C:\SRE01.dat
```

Export["C:\\SRE01b.dat", Transpose[

 $\label{loss_constraints} Join[Transpose[L], \{Table[0.05, \{i, Length[L]\}], Table[0.05, \{i, Length[L]\}]\}]] \\ \\$

C:\SRE01b.dat

NonlinearRegress[L, m $(1 - Exp[-x/t]), \{m, t\}, x]$

 $\big\{ \mathtt{BestFitParameters} \, o \, \{\mathtt{m} \, o \, 5.28091 \, , \, \mathtt{t} \, o \, 4.66211 \, \} \, ,$

EstimatedVariance \rightarrow 0.340451,

 $\label{eq:asymptoticCorrelationMatrix} \mbox{\rightarrow} \left(\begin{array}{ll} 1. & 0.710949 \\ 0.710949 & 1. \end{array} \right) \mbox{,}$

FitCurvatureTable
$$\rightarrow$$
 Max Intrinsic 0.238802 Max Parameter-Effects 0.285512 95. % Confidence Region 0.415725

4.662109482596877 - 7.419237638723131

-2.75713

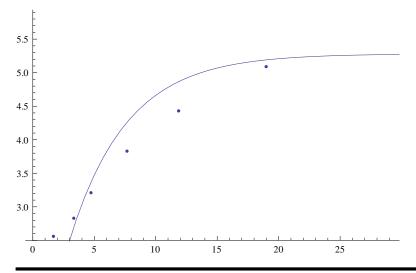
$$FFL = FindFit[L, \{m (1 - Exp[-x/t]), \{0 \le m \le 10, 0 \le t \le 50\}\}, \{m, t\}, x]$$

FindFit::eit:

The algorithm does not converge to the tolerance of 4.806217383937354`*^-6 in 500 iterations. The best estimated solution, with feasibility residual, KKT residual or complementary residual of $\left\{0.0000106627, 6.85956 \times 10^{-7}, 4.71544 \times 10^{-6}\right\}$, is returned.

```
\{m \rightarrow 5.28086, t \rightarrow 4.66199\}
```

Show [ListPlot[L], Plot[m (1 - Exp[-x/t]) /. FFL, $\{x, 0, 35\}$, PlotRange \rightarrow Full]]



 $M = Transpose[{0.5, 4.881, 6.488, 9.148, 10.897, 14.265, 17.384, 22.153, 32.521},$ {3.03, 2.66, 2.09, 1.85, 1.35, 0.99, 0.622, 0.209}}]

```
\{\{2.4405, 3.03\}, \{3.244, 2.66\}, \{4.574, 2.09\}, \{5.4485, 1.85\},
 \{7.1325, 1.35\}, \{8.692, 0.99\}, \{11.0765, 0.622\}, \{16.2605, 0.209\}\}
```

C:\SPE01.dat

NonlinearRegress[M, m Exp[-2x/t], {m,t}, x]

{BestFitParameters \rightarrow {m \rightarrow 4.73241, t \rightarrow 11.2133},

EstimatedVariance \rightarrow 0.00153012,

AsymptoticCorrelationMatrix
$$\rightarrow \begin{pmatrix} 1. & -0.898956 \\ -0.898956 & 1. \end{pmatrix}$$
,

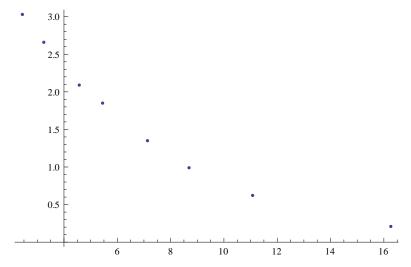
FitCurvatureTable
$$\rightarrow$$
 Max Intrinsic 0.0195123 Max Parameter-Effects 0.166056 95. % Confidence Region 0.440942

4.732412905944776 - 4.93042836355717

-0.198015

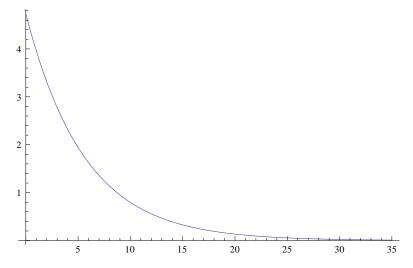
```
Export["C:\\SPE01b.dat", Transpose[
   Join[Transpose[M], {Table[0.05, {i, Length[M]}], Table[0.05, {i, Length[M]}]]]]
C:\\SPE01b.dat
```

MP = ListPlot[M]

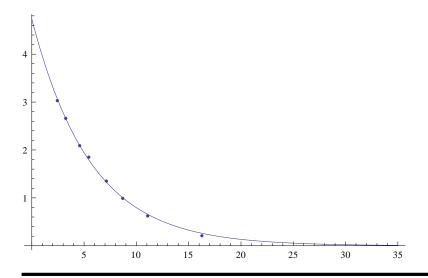


FFM = FindFit[M, {m (Exp[-2 x/t]), {0 \le m <= 10, 0 \le t \le 50}}, {m, t}, x] {m \rightarrow 4.73239, t \rightarrow 11.2134}

 $FM = Plot[m (Exp[-2x/t]) /. FFM, \{x, 0, 35\}, PlotRange \rightarrow Full]$



Show [FM , MP]



P = Transpose[{0.5 {3.542, 4.716, 8.461, 25.31, 98.75, 127.33}, {2.12, 2.000, 1.975, 1.974, 1.45, 1.11}}]

```
\{\{1.771, 2.12\}, \{2.358, 2.\}, \{4.2305, 1.975\},
 \{12.655, 1.974\}, \{49.375, 1.45\}, \{63.665, 1.11\}\}
```

Export ["C:\\SPEOw.dat", Transpose [Append [Transpose [P], Table [0.05, {i, Length [P]}]]]]

C:\SPEOw.dat

Export ["C:\\SPE0wb.dat", Transpose [

Join [Transpose [P], {Table [0.05, {i, Length [P]}], Table [0.05, {i, Length [P]}]}]]

C:\SPE0wb.dat

NonlinearRegress [P, m Exp[-2 x / t], $\{m, t\}$, x]

{BestFitParameters \rightarrow {m \rightarrow 2.11027, t \rightarrow 226.629},

EstimatedVariance \rightarrow 0.00826723,

 $\begin{pmatrix} 1. & -0 \\ -0.567234 & 1. \end{pmatrix}$ AsymptoticCorrelationMatrix →

FitCurvatureTable
$$\rightarrow$$
 Max Intrinsic 0.0175911 Max Parameter-Effects 0.362073 95. % Confidence Region 0.379478

226.62896607256073 - 301.3752393589258`

-74.7463

FFP = FindFit[P, {m (Exp[-2 x / t]), {0 \le m <= 10}}, {m, t}, x] {m \rightarrow 2.11027, t \rightarrow 226.63}

Show [ListPlot[P, PlotRange → Full],

 $Plot[m (Exp[-2x/t]) /. FFP, \{x, 0, 70\}, PlotRange \rightarrow Full]]$

