$$\begin{split} \mathbf{f}[\mathbf{i}_{-}, \mathbf{x}_{-}] &:= \text{Sum}\left[\mathbf{c}[\mathbf{i}, \mathbf{j}] \times ^{\wedge} (\mathbf{j} - 1), \{\mathbf{j}, \mathbf{n}\}\right]; \ \mathbf{a} = \text{Table}\left[\mathbf{D}[\mathbf{f}[\mathbf{i}, \mathbf{x}], \{\mathbf{x}, \mathbf{k} - 1\}], \{\mathbf{k}, \mathbf{n} / 2\}\right] \\ &\left\{\mathbf{c}[\mathbf{i}, 1] + \mathbf{x} \cdot \mathbf{c}[\mathbf{i}, 2] + \mathbf{x}^{2} \cdot \mathbf{c}[\mathbf{i}, 3] + \mathbf{x}^{3} \cdot \mathbf{c}[\mathbf{i}, 4] + \mathbf{x}^{4} \cdot \mathbf{c}[\mathbf{i}, 5] + \mathbf{x}^{5} \cdot \mathbf{c}[\mathbf{i}, 6] + \mathbf{x}^{6} \cdot \mathbf{c}[\mathbf{i}, 7] + \mathbf{x}^{7} \cdot \mathbf{c}[\mathbf{i}, 8], \\ &\mathbf{c}[\mathbf{i}, 2] + 2 \times \mathbf{c}[\mathbf{i}, 3] + 3 \times^{2} \cdot \mathbf{c}[\mathbf{i}, 4] + 4 \times^{3} \cdot \mathbf{c}[\mathbf{i}, 5] + 5 \times^{4} \cdot \mathbf{c}[\mathbf{i}, 6] + 6 \times^{5} \cdot \mathbf{c}[\mathbf{i}, 7] + 7 \times^{6} \cdot \mathbf{c}[\mathbf{i}, 8], \\ &2 \cdot \mathbf{c}[\mathbf{i}, 3] + 6 \times \mathbf{c}[\mathbf{i}, 4] + 12 \times^{2} \cdot \mathbf{c}[\mathbf{i}, 5] + 20 \times^{3} \cdot \mathbf{c}[\mathbf{i}, 6] + 30 \times^{4} \cdot \mathbf{c}[\mathbf{i}, 7] + 42 \times^{5} \cdot \mathbf{c}[\mathbf{i}, 8], \\ \end{aligned}$$

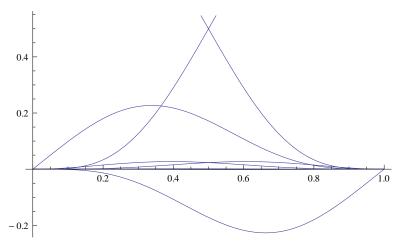
 $6 c[i, 4] + 24 x c[i, 5] + 60 x^{2} c[i, 6] + 120 x^{3} c[i, 7] + 210 x^{4} c[i, 8]$ 

 $df[j_, b_] := a/.x \rightarrow b/.i \rightarrow j$ 

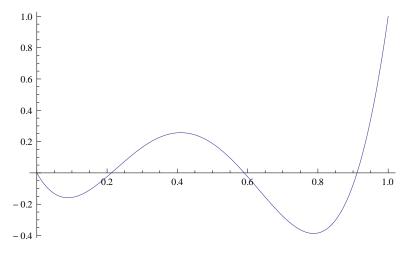
r = Solve[Flatten[Join[Table[df[i, 0][[k]] ==

 $\label{lem:heavisideTheta} \begin{subarray}{ll} HeavisideTheta [0.1+n/2-i] & (KroneckerDelta [i, k+n/2]), \\ \{k,1,n/2\}, \{i,n\}], Table [df [i,1][[k]] = HeavisideTheta [-0.1+i-n/2] \\ & (KroneckerDelta [i,k] + KroneckerDelta [i,k+n/2]), \{k,1,n/2\}, \{i,n\}]]], \\ Flatten [Table [c[i,j], \{i,n\}, \{j,n\}]]][[1]]; \end{subarray}$ 

Plot[Table[f[i, x], {i, n}] /. r, {x, 0, 1}]



Plot[df[8, x][[4]] /. r, {x, 0, 1}]



df[1, x][[1]]

 $c[i, 1] + x c[i, 2] + x^{2} c[i, 3] + x^{3} c[i, 4] + x^{4} c[i, 5] + x^{5} c[i, 6]$