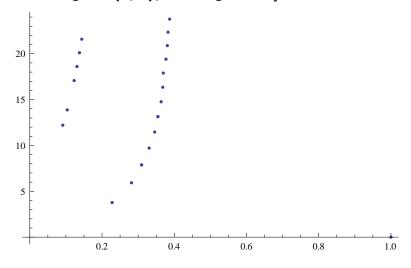
```
Exit[];
Assumptions = r > 0 \& Element[m, Integers] \& Element[m, Integers] & Element[m, Integers] 
        Element [n, Integers] && s > 0 && Element [k, Integers] && k > 0
r > 0 \&\& m \in Integers \&\& n \in Integers \&\& s > 0 \&\& k \in Integers \&\& k > 0
m = 5;
f[r_{r}, En_{r}] := \{ \{(m-1)/r, I*(En-r^p)\}, \{I*(En-r^p), -m/r\} \}
        0 * IdentityMatrix[2] * I * r ^ p; f[r, En] // MatrixForm
En = .; n = .; p = 4
fE = D[f[r, En], En]
\{\{0, i\}, \{i, 0\}\}
u = \{a[n] * x^{(2*n)}, b[n] * x^{(2*n+1)}\} * x^s
\{x^{2n+s} a[n], x^{1+2n+s} b[n]\}
r[x_] := x;
g1 = Collect[Expand[Simplify[Expand[(D[u, x] - r'[x] * f[r[x], En].u) * x ^ (-s+1)]]],
            {x ^n, a[n], b[n]}];
 g1 // MatrixForm
 s = -1 + m;
g2 = Table[Simplify[Sum[D[g1, {x, n2}] / n2!, {n, 0, 10}] /. x \rightarrow 0], {n2, 0, 10}];
g2 // MatrixForm
    0 0
     0 0
     0 0
     0 0
a[0] = 1; b[0] = i En a[0] / 2/m; a[1] = i En b[0] / 2;
b[1] = -\frac{i En^3}{4 m} / 2 / (1+m); a[2] = i En b[1] / 4;
```

```
b[n_{-}] := Simplify[(-ia[n-2] + iEna[n]) / (2(n+m))];
a[n_{-}] := Simplify[-i(b[n-3] - En b[n-1])/2/n]
b[4]
i En^4 (-22464 + En^5)
      185 794 560
Un[En_{n, m_{n}}, nN_{n, x_{n}}] := Module \{n, U\},
  U = \{1\}; \text{ AppendTo} \left[ U, -\frac{En^2}{4 \text{ m}} \right]; \text{ AppendTo} \left[ U, \frac{En \left( 4 + En^3 + 8 \text{ m} \right)}{32 \text{ m} (1 + m)} \right]; \text{ G = } \{ \text{in En } / 2 / \text{ m} \};
   For [n = 3, n < nN, n++,
    AppendTo[U,
       -((-1+m+n) U[[-2+n]] + En ((3-2m-2n) U[[-1+n]] + En (-2+m+n) U[[n]])) /
          (4 n (-2+m+n) (-1+m+n));
   ];
   ({1, i En / 2/m * x}) +
         Sum \left[ \left\{ U \left[ \left[ n+1 \right] \right] * x ^ (2*n), I * \left( En * U \left[ \left[ n+1 \right] \right] - U \left[ \left[ n \right] \right] \right) / 2 / (n+m) * x ^ (2*n+1) \right\},
          {n, 1, nN - 1}] \times x^{-1+m} // N
G = \{Re[#], Im[#]\} & [Un[3, 5, 150, x]]; Plot[G, {x, 0, 4}, PlotRange <math>\rightarrow All]
 15
 10
  5
- 5
-10
-15
U[En_, m_, g_, X_] := Module[{n = 10, U, G},
   U = Un[En, m, n, X]; G = -Un[En, m, n+1, X];
   While [Sqrt [Abs [Conjugate [U - G].(U - G)]] > g,
    n++;
    U = G; G = -Un[En, m, n+1, X];
   {Un[En, m, n, X], n}]
U[9, 5, 0.0001, 1]
\{\{-0.0126898, 0.+0.00407705 i\}, 14\}
```

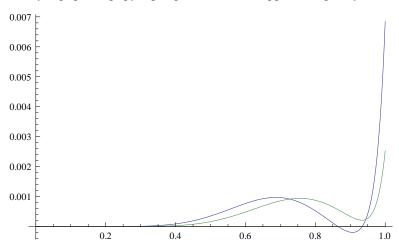
```
Ener [Ene_] :=
 Module[{U1, U2, U1S, U2S, VV = {\{0, 1\}, \{-1, 0\}\}, En, Enn, NN, Erg, kE, k, n, m, r, h\},}
  En = Ene;
  Label[begin];
  n = 5000;
  m = 5;
  r = 7.2 // N; h = -7.0 / n;
  k = \{1, -1\};
  kE = \{0, 0\};
  Do [
   k0 = h * f[r, En].k; k1 = h * f[r + h / 2, En].(k + k0 / 2);
   k2 = h * f[r + h / 2, En].(k + k1 / 2); k3 = h * f[r + h, En].(k + k2);
   k += 1/6 * (k0 + 2 * k1 + 2 * k2 + k3);
   k0 = h * (fE.k + f[r, En].kE); k1 = h * (fE.k + f[r + h / 2, En].(kE + k0 / 2));
   k2 = h * (fE.k + f[r + h / 2, En].(kE + k1 / 2)); k3 = h * (fE.k + f[r + h, En].(kE + k2));
   kE += 1 / 6 * (k0 + 2 * k1 + 2 * k2 + k3);
   r += h;
   , {n}];
  NN = U[En, m, 0.0001, r][[2]];
  {U1, U2} = Un[En, m, NN, r];
  \{U1S, U2S\} = D[Un[Enn, m, NN, r], Enn] /. Enn \rightarrow En;
  Erg = k[[1]] * U2 - U1 * k[[2]];
  If [Abs[Erg / U2 / k[[2]]] > 0.02,
   En -= Erg / (U2S k[1] - U1S k[2] + U2 kE[1] - U1 kE[2]);
   Print [{En, Erg / U2 / k[[2]]}]; Goto [begin];
   ];
  \{En, Erg/U2/k[[2]]\}
 ]
For [i = 0, i < 10, i += 0.1, Sepp = Ener [i];
 Print[{i, Sepp}]; AppendTo[Energie, {i, Sepp}];]
Ener [22]
```

```
\{21.8924+0.168499 i, -0.262337+1.54006 i\}
\{21.7276+0.288878 i, 0.0977574+1.99468 i\}
\{21.5078+0.261371 i, 1.15369+1.40345 i\}
\{21.6825+0.0732421 i, 0.410727+0.725268 i\}
\{21.6223+0.137127 i, -1.84205+0.583011 i\}
\{21.5895+0.1468 i, -0.181458-0.525624 i\}
\{21.5862+0.143899 i, 0.0316819-0.0363388 i\}
     \{21.5862+0.143899 i, 0.000384958+0.000557679 i\}
     Energie = {3.77486283903418`+0.22786873407418717` i,
       5.928479968617718`+0.2815986526347655` i,
       7.8813588488087065`+0.30953294412328675` i,
       7.881329304880588`+0.3095336916562825` i,
       9.71036454189739`+ 0.3304415424573178` i,
       11.458077781781169~+ 0.3457848857997222~ i,
       13.139764183242892~+0.3546744769440479~ i,
       13.139114444715846`+0.3548172513559829` i,
       16.34527139193304\+0.3681521067888729\in,
       17.892138695416435`+0.3696213478944415` i,
       19.40831608562361 + 0.37704222997528414 i,
       20.886015743223094 + 0.38097023642873473 i,
       22.34958939297449`+0.38276309915136164` i,
       23.777494591007947 + 0.3872991704766671 i, 12.207301904640477 + 0.09130244038237889 i,
       13.879319291317909`+0.10359131716054014` i, 17.071331521063737`+0.12274708920757649` i,
       18.607651751873114 + 0.1305970820854307 i, 20.11139546248976 + 0.1375815129955693 i,
       21.586240037178456`+0.14389862151162078` i}; Energie // MatrixForm
      3.77486+0.227869 i
      5.92848+0.281599 i
      7.88136+0.309533 i
      7.88133+0.309534 i
       9.71036+0.330442 i
      11.4581 + 0.345785 i
      13.1398+0.354674 i
      13.1391+0.354817 i
      14.7657+0.363664 i
      16.3453+0.368152 i
      17.8921+0.369621 i
      19.4083+0.377042 i
       20.886+0.38097 i
       22.3496+0.382763 i
      23.7775+0.387299 i
      12.2073+0.0913024 i
      13.8793+0.103591 i
      17.0713+0.122747 i
      18.6077+0.130597 i
       20.1114+0.137582 i
      21.5862+0.143899 i
```

AxesOrigin $\rightarrow \{0, 0\}$, PlotRange \rightarrow All]

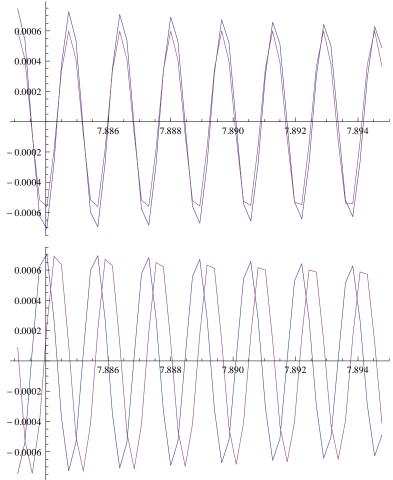


 $\texttt{G} = \{\texttt{Re}\,[\#]\,,\,\texttt{Im}\,[\#]\}\,\,\&\,[\texttt{Un}\,[16\,,\,10\,,\,15\,,\,x\,]\,]\,;\,\,\texttt{Plot}\,[\texttt{G}\,,\,\{x\,,\,0\,,\,1\}\,,\,\,\texttt{PlotRange}\,\rightarrow\,\texttt{All}\,]$



```
n = 8000; S = 1; h = 6 / n; ra = 1; En = Energie[[17]]; m = 5; r = 1;
U[En, m, 10 ^-10, r][[2]]
k = U[En, m, 10 ^-10, r][[1]];
kK = \{\{r, k\}\};
Do [
  k0 = h * f[r, En].k; k1 = h * f[r + h / 2, En].(k + k0 / 2);
  k2 = h * f[r + h / 2, En].(k + k1 / 2); k3 = h * f[r + h, En].(k + k2);
  k += 1/6 * (k0 + 2 * k1 + 2 * k2 + k3); r += h;
  AppendTo [kK, \{r, k\}], \{n\}];
ListPlot[Join[{ \#[[1]], Re[\#[[2,1]]]} & /@ kK[[S;; n]] // N},
  \{ \#[[1]], Im[\#[[2,1]]] \} \& /@ kK[[S;;n]] // N \} ], PlotRange <math>\rightarrow All, Joined \rightarrow True \}
\{ \#[[1]], Im \#[[2, 2]] \} \& /@ kK [[S ;; n]] // N \} ], PlotRange <math>\rightarrow All, Joined \rightarrow True \}
En = .;
r =.;
27
 0.002
 0.001
-0.001
-0.002
 0.002
 0.001
-0.001
-0.002
U[En, m, 10 ^-10, r][[1]]
```

```
S = 29500; n = 50; ListPlot[Join[{ {#[[1]], Re[#[[2,1]]]} & /@ kK[[S;;S+n]] // N},
   { \{\#[[1]], -0.0006 * Sin[\#[[1]] ^5 / 5 + 1 - \#[[1]] * Re[Energie[[11]]]]\} & /@
        \texttt{kK} \hspace{.1cm} \texttt{[[S ;; S+n]] // N}], \hspace{.1cm} \texttt{PlotRange} \hspace{.1cm} \rightarrow \hspace{.1cm} \texttt{All, Joined} \hspace{.1cm} \rightarrow \hspace{.1cm} \texttt{True]}
\label{eq:localization} \begin{center} \{\#[[1]], Im[\#[[2,2]]]\} \& /@ kK[[S ;; S+n]] // N\}], PlotRange $\to$ All, Joined $\to$ True] \end{center}
```



Exp[I * Im[Energie[[1]]] * x]

e^{0.278733 i x}