

```

sigma = {{0, 1}, {1, 0}}, {{0, -I}, {I, 0}}, {{1, 0}, {0, -1}}, {{1, 0}, {0, 1}}
{{0, 1}, {1, 0}}, {{0, -i}, {i, 0}}, {{1, 0}, {0, -1}}, {{1, 0}, {0, 1}}

A = Table[ArrayFlatten[Outer[Times, sigma[[4]], sigma[[i]]]], {i, 3}]
{{0, 1, 0, 0}, {1, 0, 0, 0}, {0, 0, 0, 1}, {0, 0, 1, 0}},
{{0, -i, 0, 0}, {i, 0, 0, 0}, {0, 0, 0, -i}, {0, 0, i, 0}},
{{1, 0, 0, 0}, {0, -1, 0, 0}, {0, 0, 1, 0}, {0, 0, 0, -1}}

B = Table[ArrayFlatten[Outer[Times, sigma[[i]], sigma[[4]]]], {i, 3}]
{{0, 0, 1, 0}, {0, 0, 0, 1}, {1, 0, 0, 0}, {0, 1, 0, 0}},
{{0, 0, -i, 0}, {0, 0, 0, -i}, {i, 0, 0, 0}, {0, i, 0, 0}},
{{1, 0, 0, 0}, {0, 1, 0, 0}, {0, 0, -1, 0}, {0, 0, 0, -1}}

J = {{0, 0, 0, 0}, {0, 0, 0, 0}, {0, 0, 0, -i}, {0, 0, i, 0}},
{{0, 0, 0, 0}, {0, 0, 0, i}, {0, 0, 0, 0}, {0, -i, 0, 0}},
{{0, 0, 0, 0}, {0, 0, -i, 0}, {0, i, 0, 0}, {0, 0, 0, 0}};

K = I * {{0, 1, 0, 0}, {1, 0, 0, 0}, {0, 0, 0, 0}, {0, 0, 0, 0}}, {{0, 0, 1, 0}, {0, 0, 0, 0},
{1, 0, 0, 0}, {0, 0, 0, 0}}, {{0, 0, 0, 1}, {0, 0, 0, 0}, {0, 0, 0, 0}, {1, 0, 0, 0}};

a = J + I * K; b = J - I * K;

S = Eigenvectors[a[[3]]]
{{1, 0, 0, 1}, {0, i, 1, 0}, {-1, 0, 0, 1}, {0, -i, 1, 0}}

S.a[[1]].Inverse[S] // MatrixForm
S.a[[2]].Inverse[S] // MatrixForm
S.a[[3]].Inverse[S] // MatrixForm

$$\begin{pmatrix} 0 & i & 0 & 0 \\ -i & 0 & 0 & 0 \\ 0 & 0 & 0 & i \\ 0 & 0 & -i & 0 \end{pmatrix}$$


$$\begin{pmatrix} 0 & -1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{pmatrix}$$


$$\begin{pmatrix} -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}$$


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```
S.b[[1]].Inverse[S] // MatrixForm
S.b[[2]].Inverse[S] // MatrixForm
S.b[[3]].Inverse[S] // MatrixForm
```

$$\begin{pmatrix} 0 & 0 & 0 & i \\ 0 & 0 & -i & 0 \\ 0 & i & 0 & 0 \\ -i & 0 & 0 & 0 \end{pmatrix}$$

$$\begin{pmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & -1 & 0 \\ 0 & -1 & 0 & 0 \\ 1 & 0 & 0 & 0 \end{pmatrix}$$

$$\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}$$

```
A[[1]] // MatrixForm
A[[2]] // MatrixForm
A[[3]] // MatrixForm
```

$$\begin{pmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & -1 \\ 0 & 0 & -1 & 0 \end{pmatrix}$$

$$\begin{pmatrix} 0 & -i & 0 & 0 \\ i & 0 & 0 & 0 \\ 0 & 0 & 0 & i \\ 0 & 0 & -i & 0 \end{pmatrix}$$

$$\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

```
A[[1]].A[[2]] - A[[2]].A[[1]] - 2*I*A[[3]]
```

```
{0, 0, 0, 0}, {0, 0, 0, 0}, {0, 0, 0, 0}, {0, 0, 0, 0}
```