## Exit[];

PrependTo [\$Path, "D:\\Users\\Johannes\\Promotion\\Mathematica\\Packages"]; << JoFin`

a = .

$$\frac{1}{2} \left( s^2 S^2 V^{(0,0,2)}[t,P,S] + 2 P q s^2 S V^{(0,1,1)}[t,P,S] + P^2 q^2 s^2 V^{(0,2,0)}[t,P,S] \right) + V^{(1,0,0)}[t,P,S]$$

r 
$$(-q+x)$$
  $V^{(0,1)}[t,x[1]] + \frac{1}{2} s^2 (q-x)^2 V^{(0,2)}[t,x[1]] /.q \rightarrow 1$ 

Simplify 
$$\left[ r \left( -1 + x \right) V^{\left( 0,1 \right)} \left[ t, x \left[ 1 \right] \right] + \frac{1}{2} s^{2} \left( 1 - x \right)^{2} V^{\left( 0,2 \right)} \left[ t, x \left[ 1 \right] \right] - \frac{1}{2} s^{2} \left( 1 - x \right)^{2} \left[ t, x \left[ 1 \right] \right] \right] - \frac{1}{2} s^{2} \left[ t, x \left[ 1 \right] \right] + \frac{1}{2}$$

$$\left( r (1+x) V^{(0,1)} [t, x[1]] + \frac{1}{2} s^{2} (-1-x)^{2} V^{(0,2)} [t, x[1]] \right) \right]$$

$$-2 (r V^{(0,1)}[t, x[1]] + s^2 x V^{(0,2)}[t, x[1]])$$

$$P[1] = S; kt[1] = r S; kX[1, 1] = \sigma S;$$

$$P[2] = a; kt[2] = r a; kX[2,1] = q S \sigma;$$

Expand [DFK [V, P, kt, kX, 2, r]]

$$-\text{r V}[\text{t,S,a}] + \text{a r V}^{\left(0,0,1\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \text{r S V}^{\left(0,1,0\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2 \, S^2 \, \sigma^2 \, V^{\left(0,0,2\right)}[\text{t,S,a}] + \frac{1}{2} \, q^2$$

$$q \, S^2 \, \sigma^2 \, V^{\left(0,1,1\right)}\left[\text{t,S,a}\right] + \frac{1}{2} \, S^2 \, \sigma^2 \, V^{\left(0,2,0\right)}\left[\text{t,S,a}\right] + V^{\left(1,0,0\right)}\left[\text{t,S,a}\right] \\$$