

Exit[]

```
In[363]:= s = 0.2; L = 0.1; xq = 10; r = 0.03; k = 0.4; t = 0.5; xMin = 5; xMax = 15;
Nx = 1000; dx = (xMax - xMin) / Nx; Nt = 400; dt = t / Nt;
```

```
xs = N[Range[xMin, xMax, dx]];
```

```
(*Analytic solution*)
```

```
m[x_, t_] := Exp[-L t] x + (1 - Exp[-L t]) xq
```

```
v[t_] :=  $\frac{s^2}{2 L} (1 - \text{Exp}[-2 L t])$ 
```

```
analytic[x_] := Exp[-r t - k m[x, t] +  $\frac{1}{2} v[t] k^2$ ]
```

```
(*numerical solution*)
```

```
h[x_] := Exp[-k x]
```

```
step[i_, a_] := If[a (xs[[i]] - xq) < 0, a, 0]  $\frac{L}{dx} (xq - xs[[i]])$ 
```

```
G = SparseArray[{ {i_, i_} => 1 + dt  $\left( r + \frac{s^2}{dx^2} + \text{step}[i, 1] + \text{step}[i, -1] \right)$ ,
  {i_, j_} /; Abs[i - j] == 1 => - dt  $\left( \frac{s^2}{2 dx^2} + \text{step}[i, \text{If}[j == i + 1, 1, -1]] \right)$  },
  {Nx + 1, Nx + 1}];
```

```
ListLinePlot[Transpose[{xs, MatrixPower[G, -Nt].(N[h/@xs]) / (analytic/@xs) - 1}]]
```

