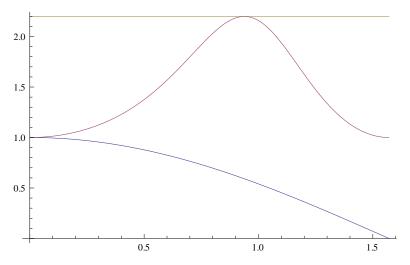
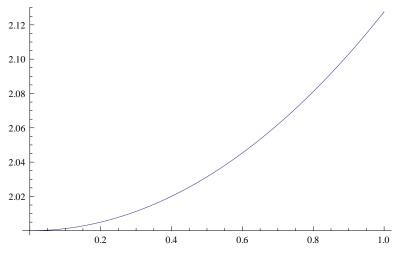
$$\begin{split} &f[a_, E_] := (\cos[a] ^ 2 + \text{Exp}[-E] * \sin[a] ^ 2) / (\cos[a] ^ 4 + \text{Exp}[-E] * \sin[a] ^ 4) \\ &e = .138 * 9; &\cos[ArcTan[Exp[e / 4]]] \\ &\text{Plot}\left[\left\{\cos[a], f[a, e], 1 + \cosh\left[\frac{e}{2}\right]\right\}, \left\{a, 0, Pi / 2\right\}\right] \end{aligned}$$

0.591231



Plot
$$\left[\frac{1}{2} e^{-tE/2} (1 + e^{tE/2})^2, \{tE, 0, 1\}\right]$$



 ${\tt Simplify} \, [\, {\tt f} \, [\, {\tt ArcTan} \, [\, {\tt Exp} \, [\, {\tt tE} \, / \, 4\,]\,] \, , \, \, {\tt tE} \,] \,]$

$$\frac{1}{2} e^{-tE/2} \left(1 + e^{tE/2}\right)^2$$

Expand
$$\begin{bmatrix} \frac{1}{2} & e^{-tE/2} & (1 + e^{tE/2})^2 \end{bmatrix}$$

$$1 + \frac{e^{-tE/2}}{2} + \frac{e^{tE/2}}{2}$$

$$1 + Cosh[-tE/2]$$

$$1 + Cosh\left[\frac{tE}{2}\right]$$

Simplify
$$\left[D[f[a, e], a] * \left(Cos[a]^4 + e Sin[a]^4\right) ^ 2\right]$$

$$\left(\left(\cos\left[a\right]^{4}+1.242\,\sin\left[a\right]^{4}\right)^{2}\,\left(2.57761\,\cos\left[a\right]^{5}\,\sin\left[a\right]-0.74443\,\cos\left[a\right]\,\sin\left[a\right]^{5}\right)\right)\bigg/\\ \left(\cos\left[a\right]^{4}+0.288806\,\sin\left[a\right]^{4}\right)^{2}$$

Solve
$$\left[\cos\left[a\right]^4 - e\sin\left[a\right]^4 = 0, a\right]$$

Solve::ifun:

Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. \gg

$$\begin{split} &\left\{\left\{a \rightarrow -\text{ArcCos}\left[-\sqrt{-\frac{\sqrt{e}}{-1+e}} + \frac{e}{-1+e}\right]\right\}, \, \left\{a \rightarrow \text{ArcCos}\left[-\sqrt{-\frac{\sqrt{e}}{-1+e}} + \frac{e}{-1+e}\right]\right\}, \\ &\left\{a \rightarrow -\text{ArcCos}\left[\sqrt{-\frac{\sqrt{e}}{-1+e}} + \frac{e}{-1+e}\right]\right\}, \, \left\{a \rightarrow \text{ArcCos}\left[\sqrt{-\frac{\sqrt{e}}{-1+e}} + \frac{e}{-1+e}\right]\right\}, \\ &\left\{a \rightarrow -\text{ArcCos}\left[-\sqrt{\frac{\sqrt{e}}{-1+e}} + \frac{e}{-1+e}\right]\right\}, \, \left\{a \rightarrow \text{ArcCos}\left[-\sqrt{\frac{\sqrt{e}}{-1+e}} + \frac{e}{-1+e}\right]\right\}, \\ &\left\{a \rightarrow -\text{ArcCos}\left[\sqrt{\frac{\sqrt{e}}{-1+e}} + \frac{e}{-1+e}\right]\right\}, \, \left\{a \rightarrow \text{ArcCos}\left[\sqrt{\frac{\sqrt{e}}{-1+e}} + \frac{e}{-1+e}\right]\right\}\right\}. \end{split}$$