## Lab3

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#### Task 1

a) 
$$\{C\} \rightarrow \{B\}$$

We use decomposition on  $\{C\} \rightarrow \{A,D\}$ , which entails that if  $\{C\} \rightarrow \{A,D\}$  then  $\{C\} \rightarrow \{A\}$  and  $\{C\} \rightarrow \{D\}$ .

We use decomposition again on  $\{A\} \rightarrow \{B,C\}$  which gives  $\{A\} \rightarrow \{B\}$  and  $\{A\} \rightarrow \{C\}$ . Finally transitivity is used on  $\{C\} \rightarrow \{A\}$  and  $\{A\} \rightarrow \{B\}$  which results in  $\{C\} \rightarrow \{B\}$ .

b) 
$$\{A,E\} \rightarrow \{F\}$$

We use decomposition on  $\{C\} \rightarrow \{A,D\}$ , which entails that if  $\{C\} \rightarrow \{A,D\}$  then  $\{C\} \rightarrow \{A\}$  and  $\{C\} \rightarrow \{D\}$ .

We use decomposition again on  $\{A\} \to \{B,C\}$  which gives  $\{A\} \to \{B\}$  and  $\{A\} \to \{C\}$ . Since  $\{A\} \to \{C\}$  and  $\{C\} \to \{D\}$  then decomposition gives  $\{A\} \to \{D\}$ .

Now we use pseudo-transitivity:

If 
$$\{A\} \rightarrow \{D\}$$
 and  $\{D,E\} \rightarrow F$  then  $\{A,E\} \rightarrow \{F\}$ .

#### Task 2

a)

 $X+ = \{A\} = \{A, B, C, D\}$  because A points to B and C and C points to A and D which gives us X+ without E and F.

#### Task 3

#### a) Determine the candidate key(s) for R.

We want to find the attributes which are not present on the right hand side of the FDs. In our case only A is not present on the right hand side, meaning that it can not be determined by other attributes. Therefore A will definitely be part of the candidate keys. A+ is also equal to only A (since we do not have B), therefore we can not determine further candidate keys, meaning that there must be more. If we then choose A and B, and find the closure of (A,B)+, we can see that it is one candidate key because it gives all the attributes from the given relation R. The same result comes from finding the closure of (A,D)+, since it returns all of the attributes from R. No further minimum candidate keys can be found.

b) Note that R is not in BCNF. Which FD(s) violate the BCNF condition? FD2 and FD3 violate the BCNF condition.

Input relation is not in BCNF: it is not in 3NF and not all functional dependencies satisfy at least one of the following conditions: (1) The right-hand side is a subset of the left hand side,

or (2) the left-hand side is a superkey (or minimum key) of the relation. The functional dependencies that failed are:  $D \rightarrow B$ ;  $E \rightarrow F$ .

# c) Decompose R into a set of BCNF relations, and describe the process step by step (don't forget to determine the FDs and the candidate key(s) for all of the relation schemas along the way).

The candidate key (A,B) is a superkey for R and therefore doesn't violate BCNF. FD2 violates BCNF since E is not a key. FD3 also violates BCNF, since D is not a key. Choosing to start with FD2 and therefore we decompose the original attributes into two relations - R1(EF) and R2(ABCDE), R2 we get by subtracting the right handside of the violating FD from the original attributes.

- For R1(EF) the candidate key is E and the only FD that applies to this is FD2
  E → F. Therefore it's in the BCNF.
- For R2(ABCDE) candidate keys are (A,B) and (A,D). Now we check if it is in BCNF. The third FD's LHS is not a superkey and the relation R2 is decomposed into R3(DB) and R4(ACDE).
- For R3(DB) the candidate key is D, the only FD applicable here is FD3 so it is in the BCNF.
- For R4(ACDE) we check if it is in the BCNF and can tell that the candidate key is (A,D) the functional dependency applicable here will be AD → EC.

The relations we get are therefore: AD  $\rightarrow$  EC, E  $\rightarrow$  F and D  $\rightarrow$  B.

#### Task 4

### a) Show that R is not in BCNF.

We want to find the attributes which are not present on the right hand side of the FDs. In our case B and C is not present on the right hand side, meaning that it can not be determined by other attributes. If we have B and C, and find the closure of (B,C)+, we can see that it is the only candidate key because it gives all the attributes from the given relation R.

# b) Decompose R into a set of BCNF relations (describe the process step by step).

We start by finding the minimal cover of our FDs. Step 1 is to rewrite the FDs so that the right hand side only contains one attribute. FD3 will remain as is  $(C \to D)$ . FD2 will be decomposed into BCD  $\to$  A and BCD  $\to$  E. FD1 will be decomposed into ABC  $\to$  D and ABC  $\to$  E. Due to FD3 we can now rewrite the left hand side of some FDs, which will give us:  $C \to D$ , BC  $\to$  E and BC  $\to$  A. This gives us our minimal cover: FDX  $C \to D$  & FDY BC  $\to$  AE.

Now we want to determine if FDs are in BCNF. FDX is not in BCNF since C is not a superkey and therefore we decompose into two relations: R1(CD) and R2(ABCE).

For R1(CD) the candidate key is C and the only FD that applies to this is FDX
 C → D. Therefore it's in the BCNF.

For R2(ABCE) candidate keys are (B,C). Now we check if it's in the BCNF.
 Since FDY BC->AE is applicable here, this means that it's already in the BCNF.

The relations we get are therefore  $C \rightarrow D$  and  $BC \rightarrow AE$ .