CUNY MSDS Capstone Project

COMMERCIAL BUILDING ENERGY CONSUMPTION

ANALYSIS AND PREDICTION

March 10, 2019

John Grando john.grando@spsmail.cuny.edu

Contents

| Research 2 Related Work 2 Literature Review 2 Theory and Hypothesis 2 Data and Methods 3 General Process 3 Data Pre-Processing 4 Electricity 4 General 4 Response Analysis 4 Variable Selection - PCA 5 Variable Selection - PLS 5 Variable Selection - Random Forest 5 Variable Selection - Lasso 5 Variable Selection - Forward Selection 5 Variable Selection - Simple Neural Network 5 Variable Selection - Recursive Feature Elimination 6 Variable Selection - Selected Variable Analysis 6 Natural Gas 6 General 6 District Heat 6 General 6 Fuel Oil 6 General 6 | Abstract | 1 |
|---|--|---|
| Related Work 2 Literature Review 2 Theory and Hypothesis 2 Data and Methods 3 General Process 3 Data Pre-Processing 4 Electricity 4 General 4 Response Analysis 4 Variable Selection - PCA 5 Variable Selection - PLS 5 Variable Selection - Random Forest 5 Variable Selection - Lasso 5 Variable Selection - Forward Selection 5 Variable Selection - Forward Selection 5 Variable Selection - Forward Selection Elimination 6 Variable Selection - Recursive Feature Elimination 6 Variable Selection - Selected Variable Analysis 6 Natural Gas 6 General 6 Fuel Oil 6 General 6 Fuel Cil 6 General 6 Fuel Oil 6 General 6 Fuel Oil 6 General 6 Fuel Oil | Introduction | 1 |
| Literature Review 2 Theory and Hypothesis 2 Data and Methods 3 General Process 3 Data Pre-Processing 4 Electricity 4 General 4 Response Analysis 4 Variable Selection - PCA 5 Variable Selection - PLS 5 Variable Selection - Random Forest 5 Variable Selection - Lasso 5 Variable Selection - Forward Selection 5 Variable Selection - Simple Neural Network 5 Variable Selection - Recursive Feature Elimination 6 Variable Selection - Selected Variable Analysis 6 Natural Gas 6 General 6 District Heat 6 General 6 Neural Network Models 6 General 6 N | Research | |
| Data and Methods 3 General Processing 4 Electricity 4 General 4 Response Analysis 4 Variable Selection - PCA 5 Variable Selection - PLS 5 Variable Selection - Random Forest 5 Variable Selection - Lasso 5 Variable Selection - Forward Selection 5 Variable Selection - Forward Selection 5 Variable Selection - Simple Neural Network 5 Variable Selection - Recursive Feature Elimination 6 Variable Selection - Selected Variable Analysis 6 Natural Gas 6 General 6 District Heat 6 General 6 District Heat 6 General 6 Neural Network Models 6 General 6 Electricity 7 Summary 7 Performance 7 Natural Gas 7 | | |
| General Process 3 Data Pre-Processing 4 Electricity 4 General 4 Response Analysis 4 Variable Selection - PCA 5 Variable Selection - PLS 5 Variable Selection - Random Forest 5 Variable Selection - Lasso 5 Variable Selection - Forward Selection 5 Variable Selection - Simple Neural Network 5 Variable Selection - Recursive Feature Elimination 6 Variable Selection - Selected Variable Analysis 6 Natural Gas 6 General 6 District Heat 6 General 6 Fuel Oil 6 General 6 Neural Network Models 6 General 6 Electricity 7 Summary 7 Performance 7 Natural Gas 7 | Theory and Hypothesis | 2 |
| Data Pre-Processing 4 Electricity 4 General 4 Response Analysis 4 Variable Selection - PCA 5 Variable Selection - PLS 5 Variable Selection - Random Forest 5 Variable Selection - Lasso 5 Variable Selection - Forward Selection 5 Variable Selection - Simple Neural Network 5 Variable Selection - Recursive Feature Elimination 6 Variable Selection - Selected Variable Analysis 6 Natural Gas 6 General 6 District Heat 6 General 6 Fuel Oil 6 General 6 Neural Network Models 6 General 6 Electricity 6 Summary 7 Performance 7 Natural Gas 7 | Data and Methods | 3 |
| Data Pre-Processing 4 Electricity 4 General 4 Response Analysis 4 Variable Selection - PCA 5 Variable Selection - PLS 5 Variable Selection - Random Forest 5 Variable Selection - Lasso 5 Variable Selection - Forward Selection 5 Variable Selection - Simple Neural Network 5 Variable Selection - Recursive Feature Elimination 6 Variable Selection - Selected Variable Analysis 6 Natural Gas 6 General 6 District Heat 6 General 6 Fuel Oil 6 General 6 Neural Network Models 6 General 6 Electricity 6 Summary 7 Performance 7 Natural Gas 7 | General Process | 3 |
| General 4 Response Analysis 4 Variable Selection - PCA 5 Variable Selection - PLS 5 Variable Selection - Random Forest 5 Variable Selection - Lasso 5 Variable Selection - Forward Selection 5 Variable Selection - Simple Neural Network 5 Variable Selection - Recursive Feature Elimination 6 Variable Selection - Selected Variable Analysis 6 Natural Gas 6 General 6 District Heat 6 General 6 Fuel Oil 6 General 6 Neural Network Models 6 General 6 Electricity 7 Summary 7 Performance 7 Natural Gas 7 | | 4 |
| Response Analysis 4 Variable Selection - PCA 5 Variable Selection - PLS 5 Variable Selection - Random Forest 5 Variable Selection - Lasso 5 Variable Selection - Forward Selection 5 Variable Selection - Simple Neural Network 5 Variable Selection - Recursive Feature Elimination 6 Variable Selection - Selected Variable Analysis 6 Natural Gas 6 General 6 District Heat 6 General 6 Fuel Oil 6 General 6 Neural Network Models 6 General 6 Electricity 7 Summary 7 Performance 7 Natural Gas 7 | Electricity | 4 |
| Variable Selection - PCA 5 Variable Selection - PLS 5 Variable Selection - Random Forest 5 Variable Selection - Lasso 5 Variable Selection - Forward Selection 5 Variable Selection - Simple Neural Network 5 Variable Selection - Recursive Feature Elimination 6 Variable Selection - Selected Variable Analysis 6 Natural Gas 6 General 6 District Heat 6 General 6 Fuel Oil 6 General 6 Neural Network Models 6 General 6 Electricity 7 Summary 7 Performance 7 Natural Gas 7 | General | 4 |
| Variable Selection - PLS 5 Variable Selection - Random Forest 5 Variable Selection - Lasso 5 Variable Selection - Forward Selection 5 Variable Selection - Simple Neural Network 5 Variable Selection - Recursive Feature Elimination 6 Variable Selection - Selected Variable Analysis 6 Natural Gas 6 General 6 District Heat 6 General 6 Fuel Oil 6 General 6 Neural Network Models 6 General 6 Electricity 7 Summary 7 Performance 7 Natural Gas 7 | Response Analysis | 4 |
| Variable Selection - Random Forest 5 Variable Selection - Lasso 5 Variable Selection - Forward Selection 5 Variable Selection - Simple Neural Network 5 Variable Selection - Recursive Feature Elimination 6 Variable Selection - Selected Variable Analysis 6 Natural Gas 6 General 6 District Heat 6 General 6 Fuel Oil 6 General 6 Neural Network Models 6 General 6 Electricity 7 Summary 7 Performance 7 Natural Gas 7 | Variable Selection - PCA | 5 |
| Variable Selection - Lasso 5 Variable Selection - Forward Selection 5 Variable Selection - Simple Neural Network 5 Variable Selection - Recursive Feature Elimination 6 Variable Selection - Selected Variable Analysis 6 Natural Gas 6 General 6 District Heat 6 General 6 Fuel Oil 6 General 6 Neural Network Models 6 General 6 Electricity 7 Summary 7 Performance 7 Natural Gas 7 | Variable Selection - PLS | 5 |
| Variable Selection - Forward Selection 5 Variable Selection - Simple Neural Network 5 Variable Selection - Recursive Feature Elimination 6 Variable Selection - Selected Variable Analysis 6 Natural Gas 6 General 6 District Heat 6 General 6 Fuel Oil 6 General 6 Neural Network Models 6 General 6 Electricity 7 Summary 7 Performance 7 Natural Gas 7 | Variable Selection - Random Forest | 5 |
| Variable Selection - Simple Neural Network 5 Variable Selection - Recursive Feature Elimination 6 Variable Selection - Selected Variable Analysis 6 Natural Gas 6 General 6 District Heat 6 General 6 Fuel Oil 6 General 6 Neural Network Models 6 General 6 Electricity 7 Summary 7 Performance 7 Natural Gas 7 | Variable Selection - Lasso | 5 |
| Variable Selection - Recursive Feature Elimination 6 Variable Selection - Selected Variable Analysis 6 Natural Gas 6 General 6 District Heat 6 General 6 Fuel Oil 6 General 6 Neural Network Models 6 General 6 Electricity 7 Summary 7 Performance 7 Natural Gas 7 | Variable Selection - Forward Selection | 5 |
| Variable Selection - Selected Variable Analysis 6 Natural Gas 6 General 6 District Heat 6 General 6 Fuel Oil 6 General 6 Neural Network Models 6 General 6 Electricity 7 Summary 7 Performance 7 Natural Gas 7 | Variable Selection - Simple Neural Network | 5 |
| Natural Gas 6 General 6 District Heat 6 General 6 Fuel Oil 6 General 6 Neural Network Models 6 General 6 Electricity 7 Summary 7 Performance 7 Natural Gas 7 | Variable Selection - Recursive Feature Elimination | 6 |
| General 6 District Heat 6 General 6 Fuel Oil 6 General 6 Neural Network Models 6 General 6 Electricity 7 Summary 7 Performance 7 Natural Gas 7 | Variable Selection - Selected Variable Analysis | 6 |
| District Heat 6 General 6 Fuel Oil 6 General 6 Neural Network Models 6 General 6 Electricity 7 Summary 7 Performance 7 Natural Gas 7 | Natural Gas | 6 |
| General 6 Fuel Oil 6 General 6 Neural Network Models 6 General 6 Electricity 7 Summary 7 Performance 7 Natural Gas 7 | General | 6 |
| Fuel Oil 6 General 6 Neural Network Models 6 General 6 Electricity 7 Summary 7 Performance 7 Natural Gas 7 | District Heat | 6 |
| General 6 Neural Network Models 6 General 6 Electricity 7 Summary 7 Performance 7 Natural Gas 7 | General | 6 |
| Neural Network Models 6 General 6 Electricity 7 Summary 7 Performance 7 Natural Gas 7 | Fuel Oil | 6 |
| General 6 Electricity 7 Summary 7 Performance 7 Natural Gas 7 | General | 6 |
| Electricity 7 Summary 7 Performance 7 Natural Gas 7 | Neural Network Models | 6 |
| Summary 7 Performance 7 Natural Gas 7 | General | 6 |
| Performance | Electricity | 7 |
| Natural Gas | · | 7 |
| | Performance | 7 |
| | | 7 |
| • | | 7 |
| Performance | · | |
| District Heat | | 7 |

| Summary | | | | | | | | | | | | | | . 7 |
|--------------|-------------|--------|----|------|------|------|-------|--|--|--|---|---|---|----------|
| Performanc | е | | | | | | | | | | | | | . 7 |
| Fuel Oil | | | | | | | | | | | | | | . 7 |
| Summary | | | | | | | | | | | | | | . 7 |
| Performanc | e | | | | | | | | | | • | • | | . 7 |
| Appendix | | | | | | | | | | | | | | 8 |
| Electricity | | | | | | | | | | | | | | . 8 |
| Response | | | | | | | | | | | | | | . 8 |
| PCA | | | | | | | | | | | | | | . 8 |
| PLS | | | | | | | | | | | | | | 9 |
| Random Fo | prest | | | | | | | | | | | | | . 11 |
| Lasso | | | | | | | | | | | | | | . 13 |
| Forward Se | election | | | | | | | | | | | | | . 15 |
| Recursive F | eature Ext | ractio | n. | | | | | | | | | | | . 17 |
| Simple Neu | ıral Networ | k | | | | | | | | | | | | . 19 |
| Select Varia | able Analys | sis . | | | | | _ | | | | _ | | _ | 21 |

Abstract

Commercial Building Energy Consumption accounts for approximately 25%¹ of the United States energy production profile. Many economical and sociological factors are pushing owners of these buildings to reduce energy consumption and optimize performance. However, it is difficult to say whether a building is operating efficiently or not. Using publicly available data, models can be constructed to predict major fuel consumption. Keywords: building energy consumption, predicted energy consumption, baseline energy model.

Introduction

Building owners, local governments, and utility providers are all looking for ways to reduce energy consumption. Reasons for doing so can vary all the way from social responsibility to economic gain. Some people want to show off an efficient building, others want to identify properties that are in need of improvement. However, this concept of evaluating building performance typically requires two things; measuring the property in question's consumption, and comparing it to a standard practice equivalent. Additionally, in order for the final product to be useful, it is important that the final set of predictors be parsimonious and be realistically available to users.

Comparing summary statistics between buildings, such as energy use per square foot, is not as simple as it seems because there are a multitude of factors that affect a building's energy consumption profile. The building use type can cause energy use to vary by a large amount; such as office buildings and refrigerated warehouses. Also, some factors may have critical importance for some buildings and not others, which can lead to significant differences in consumption. This complexity of making similar comparisons creates a situation where it is difficult to determine whether a building is performing consistent with, or better than, other standard practice buildings.

Commercially, using the most popular example, ENERGY STAR 2 has implemented a benchmarking algorithm that scores buildings on a scale from 1-100 using market-available data. The output of this benchmarking algorithm is a unit-less score, as well as a reference 'baseline' building. However, the methodology is not released and it is unclear what factors are important to influence the energy consumption of the building. These barriers make it difficult to provide custom comparisons and nearly impossible to make batch predictions from a set of buildings, or variations of buildings.

Every few years, the U.S. Energy Information Administration (EIA) conducts a survey attempting to record pertinent features of these buildings, known officially as the Commercial Buildings Energy Consumption Survey (CBECS)³. While the survey is expansive (i.e. more than 600 tracked features), it is essential to create a model that is usable and only requires predictors that can easily be attained by building operators. Therefore, in this study a series of models will be evaluated in order to determine the most important predictors which will then be used to train a final, more complex, model. After completion of the model, the predictors will be evaluated on how easy they are to attain, and will possibly be exchanged with simpler variables that are highly correlated.

¹EIA - https://www.eia.gov/energyexplained/index.php?page=us_energy_commercial

²ENERGY STAR - https://www.energystar.gov/

³EIA Microdata

Research

Related Work

The idea of determing building energy efficiency is not a novel concept in itself. As previously mentioned, ENERGY STAR has a building benchmarking tool⁴. Additionally, the United States Green Building Council has created the Arc Platform⁵ which provides benchmarking and active monitoring features. While these platforms provide building comparisons in the form of an overall score, it is difficult to explore the space around the building attribute inputs themselves as well as compare consumption of a specific building to its equivalent standard practice building. With this functionality, a more direct comparison can be made and relative environmental impact can be measured.

Literature Review

There are a variety of texts that are dedicated to the analysis of building energy consumption, and determining operating efficiency, such as ASHRAE Guildine 14. Also, there are guidelines that must be followed for buildings undergoing new construction or major renovation, which have energy compliance sections (ASHRAE Guideline 90.1, 189.1, and International Energy Conservation Code). Particularly, there is a well thought out process for auditing commercial buildings, known as ASHRAE Audits, which start at the lowest level (I) and progress to the highest level (III) as the opportunity for energy and cost savings becomes more apparent ⁶.

Theory and Hypothesis

Commercial buildings are complex and encompass a wide variety of purposes. However, they all must be powered, and require a considerable amount of energy to operate properly. The most direct example of this complex issue is the ASHRAE energy audit process. As part of the initial audit process, an assessment of the building's overall operational efficiency is gauged. Typically, an auditor will walk through the building, analyze utility bills, and make the closest energy consumption comparisons they can. This takes years of experience and sometimes requires highly tuned spreadsheets that have been developed over a long period of time. It can take a surprising amount of effort just to determine if a building is operating efficiently or not.

The CBECS data set provide some insight as to what building attributes most greatly affect building energy consumption. Over 400 survey questions are recorded and coupled with major fuel consumption. These fuel sources are Electricity, Natural Gas, District Heat, and Fuel Oil. However, it would not be useful to construct a model with a large number of predictors, as it would require a large amount of time and effort to compile the necessary information in order to provide a prediction. Therefore, one of the main focuses for this study will be to extract the fewest amount of predictors necessary in order to make accurate predictions.

 $^{^4 \}verb|https://www.energystar.gov/buildings/about-us/how-can-we-help-you/benchmark-energy-use/benchmarking$

⁵https://arcskoru.com/

⁶http://aea.us.org/3143-2.html

Given the complex nature, it is unlikely a linear regression will provide the best prediction accuracy. This point is especially highlighted by the fact the the goal of this study is produce a parsimonious set of predictors, which means a small subset must be selected. Therefore, an investigation into more complex, nonlinear, algorithms will be performed in order to keep the number of necessary predictors as low as possible while still capturing complex interactions.

Data and Methods

General Process

Due to the large number of features in the survey responses, it is not possible to analyze each one individually. Therefore, the first steps in the process will be centered around selecting a smaller subset. A few algorithms will be used in order to try and reduce bias. First, a principle component analysis will be performed. Second, a partial least squares model will be fit to the response. Third, a random forest regression will be used in order to try and extract any nonlinear relationships. Fourth, an attempt to construct a lasso regression model will be made. Fifth, a forward selection linear model will also be fit in order to see if an automated approach can be taken. Finally, a simple neural network model will be trained to gauge the possible effectiveness of using this model type. The magnitude and contribution percentage of each variable will be considered in selecting features from this model. Also, the various error rates from each preliminary model will be used as a benchmark for the final model performance.

After the prelminary set of models have been run and summarized, the extracted variables will be analyzed in order to verify their importance, gauge their potential predictive power, and to check whether they are easily attainable for a building operator/owner. This step is very important because it is essential worthwhile variables are used to predict the outcome. Selecting a variable that, for one reason or another, is erroneous may lead to reduced predictive power in the final model. If a variable did pass our initial analysis but doesn't actually have much predictive power (i.e. it only changes values by a slight amount) then it may not be worthwhile to select it at all. All selected variables increase the complexity of the model; therefore, we wish to only select those that will matter. Finally, the predictor must be usable, and 'knowable'. Ultimately, this tool will not be usable if a very difficult and hard to understand, and/or attain, variable value is used. These three concepts will be used in the analyzation of the candidate variables from the the preliminary analysis.

Finally, a neural network model will be built to take the verified subset of features and make predictions for the selected major fuel use. A variety of hyperparameters will be tested, using cross-validation, and compared on a common error metric. This step will reveal the optimal hyperparameter combination to use for the model. The prospective model will then be retrained on the entired entire training and validation data. This model's selected error metrics will then be compared to the preliminary models, which should be considered a floor for performance. Once this is done, the model can then be re-assessed for feature selection as well as analyzed for the value/tradeoff of adding/removing certain features.

Data Pre-Processing

The raw data set consists of 6,720 samples and 1,119 features. However, multiple steps of preprocessing were required in order to prepare the data. Note, there are many columns which are being used as imputation flags and statistical weights which, when removed, reduced the number of features down to more than 400. While these columns are useful to indicate where values have been imputed into the dataset by the source's own methodologies, rather than try to change back the data to the original records it has been determined that the imputed values were sufficiently applied and the dataset will not be blindly imputed any further.

After evaluating the reduced data set, some feature engineering efforts were taken. First, very specific cases which resulted in many null responses to follow-up survey questions (e.g. buildings less than 1,000 gross square feet), buildings open for less than a year, and features with a large amount of nulls were removed. Second, some null entries were converted to zero when logically appropriate. For example, if a building was indicated to not be cooled, then a follow up question asking what percentage of the building is cooled was not asked, resulting in an null. In this instance, the null value was replaced with a zero. Third, some values were removed as they simply did not apply to the study (e.g. expenditure for energy sources in USD). Fourth, nominal categorical values that had null responses were encoded to a special value. The thinking for this approach is that if, in fact, an null value for a feature ends up being a significant predictor, then it can be analzyed what factors make this situation occur. Fifth, the categorical features were then one-hot encoded to separate columns. The preprocessed data set was transformed to 6661 rows and 456 features (before one-hot encoding).

Electricity

General

The preprocessed data was passed to the following process in order to determine the best possible set of candidate predictors with one additional filter. Only buildings that indicated electricity being used ELUSED were included in the samples for this major fuel use. Then, one of each pair of predictors with correlations above 0.75 were removed, to avoid model selection issues. Additionally, the other major fuel consumption values were removed from the set of possible predictors since separate models will be made to predict these values as well. Also, the numeric predictors were transformed via BoxCox methodology as well as centered and scaled due to the varying scales and skewness.

Response Analysis

The response data appear to be unimodal and have a heavy right skew. After filtering for this model's end-use, there are 6498 samples in the data set. The energy use was convert to units mmBTU (1e6 BTU) and the log was taken in an attempt to maintain homoscadicity as the variance of the energy used also scales with the magnitude.

Variable Selection - PCA

RMSE: 0.0, Rsquared: NA, Top 5: RFG

The principle component analysis indicates that only 4.6% of the variance in the data can be explained in the first principle component, which then drops to 1.7% for the second principle component. These results reveal that there does not appear to be clear axes that can explain the variance of the data very well, which indicates there may be some very complex interactions taking place in the predictors.

Variable Selection - PLS

RMSE: 0.0, Rsquared: NA, Top 5: RFG

This model returned a promising result with an Rsquared value of 0.868; however, it must be noted that all predictors were used in this process. Looking at the result, it is obvious that the use of refrigeration equipment is dominating the variable importance plot (RFG prefix) as well as some other seemingly reasonable predictors, such as the number of registers within the building.

Variable Selection - Random Forest

RMSE: 0.0, Rsquared: NA, Top 5: RFG

As with the PLS, model, the resulting error metrics were promising, with slightly better RMSE and Rsquared values. The selected variables are ver similar with a few exceptions. This model has placed higher importance on a yes/no response to the presence of walk in refrigerators as well as whether or not a building is a fast food establishment

Variable Selection - Lasso

RMSE: 0.0, Rsquared: NA, Top 5: RFG

This resulted in a very poor fit, which is not unexpected. Lasso models typically work when a few variables can be used to predict the response, which does not appear to be the case in this instance. Due to the lack of fit, this model will not be used in the variable selection process.

Variable Selection - Forward Selection

RMSE: 0.0, Rsquared: NA, Top 5: RFG

This model was building using the leaps package which iteratively selected the best predictor variable up to a limit of 100. Unsurprisingly, the best model turned out to be the maximum setting; however, encouraging model metrics were returned.

Variable Selection - Simple Neural Network

RMSE: 0.0, Rsquared: NA, Top 5: RFG

Given that the final model will be a neural network, it made sense to try a simple out-of-the-box training model to see if any particular features worked better with this specific process. However,

low metrics were returned but it was decided to keep the predictor set and include it in the final selection summary.

Variable Selection - Recursive Feature Elimination

RMSE: 0.0, Rsquared: NA, Top 5: RFG

A more direct approach was taken with this model, which is specifically used to extract useful features from data sets. As can be seen,

Variable Selection - Selected Variable Analysis

In order to rank the most important features, the variable importance metrics from the selected models were all set to the same scale, the summed up. The number of selected features were then used as hyperparameters in the final model training. As a preliminary check, the top 20 predictors are plotted in the appendix and discussed here;

Natural Gas

General

Test

District Heat

General

Test

Fuel Oil

General

Test

Neural Network Models

General

Reasons for this model type; can capture high levels of complexity, customized loss functions, robust, flexible, etc.

| Natural Gas |
|---------------------|
| Summary |
| Test |
| Performance |
| |
| Test |
| District Heat |
| Summary |
| Test |
| Performance |
| Test |
| Fuel Oil Summary |
| Test |
| Performance |
| Test |
| |
| |
| |
| |
| |
| |

Electricity

Performance

Summary

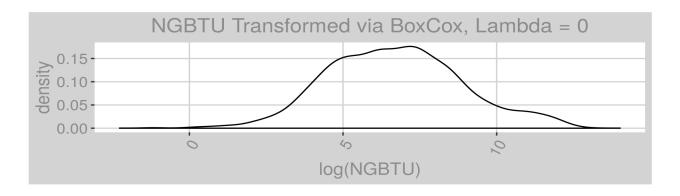
Test

Test

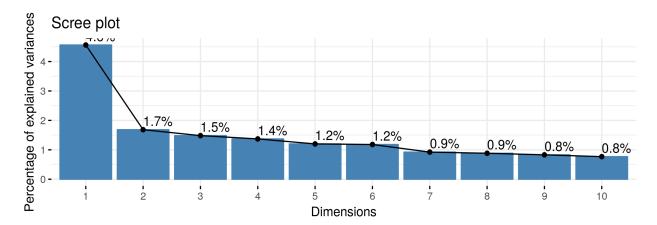
Appendix

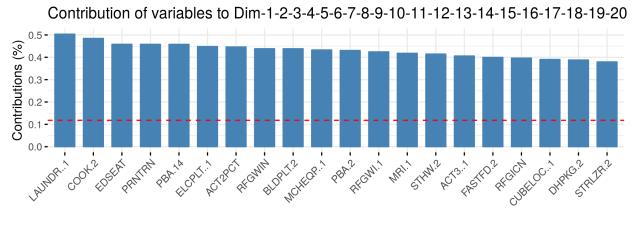
Electricity

Response

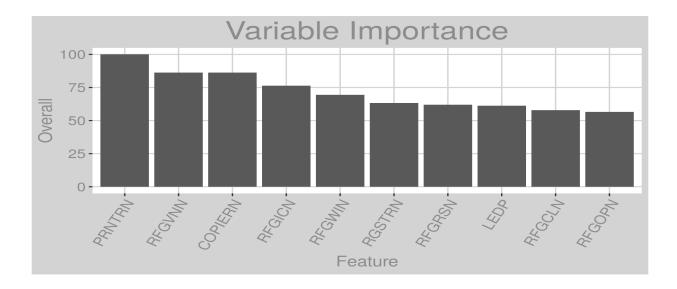


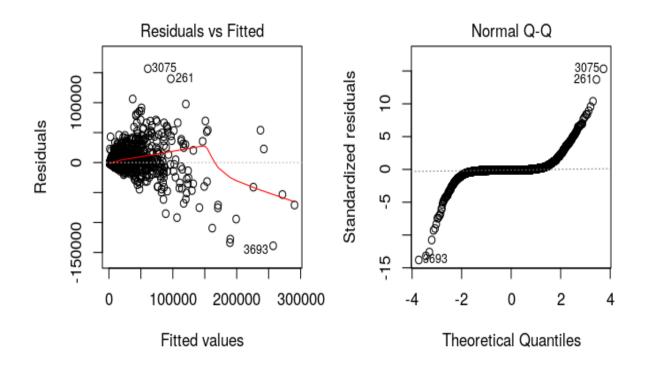
PCA

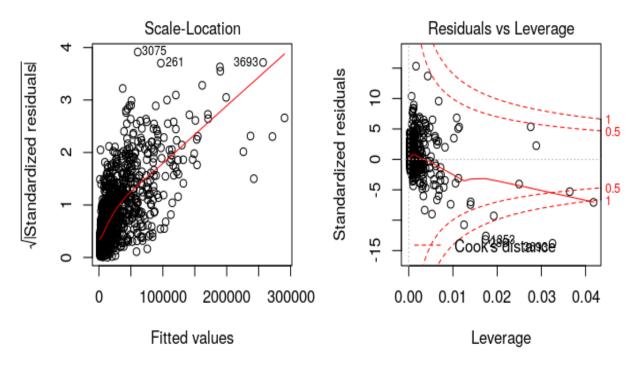


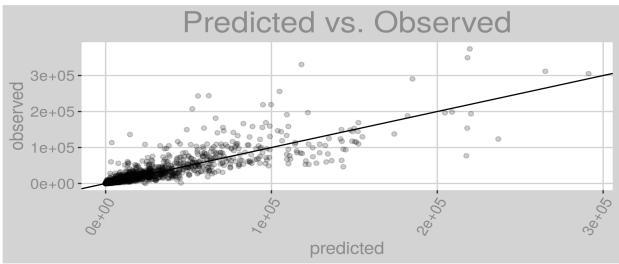


PLS

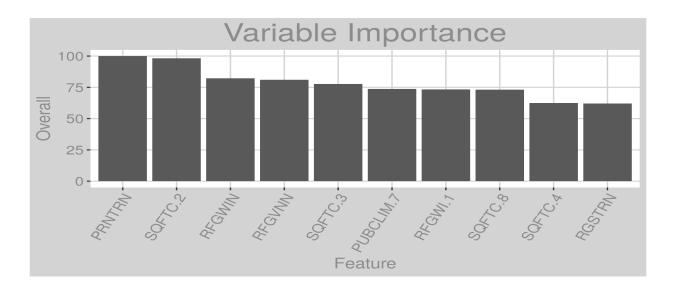


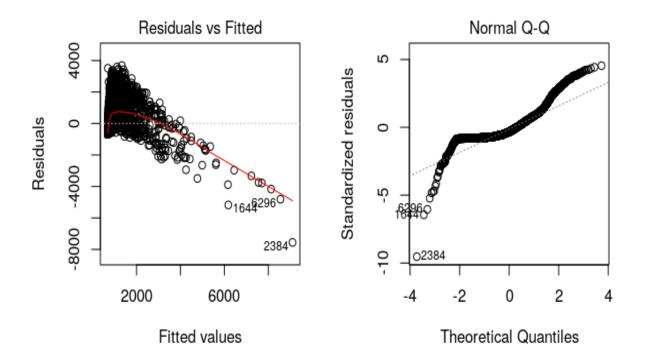


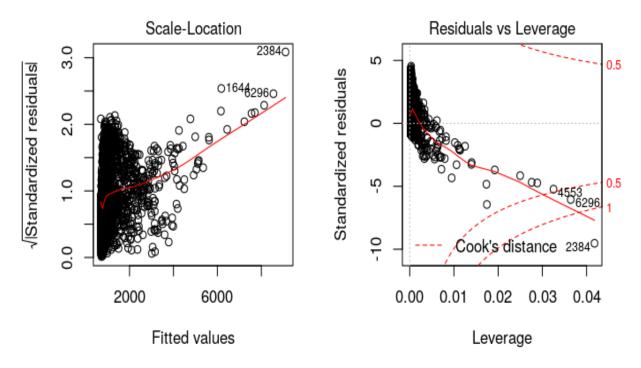


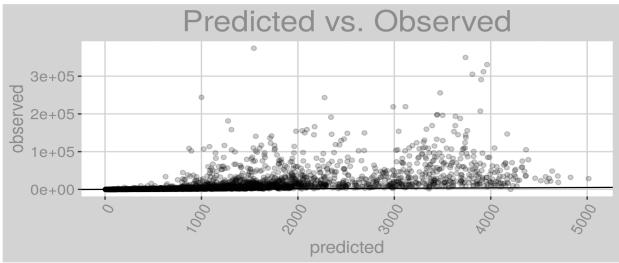


Random Forest

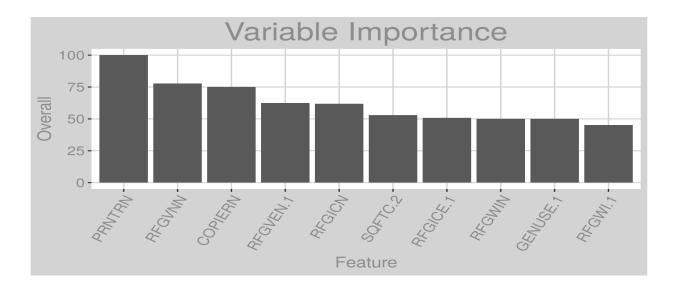


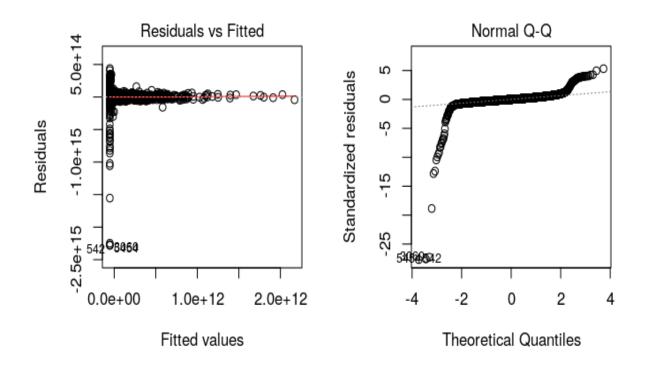


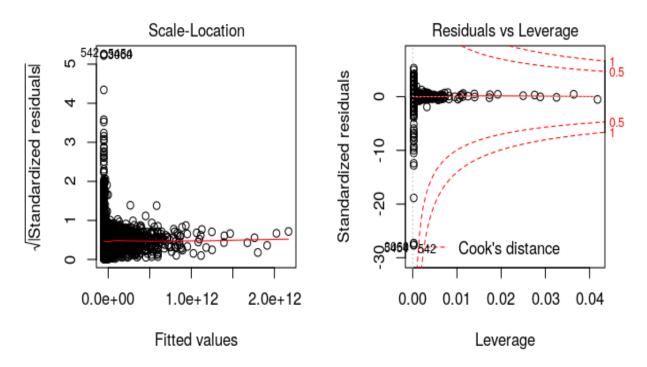


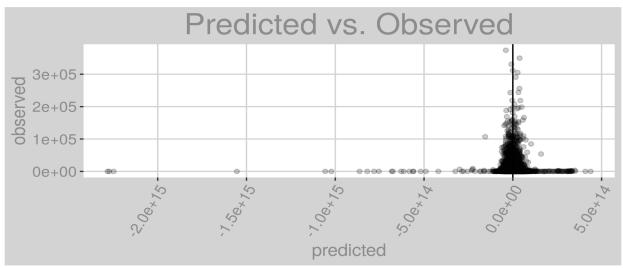


Lasso

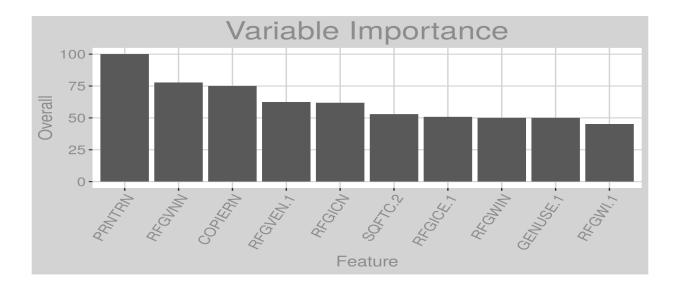


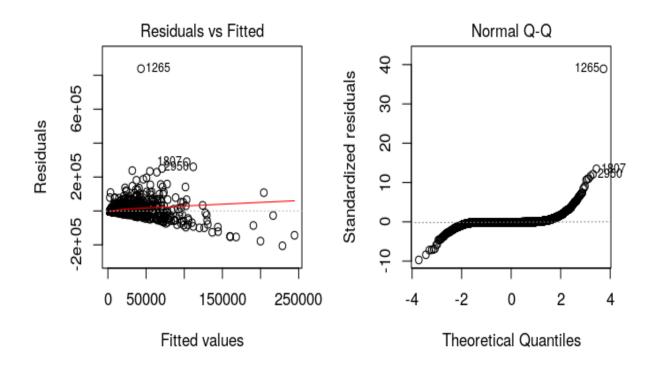


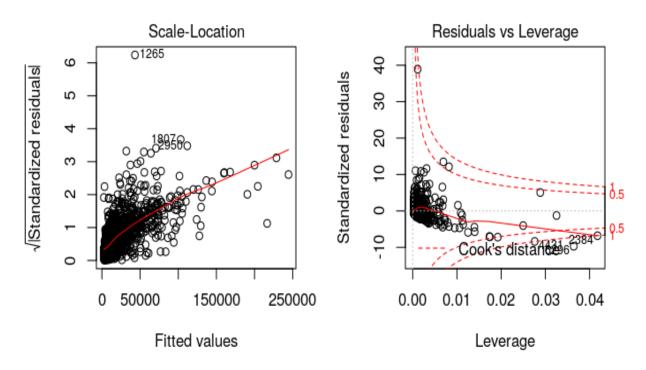


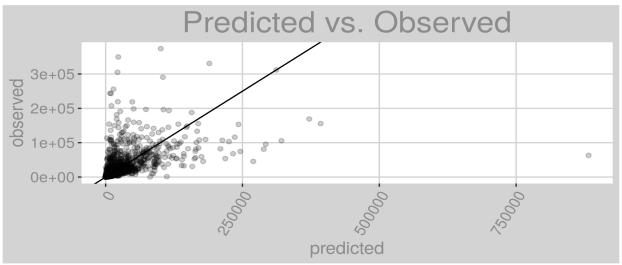


Forward Selection

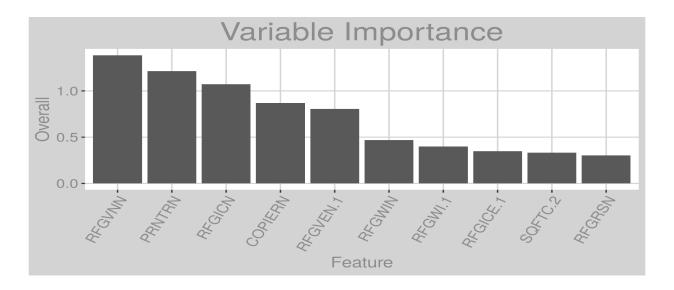


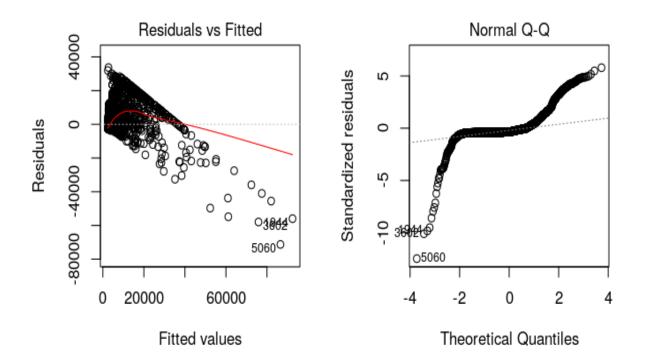


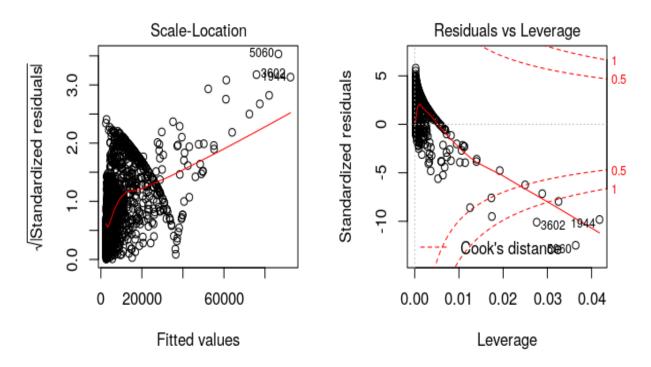


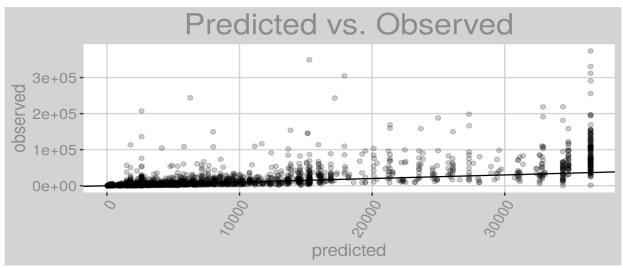


Recursive Feature Extraction

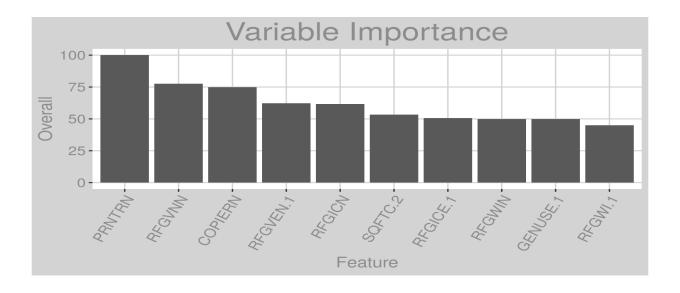


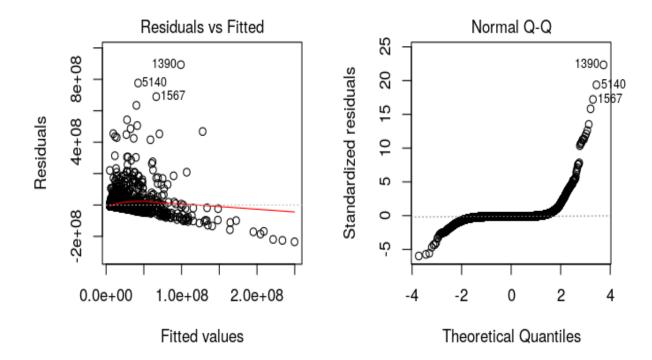


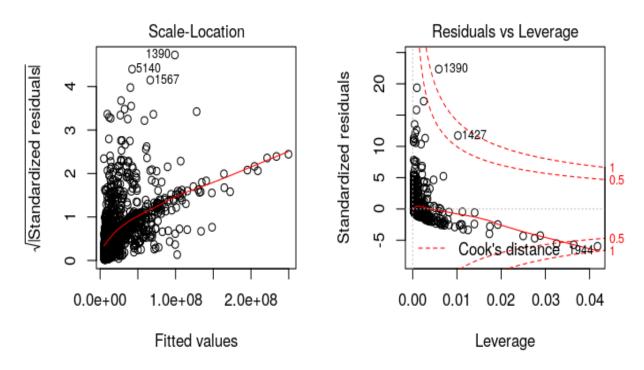


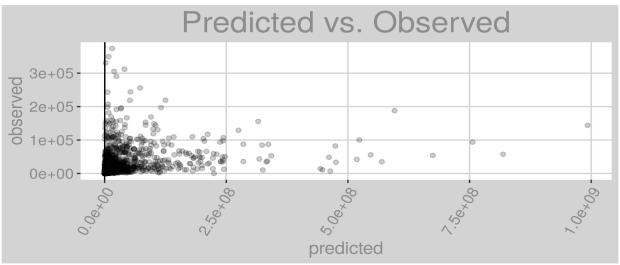


Simple Neural Network









Select Variable Analysis

| Model | RMSE | R2 | MAE |
|----------------------------|--------------|-----------|--------------|
| partialLeastSquares | 1.169408e+04 | 0.7780371 | 3.237700e+03 |
| leaps | 2.327804e+04 | 0.3559985 | 5.652596e+03 |
| randomForest | 1.182305e+06 | 0.2788200 | 8.100512e+05 |
| recursiveFeatureExtraction | 2.221181e+07 | 0.8247289 | 8.762935e+06 |
| neuralNetwork | 4.453689e+07 | 0.1406134 | 1.061397e+07 |
| lasso | 8.242048e+13 | 0.0000032 | 2.936412e+13 |

